

## Week 8 questions and answers

### Performing Linear Regressions with Technology

An amateur astronomer is researching statistical properties of known stars using a variety of databases. They collect the absolute magnitude or  $M_V$  and stellar mass or  $M_\odot$  for 30 stars. The absolute magnitude of a star is the intensity of light that would be observed from the star at a distance of 10 parsecs from the star. This is measured in terms of a particular band of the light spectrum, indicated by the subscript letter, which in this case is  $V$  for the visual light spectrum. The scale is logarithmic and an  $M_V$  that is 1 less than another comes from a star that is 10 times more luminous than the other. The stellar mass of a star is how many times the sun's mass it has. The data is provided below. Use Excel to calculate the correlation coefficient  $r$  between the two data sets, rounding to two decimal places.

**Correct! You nailed it.**

$r = -0.93$

### Answer Explanation

The correlation coefficient, rounded to two decimal places, is  $r \approx -0.93$ .

A market researcher looked at the quarterly sales revenue for a large e-commerce store and for a large brick-and-mortar retailer over the same period. The researcher recorded the revenue in millions of dollars for 30 quarters. The data are provided below. Use Excel to calculate the correlation coefficient  $r$  between the two data sets. Round your answer to two decimal places.

**Yes that's right. Keep it up!**

$r = -0.81$

### Answer Explanation

The correlation coefficient, rounded to two decimal places, is  $r \approx -0.81$ .

The table below contains the geographic latitudes,  $X$ , and average January temperatures,  $y$ , of 20 cities. Use Excel to find the best fit linear regression equation. Round the slope and intercept to two decimal places.

x	y
46	
23	
32	
60	
39	
40	
33	
59	
38	
57	
40	
33	
42	
33	
30	
64	
34	
56	

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**Yes that's right. Keep it up!**

$$y = -2.68, \quad x = 147.24$$

Thus, the equation of line of best fit with slope and intercept rounded to two decimal places is  $\hat{y} = -2.68x + 147.24$ .

An organization collects information on the life expectancy (in years) of a person in certain countries and the fertility rate per woman in those countries. The data for 21 randomly selected countries for the year 2011 is given below. Use Excel to find the best fit linear regression equation, where fertility rate is the explanatory variable. Round the slope and intercept to two decimal places.

$y = -4.21, \quad x = 83.68$  **Answer Explanation**  $\hat{y} = -4.21, \quad x = 83.68$ .

An economist is trying to understand whether there is a strong link between CEO pay ratio and corporate revenue. The economist gathered data including the CEO pay ratio and corporate revenue for 30 companies for a particular year. The pay ratio data is reported by the companies and represents the ratio of CEO compensation to the median employee salary. The data are provided below. Use Excel to calculate the correlation coefficient  $r$  between the two data sets. Round your answer to two decimal places.

**Perfect. Your hard work is paying off 😊**

$r = -0.17$

The correlation coefficient, rounded to two decimal places, is  $r \approx -0.17$ .

A researcher is interested in whether the variation in the size of human beings is proportional throughout each part of the human. To partly answer this question they looked at the correlation between the foot length (in millimeters) and height (in centimeters) of 30 randomly selected adult males. The data is provided below. Use Excel to calculate the correlation coefficient  $r$  between the two data sets. Round your answer to two decimal places.

**Great work! That's correct.**

$r = 0.50$

The correlation coefficient, rounded to two decimal places, is  $r \approx 0.50$ .

The table below gives the average weight (in kilograms) of certain people ages 1–20. Use Excel to find the best fit linear regression equation, where age is the explanatory variable. Round the slope and intercept to two decimal places.

**Answer 1:**

**That's not right - let's review the answer.**

$y = 0.35, x28.99$

**Answer 2:**

**Well done! You got it right.**

$y = 2.89$ ,  $x = 4.69$

Thus, the equation of line of best fit with slope and intercept rounded to two decimal places is  $\hat{y} = 2.86x + 4.69$ .

In the following table, the age (in years) of the respondents is given as the  $X$  value, and the earnings (in thousands of dollars) of the respondents are given as the  $Y$  value. Use Excel to find the best fit linear regression equation in thousands of dollars. Round the slope and intercept to three decimal places.

**Yes that's right. Keep it up!**

$y = 0.433$ ,  $x = 24.493$

## Answer Explanation

Thus, the equation of line of best fit with slope and intercept rounded to three decimal places is  $\hat{y} = 0.433x + 24.493$ .

### PREDICITONS USING LINEAR REGRESSION

## Question

The table shows data collected on the relationship between the time spent studying per day and the time spent reading per day. The line of best fit for the data is  $\hat{y} = 0.16x + 36.2$ . Assume the line of best fit is significant and there is a strong linear relationship between the variables.

Studying (Minutes) 507090110 Reading (Minutes) 44485054

(a) According to the line of best fit, what would be the predicted number of minutes spent reading for someone who spent 67 minutes studying? Round your answer to two decimal places.

**Yes that's right. Keep it up!**

The predicted number of minutes spent reading is \$46.92.

## Answer Explanation

The predicted number of minutes spent reading is **1\$\$**.

**Correct answers:**

- 46.92

Substitute **67** for X into the line of best fit to estimate the number of minutes spent reading for someone who spent **67** minutes studying:  $y^=0.16(67)+36.2=46.92$ .

