Macroeconomics Project

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07/06/2021

Idea

We want to look at the relationship between certain prices and the respective search interest on google for these prices. Can we find granger causality for this relationship? What are possible issues? For example: modern trading algorithms scrape data from the internet and then buy or sell based on the sentiment. Large spikes in search interest may trigger such algorithms. As media spreads the news of price increases more people will look up prices of goods and commodities, again triggering the algorithms. This is basically a feedback loop.

Data

First some notes on the data. The data on the search index of certain prices is taken from Google trends which collects the search queries of people within a specific region (here: United States of America). This data is aggregated on a monthly basis and normalized with a range from zero to 100. Already filtered out are duplicate searches in the sense that the same user made the same search multiple times within a short time-frame. This way we exclude the users which have already invested and constantly check the prices to look how their investment is doing. Data points are divided by total searches for the month and region to represent the relative popularity, i.e. no over-weighting of regions with more people than others which would given the same search behavior lead to differing popularities otherwise.

The data on gold prices comes form the London Bullion Market Association Gold Price and the Federal Reserve Bank of St. Louis, it is measured in USD per troy ounce at 3:00pm. Aggregation is done via prices at the end of each month and not seasonally adjusted.

In parts of this project we scale the price and search index to a range from zero to one in order to compare the relative movements more easily.

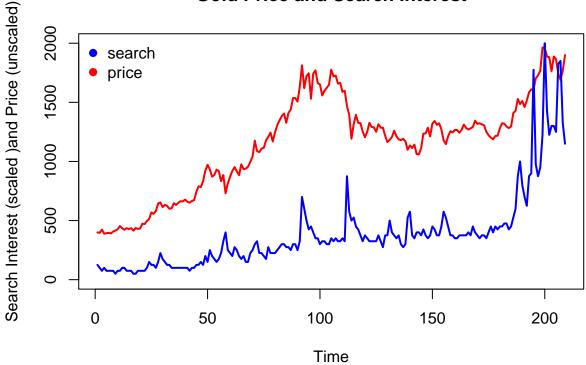
Project Code

```
# clear workspace
rm(list=ls())

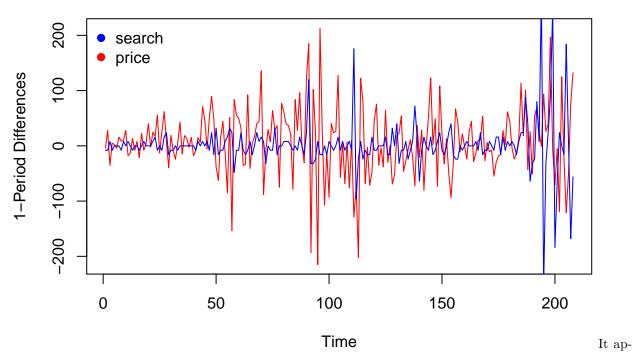
# load needed libraries
library(readr)
library(vars)

# set working directory
#setwd("/Users/samue/Downloads/Studium/Economics (Master - Vienna)/2. Semester/Macroeconometrics/Projectory
```

Gold Price and Search Interest



First Differences: Gold Price and Search Interest



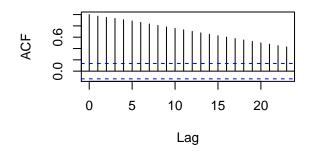
pears that the more volatile regions match. Issue seems to be the scaling of the variables.

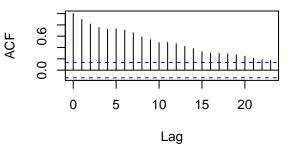
```
# plot ACF for unmodified variables:
par(mfrow=c(2,2))  # changes the plot layout to more easily compare them
acf(gold_pr$GOLDPMGBD228NLBM, main = 'ACF Gold Price')
acf(data$GOLD, main = 'ACF Gold Search Interest')

# plot ACF for differenced variables
acf(gold_price_FD,main = 'ACF Gold Price FD')
acf(gold_search_FD, main = 'ACF Gold Search Interest FD')
```

