# Tree Based Ensembles for Predicting Survival from Thoracic Surgery

Samuel Jackson, Aberystwyth University

#### I. INTRODUCTION

Thoracic surgery is a major invasive surgery involving operating on the lungs of a patient. The authors of ref. [1] collected several pieces of possibly relevant data on a number patients who went on to have thoracic surgery. The data also includes a record of whether a given patient survived for longer than one year after the surgery. This paper looks at using a reduced subset of the features and patients from the dataset in [1] to classify patients based on whether or not they will survive for one year after the surgery. This paper compares three different classifiers: random forests [2], extremely randomised trees [3], and gradient boosting [4].

The format of the result of this paper is structured as follows: section II outlines the preprocessing steps performed on the dataset and describes the classifiers used. Section III presents the performance of the classifiers on the dataset. Section IV discusses the results and presents possible justification for the performance based on the properties of the classifier and dataset. Finally, a summary and discussion of possible future directions are discussed in section V.

#### II. METHODS

# A. Dataset and Preprocessing

The thoracic surgery dataset used consists of 16 predictors and 300 instances. Table I gives a description of each predictor derived from the original UCI dataset repository [5]. The dataset includes a mixture of both categorical (nominal and ordinal) and continuous data. The final  $(17^{th})$  column of the dataset is the binary class label with value 0 if the patient survived and 1 if they died within one year of surgery.

Several initial observations can be made about dataset prior to any preprocessing steps. One key thing to note about the dataset as a whole is that there is a slight imbalance between the two classes. Only 28% of the dataset is of the positive class (28% of patients died). While this imbalance is not extreme, it can have repercussions for the performance of the classifiers. The accuracy paradox [6] states that a classifier with high accuracy can be built from highly imbalanced training by always predicting the negative class.

The predictor PRE32 is zero for all of the patients in the training dataset. This predictor therefore has zero variation and will not help to discriminate between instance. PRE32 is therefore discarded during preprocessing.

PRE5 appears to have some extreme values. PRE5 corresponds to the FEV1 measure. This would suggest that some patients have an unusually high forced expiration volume. Also, all of the outliers are of the same class. This could

TABLE I
DESCRIPTION OF COLUMNS IN THE THORACIC SURGERY DATASET

Column	Type	Description
DGN	Nominal	Diagnosis: Specific combination of ICD-10 codes for
		primary and secondary as well multiple tumours if
		any (DGN3, DGN2, DGN4, DGN6, DGN5, DGN8,
		DGN1)
PRE4	Numeric	Forced vital capacity (FVC)
PRE5	Numeric	Volume that has been exhaled at the end of the first
		second of forced expiration (FEV1)
PRE6	Ordinal	Performance status - Zubrod scale (PRZ2, PRZ1,
		PRZ0)
PRE7	Nominal	Pain before surgery (T,F)
PRE8	Nominal	Haemoptysis before surgery (T,F)
PRE9	Nominal	Dyspnoea before surgery (T,F)
PRE10	Nominal	Cough before surgery (T,F)
PRE11	Nominal	Weakness before surgery (T,F)
PRE14	Ordinal	T in clinical TNM - size of the original tumour, from
		OC11 (smallest) to OC14 (largest) (OC11, OC14,
		OC12, OC13)
PRE17	Nominal	Type 2 DM - diabetes mellitus (T,F)
PRE25	Nominal	Peripheral arterial diseases (PAD) (T,F)
PRE30	Nominal	Smoking (T,F)
PRE32	Nominal	Asthma (T,F)
AGE	Numeric	Age at surgery
Risk1Y	Nominal	1 year survival period - (T)rue value if died (T,F)
		(Class Label)

cause the classifiers to fit to noise rather than to properly generalise. These instances were therefore removed from the dataset. No reduction in performance was witnessed during cross validation for all classifiers after their removal.

The feature DGN is a nominal categorical predicator. This feature was transformed into series of new features via one hot encoding. Each new predictor is a binary feature which is one if the patient falls into the category and zero otherwise. The original DGN feature is drop after the 7 new binary features are created.

Finally, after all preprocessing is complete, a random forest is trained on the dataset (with default parameters) and the resulting variable importance measure is computed. Any features with a variable importance of zero are dropped. The variable importance of the preprocessed features (before any are dropped) is shown in figure 1.

#### B. Classifiers

Four classifiers were chosen for use on the dataset. The four classifiers used are Random Forests, Gradient Boosting, AdaBoost, and Extra Trees. The implementations of all four classifiers are taken directly from the scikit-learn library [7]. All of these methods are known as ensemble methods. Ensemble methods compose together multiple weak learners

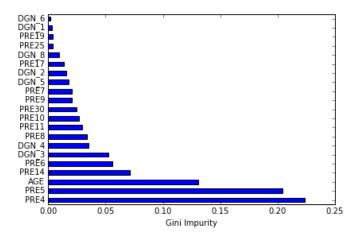


Fig. 1. Feature importance for all of the features after preprocessing.

to produce a single strong classifier. In this paper, all of the algorithms used are also tree based (although this is not necessarily the case with Gradient Boosting and AdaBoost). This means that for each classifier the base learner is a decision tree.

Random forests [2] are perhaps the simplest method of the four. Random forests are simply a collection of n decision trees which are individually trained on the data. The "random" in the name comes from the fact that each tree is trained on both a random sample of the dataset (tree bagging) and also on a random subset of the features (feature bagging). The decision tree weak learners typically overfit to the data. However because the results all trees are averaged over the resulting classification the overall variance in the final model is significantly reduced. The random element for both training instances and features is used to prevent many highly correlated trees from occurring which should reduce overfitting.

Extremely Randomized trees [3] (also called Extra Trees) takes the randomisation aspect of random forests one step further. Both bagging and random features are used, but additionally a random split for each feature in the subset of features is chosen instead of the just computing the optimal feature and split combination.

The AdaBoost algorithm [8] is a generalised method from combining the performance of many weak learners. AdaBoost stands for "adaptive boosting" and boosting is a core component in the training stage. AdaBoost works by first fitting a weak learner to the training dataset and classifying each instance. The error in the classification can be used to re-weight each example in the dataset. This means that misclassified samples are then more likely to be classified correctly in future iterations. Likewise, instances that are correctly classifier can be weighted much lower, as they are easier to correctly identify. Thus AdaBoost can be seen as an additive method in that each tree is built on the error of the previous one. Adaboost does not necessarily have to be used with decision trees, but in this paper we only consider decision tree based AdaBoost.

Gradient Boosting Machines [4] also use a boosting based approach to learning. Like AdaBoost they are an additive

method that iteratively fits a collection of weak learners. Where the two differ is in the way that instances are "weighted". The weighting function in AdaBoost can be seen as a special type of loss function. The gradient of a differentiable loss function can be use to steer the search towards the optimum decision function. In gradient boosting machines the new function added to the mix is the one which is the closest to parallel with the negative gradient of the observed data.

These algorithms were chosen to showcase a broad range of different ensemble algorithms. Ensemble methods often outperform a single strong learner due to the diversity present in the model. All of the models are also decision tree based which work well with a mixture of continuous and discrete values like those present in our dataset.

Two common techniques used in training ensemble algorithms are bagging and boosting. This paper compares two algorithms based on boosting (AdaBoost and Gradient Boosting) and two based on bagging (Random Forests and Extra Trees). These seem like good candidates based on the dataset for two reasons: 1) bagging can be used address the imbalance in the dataset by equally resampling each of the datasets and 2) there doesn't seem to be a clear separation between classes in the dataset which potentially makes boosting a good technique as it should help to push the algorithm towards classify the difficult examples it's it misses.

#### C. Hyperparameters & Tuning

Before all experiments were carried out on the dataset, the hyper-parameters of each classifier were tuned to hopefully achieve optimum performance. The values and number hyper-parameters are dependant both on the implementation of the classifier and the dataset itself. If there is more than one hyper-parameter for a classifier (as is the case with all classifiers used here) then ideally combinations of all hyper-parameters should be explored. Sadly, this means that the space of potential hyper-parameters explodes with the number of hyper-parameters increases.

Due to the relatively small size of the dataset, the space of potential parameters for each classifier is explored using a grid search. In a grid search, all a selection of hyper-parameter values are explicitly enumerated. Each potential value for a hyper-parameter is tested in combination with every other hyper-parameter value. The speed of the grid search is bearable due to the classifier being relatively quick to train on this small dataset. The performance of a set of parameters was evaluated using stratified k-fold cross validation with ROC AUC as the scoring metric.

For Random Forests a grid search was performed over the tree parameters  $max\_depth$ ,  $max\_features$ ,  $min\_samples\_split$  and  $min\_samples\_leaf$ .  $max\_depth$  and  $max\_features$  were trained over the range 2 - 20 in steps of 3.  $min\_samples\_split$  and  $min\_samples\_leaf$  were trained over all values in the range 1 - 5. The number of trees used was fixed to 50 during this search. This is because a small number of trees will be quick to train (and hence the search will complete faster). Generally speaking the performance of the forest should improve as the number of trees increases, so this can be trained afterwards.

TABLE II
TUNED PARAMETERS FOR THE GRADIENT BOOSTING CLASSIFIER

Parameter	Value
learning_rate	0.01
max_depth	9
max_features	11
min_samples_leaf	1
min_samples_split	7
n_estimators	1000
subsample	0.8

The results of tuning the tree parameters showed that *min\_samples\_split* and *min\_samples\_leaf* should be set to 1. This seems logical due to the small number of positive samples. *max\_depth*, *max\_features* were optimised as 16 and 5 respectively. These seem reasonable given the low number of predictive features and the fact that trees in random forests should typically overfit (hence the large maximum depth). After this trial another grid search was performed to find the optimum number of trees over the range 50 - 500 in steps of 50. This suggested that 100 trees should be used.