## Question

*The table shows data collected on the relationship between the time spent studying per day and the time spent reading per day. The line of best fit for the data is  $y^=0.16x+36.2$ .*

**Studying (Minutes) 507090110 Reading (Minutes) 44485054**

(a) According to the line of best fit, the predicted number of minutes spent reading for someone who spent **67** minutes studying is **46.92**.

(b) Is it reasonable to use this line of best fit to make the above prediction?

**That's incorrect - mistakes are part of learning. Keep trying!**



The estimate, a predicted time of **46.92** minutes, is both reliable and reasonable.



The estimate, a predicted time of **46.92** minutes, is both unreliable and unreasonable.



The estimate, a predicted time of **46.92** minutes, is reliable but unreasonable.



The estimate, a predicted time of **46.92** minutes, is unreliable but reasonable.

## Answer Explanation

**Correct answer:**

The estimate, a predicted time of **46.92** minutes, is both reliable and reasonable.

The data in the table only includes studying times between **50** and **110** minutes, so the line of best fit gives reliable and reasonable predictions for values of X between **50** and **110**. Since **67** is between these values, the estimate is both reliable and reasonable.

**Your answer:**

The estimate, a predicted time of **46.92** minutes, is unreliable but reasonable.

This estimate is both reliable and reasonable because **67** is inside the range **50** to **110** given in the table.

*Janet is studying the relationship between the average number of minutes spent exercising per day and math test scores and has collected the data shown in the table. The line of best fit for the data is  $\hat{y} = 0.46x + 66.4$ .*

Minutes 15202530 Test Score 73767880

(a) According to the line of best fit, the predicted test score for someone who spent **23** minutes exercising is **76.98**.

(b) Is it reasonable to use this line of best fit to make the above prediction?

**Not quite - review the answer explanation to help get the next one.**



The estimate, a predicted test score of **76.98**, is reliable and reasonable.



The estimate, a predicted test score of **76.98**, is unreliable but reasonable.



The estimate, a predicted test score of **76.98**, is unreliable and unreasonable.



The estimate, a predicted test score of **76.98**, is reliable but unreasonable.

## Answer Explanation

**Correct answer:**

The estimate, a predicted test score of **76.98**, is reliable and reasonable.

The data in the table only includes exercise times between **15** and **30** minutes, so the line of best fit gives reliable and reasonable predictions for values of **X** between **15** and **30**. Since **23** is between these values, the estimate is reasonable.

**Your answer:**

The estimate, a predicted test score of **76.98**, is unreliable and unreasonable.

This estimate is reliable, because **23** is inside the range **15** to **30** given in the table. And, it is a realistic score, so it is reasonable.

### Nomenclature

- When using regression lines to make predictions, if the **X**-value is **within the range** of observed **X**-values, one can conclude the prediction is both reliable and reasonable. That is, the prediction is accurate and possible. For example, if a prediction were made using **x=1995** in the video above, one could conclude the predicted **y**-value is both reliable (quite accurate) and reasonable (possible). This is an example of **interpolation**.
- When using regression lines to make predictions, if the **X**-value is **outside the range** of observed **X**-values, one cannot conclude the prediction is both reliable and reasonable. That is, the prediction will be much less accurate and the prediction may, or may not, be possible. For example, **X=2020** is not within the range of 1950 to 2000. Therefore, the prediction is much less reliable (not as accurate) even though it is reasonable (it is possible that a person will live to be 79.72 years old). This is an example of **extrapolation**.

## Reasonable Predictions

Note that not all predictions are reasonable using a line of best fit. Typically, it is considered reasonable to make predictions for **X**-values which are between the smallest and largest observed **X**-values. These are known as interpolated values. Typically, it is

considered unreasonable to make predictions for  $X$ -values which are not between the smallest and largest observed  $X$ -values. These are known as extrapolated values.

A scatterplot has a horizontal axis labeled  $x$  from 0 to 20 in increments of 1 and a vertical axis labeled  $y$  from 0 to 28 in increments of 2. 15 plotted points strictly follow the pattern of a line that rises from left to right and passes through the points  $(6, 10)$ ,  $(8, 13)$ , and  $(14, 2)$ . There are other plotted points at  $(10, 15)$  and  $(13, 19)$ . The regions between the horizontal axis points from 1 to 6 and 14 to 20 are shaded as unreasonable. The region between the horizontal axis points from 6 to 14 is shaded as reasonable. All coordinates are approximate

In the figure above, we see that the observed values have  $X$ -values ranging from **6 to 14**. So it would be reasonable to use the line of best fit to make a prediction for the  $X$  value of **9** (because it is between **6** and **14**), but it would be unreasonable to make a prediction for the  $X$ -value of **20** (because that is outside of the range).

## Nomenclature

- When using regression lines to make predictions, if the  $X$ -value is **within the range** of observed  $X$ -values, one can conclude the prediction is both reliable and reasonable. That is, the prediction is accurate and possible. For example, if a prediction were made using  $x=1995$  in the video above, one could conclude the predicted  $Y$ -value is both reliable (quite accurate) and reasonable (possible). This is an example of **interpolation**.
- When using regression lines to make predictions, if the  $X$ -value is **outside the range** of observed  $X$ -values, one cannot conclude the prediction is both reliable and reasonable. That is, the prediction will be much less accurate and the prediction may, or may not, be possible. For example,  $X=2020$  is not within the range of 1950 to 2000. Therefore, the prediction is much less reliable (not as accurate) even though it is reasonable (it is possible that a person will live to be 79.72 years old). This is an example of **extrapolation**.