ACF Gold Price

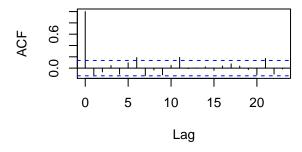
ACF Gold Search Interest

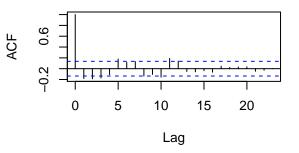




ACF Gold Price FD

ACF Gold Search Interest FD



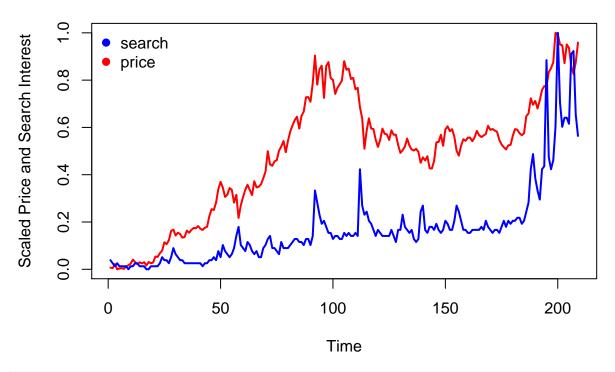


```
par(mfrow = c(1,1)) # revert layout changes
```

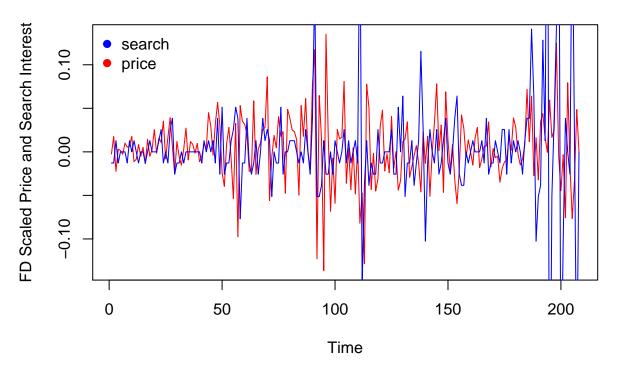
Autocorrelation for the differenced variables seems like no month-on-month relationship between the changes. Kind of like a random walk?

Might help with the interpretation: scale all variables **X** such that $X_t \in [0,1] \forall t \in T$.

```
range01 <- function(x){(x-min(x))/(max(x)-min(x))}
plot(range01(gold_pr$GOLDPMGBD228NLBM), lwd = 2, type = 'l',
    ylab = 'Scaled Price and Search Interest',
    xlab = 'Time', col = 'red')
lines(range01(data$GOLD), lwd = 2, col = 'blue')
legend('topleft', legend = c('search', 'price'),
    col = c('blue', 'red'), bty = "n", pch = c(19,19))</pre>
```

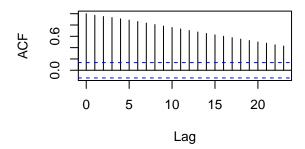


```
# save scaled variables
gold_price_scaled <- rangeO1(gold_pr$GOLDPMGBD228NLBM)</pre>
gold_search_scaled <- range01(data$GOLD)</pre>
# create first difference on scaled variables:
gold_search_scaled_FD <- rep(0,t-1)</pre>
gold_price_scaled_FD <- rep(0,t-1)</pre>
for(i in 2:t-1){
  gold_price_scaled_FD[i-1] <- gold_price_scaled[i]-gold_price_scaled[i-1]</pre>
for(i in 2:t-1){
  \verb|gold_search_scaled_FD[i-1]| <- \verb|gold_search_scaled[i]-gold_search_scaled[i-1]|
# plot first differenced:
plot(gold_price_scaled_FD, lwd = 1, type = 'l',
     ylab = 'FD Scaled Price and Search Interest',
     xlab = 'Time', col = 'red')
lines(gold_search_scaled_FD, lwd = 1, col = 'blue')
legend('topleft', legend = c('search', 'price'),
       col = c('blue', 'red'), bty = "n", pch = c(19,19))
```

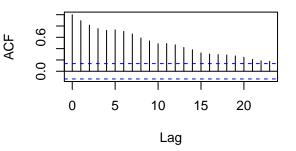


```
# plot ACFs
par(mfrow=c(2,2))  # changes the plot layout to more easily compare them
acf(gold_price_scaled, main = 'ACF Scaled Gold Price')
acf(gold_search_scaled, main = 'ACF Scaled Gold Search Interest')
acf(gold_price_scaled_FD,main = 'ACF Scaled Gold Price FD')
acf(gold_search_scaled_FD, main = 'ACF Scaled Gold Search Interest FD')
```

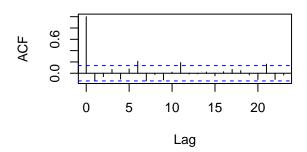
ACF Scaled Gold Price



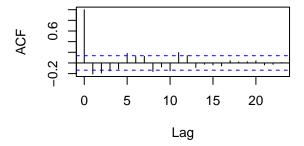
ACF Scaled Gold Search Interest



ACF Scaled Gold Price FD



ACF Scaled Gold Search Interest FD



```
par(mfrow = c(1,1)) # revert layout changes
```

Unsurprisingly the rescaling does not matter for the autocorrelation as it is a scaled measure of linear relationships anyway.