The training procedure for Extremely Random Trees was identical to Random Forests with the results being similar. After tuning 200 trees were used and *max\_features* was set to 16 and *max\_depth* set to 19.

Adaboost was tuned by fixing the maximum depth of the decision tree and performing a grid search over the number of trees (50 - 1000 in steps of 50) and the learning rate (with values 0.1, 0.5, 0.01, and 0.005) together. This was repeated for multiple values of the maximum depth (tested with values 2, 4, and 6). After tuning 400 trees were used with a *learning\_rate* of 0.5 and *max\_depth* of 4.

Gradient Boosting has many parameters that need to be explored, many of which can interact with one another and tuning in the wrong order can lead to poor results. The number of parameters can also be awkward to train due to the speed of training. The tuning procedure for gradient boosting was therefore as follows:

- Fix all of the parameters to be reasonable initial guesses and fix the learning rate to be quite high (0.1).
- Find the optimum number of estimators for the given leaning rate (searched over the range 20 - 150 in steps of 10).
- Tune the tree based parameters *max\_depth* and *min\_samples\_split* (searched over the ranges 5-16 in steps of 2 and 1-20 in steps of 3 respectively).
- Tune max\_features (5-20 in steps of 2)
- Tune the subsample ratio (values: 0.6, 0.7, 0.75, 0.8, 0.85, and 0.9).
- Finally using all previously tuned parameters increase the number of estimators while simultaneously decreasing the learning rate.

The final values for the tuned parameters used are shown in table II.

	RandomForest	ExtraTrees	GradientBoost	AdaBoost
F1	0.601006	0.606542	0.623161	0.607031
F2	0.522676	0.546392	0.567522	0.549125
F0.5	0.715848	0.688120	0.700784	0.683489

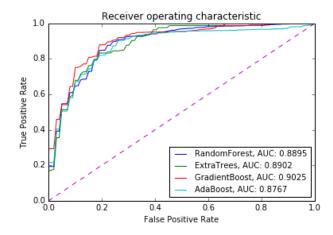


Fig. 2. Mean ROC curves and the mean AUC for all four classifiers over 10 rounds of 5-fold cross validation. All four classifiers perform similarly, with Extra Trees producing the best AUC. All four curves are slightly skewed towards the right of the plot, suggestive of poor recall. The F2 score (table III and figure 3 confirms this.

# III. RESULTS

# A. Performance Evaluation

Each classifier in section II-B was trained using stratified 5-fold cross validation. Stratification was performed to ensure that there was a representative sample of positive classes in each fold. For all classifiers cross validation was repeated ten times, each with a new set of folds to ensure consistent results.

Figure 2 shows the mean ROC curve and mean AUC for each of the classifier after cross validation. The performance of each classifier appears to be very similar. Notably the ROC curve for each type of classifier is shifted to the right of the graph, suggesting that they all exhibit a low recall rate.

Table III and figure 3 confirm this indication. Table III shows the F measure with a  $\beta$  parameter of 1, 2, and 0.5. Figure 3 shows a bar chart of the F2 scores in table III. The performance of all classifiers measured with the F2 score (which weights recall more highly than precision) is much lower in comparison to the F0.5 and F1 scores. This further confirms that all classifiers have a problem with recall.

# B. Feature Engineering

In addition to the preprocessing steps outlined in II-A several combinations of new features were generated from the existing predictors. Firstly, as a large portion of the features are binary, a set of new features were created based on logical binary operators. The creation of the binary features is as follows: all pairs of binary features are enumerated. From each pair three new features are created by combining the pair using logical OR, AND and XOR.

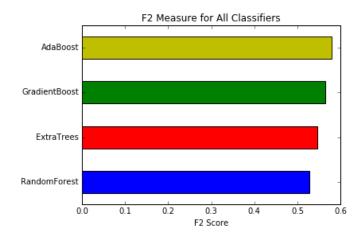
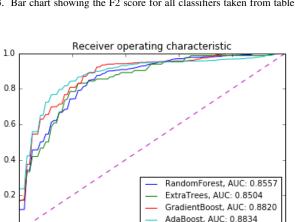


Fig. 3. Bar chart showing the F2 score for all classifiers taken from table III.



Irue Positive Rate

Fig. 4. ROC curves for each of the classifiers with the additional binary features. Performance is notably worse compared to the initial run.

False Positive Rate

0.4

0.6

0.2

Figure 4 shows the ROC curves for the same dataset but with the additional binary features. appended. Table IV shows the corresponding F-scores for each classifier. From these results it is easy to see that all of the classifiers appear to perform worse with the new features. This may be due to their already limited contribution and that fact that the additional dimensionality is hindering progress.

The second modification to the original dataset is to create a couple of new features called FER and OBS. FER is the FEV1/FVC ratio which is spirometry measurement defined as  $(FEV1/FVC) \cdot 100$  [9]. It is interpreted as the percentage of FVC expelled in the first second of a forced expiration. A ratio value below <70% can be suggestive of an obstructive disease. Using this information another feature (OBS) is generated

TABLE IV F SCORES FOR THE DATASET INCLUDING BINARY FEATURES

	RandomForest	ExtraTrees	GradientBoost	AdaBoost
F1	0.543811	0.560718	0.612539	0.646753
F2	0.465938	0.489906	0.547107	0.591129
F0.5	0.662682	0.660713	0.705097	0.721499

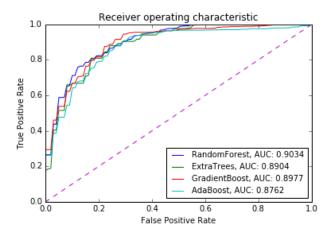


Fig. 5. ROC curves for each of the classifiers with the spirometry features.

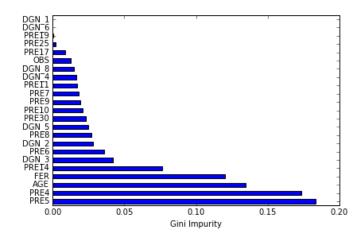


Fig. 6. Variable importance for each of the features with the spirometry features included.

from the ratio. OBS is a binary feature with value 1 when a patient has a ratio <70%.

From figure 5 it can be seen that their is a slight improvement over the original ROC AUC scores using these additional spirometry features. This is backed up by plotting the feature importance obtained from training a random forest on the dataset (see 1). The two new features, particularly the FER feature are providing useful training information. This seems sensible as the new features are just combinations of existing well performing features.

Motivated by the results of the previous test, a selection of new features were created from all order 2 polynomial combinations of the two best predictors: PRE4 and PRE5. This means that the new features are of the form  $a^2$ , ab,  $b^2$  where a and b are PRE4 and PRE5 respectively.

TABLE V F SCORES FOR THE DATASET INCLUDING SPIROMETRY FEATURES

	RandomForest	ExtraTrees	GradientBoost	AdaBoost
F1	0.566669	0.617225	0.600845	0.614050
F2	0.483774	0.549281	0.538619	0.561441
F0.5	0.699297	0.715047	0.688793	0.683218

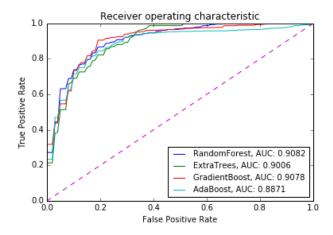


Fig. 7. ROC curves for each of the classifiers with the polynomial combination features.

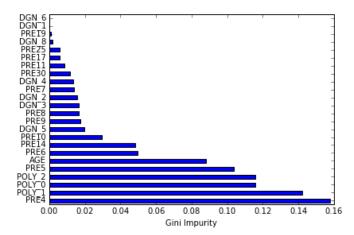


Fig. 8. Variable importance for each of the features with the polynomial combination features included.

This polynomial combination led to the best in the feature engineering results across all classifiers under cross validation. Figure 7 shows the ROC curves with the additional features included. The F-scores for each classifier are show in table VI. The contribution of the new features can be seen in the variable importance plot (figure 8).

# C. Dataset Balancing

As mentioned in section II-A the thoracic surgery dataset is class imbalanced with only 28% of the dataset being of the positive class. One technique to combat class imbalance is to resample the dataset to put more emphasis on the known positive examples. A popular technique for resampling data is

TABLE VI
F SCORES FOR THE DATASET INCLUDING POLYNOMIAL COMBINATION
FEATURES

	RandomForest	ExtraTrees	GradientBoost	AdaBoost
F1	0.604371	0.634325	0.615442	0.662434
F2	0.517592	0.563459	0.560582	0.613066
F0.5	0.736327	0.732681	0.690843	0.726515

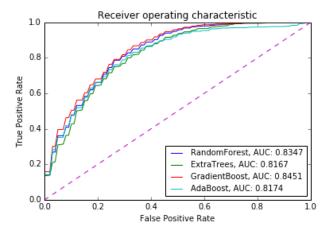


Fig. 9. ROC curves for all four classifiers with SMOTE oversampling with a ratio of 0.8. Each curve represents the average over 50 iterations of Monte Carlo validation. The ROC curves for all classifiers are less skewed compared to figure 2.

SMOTE [10]. SMOTE rebalances a dataset by creating new synthetic training to balance out the majority class. SMOTE is typically combined with under-sampling of the majority class to produce a final dataset that is re-weighted in favour of the minority class.