# Reasonable Predictions

Note that not all predictions are reasonable using a line of best fit. Typically, it is considered reasonable to make predictions for **X**-values which are between the smallest and largest observed **X**-values. These are known as interpolated values. Typically, it is considered unreasonable to make predictions for **X**-values which are not between the smallest and largest observed **X**-values. These are known as extrapolated values.

A scatterplot has a horizontal axis labeled **x** from 0 to 20 in increments of 1 and a vertical axis labeled **y** from 0 to 28 in increments of 2. 15 plotted points strictly follow the pattern of a line that rises from left to right and passes through the points left-parenthesis 6 comma 10 right-parentheses, left-parenthesis 8 comma 13 right-parenthesis, and left-parenthesis 14 comma 2 right-parentheses. There are other plotted points at left-parenthesis 10 comma 15 right-parenthesis and left-parenthesis 13 comma 19 right-parenthesis. The regions between the horizontal axis points from 1 to 6 and 14 to 20 are shaded as unreasonable. The region between the horizontal axis points from 6 to 14 is shaded as reasonable. All coordinates are approximate

In the figure above, we see that the observed values have **X**-values ranging from **6** to **14**. So it would be reasonable to use the line of best fit to make a prediction for the **X** value of **9** (because it is between **6** and **14**), but it would be unreasonable to make a prediction for the **X**-value of **20** (because that is outside of the range).

## Question

Erin is studying the relationship between the average number of minutes spent reading per day and math test scores and has collected the data shown in the table. The line of best fit for the data is  $y^=0.8x+51.2$ . According to the line of best fit, what would be the predicted test score for someone who spent **70** minutes reading? Is it reasonable to use this line of best fit to make this prediction?

Minutes 30 35 40 45 50 Test Score 75 78 85 88 90

**That's not right - let's review the answer.**



The predicted test score is **95.2**, and the estimate is not reasonable.



The predicted test score is **95.2**, and the estimate is reasonable.



The predicted test score is **107.2**, and the estimate is not reasonable.



The predicted test score is **107.2**, and the estimate is reasonable.

## Answer Explanation

### Correct answer:

The predicted test score is **107.2**, and the estimate is not reasonable.

Substitute **70** for **X** in the line of best fit to estimate the test score for someone who spent **70** minutes reading:  $y^=0.8(70)+51.2=107.2$ . The data in the table only includes reading times between **30** and **50** minutes, so the line of best fit only gives reasonable predictions for values of **X** between **30** and **50**. Since **70** is far outside of this range of values, the estimate is not reasonable.

Another thing to notice is that it predicts a test score of greater than **100**, which is typically impossible.

### Your answer:

The predicted test score is **107.2**, and the estimate is reasonable.

The predicted value is not reasonable because the value of **70** minutes is not between **30** and **50** minutes.

## Question

Data is collected on the relationship between the average number of minutes spent exercising per day and math test scores. The data is shown in the table and the line of best fit for the data is  $y^=0.42x+64.6$ . Assume the line of best fit is significant and there is a strong linear relationship between the variables.

Minutes 25 30 35 40 Test Score 75 77 80 81

(a) According to the line of best fit, what would be the predicted test score for someone who spent **38** minutes exercising? Round your answer to two decimal places.

**Well done! You got it right.**

The predicted test score is **80.56**.

## Answer Explanation

The predicted test score is **80.56**.

**Correct answers:**

- **80.56**

Substitute **38** for **X** into the line of best fit to estimate the test score for someone who spent **38** minutes exercising:  $y^=0.42(38)+64.6=80.56$ .

## Question

*Data is collected on the relationship between the average number of minutes spent exercising per day and math test scores. The data is shown in the table and the line of best fit for the data is  $y^=0.42x+64.6$ .*

Minutes 25303540 Test Score 75778081

(a) According to the line of best fit, the predicted test score for someone who spent **38** minutes exercising is **80.56**.

(b) Is it reasonable to use this line of best fit to make the above prediction?

**Perfect. Your hard work is paying off 😊**



The estimate, a predicted test score of **80.56**, is both reliable and reasonable.



The estimate, a predicted test score of **80.56**, is reliable but unreasonable.



The estimate, a predicted test score of **80.56**, is both unreliable and unreasonable.



The estimate, a predicted test score of **80.56**, is unreliable but reasonable.

## Answer Explanation

**Correct answer:**

The estimate, a predicted test score of **80.56**, is both reliable and reasonable.

The data in the table only includes exercise times between **25** and **40** minutes, so the line of best fit gives reasonable predictions for values of **X** between **25** and **40**.

Since **38** is between these values, the estimate is both reliable and reasonable.

## Question

Data is collected on the relationship between the average daily temperature and time spent watching television. The data is shown in the table and the line of best fit for the data is  $y^{\wedge} = -0.81x + 96.7$ . Assume the line of best fit is significant and there is a strong linear relationship between the variables.

**Temperature (Degrees)** 30 40 50 60  
**Minutes Watching Television** 73 63 57 48

(a) According to the line of best fit, what would be the predicted number of minutes spent watching television for an average daily temperature of **45** degrees? Round your answer to two decimal places.

**Answer 1:**

That's not right - let's review the answer.

The predicted number of minutes spent watching television is **133.15**.

**Answer 2:**

**Keep trying - mistakes can help us grow.**

The predicted number of minutes spent watching television is \$133.15.

