**Introduction**

“Pump it Up: Data Mining the Water Table” is a charity-motivated competition hosted by Driven Data to help classify water wells in Tanzania. Ground data is supplied as a pair of CSV files with 39 feature observations and the corresponding well class: “functional”, “functional needs repair”, and “non functional”. In this report we describe a method for eliminating irrelevant and redundant categorical features, preprocessing steps to help random forests classify data associated with GPS coordinates of the wells, and a parallelization strategy to expedite generation of large random forests.

**Background**

Access to clean drinking water is a critical element of infrastructure for developing third-world countries. Tanzania is no exception, and due to widespread poverty and unsuccessful government programs, access to clean drinking water remains a challenge. To help address this issue, Driven Data is working with the Tanzanian Ministry of Water to host the competition “Pump it Up: Data Mining the Water Table.” The idea is simple: given 39 different feature observations, is it possible to determine the operating status of a well? For this competition the features are a mix of continuous numerical data (e.g. GPS coordinates) and categorical data (e.g. type of water source).

**Approach and Secret Weapons**

Our approach to this process is composed of three components: preprocessing categorical features using the Minimal Redundancy - Maximal Relevance method (mRMR), preprocessing GPS coordinate data, training random forest classifiers in parallel on all preprocessed data.

**Decision Trees**

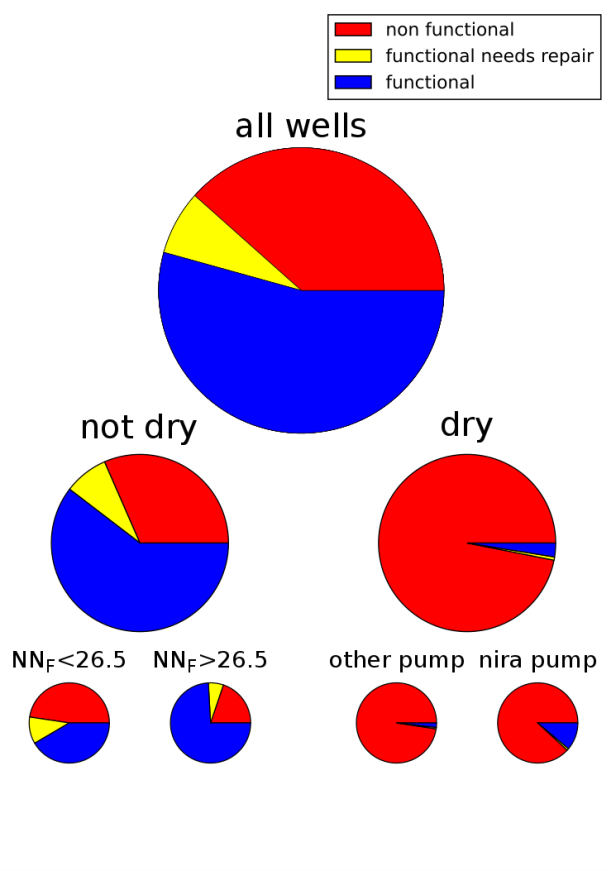
To tackle the classification challenge we decided to use random forests [Breinman reference] as implemented in scikit-learn package for Python. [#FIXME cite sklearn]. Random forest classifiers are ensemble learners composed of many randomized decision trees. Their key advantages for this challenge include unbiased estimates of the generalization error [Breinman reference], near immunity to irrelevant and correlated features, invariance under monotonic feature transformations, and the ability to simultaneously treat numerical and categorical data.

A decision tree classifier uses training data to construct a series of locally-optimal, if-else decision rules to obtain a unique classification of data. For a given set of features with corresponding observations, all possible partitions for each feature are considered. The optimal choice is the one that maximizes the overall class purity of the leaves, leading to (locally) maximum predictive power. An example is shown in Fig. [FIXME]. The first decision selects dry vs. not dry wells, leading to the “not dry” leaf with slightly increased purity, and a “dry” leaf with substantial purity. The next optimal decision for each leaf is different, but in both cases maximize the resulting purity of their children. A decision tree is thus built recursively, in our case until the purity cannot be improved.

Figure [#FIXME]: Recursive splits maximize purity. Red - non

functional. Yellow - functional needs repair. Blue - functional.

NN\_F is the number of functional nearest neighbors.