The results for the classifiers in part III-A shows that they have lower recall than precision. Rebalancing the dataset should show a decrease in precision and an increase in recall rate. This can be desirable in a dataset such as this where recall may be more important than precision. It is probably more desirable overestimate the number people who are likely to die from surgery than to achieve better precision.

SMOTE datasets cannot be validated using conventional k-fold cross validation. This is because the testing fold would contain synthetically generated training examples which are obviously not representative of the ground truth. Instead, in order to achieve a representative sample of performance, "Monte Carlo" cross-validation [11] is used. Before a any resampling is applied, the data set is randomly split into a training and testing set. The split is stratified according to the class labels. All reported experiments use and 80/20 split. Resampling is then applied to the training dataset only, with the testing set remaining untouched. This process is then repeated for the desired number of iterations and the resulting performance measures are averaged. In all experiments the number of iterations performed was 50.

Figure 9 shows ROC curve and mean AUC scores for each of the classifiers using SMOTE with a resampling ratio of 0.8. Table VII shows the F1, F2, and F0.5 scores for each of the classifiers. Comparing this table to the results of III shows a clear difference in the F2 score. Recall weighted performance is now better both than F1 and F0.5. This improvement comes at the cost of a decrease in both the AUC and F0.5 measures. Increasing the oversampling ratio or under-sampling the majority class accentuates this effect.

TABLE VII MEAN F1, F2 AND F0.5 SCORES FOR ALL CLASSIFIERS AFTER MONTE CARLO CROSS VALIDATION WITH SMOTE RESAMPLING WITH A RATIO OF 0.8

	RandomForest	ExtraTrees	GradientBoost	AdaBoost
F1	0.614570	0.613840	0.615768	0.611035
F2	0.648492	0.650097	0.648949	0.643250
F0.5	0.587619	0.585145	0.589706	0.586983

#### IV. DISCUSSION

The experiments in section III have shown a variety of different approaches to predicting surgery survival with ensemble methods. Some of the best performance was achieved using the just the basic preprocessing steps outlined in section II-A.

Looking at the initial performance evaluation (figure 2) it can be seen that all classifiers performed reasonable similarly with Gradient Boosting narrowly coming out ahead. The weakest performer was AdaBoost. Looking at the F-scores for each of the classifiers (table III) is more informative. All classifiers can be seen to perform comparable. Each performed weaker under the F2 measure which weights recall more highly than precision. It is the higher recall rate which is primarily driving the improvement of Gradient Boosting over the other classifiers in this trial.

Motivated by this baseline evaluation, this paper explored alternative feature representations through "feature engineering". The first attempt was to create combinations of binary features from the existing dataset. This actually lead to worse results compared to the original preprocessing steps. None of the new binary features significantly contributed new information for the algorithm to work with. This probably meant that the increase in dimensionality out weighed any small gains delivered by the new representation. Each tree in the ensembles will only look at a limited number of features, so adding lots of redundant features is only likely to decrease performance while increasing training time. Note that an attempt was made to reduce the number of features by discarding the *n* weakest features using both variable importance and PCA, but neither method improved the results of this test.

The second feature engineering experiment was to a couple of features generated from spirometry theory. Both the FER and OBS feature suggested are directly derived from the existing predictors in the dataset. The bar chart in figure 6 shows that these features do appear to contribute some additional information for the classifiers to work with. This is reflected in the AUC scores and the corresponding F-scores. The result for AUC is nearly identical between Gradient Boosting, Extra-Trees, and Random forests. The most successful (by a tiny margin) showed that Random forests performed the best in terms in AUC but this was only due to high precision. The F2 and F1 score are both much reduced in in the Random Forest trial. With these new features the best candidate appears to be Extra-Trees which has an improvement across all three F-scores.

The third experiment involving feature engineering was to create a new batch of features by creating polynomial combinations of the features PRE4 and PRE5 which were shown to be the strongest predictors in figure 1. This lead to the best

AUC scores out of all the trails with three out of the four classifiers pushing into the 0.9 range. The variable importance plot (8) shows that many of the polynomial features are the most successful contributors. The F-scores reflect this result and show higher scores across the board. By far the biggest increase was in terms of precision. In particular, AdaBoost faired much better with polynomial features.

Finally an experiment was carried looking at improving the performance by resampling the dataset using SMOTE. While random forests and extra-trees already carry out bagging which already balances the dataset during training, this method could of potentially helped the performance of the boosting classifiers. Figure 9 shows a marked decrease in performance across all classifiers. This is probably due to the synthetic examples not realistically reflecting the distribution of positive examples in the dataset. What is more interesting is the fact that the F2 scores for each classifier are improved by applying SMOTE but the precision is dramatically hindered. This is could be due to the synthetic examples "expanding" the region around positive examples which the algorithm considers to be positive. This is probably not representative of the true decision boundary, but has the effect of increasing recall as more examples are likely to land with the expanded positive region. While this test resulted in much worse performance it could still be of interest. In predicting thoracic surgery survival it is more desirable to have high recall than high precision.

# V. CONCLUSIONS

In conclusion this paper examined the effect of four different ensemble methods on a variety of engineered features. The effect of resampling the dataset was also explored. The final classifier used on the unused testing data for submission was trained using both the additional polynomial and spirometry features. This lead to best performance with the classifier. This classifier had a final AUC after cross validation of .

While this is one of the best AUC scores achieved across all experiments there is clearly some room from improvement. One area of improvement worth exploring would be to look at more automated methods of feature selection. One such method could be recursive feature elimination in conjunction with a model that estimates feature relevance (such as random forests). Alternatively a non-linear dimensionality reduction technique could be used to find projections of the feature space onto a lower dimensional embedding. This could be particular beneficial in the case of the binary features where the feature space is relatively much larger.

Another avenue for exploration would be to look at a different branch of algorithms. For example a penalised SVM could be experimented with. The original authors of [1] propose a boosted SVM which performs reasonable well on the expanded dataset. Any alternative classifier will probably benefit from some from of bagging or resampling more than the ensemble methods.

The experiments in this paper show that any further predictive progress appears to be hindered by the low recall rate. This is a common trade-off in machine learning. Implementing this system in the real world would most likely require favouring

a lower F0.5 score for a higher F2 for safety reasons. Any progress beyond the AUC achieved in this paper is likely to require a combination of further creative feature engineering and a good mix of bagging/resampling.

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# APPENDIX A THIRD PARTY LIBRARIES

The code use to produce the results in the paper rely upon a number of different third party libraries. The libraries used and the relevant version of each is show in the table below. lease note that the *UnbalancedData* library is not currently directly available through *pip* by default and so must be installed directly from the GitHub repository using the following command:

```
pip install git+https://github.com/fmfn/UnbalancedDataset
```

TABLE VIII
THIRD PARTY LIBRARIES AND THE ACCOMPANYING VERSIONS USED IN ALL THE FOLLOWING CODE SAMPLES.

Name	Version
pandas	0.18.0
sklearn	0.17.1
UnbalancedDataset	0.1
matplotlib	1.5.1
numpy	1.11.0
scipy	0.17.0

# APPENDIX B PYTHON SCRIPT FOR FINAL CLASSIFIER

This appendix contains the python script for creating the final classifier used to make the predictions on the test dataset for this assignment. This will save a CSV file in the data folder called *submission.csv*.

```
import pandas as pd
  import numpy as np
  from sklearn import preprocessing
  from sklearn.pipeline import Pipeline
  from sklearn.ensemble import GradientBoostingClassifier
  df = pd.DataFrame.from_csv("../data/train_risk.csv", index_col=False)
test = pd.DataFrame.from_csv("../data/test_risk.csv", index_col=False)
  X, y = df[df.columns[:-1]], df[df.columns[-1]]
  def encode\_onehot(x\_data, column\_name, digitize=False):
        "" Encode a catagorical column from a data frame into a
       data frame of one hot features
14
15
       data = x_data[[column_name]]
16
       if digitize:
           data = np.digitize(data, np.arange(data.min(), data.max(), 10))
19
       enc = preprocessing.OneHotEncoder()
       features = enc.fit_transform(data).toarray()
       names = ['%s_%d' % (column_name, i) for i in enc.active_features_]
       features = pd. DataFrame (features, columns=names, index=x_data.index)
24
       return features
26
  def create_spiro_features(x_data):
29
        "" Creare spriometry based features """
       # create new feature FER
       # this is the raito of FEV1 and FVC
31
      FER = (x_data.PRE5 / x_data.PRE4) * 100
       FER.index = x_data.index
       # create a new feature OBS
       # this is whether the instance has a FER below 70%
       # which implies an obstructive disease.
       OBS = pd. Series(np. zeros(x_data.AGE. shape))
       OBS.index = x_data.index
       OBS. loc[FER < 70] = 1.0
       spiro = pd.concat([FER, OBS], axis=1)
42
       spiro.columns = ['FER', 'OBS']
44
       return spiro
```

```
def create_poly_features(x_data, names):
       """ Create new features base on Polynomials of the original best two predictors """
48
       poly = preprocessing.PolynomialFeatures(2, include_bias=False, interaction_only=True)
49
       poly\_features = pd.DataFrame(poly.fit\_transform(x\_data[names]), index = x\_data.index)
50
       poly_features.columns = ["POLY_%d" % i for i in poly_features.columns]
52
       return poly_features
53
54
  def preprocess(x_data, y_data=None):
55
       # drop zero var PRE32
56
57
       Xp = x_data.drop("PRE32", axis=1)
58
59
       # remove outliers
60
       if y_data is not None:
           mask = Xp.PRE5 < 30
61
62
           Xp = Xp.loc[mask]
           Yp = y_data.copy()
63
64
           Yp = Yp.loc[mask]
65
       else:
           Yp = None
66
67
       # encode catagorical data as one hot vectors
68
69
       one\_hot\_names = ["DGN"]
       encoded = map(lambda name: encode_onehot(Xp, name), one_hot_names)
       # combine into a single data frame
       new_features = pd.concat(encoded, axis=1)
73
       # drop the catagorical variables that have been encoded
       Xp.drop(["DGN"], inplace=True, axis=1)
       # add new features
       Xp = pd.concat([Xp, new_features], axis=1)
79
       return Xp, Yp
80
  Xp, Yp = preprocess(X, y)
82
  scaler = preprocessing.StandardScaler()
83
  gbc_params = {
       'min_samples_leaf': 1,
86
       'min_samples_split': 7,
87
       'max_depth': 9,
88
       'max_features': 11,
89
       'subsample': 0.8,
       'n_estimators': 1000,
91
       'learning_rate': 0.01
93
  gbc = GradientBoostingClassifier(**gbc_params)
94
  gbc_pipe = Pipeline([('scaler', scaler), ('GradientBoostingClassifer', gbc)])
  model = {'name': 'GradientBoost', 'model': gbc_pipe}
97
  # Create training features
  spiro_features = create_spiro_features(Xp)
  poly_features = create_poly_features(Xp, ['PRE4', 'PRE5'])
101
  Xp_all = pd.concat([Xp, poly_features, spiro_features], axis=1)
  Xp_all.drop(['DGN_1', 'DGN_8'], axis=1, inplace=True)
103
104
  # Create testing features
  Xtest , _ = preprocess(test , y_data=None)
106
  Xtest = Xtest.drop('test_id', axis=1)
107
108
109
  test_spiro_features = create_spiro_features(Xtest)
  test_poly_features = create_poly_features(Xtest, ['PRE4', 'PRE5'])
  X test = pd.concat([X test, test\_spiro\_features, test\_poly\_features], axis=1)
  # Build model
  gbc_final = model['model']
114
  gbc_final.fit(Xp_all, Yp)
  predicted_prob = pd. Series(gbc_final.predict_proba(Xtest)[:, 0])
116
  # Format output
  predicted_label = predicted_prob.copy()
  predicted_label[predicted_label >= 0.5] = 1
  predicted_label[predicted_label < 0.5] = 0</pre>
  predicted_label = predicted_label.astype(int)
```

```
final_submission = pd.concat([test.test_id , predicted_label , predicted_prob], axis=1)
final_submission.columns = ['test_id', 'predicted_label', 'predicted_output']
final_submission.to_csv('.../data/submission.csv', index=False)
```