## Answer Explanation

The predicted number of minutes spent watching television is **1\$\$.**

**Correct answers:**

- **1\$60.25\$60.25**

Substitute **45** for **X** into the line of best fit to estimate the number of minutes spent watching television for an average daily temperature of **45** degrees:  $y^{\wedge} = -0.81(45) + 96.7 = 60.25$ .

## Question

*Data is collected on the relationship between the average daily temperature and time spent watching television. The data is shown in the table and the line of best fit for the data is  $y^{\wedge} = -0.81x + 96.7$ .*

Temperature (Degrees) 30405060 Minutes Watching Television 73635748

(a) According to the line of best fit, the predicted number of minutes spent watching television for an average daily temperature of **45** degrees is **60.25**.

(b) Is it reasonable to use this line of best fit to make the above prediction?

**Correct! You nailed it.**



The estimate, a predicted time of **60.25** minutes, is unreliable but reasonable.



The estimate, a predicted time of **60.25** minutes, is both reliable and reasonable.



The estimate, a predicted time of 60.25 minutes, is both unreliable and unreasonable.



The estimate, a predicted time of 60.25 minutes, is reliable but unreasonable.

## Answer Explanation

### Correct answer:

The estimate, a predicted time of 60.25 minutes, is both reliable and reasonable.

The data in the table only includes temperatures between 30 and 60 degrees, so the line of best fit only gives reliable and reasonable predictions for values of X between 30 and 60. Since 45 is between these values, the estimate is both reliable and reasonable.

## Question

Homer is studying the relationship between the average daily temperature and time spent watching television and has collected the data shown in the table. The line of best fit for the data is  $\hat{y} = -0.6x + 94.5$ . Assume the line of best fit is significant and there is a strong linear relationship between the variables.

Temperature (Degrees)	Minutes Watching Television
40	50
50	60
60	70
70	65
55	59
52	52

(a) According to the line of best fit, what would be the predicted number of minutes spent watching television for an average daily temperature of 39 degrees? Round your answer to two decimal places, as needed.

Yes that's right. Keep it up!

The predicted number of minutes spent watching television is \$71.1.

## Answer Explanation

The predicted number of minutes spent watching television is 71.1.

### Correct answers:

- \$71.1

Substitute 39 for X into the line of best fit to estimate the number of minutes spent watching television for an average daily temperature of 39 degrees:  $y^{\wedge} = -0.6(39) + 94.5 = 71.1$ .

## Question

Homer is studying the relationship between the average daily temperature and time spent watching television and has collected the data shown in the table. The line of best fit for the data is  $y^{\wedge} = -0.6x + 94.5$ .

Temperature (Degrees)	Minutes Watching Television
40	50
56	60
70	70
55	59
52	52

(a) According to the line of best fit, the predicted number of minutes spent watching television for an average daily temperature of 39 degrees is 71.1.

(b) Is it reasonable to use this line of best fit to make the above prediction?

**Not quite - review the answer explanation to help get the next one.**



The estimate, a predicted time of 71.1 minutes, is both unreliable and unreasonable.



The estimate, a predicted time of 71.1 minutes, is both reliable and reasonable.



The estimate, a predicted time of 71.1 minutes, is unreliable but reasonable.



The estimate, a predicted time of 71.1 minutes, is reliable but unreasonable.

## Answer Explanation

**Correct answer:**

The estimate, a predicted time of 71.1 minutes, is unreliable but reasonable.

The data in the table only includes temperatures between 40 and 70 degrees, so the line of best fit gives reliable and reasonable predictions for values of X between 40 and 70. Since 39 is not between these values, the estimate is not reliable. However, 71.1 minutes is a reasonable time.

**Your answer:**

The estimate, a predicted time of 71.1 minutes, is both reliable and reasonable.

This estimate is not reliable, because 39 is outside of the range 40 to 70 given in the table.

## Question

Daniel owns a business consulting service. For each consultation, he charges \$95 plus \$70 per hour of work. A linear equation that expresses the total amount of money Daniel earns per consultation is  $y=70x+95$ . What are the independent and dependent variables? What is the y-intercept and the slope?

**Keep trying - mistakes can help us grow.**



The independent variable ( $x$ ) is the amount, in dollars, Daniel earns for a consultation. The dependent variable ( $y$ ) is the amount of time Daniel consults.

Daniel charges a one-time fee of \$95 (this is when  $x=0$ ), so the y-intercept is 95. Daniel earns \$70 for each hour he works, so the slope is 70.



The independent variable ( $x$ ) is the amount of time Daniel consults. The dependent variable ( $y$ ) is the amount, in dollars, Daniel earns for a consultation.

Daniel charges a one-time fee of \$95 (this is when  $x=0$ ), so the y-intercept is 95. Daniel earns \$70 for each hour he works, so the slope is 70.



The independent variable ( $x$ ) is the amount, in dollars, Daniel earns for a consultation. The dependent variable ( $y$ ) is the amount of time Daniel consults.

Daniel charges a one-time fee of \$70 (this is when  $x=0$ ), so the y-intercept is 70. Daniel earns \$95 for each hour he works, so the slope is 95.



The independent variable ( $x$ ) is the amount of time Daniel consults. The dependent variable ( $y$ ) is the amount, in dollars, Daniel earns for a consultation.