######## From here on: data saved as time series #####

```
# save variable vectors as time series format:
gold_price_scaled <- ts(gold_price_scaled, frequency = 12,</pre>
                      start = c(2004, 1), end = c(2021, 5))
gold_search_scaled <- ts(gold_search_scaled, frequency = 12,</pre>
                       start = c(2004,1), end = c(2021,5))
# set up data for estimation using 'VAR()'
VAR_data <- window(ts.union(gold_price_scaled, gold_search_scaled),</pre>
                  start = c(2004, 1), end = c(2021, 5))
# estimate model coefficients using 'VAR()'
VAR_{est} \leftarrow VAR(y = VAR_{data}, p = 2)
summary(VAR est)
##
## VAR Estimation Results:
## Endogenous variables: gold_price_scaled, gold_search_scaled
## Deterministic variables: const
## Sample size: 207
## Log Likelihood: 636.839
## Roots of the characteristic polynomial:
## 0.9924 0.8559 0.1625 0.1625
## Call:
## VAR(y = VAR_{data}, p = 2)
##
##
## Estimation results for equation gold_price_scaled:
## gold_price_scaled = gold_price_scaled.11 + gold_search_scaled.11 + gold_price_scaled.12 + gold_search
##
##
                        Estimate Std. Error t value Pr(>|t|)
## gold_price_scaled.l1
                        0.869163
                                  0.070442 12.339
                                                     <2e-16 ***
## gold_search_scaled.l1 -0.020645
                                   0.039085 -0.528
                                                     0.5979
## gold_price_scaled.12
                        0.110635
                                   0.070855 1.561
                                                     0.1200
                                                     0.2862
## gold_search_scaled.12 0.042045
                                   0.039316
                                            1.069
## const
                        0.011315
                                  0.005945
                                            1.903
                                                     0.0584 .
## ---
```

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.0395 on 202 degrees of freedom
Multiple R-Squared: 0.9771, Adjusted R-squared: 0.9766
F-statistic: 2151 on 4 and 202 DF, p-value: < 2.2e-16</pre>

##

```
##
##
## Estimation results for equation gold search scaled:
## -----
## gold_search_scaled = gold_price_scaled.l1 + gold_search_scaled.l1 + gold_price_scaled.l2 + gold_sear
##
                      Estimate Std. Error t value Pr(>|t|)
##
## gold_price_scaled.l1
                       0.34683
                                 0.12492
                                          2.776 0.00601 **
## gold_search_scaled.11 0.74430
                                 0.06931 10.738 < 2e-16 ***
## gold_price_scaled.12 -0.26598
                                 0.12565 -2.117 0.03551 *
## gold_search_scaled.12 0.10172
                                 0.06972
                                          1.459 0.14615
                                 0.01054 -1.050 0.29498
## const
                      -0.01107
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.07006 on 202 degrees of freedom
## Multiple R-Squared: 0.8372, Adjusted R-squared: 0.834
## F-statistic: 259.8 on 4 and 202 DF, p-value: < 2.2e-16
##
##
## Covariance matrix of residuals:
                    gold_price_scaled gold_search_scaled
## gold_price_scaled
                          1.561e-03
                                          -4.454e-05
## gold_search_scaled
                          -4.454e-05
                                            4.908e-03
##
## Correlation matrix of residuals:
##
                    gold_price_scaled gold_search_scaled
## gold_price_scaled
                              1.0000
                                              -0.0161
## gold_search_scaled
                             -0.0161
                                               1.0000
# augmented df test on only the gold price
df_test_gold <- urca::ur.df(gold_price_scaled, type = c('drift'),</pre>
                     selectlags = 'BIC')
summary(df_test_gold)
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression drift
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + z.diff.lag)
##
## Residuals:
##
                  1Q
                       Median
                                    3Q
                                            Max
## -0.137377 -0.019230 -0.000925 0.022274 0.126963
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept) 0.010394
                          0.005824
                                    1.785
                                             0.0758 .
                          0.010659 -1.029
                                             0.3049
## z.lag.1
              -0.010964
## z.diff.lag -0.116850
                          0.070135 - 1.666
                                             0.0972 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.03946 on 204 degrees of freedom
## Multiple R-squared: 0.01948,
                                   Adjusted R-squared:
## F-statistic: 2.026 on 2 and 204 DF, p-value: 0.1345
##
##
## Value of test-statistic is: -1.0286 2.2503
## Critical values for test statistics:
##
        1pct 5pct 10pct
## tau2 -3.46 -2.88 -2.57
## phi1 6.52 4.63 3.81
```