../src/classify.py

#### APPENDIX C

#### IPYTHON NOTEBOOK AND ADDITIONAL PYTHON MODULES FOR ANALYSIS, TRAINING AND TUNING

This listing shows the contents of the analysis IPython notebook as a python script. For a better formatted version of this code install IPython and open the Analysis.ipynb file provided with the assignment submission. This IPython notebook contains all of the code for analysing the data, tuning the algorithms, and performing both stratified k-fold and Mote Carlo cross validation. Two additional modules (*pipeline* and *roc\_analysis*) are also provided as listing as the end of this section.

```
# coding: utf-8
  # In[1536]:
  get_ipython().magic(u'matplotlib inline')
  import pandas as pd
  import numpy as np
  import matplotlib.pyplot as plt
  # ### Loading the Datasets
  # In[2556]:
14
  df = pd.DataFrame.from_csv("../data/train_risk.csv", index_col=False)
test = pd.DataFrame.from_csv("../data/test_risk.csv", index_col=False)
  X, y = df[df.columns[:-1]], df[df.columns[-1]]
21
  # ## Analysing the Data
  # Looking at the difference between the number of positive and negative samples in the dataset shows that
       there are more negative examples than positive examples. Only 28% of all samples are of the positive
       class.
24
  # In[428]:
  def class_balance_summary(y):
        "" Summarise the imbalance in the dataset"""
       total\_size = y.size
29
      negative\_class = y[y == 0].size
       positive\_class = y[y > 0]. size
       ratio = positive_class / float(positive_class + negative_class)
       print "Total number of samples: %d" % total_size
       print "Number of positive samples: %d" % positive_class
       print "Number of negative samples: %d" % negative_class
       print "Ratio of positive to total number of samples: %.2f" % ratio
  class_balance_summary(y)
42
  # Some initial observations about the data before it is preprocessed:
43
    - PRE32 is all zeros. This can be removed
     - PRE14 looks catagorical. Should be split into multiple binary variables
45
     - DGN looks catagorical. As above.
    - PRE5 looks to have some outliers. See box plot below. Potentially remove or split into two extra
       variable?
  # In [2391]:
51
  X. head()
  # Box plot below shows the outliers in PRE5. It is worth noting that all of these outliers are of the
       negative class. This variable is the volume that can be exhaled in one second given full inhilation. It
        is likely that these values are therefore errors in reporting as it is unlikely that humans can exhale
        such a large volume so quickly.
55
```

```
56 # In [3501]:
57
  # X.PRE5.plot(kind='box')
58
  X.PRE5.plot(kind='box')
59
  print y[X.PRE5 > 30]
60
62
  # ## Preprocessing
63
  #
64
  # Create a new matrix of preprocessed features. This will encode catagorical data as one hot vectors,
65
       remove outliers, and normalise the data.
66
  # In[4081]:
67
68
  from sklearn import preprocessing
69
70
   def encode_onehot(x_data, column_name, digitize=False):
        "" Encode a catagorical column from a data frame into a data frame of one hot features"""
       data = x_data[[column_name]]
74
       if digitize:
           data = np.digitize(data, np.arange(data.min(), data.max(), 10))
76
78
       enc = preprocessing.OneHotEncoder()
       features = enc.fit_transform(data).toarray()
       names \ = \ [\ '\%s\_\%d\ '\ \%\ (column\_name\ ,\ i\ ) \ \ for\ i\ in\ enc\ .\ active\_features\_\ ]
80
       features = pd.DataFrame(features, columns=names, index=x_data.index)
81
82
       return features
83
84
85
   def preprocess(x_data, y_data=None):
       # drop zero var PRE32
86
       Xp = x_data.drop("PRE32", axis=1)
87
88
       # remove outliers
89
90
       if y_data is not None:
91
           mask = Xp.PRE5 < 30
           Xp = Xp.loc[mask]
92
93
           Yp = y_data.copy()
           Yp = Yp.loc[mask]
94
95
       else:
           Yp = None
96
97
98
       # encode catagorical data as one hot vectors
       one_hot_names = [ "DGN" ]
99
100
       encoded = map(lambda name: encode_onehot(Xp, name), one_hot_names)
       #combine into a single data frame
101
       new_features = pd.concat(encoded, axis=1)
102
103
       # drop the catagorical variables that have been encoded
104
       Xp.drop(["DGN"], inplace=True, axis=1)
105
       # add new features
106
       Xp = pd.concat([Xp, new_features], axis=1)
107
108
       return Xp, Yp
109
110
  Xp, Yp = preprocess(X, y)
  Xp. head ()
114
  # Measure the effectiveness of each feature using the variable importance measure from a Random Forest
115
116
  # In [40431:
117
   def measure_importance(x_data, y_data):
       rf_selector = RandomForestClassifier(criterion='gini', class_weight='balanced')
120
121
       rf_selector.fit(scaler.fit_transform(x_data), y_data)
       feature_importance = pd. Series(rf_selector.feature_importances_ , index=x_data.columns).sort_values(
       ascending=False)
       feature_importance.plot(kind='bar')
124
       return feature_importance
  feature_importance = measure_importance(Xp, Yp)
126
  Xp.drop(feature_importance[feature_importance == 0].index, inplace=True, axis=1)
128
129
  # In [3967]:
130
```

```
feature_importance.plot(kind='barh')
   plt.xlabel('Gini Impurity')
134
  plt.tight_layout()
   plt.savefig("img/feature_importance.png")
135
136
   # The numerical features appear to be the most important ones. Plot a scatter plot matrix to see how the
138
       how the correlate with each other
139
140
   # In[3757]:
141
  pd.tools.plotting.scatter_matrix(Xp[['PRE4', 'PRE5', 'AGE']], c=Yp)
142
143
144
145
  # ## Tuning Model Parameters
146
  # Given the current status of the data tune the model parameters to it before we evalute the overall
147
       performance. Note that all of the tuning presented here is orientated towards obtaining the highest AUC
        score. Other metrics might be more desirable given the problem domain, but AUC is the measurement used
        for assignment points.
148
  # In[3532]:
149
150
  from sklearn import cross validation
151
   skf = cross_validation.StratifiedKFold(Yp, n_folds=5)
152
154
155
  # ### Random Forest Tuning
156 # Run a grid search over a range of parameters for a Random Forest. The dataset is small enough that we can
        do them all at once. ""n_estimators" is neglected because this should always improve as it is
       increased so we should attempt to make it as large as possible subject to lack of improvement
157
   # In[3835]:
158
159
   param_grid = {"max_depth": range(2, 20, 3),}
160
                  "max_features": range(2, 20, 3),
161
                 "min_samples_split": range(1, 5),
163
                 "min_samples_leaf": range(1, 5),
163
164
165
  rf = RandomForestClassifier(class_weight='balanced', n_estimators=50, random_state=50)
166
  rf_clf = grid_search.GridSearchCV(rf, param_grid, n_jobs=-1, cv=skf, scoring='roc_auc')
167
168
   rf_clf.fit(Xp, Yp)
169
170
  # In[3836]:
171
  print rf_clf.best_params_
174
175
176
  # Now take a look at the number of estimators and see where performance begins to level off.
   # In[3838]:
178
179
  param\_grid = \{"n\_estimators": range(50, 500, 50)\}
180
181
   const_params = {'max_features': 1, 'min_samples_split': 1, 'max_depth': 16, 'min_samples_leaf': 1}
182
  rf = RandomForestClassifier(class_weight='balanced', n_estimators=50, random_state=50, **const_params)
  rf_clf2 = grid_search.GridSearchCV(rf, param_grid, n_jobs=-1, cv=skf, scoring='roc_auc')
184
185
  rf_c1f2.fit(Xp, Yp)
186
187
   # The best parameters for ""n_estimators" levels off after around 300 estimators
188
189
190
  # In [3840]:
191
  plt.plot([d[0]['n_estimators'] for d in rf_clf2.grid_scores_], [d[1] for d in rf_clf2.grid_scores_])
192
   print rf_clf2.best_params_
193
194
  print rf_clf2.best_score_
195
196
  # In[3725]:
197
198
  rf_c1f2.best_estimator_.get_params()
199
200
201
```

```
202 # ### Gradient Boosting Tuning
203
204 Gradient boosting is difficult to tune effectively. [This guide](http://www.analyticsvidhya.com/blog
       /2016/02/complete-guide-parameter-tuning-gradient-boosting-gbm-python/) suggests starting by fixing the
        learning rate and number of estimators to a relatively low number in order to tune the other
       hyperparameters. After they are optimised the learning rate is gradually lowered and the number of
       estimators increased until we find convergance on the optimum parameters
205
   # In[3587]:
206
207
208
   param_grid = [
      \{'n_{estimators}': range(20,150,10)\}
209
210
  1
211
   const_params = {'learning_rate': 0.1, 'min_samples_split': 1, 'min_samples_leaf': 3, 'max_depth': 8, '
       max_features': 'sqrt', 'subsample': 0.8}
   gbc = GradientBoostingClassifier(random_state=50, **const_params)
214
215
   gbc_clf = grid_search.GridSearchCV(gbc, param_grid, cv=skf, scoring='roc_auc')
   gbc\_clf.fit(Xp, Yp)
217
218
    ""n_estimators" plateaus at around 100, so we'll use this instead of the optimum as less trees ==
  #
219
       quicker training and we'll need to decrease the learning rate and increase the number of trees later in
        the tuning anyway.
220
   # In[3588]:
223
  plt.plot([d[0]['n_estimators'] for d in gbc_clf.grid_scores_], [d[1] for d in gbc_clf.grid_scores_])
   print gbc_clf.best_params_
226
  # Now tune the '''max_depth''' and the '''min_samples_split''' parameters.
227
228
   # In[3594]:
229
230
231
   const_params = { 'n_estimators':100,
                     'learning_rate': 0.1,
                    'min_samples_leaf': 3,
                     max_features': 'sqrt',
234
                    'subsample': 0.8
235
236
238
   param_grid = [