Daniel charges a one-time fee of **\$70** (this is when  $x=0$ ), so the  $y$ -intercept is **70**. Daniel earns **\$95** for each hour he works, so the slope is **95**.

## Answer Explanation

### Correct answer:

The independent variable ( $X$ ) is the amount of time Daniel consults. The dependent variable ( $y$ ) is the amount, in dollars, Daniel earns for a consultation.

Daniel charges a one-time fee of **\$95** (this is when  $x=0$ ), so the  $y$ -intercept is **95**. Daniel earns **\$70** for each hour he works, so the slope is **70**.

The independent variable ( $X$ ) is the amount of time Daniel consults because it is the value that changes. He may work different amounts per consultation, and his earnings are dependent on how many hours he works. This is why the amount, in dollars, Daniel earns for a consultation is the dependent variable ( $y$ ).

The  $y$ -intercept is **95** ( $b=95$ ). This is his one-time fee. The slope is **70** ( $a=70$ ). This is the increase for each hour he works.

### Your answer:

The independent variable ( $X$ ) is the amount of time Daniel consults. The dependent variable ( $y$ ) is the amount, in dollars, Daniel earns for a consultation.

Daniel charges a one-time fee of **\$70** (this is when  $x=0$ ), so the  $y$ -intercept is **70**. Daniel earns **\$95** for each hour he works, so the slope is **95**.

## Question

Given the following line, find the value of  $y$  when  $x=2$ .

$$y = -4x - 12$$

**Well done! You got it right.**

$$\$y = -20$$

## Answer Explanation

### Correct answers:

- $y = -20$

Substituting  $x = 2$  in the equation, and simplifying to find  $y$ , we find

$$y = -4x - 12 = -4(2) - 12 = -8 - 12 = -20$$

## Question

Evaluate the linear equation,  $y = 4x - 7$ , at the value  $x = 2$ .

**Yes that's right. Keep it up!**

$\$y = 1$

## Answer Explanation

### Correct answers:

- $y = 1$

To evaluate a linear equation at a specific value, substitute the value  $x = 2$  into the equation for the variable,  $X$ .

$$y = 4x - 7 = 4(2) - 7 = 8 - 7 = 1$$

## Question

Evan owns a house cleaning service. For each house visit, he charges \$55 plus \$30 per hour of work. A linear equation that expresses the total amount of money Evan earns per visit is  $y = 55 + 30x$ .

What are the independent and dependent variables? What is the  $y$ -intercept and the slope?

**Perfect. Your hard work is paying off 😊**



The independent variable ( $x$ ) is the amount, in dollars, Evan earns for each session. The dependent variable ( $y$ ) is the amount of time Evan works each house visit.

At the start of the repairs, Evan charges a one-time fee of \$55 (this is when  $x=0$ ), so the  $y$ -intercept is 55. Evan earns \$30 for each hour he works, so the slope is 30.



The independent variable ( $x$ ) is the amount of time Evan works each house visit. The dependent variable ( $y$ ) is the amount, in dollars, Evan earns for each session.

At the start of the repairs, Evan charges a one-time fee of \$55 (this is when  $x=0$ ), so the  $y$ -intercept is 55. Evan earns \$30 for each hour he works, so the slope is 30.



The independent variable ( $x$ ) is the amount, in dollars, Evan earns for each session. The dependent variable ( $y$ ) is the amount of time Evan works each house visit.

At the start of the repairs, Evan charges a one-time fee of \$30 (this is when  $x=0$ ), so the  $y$ -intercept is 30. Evan earns \$55 for each hour he works, so the slope is 55.



The independent variable ( $x$ ) is the amount of time Evan works each house visit. The dependent variable ( $y$ ) is the amount, in dollars, Evan earns for each session.

At the start of the repairs, Evan charges a one-time fee of \$30 (this is when  $x=0$ ), so the  $y$ -intercept is 30. Evan earns \$55 for each hour he works, so the slope is 55.

## Answer Explanation

### Correct answer:

The independent variable ( $X$ ) is the amount of time Evan works each house visit. The dependent variable ( $y$ ) is the amount, in dollars, Evan earns for each session.

At the start of the repairs, Evan charges a one-time fee of \$55 (this is when  $x=0$ ), so the  $y$ -intercept is 55. Evan earns \$30 for each hour he works, so the slope is 30.

The independent variable ( $X$ ) is the amount of time Evan works each house visit because it is the value that changes. He may work different amounts per day, and his earnings are dependent on how many hours he works. This is why the amount, in dollars Evan earns for each session is the dependent variable ( $y$ ).

The  $y$ -intercept is 55 ( $b=55$ ). This is his one-time fee. The slope is 30 ( $a=30$ ).  
This is the increase for each hour he works

## Question

Using a calculator or statistical software, find the linear regression line for the data in the table below.

Enter your answer in the form  $y=mx+b$ , with  $m$  and  $b$  both rounded to two decimal places.

x
y
0
2.12
1
2.19
2
1.92
3
2.79
4
3.81
5
4.72

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### Answer 1:

Keep trying - mistakes can help us grow.

$$y=0.53x+1.58$$

### Answer 2:

Keep trying - mistakes can help us grow.

$$y=0.53x+1.59$$

## Answer Explanation

### Correct answers:

- $y=0.54x+1.59$

If you use a TI-83 or TI-84 calculator, you press STAT, and then ENTER, which brings you to the edit menu where you can enter values. In the L1 list, you enter the values of X from the table above, 0,1,2,3,4,5. Then, in the L2 list, you enter the values of y from the table above, 2.12,2.19,1.92,2.79,3.81,4.72.