Null cannot be rejected given the data, the null is non-stationarity. Not very unexpected as prices are often thought about as following a random walk and thus being non-stationary. But we can also look at difference-stationarity.

```
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression none
##
##
## lm(formula = z.diff ~ z.lag.1 - 1 + z.diff.lag)
##
## Residuals:
                      Median
       Min
                 1Q
                                  3Q
                                          Max
## -0.139705 -0.013946  0.004984  0.026891  0.129077
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## z.lag.1
           -1.19119
                      0.10475 -11.372
                                    <2e-16 ***
                      0.07010
## z.diff.lag 0.06367
                              0.908
                                      0.365
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.0393 on 204 degrees of freedom
## Multiple R-squared: 0.562, Adjusted R-squared: 0.5577
## F-statistic: 130.9 on 2 and 204 DF, p-value: < 2.2e-16
##
```

```
##
## Value of test-statistic is: -11.3722
##
## Critical values for test statistics:
## 1pct 5pct 10pct
## tau1 -2.58 -1.95 -1.62
```

As the test rejects, given the data we cannot say that the data is not stationary.

```
## VAR Estimation Results:
## =========
## Endogenous variables: gold_price, gold_search
## Deterministic variables: both
## Sample size: 208
## Log Likelihood: -1799.017
## Roots of the characteristic polynomial:
## 0.9694 0.7759
## Call:
## VAR(y = VAR_data, p = 1, type = "both")
##
##
## Estimation results for equation gold_price:
## gold_price = gold_price.l1 + gold_search.l1 + const + trend
##
##
                Estimate Std. Error t value Pr(>|t|)
## gold_price.l1
                 0.96788
                           0.01798 53.837 <2e-16 ***
## gold_search.l1 0.10532
                           0.50011 0.211
                                            0.8334
## const
                25.95499
                          13.78646
                                    1.883
                                            0.0612 .
## trend
                0.15617
                           0.13017
                                   1.200 0.2317
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 62.32 on 204 degrees of freedom
## Multiple R-Squared: 0.9772, Adjusted R-squared: 0.9769
## F-statistic: 2913 on 3 and 204 DF, p-value: < 2.2e-16
```

```
##
##
## Estimation results for equation gold search:
## gold_search = gold_price.l1 + gold_search.l1 + const + trend
##
                  Estimate Std. Error t value Pr(>|t|)
## gold_price.l1
                  0.002848
                             0.001578
                                       1.805
                                                0.0725 .
## gold_search.ll 0.777456
                             0.043888 17.715
                                                <2e-16 ***
                             1.209834 -1.784
                                                0.0758 .
## const
                 -2.158855
                             0.011423
## trend
                  0.023485
                                       2.056
                                                0.0411 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
##
## Residual standard error: 5.469 on 204 degrees of freedom
## Multiple R-Squared: 0.8359, Adjusted R-squared: 0.8335
## F-statistic: 346.5 on 3 and 204 DF, p-value: < 2.2e-16
##
##
##
## Covariance matrix of residuals:
              gold_price gold_search
##
## gold_price
                  3883.7
                              -12.50
                   -12.5
                               29.91
## gold_search
## Correlation matrix of residuals:
              gold_price gold_search
                          -0.03669
                 1.00000
## gold_price
                             1.00000
## gold_search
                -0.03669
# compare the VAR to the AR(1) model for the prices
T <-length(gold_price)</pre>
gold_price_2 <- as.numeric(gold_price[-1])</pre>
gold_price_lagged <- as.numeric(gold_price[-T])</pre>
plot(gold_price_2, type = 'l', lwd = 1, col = 'red',
    main = 'Gold Price and Lagged Gold Price',
    ylab = 'Gold Price', xlab = 'Months from 01.2004')
lines(gold_price_lagged, lwd = 1, col = 'blue')
legend('topleft', legend = c('Lagged Price', 'Price'),
      col = c('blue', 'red'), bty = "n", pch = c(19,19))
```

Gold Price and Lagged Gold Price



```
# estimate model
gold_price_AR1 <- lm(gold_price_2 ~ gold_price_lagged)
# estimate robust standard errors
coeftest(gold_price_AR1, vcov. = vcovHC, type = "HC1")</pre>
```