       {'max_depth':range(5,16,2), 'min_samples_split':range(1, 20, 3)}
240
241
242
  gbc = GradientBoostingClassifier(random_state=50, **const_params)
   gbc_clf = grid_search.GridSearchCV(gbc, param_grid, cv=skf, scoring='roc_auc')
244
245
   gbc_clf.fit(Xp, Yp)
246
247
  # In[3595]:
248
249
250
   print gbc_clf.best_params_
251
   gbc_clf.grid_scores_
252
253
  # Now train ''max_features'':
254
255
  # In[3600]:
256
257
   const_params = { 'n_estimators':100,
258
                    'learning_rate': 0.1,
259
                    'min_samples_leaf': 3,
260
261
                     'max_features': 'sqrt',
                    'max_depth': 9,
262
                    'min_samples_split': 7,
263
                     subsample': 0.8
264
265
266
   param_grid = [
267
       { 'max_features': range(5,20,2)}
268
269
270
271
```

```
gbc = GradientBoostingClassifier(random_state=50, **const_params)
   gbc_clf = grid_search.GridSearchCV(gbc, param_grid, cv=skf, scoring='roc_auc')
273
   gbc_clf.fit(Xp, Yp)
275
276
277
   # In [3601]:
278
   plt.plot([d[0]['max_features'] for d in gbc_clf.grid_scores_], [d[1] for d in gbc_clf.grid_scores_])
279
   print gbc_clf.best_params_
280
281
282
   # Now train to tune the "subsample" rate.
283
285
   # In [3603]:
286
   const_params = { 'n_estimators':100,
                      'learning_rate': 0.1,
288
                      'min_samples_leaf': 3,
289
290
                      'max_features': 'sqrt',
                      'max_depth': 9,
291
                      'min_samples_split': 7,
292
                      'max_features': 11,
293
                      'subsample': 0.8
294
295
296
297
   param_grid = [
       {'subsample': [0.6, 0.7, 0.75, 0.8, 0.85, 0.9]}
298
299
300
301
   gbc = GradientBoostingClassifier(random_state=50, **const_params)
302
   gbc_clf = grid_search.GridSearchCV(gbc, param_grid, cv=skf, scoring='roc_auc')
303
304
   gbc_clf.fit(Xp, Yp)
305
306
   # In [3604]:
307
308
   plt.plot([d[0]['subsample'] for d in gbc_clf.grid_scores_], [d[1] for d in gbc_clf.grid_scores_])
309
310
   print gbc_clf.best_params_
312
   # Now cross validate with all the parameters set:
313
314
315
   # In [3614]:
317
   const_params = {
                      'min_samples_leaf': 1,
318
                      'min_samples_split': 7,
319
                      'max_depth': 9,
320
                      max_features': 11,
                      'subsample': 0.8
322
   param_grid = [
325
       {'n_estimators': [100], 'learning_rate': [0.1]}, {'n_estimators': [200], 'learning_rate': [0.05]},
326
327
       {'n_estimators': [1000], 'learning_rate': [0.01]}, 
{'n_estimators': [1500], 'learning_rate': [0.005]},
328
330
   ]
   gbc = GradientBoostingClassifier(random_state=50, **const_params)
333
   gbc_clf = grid_search.GridSearchCV(gbc, param_grid, cv=skf, scoring='roc_auc')
334
335
   gbc_clf.fit(Xp, Yp)
336
337
   # In[3718]:
338
339
340
   print gbc_clf.best_params_
341
   gbc_clf.grid_scores_
342
343
   # In[3854]:
344
345
346 p = pd.DataFrame(gbc_clf.best_estimator_.get_params(), index=['Value']).T
347 p.index.name = "Parameter"
348 print p.to_latex()
```

```
350
  # ### AdaBoost Tuning
351
    Perhaps the easiest train due to a fairly limited number of parameters. Adjusting the ""max_depth"
352
       suggests that 4 appears to be roughly the best option for the depth of the decision trees.
   # In[3764]:
355
   param_{grid} = \{ "n_{estimators}" : range(50, 1000, 50), 'learning_rate' : [0.1, 0.5, 0.01, 0.005] \}
356
357
358
   dt = DecisionTreeClassifier(class_weight='balanced', max_depth=4)
  adb = AdaBoostClassifier(dt)
359
   adb\_clf = grid\_search . GridSearch CV (adb \,, \ param\_grid \,, \ n\_jobs = -1, \ cv = skf \,, \ scoring = `roc\_auc')
   adb_clf.fit(Xp, Yp)
362
   # In[3781]:
364
365
  print adb_clf.best_params_
366
   print adb_clf.best_score_
367
   adb_clf.grid_scores_
369
370
371
   # ### Extremely Random Trees Tuning
372
  # This is very similar to Random Forests. In fact we will start with the same parameter set for the grid
373
       search.
375
  # In[3800]:
376
   param_grid = \{ max_depth : range(2, 20, 3), \}
377
                  "max_features": range(2, 20, 3),
378
                  "min_samples_split": range(1, 5),
379
                  "min_samples_leaf": range(1, 5),
380
381
   etc = ExtraTreesClassifier(class_weight='balanced', bootstrap=True, n_estimators=50, random_state=50)
382
   etc_clf = grid_search.GridSearchCV(etc, param_grid, n_jobs=-1, cv=skf, scoring='roc_auc')
383
   etc_clf.fit(Xp, Yp)
384
386
  # In[3801]:
387
388
   print etc_clf.best_params_
389
390
   print etc_clf.best_score_
391
392
   # Now check increasing the number of estimators and find the drop off point
393
394
  # In[3805]:
396
   param\_grid = \{"n\_estimators": range(50, 500, 50)\}
397
398
   const_params = { 'max_features': 16, 'min_samples_split': 1, 'max_depth': 19, 'min_samples_leaf': 1}
390
   etc = ExtraTreesClassifier(class_weight='balanced', bootstrap=True, random_state=50, **const_params)
400
   etc_clf2 = grid_search.GridSearchCV(etc, param_grid, n_jobs=-1, cv=skf, scoring='roc_auc')
401
   etc_clf2.fit(Xp, Yp)
402
403
404
  # In[3806]:
405
406
   plt.plot([d[0]['n_estimators'] for d in etc_clf2.grid_scores_], [d[1] for d in etc_clf2.grid_scores_])
407
   print etc_clf2.best_params_
408
409
  print etc_clf2.best_score_
411
  # In [3807]:
412
413
  etc_clf2.best_estimator_.get_params()
414
415
416
  # ## Model Performance
417
418 Test the performance of each of the models on the preprocessed dataset before trying any more complicated
        feature engineering/resampling. This should give us some rough baseline AUC measures to work with.
       Firstly, set up the models. This creates a set of pipelines for each of the models we want to use.
419
  # In[3971]:
420
421
```

```
422 from sklearn.pipeline import Pipeline
   from sklearn.svm import SVC
423
424 from sklearn.ensemble import ExtraTreesClassifier, AdaBoostClassifier
   from sklearn.neighbors import KNeighborsClassifier
425
   from sklearn.tree import DecisionTreeClassifier
   reload (pipeline)
   import pipeline
428
429
   reload (roc_analysis)
   from roc_analysis import ROCAnalysisScorer
430
431
432
   scaler = preprocessing.StandardScaler()
433
434
   # set up classifier objects
435
   knn = KNeighborsClassifier(n_neighbors=5, weights='distance')
   dct = DecisionTreeClassifier(class_weight='balanced', max_depth=4)
436
437
   abt = AdaBoostClassifier(dct, n_estimators=400, learning_rate=0.5)
438
439
   gbc_params = {
440
          min_samples_leaf': 1,
         'min_samples_split': 7,
441
442
         'max_depth': 9,
         'max_features': 11,
443
         'subsample': 0.8,
444
445
         'n_estimators': 1000,
         'learning_rate': 0.01
446
447
   gbc = GradientBoostingClassifier(**gbc_params)
448
449
450
   exf_params = {
          bootstrap': True,
451
         'class_weight': 'balanced',
'criterion': 'gini',
452
453
         'max_depth': 19,
454
         'max_features': 16,
'max_leaf_nodes': None,
455
456
         'min_samples_leaf': 1,
457
458
         'min_samples_split': 1,
         "min\_weight\_fraction\_leaf": 0.0",
450
         'n_estimators': 200,
         'n_jobs': 1,
461
462
         'oob_score': False
         'random_state': 50,
463
         'verbose': 0,
464
465
         'warm_start': False
   }
466
467
468
   exf = ExtraTreesClassifier(**exf_params)
469
470
471
   rf_params = {
         'bootstrap': True,
472
473
         'class_weight': 'balanced',
         'criterion': 'gini',
474
         'max_depth': 16,
475
         'max_features': 1,
476
         'max_leaf_nodes': None,
477
         'min_samples_leaf': 1,
'min_samples_split': 1,
478
479
         'min_weight_fraction_leaf': 0.0,
480
         'n_estimators': 300
481
482
   rf_balanced = RandomForestClassifier(**rf_params)
483
484
   # create pipelines for each model
   abt_pipe = Pipeline([('scaler', scaler), ('AdaBoost', abt)])
486
   exf_pipe = Pipeline([('scaler', scaler), ('ExtraTrees', exf)])
gbc_pipe = Pipeline([('scaler', scaler), ('GradientBoostingClassifer', gbc)])
rfs_pipe = Pipeline([('scaler', scaler), ('RandomForest', rf_balanced)])
487
488
489
490
491
   # create list of model data
492
   models = [
        { 'name': 'AdaBoost', 'model': abt_pipe},
{ 'name': 'ExtraTrees', 'model': exf_pipe},
{ 'name': 'RandomForest', 'model': rfs_pipe},
{ 'name': 'GradientBoost', 'model': gbc_pipe},
493
494
495
496
497
   ]
498
```

```
499 # set the same training set for all models.
500 # this is just the preprocessed dataset.
501 for model in models:
       model['train_data'] = (Xp, Yp)
502
503
504
   # Define some useful helper functions for summarising the results of k-fold/monte carlo cross validation
505
506
   # In[3829]:
507
508
509
   def f_score_summary(scorers):
           Create a summary of the average f-scores for all folds/trials"""
510
511
        series = []
512
       columns = []
       for key, scorer in scorers, iteritems():
513
            f_scores = [np.mean(scorer.f1scores_), np.mean(scorer.f2scores_), np.mean(scorer.fhalf_scores_)]

s = pd.Series(f_scores, index=['F1', 'F2', 'F0.5'])
514
515
516
            series.append(s)
517
            columns.append(key)
519
       frame = pd.concat(series, axis = 1)
       frame.columns = columns
520
       return frame
521
522
   def summarise_scorers(scorers):
523
         "" Create a summary of the scorers AUCs for all folds/trials"""
524
       names = [name for name in scorers.keys()]
525
       aucs = [scorer.aucs_ for scorer in scorers.values()]
526
527
       aucs = pd.DataFrame(np.array(aucs).T, columns=names)
       return aucs.describe()
528
529
530