Now, press STAT again, and arrow to the right, to CALC. Arrow down to the LinReg

option and press ENTER. The resulting  $a$  and  $b$  are the slope  $m$  and  $y$ -intercept  $b$  of the linear regression line. You should find that  $m \approx 0.54$  and  $b \approx 1.59$ . So the final answer is

$$y = 0.54x + 1.59$$

Using spreadsheet software or other statistical software should give you the same result.

## Question

Using a calculator or statistical software, find the linear regression line for the data in the table below.

Enter your answer in the form  $y = mx + b$ , with  $m$  and  $b$  both rounded to two decimal places.

x
y
0
2.83
1
3.33
2
6.99
3
8.01
4
7.62
5
7.66

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Perfect. Your hard work is paying off 😊

$$\$ \$ y = 1.09x + 3.36$$

## Answer Explanation

**Correct answers:**

- $\$ y = 1.09x + 3.36 \$$

If you use a TI-83 or TI-84 calculator, you press STAT, and then ENTER, which brings you to the edit menu where you can enter values. In the L1 list, you enter the values of X from the table above, 0,1,2,3,4,5. Then, in the L2 list, you enter the values of y from the table above, 2.83,3.33,6.99,8.01,7.62,7.66.

Now, press STAT again, and arrow to the right, to CALC. Arrow down to the LinReg option and press ENTER. The resulting **a** and **b** are the slope **m** and y-intercept **b** of the linear regression line. You should find that  $m \approx 1.09$  and  $b \approx 3.36$ . So the final answer is

$$y = 1.09x + 3.36$$

Using spreadsheet software or other statistical software should give you the same result.

## Question

A least squares regression line (best-fit line) has the equation,  $y^{\wedge} = 2.87x - 43.5$ . What is the **slope** of this linear regression equation?

**Great work! That's correct.**



The **slope** of the line is **2.87**, which tells us that the dependent variable (**y**) decreases **2.87** for every one unit increase in the independent (**x**) variable, on average.



The **slope** of the line is **2.87**, which tells us that the dependent variable (**y**) increases **2.87** for every one unit increase in the independent (**x**) variable, on average.



The **slope** of the line is **-43.5**, which tells us that the dependent variable (**y**) increases **43.5** for every one unit increase in the independent (**x**) variable, on average.



The **slope** of the line is **-43.5**, which tells us that the dependent variable (**y**) decreases **43.5** for every one unit increase in the independent (**x**) variable, on average.

## Answer Explanation

**Correct answer:**

The **slope** of the line is **2.87**, which tells us that the dependent variable (y) increases **2.87** for every one unit increase in the independent (X) variable, on average.

## Question

Researchers want to find the relationship between age and average weight in female children. Using a calculator or statistical software, find the linear regression line for the 2012 CDC data below for average weights of female children by age.

age (years)	weight (lbs)
1	24.1
2	29.5
3	34.5
4	39.1
5	46.6
6	51.9
7	59.1

**Well done! You got it right.**



$$y=5.78x+17.56$$



$$y=1.0x+15.69$$



$$y=-5.78x+14.32$$



$$y=1.0x+15.55$$

## Answer Explanation

Correct answer:

$$y=5.78x+17.56$$

If you use a TI-83 or TI-84 calculator, you press STAT, and then ENTER, which brings you to the edit menu where you can enter values. In the L1 list, you enter the values of X from the table above, 1,2,3,4,5,6,7. Then, in the L2 list, you enter the values of Y from the table above.

Now, press STAT again, and arrow to the right, to CALC. Arrow down to the LinReg option and press ENTER. The resulting  $a$  and  $b$  are the slope  $a$  and  $y$ -intercept  $b$  of the linear regression line. You should find that  $a \approx 5.78$  and  $b \approx 17.56$ . So the final answer is

$$y=5.78x+17.56$$

Using spreadsheet software or other statistical software should give you the same result.

## Question

Given that  $n=31$  data points are collected when studying the relationship between average daily temperature and time spent sleeping, use the critical values table below to determine if a calculated value of  $r=-0.324$  is significant or not.

df	CV (+ and -)						
1	0.997	1	0.555	2	0.413	40	0.304
2	0.950	1	0.532	2	0.404	50	0.273
3	0.878	1	0.514	2	0.396	60	0.250
4	0.811	1	0.497	2	0.388	70	0.232

5	0.754	$\frac{1}{5}$	0.482	$\frac{2}{5}$	0.381	80	0.217
6	0.707	$\frac{1}{6}$	0.468	$\frac{2}{6}$	0.374	90	0.205
7	0.666	$\frac{1}{7}$	0.456	$\frac{2}{7}$	0.367	$\frac{10}{0}$	0.195
8	0.632	$\frac{1}{8}$	0.444	$\frac{2}{8}$	0.361		
9	0.602	$\frac{1}{9}$	0.433	$\frac{2}{9}$	0.355		
10	0.576	$\frac{2}{0}$	0.423	$\frac{3}{0}$	0.349		

Not quite - review the answer explanation to help get the next one.



r is significant because it is between the positive and negative critical values.



**r is not significant because it is between the positive and negative critical values.**



r is significant because it is not between the positive and negative critical values.



r is not significant because it is not between the positive and negative critical values.