**Random Forests**

A random forest, using Breinman’s original implementation, introduces randomness among trees via bagging, i.e. constructing each tree on a randomly-sampled subset of the training data, and by restricting each node to split on a random subset of the features. Combining these helps remove the high bias inherent in decision trees, and bagging yields unbiased error estimates by calculating the classification error for each sample using the trees that were not trained on it - this is the out-of-bag (OOB) error. Random forests are generally immune to irrelevant features because their corresponding partitions rarely yield higher-purity splits than relevant features. The partitioning process also yields invariance to any transformation that maintains the strict, weak order of feature observations (e.g. constant scaling). This allows the seamless introduction of one-hot encoded features alongside raw numerical data, and removes any need to scale or shift data.

**Preprocessing Categorical Features**

Our dataset includes 32 categorical features, with 66010 distinct values; moreover, some of the features were apparently redundant. Therefore, we used a systematic multi-step method to choose relevant features and their distinct values.

**Filtration of rare values**: for each feature a list of frequency of distinct values was created, and the values occuring with frequency lower than certain threshold (1%) were replaced with ‘other’ in corresponding data entries.

**Filtration of irrelevant features and values:** Next step was to eliminate the features and distinct values which do not help in classification of the wells. For that, we resorted to theoretical criterion - *mutual information (MI)*. For 2 random variables X and Y with values https://lh5.googleusercontent.com/o91SheIVEHyarpxQFa3tBJOyU31CaN7UJdcFBvTCgFBu1PKPR_YGgEWrNEMJ5JSbMd9o3kqIeuyLMy4tkDNEFQhNgO1f-2auJfivBhQHYM6ehYJDt0eUwWwczw9g2oFrPRynM4c, https://lh3.googleusercontent.com/HUrK0t0GhsOI_or29lrdgss_M3rPTczOYOatDZdwMOqyRyiS8G24lD2wfYtX1PK4zPFxLmf2KsXksYXRivfafaqSwbUW6aOB9d8LIctUnBkH5LUPvh7s84ZzC45mGHfwl0_oetwand dataset of size https://lh4.googleusercontent.com/g7Xzg-S6EAOZFg4OuEAClwnrkB0kaJ8gLr_u9RIycMeEiIMWrFFfDZYwhDu9e_WJ7YUk-dwYCAhAyK5oJ4feEg3GdMJrR0t1dN2N9dfA3vFvSCWBdJXb9vQUnVMAZQPFup3Hx-Aone can define probabilities of outcomes https://lh3.googleusercontent.com/nJO_G7sdlsRiBfOX3ZfxityWShqvKbXeZjLJKB6-rqfMLYrhlrcTnkyZ5NEsaEkQpR4qOx6ta67CjbGBEFTm0QsZbubSVjRcWt4fpD38gp4GDwMy8vnuJanrAHDrfHPRoX44c-kas https://lh6.googleusercontent.com/fxJswvhNTC8cpVxX7_B9aQZOfGjQw4qPTcXCITMWc11mMtdzAZSNzV2VE45z6zrV-QagnErWA8xOvEFktLoAGvAUwddwmM0eD-sEWODYYeEEUQKrTxGujYQUtapaWxRng_bBP6Mand https://lh4.googleusercontent.com/QtW1mx47pgzncNezOmSIL3tRgzys0vT2g7EPme009q5dids2sXlZ8A8wBp_jcgnBkKodXrh4kRq5sZwBpaVmkEmkHWCZgeXfz4Tw_PnbBkrTkiVW03QM-TylhQNNqd_kzaz1D9Eas https://lh5.googleusercontent.com/yL_FeS4v81A5AGaTROWmfwzb28NINweDahHPsKODk6C_M7EsQ9GKeEN_Kd4Ws8gAWBwyeXASnn9-6H_bm3hONvO7rA66CnlpDmZYS6jHO76qtFDe618usJ10QOC7U8jXyDd_ISY, and of simultaneous outcome https://lh3.googleusercontent.com/MM23Q1WU8FUacYl8b1ZFNc9J5iPGO3jHXIeGoKSFAPHSjWehNkAhPo4v_tLm3Be4Y9cH1XCveeKgdBAcIKqpokocRCoaW1ZpMAMDMdIngSn-6I5oYWR_MttcoJ_nPLPqlQTSp0c. With that, MI can be defined as: https://lh4.googleusercontent.com/pbJai8AUYn5rzKXDI4Hph4op93fkbbK8yr3EXgoJtVruSOX67dHRwLVU_sjj_op0RxItCXi4ve7EOPTNnqF-aIHFtxups0mbXhjNTyeTrsje3mHIkTsoUGUrXlmdVTsLeSXfx1U. It is an analogue of correlation for discrete variables, being close to zero for independent features. We used MI between a given feature and the classification labels as a metric for that feature’s importance and a criterion for discarding the irrelevant ones. Namely, we defined a feature as irrelevant if its MI was lower than a certain threshold.