The values on the intercept seem to differ, but the estimated coefficient on the lag seems to fit.

```
# verify the 'by-hand' results with built-in function
ar.ols(gold_price, order.max = 1, intercept = T)
```

```
##
## Call:
## ar.ols(x = gold_price, order.max = 1, intercept = T)
##
## Coefficients:
## 1
## 0.9884
##
## Intercept: 7.171 (4.301)
```

```
##
## Order selected 1 sigma^2 estimated as 3848
forecast::auto.arima(gold_price, ic = 'aic')
## Registered S3 method overwritten by 'quantmod':
##
    method
                       from
##
     as.zoo.data.frame zoo
## Series: gold_price
## ARIMA(0,1,1) with drift
##
## Coefficients:
##
                   drift
            ma1
##
         -0.1411 7.1279
## s.e.
        0.0740 3.6766
## sigma^2 estimated as 3842: log likelihood=-1152.52
## AIC=2311.05
                 AICc=2311.16
                               BIC=2321.06
```

The last model is automated to difference such that the data is stationary, then the function finds the best forecasting model via the AIC. Here this would be an ARMA(0,1) model:

$$\widehat{\Delta \text{gold price}}_t = (7.1279) + \epsilon_t + (-0.1411)\epsilon_{t-1}$$
3.6766 (0.0740)

Differenced AR(1) and ARCH Model for Gold Prices

```
ED Gold Prices

4 D Gold Prices

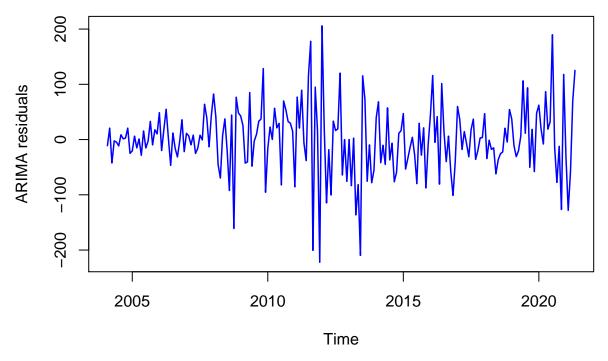
2005 2010 2015 2020

Time
```

```
ar1mod_FD <- arima(gold_price_FD, order = c(1,0,0))
ar1mod_FD
##</pre>
```

```
## Call:
## arima(x = gold_price_FD, order = c(1, 0, 0))
##
## Coefficients:
##
                  intercept
##
         -0.1205
                     7.1540
          0.0694
                     3.8237
## s.e.
##
## sigma^2 estimated as 3814: log likelihood = -1152.78, aic = 2311.57
plot(forecast::arima.errors(ar1mod_FD),type = 'l', lwd = 1.5, col = 'blue',
     ylab = 'ARIMA residuals')
```

Deprecated, use residuals.Arima(object, type='regression') instead



```
mean(forecast::arima.errors(ar1mod_FD))
```

Deprecated, use residuals.Arima(object, type='regression') instead

[1] 0.05853392

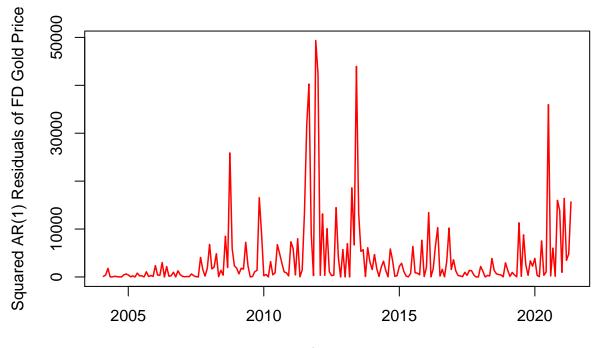
Going by the plot, it does not appear that the variance of the residuals is constant over time but rather has times of higher and lower volatility.

```
resi_ar1_FD_2 <- (forecast::arima.errors(ar1mod_FD))^2
```

Deprecated, use residuals.Arima(object, type='regression') instead

```
resi_arch1_FD_2_model <- arima(resi_ar1_FD_2, order = c(1,0,0))
resi_arch1_FD_2_model</pre>
```

```
##
## Call:
## arima(x = resi_ar1_FD_2, order = c(1, 0, 0))
##
## Coefficients:
## ar1 intercept
## 0.3095 3887.0806
## s.e. 0.0662 727.6653
##
## sigma^2 estimated as 52737140: log likelihood = -2144.4, aic = 4294.79
```



Time from 02.2004