## Answer Explanation

**Correct answer:**

r is not significant because it is between the positive and negative critical values.

There are  $n-2=31-2=29$  degrees of freedom. Looking at the table of critical values, the critical values corresponding to  $df=29$  are  $-0.355$  and  $0.355$ . Since the value of r is between  $-0.355$  and  $0.355$ , r is not significant.

**Your answer:**

r is not significant because it is not between the positive and negative critical values.

$r=-0.324$  is between the critical values  $-0.355 < -0.324 < 0.355$ .

Therefore, r is between the critical values.

## Question

In studying the relationship between age and eating fast food, suppose you computed  $r=0.133$  using  $n=19$  data points. Using the critical values table below, determine if the value of  $r$  is significant or not.

df	CV (+ and -)						
1	0.997	1	0.555	2	0.413	40	0.304
2	0.950	2	0.532	2	0.404	50	0.273
3	0.878	3	0.514	3	0.396	60	0.250
4	0.811	4	0.497	4	0.388	70	0.232
5	0.754	5	0.482	5	0.381	80	0.217
6	0.707	6	0.468	6	0.374	90	0.205
7	0.666	7	0.456	7	0.367	10	0.195
8	0.632	8	0.444	8	0.361		
9	0.602	9	0.433	9	0.355		
10	0.576	20	0.423	30	0.349		

Great work! That's correct.



$r$  is significant because it is between the positive and negative critical values.



$r$  is not significant because it is between the positive and negative critical values.



$r$  is significant because it is not between the positive and negative critical values.



$r$  is not significant because it is not between the positive and negative critical values.

## Answer Explanation

**Correct answer:**

$r$  is not significant because it is between the positive and negative critical values.

There are  $n-2=19-2=17$  degrees of freedom. Looking at the table of critical values, the critical values corresponding to  $df=17$  are  $-0.456$  and  $0.456$ . Since the value of  $r$  is between  $-0.456$  and  $0.456$ ,  $r$  is not significant.

## Question

Data is collected on the relationship between the time spent doing homework per day and the time spent taking notes per day. The data is shown in the table and the line of best fit for the data is  $y^=0.175x+31.0$ . Assume the line of best fit is significant and there is a strong linear relationship between the variables.

Doing Homework (Minutes)	Taking Notes (Minutes)
80	45
100	49
120	51
140	56

- (a) According to the line of best fit, what would be the predicted number of minutes spent taking notes for someone who spent 137 minutes doing homework? Round your answer to two decimal places, as needed.

**Perfect. Your hard work is paying off 😊**

The estimate, a predicted time of **54.98 minutes**, is both reliable and reasonable.

Substitute 137 for X into the line of best fit to estimate the number of minutes spent taking notes for someone who spent 137 minutes doing homework  $y^=0.175 * 137 + 31.0 \approx 54.98$ .

## Question

Michelle is studying the relationship between the hours worked (per week) and time spent reading (per day) and has collected the data shown in the table. The line of best fit for the data is  $y^{\wedge} = -0.79x + 98.8$ . Assume the line of best fit is significant and there is a strong linear relationship between the variables.

Hours Worked (per week) 30405060 Minutes Reading (per day)  
y) 75685852

- (a) According to the line of best fit, what would be the predicted number of minutes spent reading for a person who works 27 hours (per week)? Round your answer to two decimal places, as needed.

**Well done! You got it right.**

The predicted number of minutes spent reading is 77.47.

## Answer Explanation

The predicted number of minutes spent reading is 1\$\$.

Substitute 27 for X into the line of best fit to estimate the number of minutes spent reading for a person who works 27 hours (per week):  $y^{\wedge} = -0.79(27) + 98.8 = 77.47$ .

## Question

*Michelle is studying the relationship between the hours worked (per week) and time spent reading (per day) and has collected the data shown in the table. The line of best fit for the data is  $y^{\wedge} = -0.79x + 98.8$ .*

Hours Worked (per week) 30405060 Minutes Reading (per day)  
y) 75685852

- (a) According to the line of best fit, the predicted number of minutes spent reading for a person who works 27 hours (per week) is 77.47.

(b) Is it reasonable to use this line of best fit to make the above prediction?

**Not quite - review the answer explanation to help get the next one.**



The estimate, a predicted time of **77.47** minutes, is unreliable but reasonable.



The estimate, a predicted time of **77.47** minutes, is reliable but unreasonable.



The estimate, a predicted time of **77.47** minutes, is both unreliable and unreasonable.



The estimate, a predicted time of **77.47** minutes, is both reliable and reasonable.

## Answer Explanation

**Correct answer:**

The estimate, a predicted time of **77.47** minutes, is unreliable but reasonable.

The data in the table only includes the time worked between **30** and **60** hours, so the line of best fit gives reliable and reasonable predictions for values of X between **30** and **60**. Since **27** is not between these values, the estimate is not reliable. However, **77.47** minutes is a reasonable time.

**Your answer:**

The estimate, a predicted time of **77.47** minutes, is reliable but unreasonable.

This estimate is not reliable, because **27** is outside of the range **30** to **60** given in the table. And, it is a realistic time, so it is reasonable.

## Question

The table shows data collected on the relationship between time spent playing video games and time spent with family. The line of best fit for the data is  $\hat{y} = -0.24x + 71.7$ . Assume the line of best fit is significant and there is a strong linear relationship between the variables.