Since our version of random forest implementation required vectorization of categorical features into boolean columns, we had to treat features and distinct values on the same footing.  For that, for each feature we’ve sorted the values from most to least frequent. Then, we’ve computed the contribution to MI with classification labels for each distinct value, with example shown in Fig. X. The values with MI contribution below the given threshold were replaced with ‘other’.

**Minimal redundancy - maximal relevance (mRMR) feature filtration**: After eliminating obviously irrelevant values and features we had to deal with redundancy of almost equally important features (e.g., “quantity” and “quantity\_group”). For that purpose, we found mRMR method being useful. It relies on the concept of “mutual information quotient”, which is a ratio of MI of candidate feature with the classification labels to the average of MI of candidate feature with those already selected <TYPESET FORMULA>. In mRMR method, one starts by picking the feature with largest MI with the classification labels and adding it to the set of selected features S. Then, at each step of the algorithm, features are ranked according to mutual information quotient (MIQ), the feature with the largest MIQ is selected, and the MIQs for remaining features are recomputed (since the set of selected features was expanded). The process goes on until largest MIQ for remaining candidate features goes below certain cutoff value. As the procedure proceeds, the features which are both highly informative from classification standpoint and uncorrelated with features already selected are added to the set S. Eventually, candidate features become more and more correlated with the already chosen ones, and the process stops.

**Feature vectorization:** Finally, for each value in each remaining feature a corresponding column with boolean values showing if entries have this type of value, is added to the data set, and the original features are removed. Another pass of mRMR on the boolean features is made, which in the end leads to about 10 distinct values (out of 66k), which contribute most of the important information for classification.

**Preprocessing GPS Data**

We discovered that the GPS coordinates for wells are strongly clustered by their classification. In particular, functional and non functional wells typically appear in distinct clusters. A naive forest trained on the raw GPS coordinates, making West-East and North-South decisions only, achieves approximately 70% classification accuracy! This motivated us to engineer the GPS data in an effort to optimize the classification accuracy.

In Breinman’s original random forest paper [#FIXME] he suggests adding linear combinations of numerical features when the number of features is small to minimize correlation between trees. A linear combination of GPS coordinates corresponds to a *rotation*, allowing trees to make non-axis-aligned boundaries like Northwest-Southeast. Since random forests are invariant to the order of feature columns and scaling by a constant,,only rotation angles in [0, pi/4] are distinct. Our work uses 5 equally-spaced angles in this range. These angles yield irregular polygons in GPS space.

Finally, we considered the close relationship between forests and k-nearest neighbors (kNN).. Various methods of weighting neighbors by distance are common and are generally rotationally-symmetric. We decided to add kNN-derived data to the forest’s training and testing sets for two reasons. First, these enable nonlinear (in GPS space) and rotationally-symmetric boundaries to used for decisions. Second, partitions on this kind of data are immediately useful to the forest, e.g. wells with many nearby functional neighbors are likely functional as well. This contrasts with the raw GPS data since clusters are separated only at small length scales, requiring much deeper trees. Each tree was trained on the sum of 1/distance, two sigmoidal functions of distance, and the number of neighbors over each class. The effects are immediately obvious - forests with kNN data have higher OOB scores and exhibit more natural, curved decision boundaries between adjacent clusters.

**Performance evaluation**

**Filtration of rare values**: Inside each categorical feature, the values which occur in less than 1% of the total number of data points (59400), were replaced by label ‘other’. With such cutoff of 1%, about 260 distinct values remain. A more strict limit could have been imposed, but we wanted to keep more potentially important features for information-theoretic filtration.

**Discarding irrelevant features and values:** After some testing, for this particular case the optimal threshold was found to be 5% of the maximal MI among the present features, since in our case we did not have features with strongly dominating MI.