   # Perform n iterations of k fold cross validation. Here I am using 10 iterations and 5 folds at each
531
        iteration.
532
   # In [3972]:
533
534
   scorers = pipeline.repeated_cross_fold_validation(models, n=10, k=5)
536
537
   # Plot an ROC curve and the mean AUCs.
538
539
   # In[3973]:
540
   get_ipython().magic(u'matplotlib inline')
542
543
   for key, scorer in scorers.iteritems():
544
       scorer.plot_roc_curve(mean_label=key, mean_line=True, show_all=False)
545
   plt.plot(np.arange(0,1.1, 0.1), np.arange(0,1.1, 0.1), '---')
   # plt.savefig("img/roc_cv.png")
547
548
549
   # Plot bar chart of the F2 scores
550
551
   # In[3862]:
552
553
554
   f_scores = f_score_summary(scorers)
   ax = f_scores.loc['F2'].plot(kind='barh', title='F2 Measure for All Classifiers', color=['b', 'r', 'g', 'y'
555
       ])
   ax.set_xlabel('F2 Score')
556
   plt.tight_layout()
557
   plt.savefig('img/f2_score.png')
558
559
   # Summarise the F scores
561
562
   # In[3833]:
563
564
   f_scores = f_score_summary(scorers)
   print f_scores.to_latex()
566
567
   f scores
569
   # ## Feature Engineering
570
571 #
4 Test creating some new features based on combinations of existing ones in the dataset. Cross validate
        each set of new features to see if it improves performance.
```

```
### Binary Features
574
575
  # In [3917]:
576
577
578
  import itertools
579
580
   def binary_combinations(x_data, names):
       name_pairs = itertools.combinations(names, 2)
581
582
       features = []
583
       for a_name, b_name in name_pairs:
           a, b = x_{data}[a_{name}], x_{data}[b_{name}]
584
585
            features.append(np.logical_xor(a, b).astype(int))
58
            features.append(np.logical_and(a, b).astype(int))
            features.append(np.logical_or(a, b).astype(int))
587
588
       return pd. DataFrame (np. array (features).T, index=x_data.index)
589
590
591
   binary_features = binary_combinations(Xp, ['PRE7', 'PRE8', 'PRE9', 'PRE10', 'PRE11', 'PRE17', 'PRE30'])
  Xp_binary = pd.concat([Xp, binary_features], axis=1)
592
   feature_importance = measure_importance(Xp_binary, Yp)
  Xp_binary.drop(feature_importance[feature_importance == 0].index, inplace=True, axis=1)
594
595
596
  # In[3879]:
597
598
   for model in models:
599
       model['train_data'] = (Xp_binary, Yp)
600
601
   scorers = pipeline.repeated_cross_fold_validation(models, n=10, k=5)
602
603
604
605
  # In [3881]:
606
   get_ipython().magic(u'matplotlib inline')
607
608
   for key, scorer in scorers.iteritems():
       scorer.plot_roc_curve(mean_label=key, mean_line=True, show_all=False)
609
610
611
   plt.plot(np.arange(0,1.1, 0.1), np.arange(0,1.1, 0.1), '--')
   plt.savefig("img/roc_binary_features.png")
612
613
614
  # In[3882]:
615
616
  f_scores = f_score_summary(scorers)
617
   print f_scores.to_latex()
   f_scores
619
620
621
   # ### Spirometry Based Features
622
  # In[4031]:
624
625
   def create_spiro_features(x_data):
626
       # create new feature FER
627
628
       # this is the raito of FEV1 and FVC
       FER = (x_data.PRE5 / x_data.PRE4) * 100
629
       FER.index = x_data.index
630
631
       # create a new feature OBS
632
       # this is whether the instance has a FER below 70%
633
       # which implies an obstructive disease.
634
635
       OBS = pd. Series (np. zeros (x_data.AGE. shape))
       OBS.index = x_data.index
       OBS. loc[FER < 70] = 1.0
637
638
639
       spiro = pd.concat([FER, OBS], axis=1)
       spiro.columns = ['FER', 'OBS']
640
641
       return spiro
642
643
  # In[4032]:
644
645
   spiro_features = create_spiro_features(Xp)
  Xp_spiro = pd.concat([Xp, spiro_features], axis=1)
647
  feature_importance = measure_importance(Xp_spiro, Yp)
649 Xp_spiro.drop(feature_importance[feature_importance == 0].index, inplace=True, axis=1)
```

```
651
  # In[3954]:
652
653
   for model in models:
654
655
       model['train_data'] = (Xp_spiro, Yp)
656
   scorers = pipeline.repeated_cross_fold_validation(models, n=10, k=5)
657
658
659
660
   # In[3955]:
661
   get_ipython().magic(u'matplotlib inline')
662
663
   for key, scorer in scorers.iteritems():
       scorer.plot_roc_curve(mean_label=key, mean_line=True, show_all=False)
664
665
   plt.plot(np.arange(0,1.1, 0.1), np.arange(0,1.1, 0.1), '--')
666
667
   plt.savefig("img/roc_spiro_features.png")
668
669
670
  # In [3957]:
671
  feature_importance.plot(kind='barh')
672
673
   plt.xlabel('Gini Impurity')
  plt.tight_layout()
674
675
   plt.savefig("img/importance_spiro_features.png")
676
677
678
  # In[3958]:
679
680
  f_scores = f_score_summary(scorers)
   print f_scores.to_latex()
681
682
  f scores
683
684
  # ### Polynomial Combinations
685
686
  # In[3959]:
687
688
   def create_poly_features(x_data, names):
689
690
       # create new features base on Polynomials of the original best two predictors
       poly = sklearn.preprocessing.PolynomialFeatures(2, include_bias=False, interaction_only=True)
691
       poly_features = pd.DataFrame(poly.fit_transform(x_data[names]), index=x_data.index)
693
693
       poly_features.columns = ["POLY_%d" % i for i in poly_features.columns]
       return poly_features
694
695
   poly_features = create_poly_features(Xp, ['PRE4', 'PRE5'])
696
   Xp_poly = pd.concat([Xp, poly_features], axis=1)
697
  feature_importance = measure_importance(Xp_poly, Yp)
  Xp_poly.drop(feature_importance[feature_importance == 0].index, inplace=True, axis=1)
699
700
701
  # In[3960]:
702
703
   for model in models:
704
       model['train_data'] = (Xp_poly, Yp)
705
706
   scorers = pipeline.repeated_cross_fold_validation(models, n=10, k=5)
707
708
709
  # In [3961]:
710
711
   get_ipython().magic(u'matplotlib inline')
713
   for key, scorer in scorers.iteritems():
       scorer.plot_roc_curve(mean_label=key, mean_line=True, show_all=False)
714
   plt.plot(np.arange(0,1.1, 0.1), np.arange(0,1.1, 0.1), '--')
716
   plt.savefig("img/roc_poly_features.png")
718
719
  # In[3962]:
720
  feature_importance.plot(kind='barh')
   plt.xlabel('Gini Impurity')
  plt.tight_layout()
  plt.savefig("img/importance_poly_features.png")
726
```

```
# In[3964]:
728
729
   f_scores = f_score_summary(scorers)
730
   print f_scores.to_latex()
   f_scores
734
   # ## Resampling the Dataset
735
736
737
   # Testing whether using resampling improves performance
738
   # ### Testing with regular Over/Under sampling
739
740
   # In[3906]:
741
742
   splitter = pipeline.OverUnderSplitter(test_size = 0.2, under_sample = 0.4, over_sample = 0.8)
743
   overunder_scorers = pipeline.monte_carlo_validation(Xp, Yp, models, splitter, n=50)
744
746
747
   # In[3822]:
748
749
   for key, scorer in overunder_scorers.iteritems():
750
        scorer.plot_roc_curve(mean_label=key, mean_line=True, show_all=False)
751
752
   # In[3823]:
753
754
755
   f_score_summary (overunder_scorers)
756
   # In[3824]:
758
759
760
   summarise_scorers(smote_scorers)
761
762
763
   # ### Testing with SMOTE + Undersampling
764
   # In [3907]:
766
   smote_params = {'kind': 'regular', 'k':3, 'ratio': 0.8, 'verbose': 1}
   splitter = pipeline.SMOTESplitter(test_size = 0.2, under_sample = 1.0, smote_params = smote_params)
768
   smote_scorers = pipeline.monte_carlo_validation(Xp, Yp, models, splitter, n=50)
769
770
772
   # In [3910]:
773
   for key, scorer in smote_scorers.iteritems():
774
775
       scorer.plot_roc_curve(mean_label=key, mean_line=True, show_all=False)
776
   plt.plot(np.arange(0,1.1,\ 0.1)\,,\ np.arange(0,1.1,\ 0.1)\,,\ '---')
777
778
   plt.savefig("img/roc_smote.png")
779
780
   # In[3911]:
781
782
783
   smote_f_scores = f_score_summary(smote_scorers)
   print smote_f_scores.to_latex()
784
   smote\_f\_scores
786
787
   # ## Best Classifier
788
789
   # In [4060]:
791
   spiro_features = create_spiro_features(Xp)
792
   poly_features = create_poly_features(Xp, ['PRE4', 'PRE5'])
793
   Xp_all = pd.concat([Xp, poly_features, spiro_features], axis=1)
Xp_all.drop(['DGN_1', 'DGN_8'], axis=1, inplace=True)
794
   Xp_all.drop(['DGN_1'],
796
   for model in models:
       model['train_data'] = (Xp_all, Yp)
797
   scorers = pipeline.repeated\_cross\_fold\_validation(models, n=10, k=5)
799
800
801
   # In [4061]:
802
803
```

```
804 for key, scorer in scorers.iteritems():
       scorer.plot_roc_curve(mean_label=key, mean_line=True, show_all=False)
805
806
   plt.plot(np.arange(0,1.1, 0.1), np.arange(0,1.1, 0.1), '--')
807
808
  # In[3981]:
810
811
  f_scores = f_score_summary(scorers)
812
813
  f_scores
814
815
  # ## Predicton on Test Set
816
817
  # Finally, based on the best combination of techniques used in the preceeding sections, and using the
818
       classifier with the best AUC performance, make probalistic predictions based on the unlabelled test
819
820
  # In [4083]:
821
   Xtest , _ = preprocess(test , y_data=None)
  Xtest = Xtest.drop('test_id', axis=1)
823
824
825
   test_spiro_features = create_spiro_features(Xtest)
   test_poly_features = create_poly_features(Xtest, ['PRE4', 'PRE5'])
826
  Xtest = pd.concat([Xtest, test_spiro_features, test_poly_features], axis=1)
828
   print Xtest.columns.size, Xp_all.columns.size
829
830
831
   # In [4084]:
832
833
   gbc_final = models[3]['model']
834
   gbc_final.fit(Xp_all, Yp)
835
   predicted_prob = pd. Series(gbc_final.predict_proba(Xtest)[:, 0])
836
837
838
  # In [4085]:
839
   predicted_label = predicted_prob.copy()
841
   predicted_label[predicted_label >= 0.5] = 1
   predicted_label[predicted_label < 0.5] = 0</pre>
843
   final_submission = pd.concat([test.test_id, predicted_label, predicted_prob], axis=1)
   final_submission.columns = ['test_id', 'predicted_label', 'predicted_output']
846
  final_submission
```

../src/analysis.py

# A. ROC Analysis Module

```
from sklearn import metrics
  import numpy as np
  from scipy import interp
  import matplotlib.pyplot as plt
  from scipy stats import threshold
  class ROCAnalysisScorer:
       def __init__(self):
            self.rates_ = []
self.aucs_ = []
            self.fhalf_scores_ = []
            self.f2scores_ = []
            self.flscores_ = []
14
       \label{eq:def_call} \begin{array}{ll} \text{def} & \_\texttt{call}\_\texttt{(self, ground\_truth, predictions, **kwargs):} \end{array}
16
            return self.auc_score(ground_truth, predictions, **kwargs)
18
       def auc_score(self, ground_truth, predictions, **kwargs):
            thresholded = threshold(predictions[:, 1], threshmin=0.5)
            thresholded \ = \ threshold \, (\, thresholded \, \, , \ threshmax \, = \, 0.5 \, , \ newval \, = \, 1.0) \, . \, astype \, (\, int \, )
20
            fhalf_score = metrics.fbeta_score(ground_truth.astype(int), thresholded, beta=0.5)
            f2_score = metrics.fbeta_score(ground_truth.astype(int), thresholded, beta=2)
23
            fl_score = metrics.fbeta_score(ground_truth.astype(int), thresholded, beta=1)
```

```
fpr, tpr, _ = metrics.roc_curve(ground_truth, predictions[:, 1])
           area = metrics.auc(fpr, tpr)
26
           self.fhalf_scores_.append(fhalf_score)
28
           self.f2scores_.append(f2_score)
           self.flscores_.append(fl_score)
           self.rates_.append((fpr, tpr))
31
32
           self.aucs_.append(area)
33
           return area
34
35
      def mean_roc_metrics(self):
           mean tpr = 0.0
37
           mean\_fpr = np.linspace(0, 1, 100)
           for fpr, tpr in self.rates_:
               mean_tpr += interp(mean_fpr, fpr, tpr)
41
           mean_tpr = mean_tpr / len(self.rates_)
42
           area = metrics.auc(mean_fpr, mean_tpr)
           return mean_fpr, mean_tpr, area
44
45
       def plot_roc_curve(self, title=None, labels=None, show_all=True, chance_line=False, mean_line=False,
47
       mean_label="Mean"):
48
49
           if show_all:
               for i, ((fpr, tpr), area) in enumerate(zip(self.rates_, self.aucs_)):
50
51
                   if labels is None:
                        name = "ROC %d" % (i+1)
                    elif isinstance (labels, list):
54
                        name = labels[i]
                    elif isinstance (labels, str):
55
56
                        name = labels
57
                    plt.plot(fpr, tpr, label='%s AUC = \%0.4f' % (name, area))
58
59
           if mean_line and len(self.rates_) > 1:
               mean_fpr , mean_tpr , area = self . mean_roc_metrics()
60
               plt.plot(mean\_fpr\,,\ mean\_tpr\,,\ label="\%s\,,\ AUC:\ \%.4f"\ \%\ (mean\_label\,,\ area))
61
62
           if chance_line:
63
64
               line = np.arange(0, 1.1, 0.1)
               plt.plot(line, line, "---", label="Chance")
65
66
67
           if title is None:
               title = 'Receiver operating characteristic'
68
69
70
           plt.title(title)
           plt.xlabel('False Positive Rate')
           plt ylabel ('True Positive Rate')
72
           plt.legend(loc="lower right", prop={'size': 10})
73
74
  def plot_confusion_matrix(cm, title='Confusion matrix', cmap=plt.cm.Blues):
76
       plt.imshow(cm, interpolation='nearest', cmap=cmap)
77
78
79
       width, height = cm.shape
80
       for x in xrange (width):
           for y in xrange (height):
81
               plt.annotate(str(cm[x][y]), xy=(y, x),
                        horizontalalignment='center'
83
                        verticalalignment='center', size=20)
84
85
       plt.title(title)
86
       plt.colorbar()
       plt.show()
```