**GPS rotation and kNN features:**

Adding several representations of GPS data to the training set proved useful. Table [#FIXME] shows the OOB score (total classification accuracy) for several choices of GPS data to include.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| data | no GPS data | raw GPS only | 5 total rotations | kNN only | 5 rotations & kNN |
| OOB score | 79.25% | 80.87% | 81.18% | 82.53% | 83.04% |

We see that adding rotations yields a mildly-useful 0.3% increase to the OOB accuracy, but much better gains are observed by including kNN-derived data. Using a combination of kNN data and rotations yields the highest OOB accuracy of 83.04%, so preprocessing GPS data yields a +2.2% increase in the classification accuracy.

**Parallelization**

Random forests are embarrassingly parallel because each tree is trained independently. The most straightforward way to implement random forests in parallel is to assign an equal portion of the *n* trees to the *m* cores, so each core calculates *n/m* trees and then send them all back to the root core.

A more sophisticated approach is to use load-balancing through the master-slave approach, in which the *n* trees are divided into more than *m* groups. The master slave assigns work to any free cores until all *n* trees have been calculated, similar to the MapReduce framework. This is important because the trees do not necessarily take the same amount of time to train, and some cores may fail or become slow.

Figure 1 shows the training time as a function of cores. We see that there is an optimum number of cores - 4 cores without load-balancing, and 16 cores with load-balancing. This is likely due to the communication overhead outweighing the benefits of parallelization. Figure 2 shows the broadcast time of the data as a function of cores. As expected, this increases quickly with the number of cores. There is a big jump going from 8 to 16 cores, which may be due to non-local communication.

Figure 2 shows the training time as a function of trees in a single work-unit for the load-balancing training. There also seems to be an optimum point, due to the balance between communication time and training time.

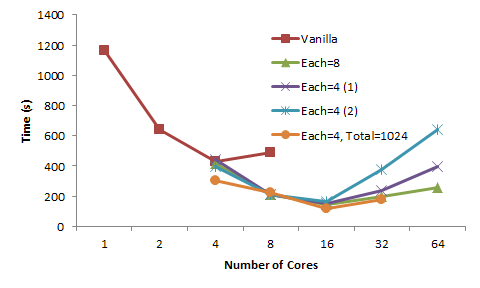


Figure 1: Training time as a function of number of cores, excluding time to broadcast data. Number in parentheses represent the trial. Total number of trees is 2048 unless otherwise specified. Vanilla refers to training without load-balancing.

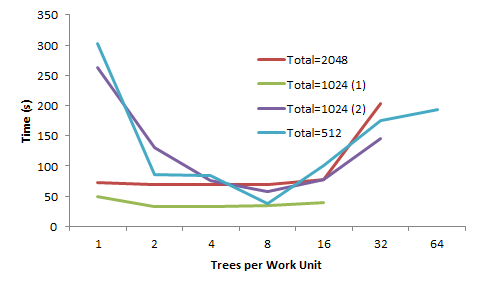


Figure 2: Training time for load-balancing version as a function of number of trees in a single work unit, using 32 cores. Excludes time to broadcast data. Number in parentheses represent the trial.

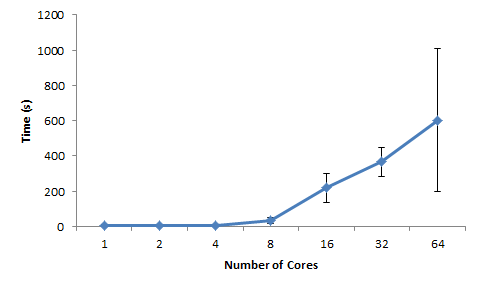


Figure 3: Time to broadcast data as a function of number of cores.

**Performance Evaluation**

* Submit our final work to Driven Data to get a ranking there
* *Discuss OOB accuracy scores? (Driven Data test set might be biased since the OOB scores don’t track particularly well at high-OOB levels)*
* Parallel scaling

**Conclusion**

* Presented a end-to-end system for preprocessing features, handling coordinates, and quickly training large forests
* Discuss how well we did on the project in terms of Driven Data and OOB scores

**References**

[1] Pump it Up: Data Mining the Water Table. Driven Data. <http://www.drivendata.org/competitions/7/>

[2] scikit-learn. <http://scikit-learn.org/stable/>

[3] L. Breinman. “Random Forests”. *Machine Learning*, vol. 45, issue 1, pp. 5-32. 2001.

* MRMR sources
* Breinman’s random forest paper