../src/roc\_analysis.py

# B. Pipeline Module

```
from roc_analysis import ROCAnalysisScorer
from sklearn import cross_validation
from sklearn.metrics import make_scorer
from unbalanced_dataset import SMOTE, UnderSampler, OverSampler
```

```
def cv_pipeline(model, x_data, y_data, cv=None):
           Cross Validate a model pipeline
      Args:
           model: A sklearn Pipeline object to cross validate
10
           x_data: Feature matrix
           y_data: Class labels
           cv: A predefined sklearn cross validation object
       Returns:
14
      A ROCAnalysisScorer object with the true/false positive rates and AUCs for all folds
15
16
      roc_data = ROCAnalysisScorer()
18
       roc_data_scorer = make_scorer(roc_data, greater_is_better=True, needs_proba=True, average='weighted')
19
       cross_validation.cross_val_score(model, x_data, y_data, cv=cv, scoring=roc_data_scorer)
      return roc_data
20
  def test_pipeline(model, x_data, y_data, x_test, y_test):
22
      model.fit(x_data, y_data)
      y_hat = model.predict_proba(x_test)
       test_result = ROCAnalysisScorer()
      test_result.auc_score(y_test, y_hat)
28
      return test_result
29
31
  def score_pipeline(data, cv=None):
      model = data['model']
34
       cv_results = None
      test_results = None
35
      x_data , y_data = data['train_data']
37
38
      if cv is not None:
39
           cv_results = cv_pipeline (model, x_data, y_data, cv=cv)
40
41
42
       if 'test_data' in data:
           x_test , y_test = data['test_data']
43
           test_results = test_pipeline(model, x_data, y_data, x_test, y_test)
45
       return (cv_results, test_results)
47
48
  def repeated_cross_fold_validation(models, n=10, k=5):
      scorers = \{\}
50
51
52
       for i in range(n):
           # create a new cross validation set for each iteration & test.
           skf = cross\_validation.StratifiedKFold(models[0]['train\_data'][1], n\_folds=k)
54
55
56
           for model in models:
57
               model_name = model['name']
               if model name not in scorers:
58
                   scorers[model_name] = ROCAnalysisScorer()
60
61
               results = score_pipeline(model, cv=skf)
62
               # for each model collect the results into a single scorer.
63
               # note: no average is made at this stage. The results of each
64
65
               # of the k folds is collected into a single k * n list for
66
               # the model.
               scorers[model_name].flscores_ += results[0].flscores_
67
68
               scorers [model_name]. f2scores_ += results [0]. f2scores_
               scorers[model_name].fhalf_scores_ += results[0].fhalf_scores_
69
               scorers[model_name].rates_ += results[0].rates_
70
               scorers [model_name]. aucs_ += results [0]. aucs_
72
       return scorers
74
75
76
  def monte_carlo_validation(x_data, y_data, models, splitter, n=10):
77
       scorers = \{\}
78
           x_{train}, y_{train}, x_{valid}, y_{valid} = splitter.split(x_{data}, y_{data})
80
81
           for model in models:
82
```

```
model_name = model['name']
                if model_name not in scorers:
84
                     scorers[model_name] = ROCAnalysisScorer()
85
86
                model['train_data'] = (x_train, y_train)
87
                model['test_data'] = (x_valid, y_valid)
89
90
                results = score_pipeline(model)
91
                # for each model collect the results into a single scorer.
92
93
                # note: no average is made at this stage. The results of each
                # of the k folds is collected into a single k * n list for
94
95
                # the model.
                scorers [model_name]. f1scores_ += results [1]. f1scores_
scorers [model_name]. f2scores_ += results [1]. f2scores_
97
98
                scorers[model_name].fhalf_scores_ += results[1].fhalf_scores_
                scorers [model_name].rates_ += results [1].rates_
scorers [model_name].aucs_ += results [1].aucs_
99
100
101
       return scorers
102
103
104
   class TestSplitter(object):
105
106
       def __init__(self, test_size = 0.2):
107
108
            self._test_size = test_size
109
       def split(self, x_data, y_data):
111
            Xtest, Xvalid = cross_validation.train_test_split(x_data, test_size=self._test_size, stratify=
       y data)
            Ytest, Yvalid = y_data.loc[Xtest.index], y_data.loc[Xvalid.index]
            return Xtest, Ytest, Xvalid, Yvalid
114
   class SMOTESplitter(TestSplitter):
116
117
       def __init__(self, under_sample=1.0, smote_params={}, **kwargs):
118
            super(SMOTESplitter, self).__init__(**kwargs)
120
            self._under_sample = under_sample
            self._smote_params = smote_params
       def split(self, x_data, y_data):
            Xt, Yt, Xv, Yv = super(SMOTESplitter, self).split(x_data, y_data)
124
            Xt_smote, Yt_smote = SMOTE(**self._smote_params).fit_transform(Xt.as_matrix(), Yt.as_matrix())
            Xt\_smote \;,\;\; Yt\_smote \;=\; UnderSampler(\; ratio = self \;. \_under\_sample) \;. \\ fit\_transform(\; Xt\_smote \;, \;\; Yt\_smote) \;. \\
126
            return Xt_smote, Yt_smote, Xv, Yv
128
   class OverUnderSplitter(TestSplitter):
129
130
       def __init__(self, under_sample=1.0, over_sample=1.0, **kwargs):
132
            super(OverUnderSplitter, self).__init__(**kwargs)
            self._under_sample = under_sample
134
            self._over_sample = over_sample
       def split(self, x_data, y_data):
136
            Xt, Yt, Xv, Yv = super(OverUnderSplitter, self).split(<math>x_data, y_data)
137
            Xt_smote, Yt_smote = OverSampler(ratio=self._over_sample).fit_transform(Xt.as_matrix(), Yt.
138
       as_matrix())
            Xt_smote, Yt_smote = UnderSampler(ratio=self._under_sample).fit_transform(Xt_smote, Yt_smote)
            return Xt_smote, Yt_smote, Xv, Yv
140
```

../src/pipeline.py

# APPENDIX D FINAL PREDICTIONS

This listing shows the final submission CSV file generated from the code in B.

```
test_id , predicted_label , predicted_output
1,1,0.930796334882
2,1,0.568602386556
3,0,0.199756244441
4,0,0.223257609134
5,0,0.108468352895
6,1,0.709492781501
7,1,0.66811145872
```

```
8,1,0.526671436189
  9,1,0.671576496177
  10,0,0.025455110533
  11,1,0.877360128857
  12,1,0.660378904833
  13,0,0.0772411738539
  14,0,0.330609992952
  15,0,0.481235379542
  16,1,0.52081781105
  17,0,0.281606722376
  18,1,0.750899234225
  19,1,0.746028344924
  20,0,0.166716367839
  21,0,0.417874548666
  22,0,0.132900496642
  23,0,0.219897431747
  24,0,0.385683520678
  25,1,0.948763261003
  26,1,0.886118661525
  27.0.0.153187765575
  28,1,0.852164540869
  29,1,0.862054431064
  30,0,0.486335619324
  31,0,0.256972605341
  32,1,0.813361534401
  33,1,0.719935958519
  34,0,0.164955118934
  35,1,0.645222046581
  36,1,0.931596388285
  37,1,0.690185156805
  38,1,0.856189695914
  39,1,0.874164532702
  40,0,0.412985681004
  41,1,0.768172217822
  42,1,0.661658525652
  43,0,0.0842976335621
  44,0,0.455756501102
  45,1,0.628059089869
  46,1,0.882605272545
  47,1,0.854273384453
  48.1.0.727771904074
  49,1,0.635179527198
  50.0.0.123188376206
  51,1,0.782379275211
  52,0,0.0228209667991
  53,1,0.789979159422
  54,1,0.592845245625
  55.0.0.468246812012
  56,0,0.124413267301
  57,1,0.762847930744
  58,1,0.66547093919
  59,0,0.0957612397443
  60,0,0.361182401436
  61,1,0.876937602066
  62,1,0.816143971828
63
  63,0,0.0190173595981
  64,0,0.0792392458244
65
  65,1,0,707652072617
  66,0,0.496436132178
  67,1,0.951665094386
  68,0,0.288903303383
  69,1,0.70995081876
  70.0.0.224498004322
  71,1,0.9183269844
  72,1,0.937519404279
  73,1,0.786448314956
  74,1,0.88587461236
  75.0.0.393104262221
  76,1,0.845700917349
  77,0,0.248636740584
  78.0.0.346568635705
  79,1,0.756725311104
  80,1,0.724599547024
  81,1,0.759772839791
  82,1,0.763201534397
  83,1,0.93771418578
  84,0,0.271315754528
```

```
86 | 85,0,0.0879091265642
87
  86,0,0.475492266561
  87,1,0.773400467965
  88,1,0.741701905905
90 89,0,0.344979199097
  90,1,0.817128811821
  91,0,0.421556736447
92
  92,1,0.920134078405
  93,1,0.945645950574
  94,1,0.691924546397
95
  95,1,0.82519102713
  96,0,0.0390692900319
  97,1,0.702271942814
  98,1,0.919053885818
  99,1,0.81743386827
100
101 100,0,0.199586488799
```

../data/submission.csv