Video Games (Minutes) 45 60 75 90  
Time with Family (Minutes)  
61 57 54 50

(a) According to the line of best fit, what would be the predicted number of minutes spent with family for someone who spent 87 minutes playing video games? Round your answer to two decimal places.

**Answer 1:**

That's not right - let's review the answer.

The predicted number of minutes spent with family is \$92.58.

**Answer 2:**

Great work! That's correct.

The predicted number of minutes spent with family is 50.82.

## Answer Explanation

Substitute 87 for X into the line of best fit to estimate the number of minutes spent with family for someone who spent 87 minutes playing video games:  $\hat{y} = -0.24(87) + 71.7 = 50.82$ .

## Question

*The table shows data collected on the relationship between time spent playing video games and time spent with family. The line of best fit for the data is  $\hat{y} = -0.24x + 71.7$ .*

Video Games (Minutes)	Time with Family (Minutes)
45	59
61	75
57	45

(a) According to the line of best fit, the predicted number of minutes spent with family for someone who spent 87 minutes playing video games is 50.82.

(b) Is it reasonable to use this line of best fit to make the above prediction?

**Great work! That's correct.**



The estimate, a predicted time of **50.82** minutes, is unreliable but reasonable.



The estimate, a predicted time of **50.82** minutes, is reliable but unreasonable.



The estimate, a predicted time of **50.82** minutes, is both reliable and reasonable.



The estimate, a predicted time of **50.82** minutes, is both unreliable and unreasonable.

## **Answer Explanation**

**Correct answer:**

The estimate, a predicted time of **50.82** minutes, is both reliable and reasonable.

The data in the table only includes video game times between **45** and **90** minutes, so the line of best fit gives reliable and reasonable predictions for values of **X** between **45** and **90**. Since **87** is between these values, the estimate is both reliable and reasonable.

## **Coefficient of Determination**

A medical experiment on tumor growth gives the following data table.

x	y
57	38
61	50
63	76
68	97
72	113

The least squares regression line was found. Using technology, it was determined that the total sum of squares (**SST**) was **3922.8** and the sum of squares of regression (**SSR**) was **3789.0**. Calculate **R<sub>2</sub>**, rounded to three decimal places.

**Great work! That's correct.**

0.966

## Answer Explanation

**Correct answers:**

- \$0.966\$0.966

$$R^2 = \frac{SSR}{SST}$$

$$R^2 = \frac{3789.039}{22.8}$$

$$R^2 = 0.966$$

A scientific study on mesothelioma caused by asbestos gives the following data table.

Micrograms of asbestos inhaled	Area of scar tissue (cm <sup>2</sup> )
58	162
62	189
63	188
67	215
70	184

Using technology, it was determined that the total sum of squares (**SST**) was **1421.2** and the sum of squares due to error (**SSE**) was **903.51**. Calculate **R<sup>2</sup>** and determine its meaning. Round your answer to four decimal places.

**Correct! You nailed it.**



**R<sup>2</sup>=0.3643**

Therefore, **36.43%** of the variation in the observed **y**-values can be explained by the estimated regression equation.



$R^2=0.3643$

Therefore, 0.3643% of the variation in the observed  $y$ -values can be explained by the estimated regression equation.



$R^2=0.6357$

Therefore, 63.57% of the variation in the observed  $y$ -values can be explained by the estimated regression equation.



$R^2=0.6357$

Therefore, 0.6357% of the variation in observed  $y$ -values can be explained by the estimated regression equation.

## Answer Explanation

**Correct answer:**

$R^2=0.3643$

Therefore, 36.43% of the variation in the observed  $y$ -values can be explained by the estimated regression equation.

$$R^2 = 1 - \frac{SSE}{SST}$$

$$R^2 = 1 - \frac{903.51}{1421.2}$$

$$R^2 = 1 - 0.6357$$

$$R^2 = 0.3643$$

$$R^2 = 36.43\%$$

A scientific study on speed limits gives the following data table.

**Average speed limit    Average annual fatalities**

25	16
27	29
29	38
32	71
35	93

Using technology, it was determined that the total sum of squares (**SST**) was **4029.2**, the sum of squares regression (**SSR**) was **3968.4**, and the sum of squares due to error (**SSE**) was **60.835**. Calculate **R<sub>2</sub>** and determine its meaning. Round your answer to four decimal places.

**Perfect. Your hard work is paying off 😊**



$$R_2=0.0153$$

Therefore, **1.53%** of the variation in the observed **y**-values can be explained by the estimated regression equation.



$$R_2=0.9849$$

Therefore, **98.49%** of the variation in the observed **y**-values can be explained by the estimated regression equation.



$$R_2=0.0151$$

Therefore, **1.51%** of the variation in the observed **y**-values can be explained by the estimated regression equation.



$$R_2=1.0153$$

Therefore, **10.153%** of the variation in the observed **y**-values can be explained by the estimated regression equation.

## Answer Explanation

**Correct answer:**

$$R_2=0.9849$$

Therefore, **98.49%** of the variation in the observed **y**-values can be explained by the estimated regression equation.

$$R_2 = \frac{SSR}{SST}$$

$$R_2 = \frac{3968.4}{4029.2} = 0.9849$$

$$R_2=0.9849$$

$$R^2=98.49\%$$

## Question

A scientific study on calorie intake gives the following data table.

Calorie intake (1000)	Hours of exercise need to maintain weight
6	13
7	12
10	17
14	15
17	23

Using technology, it was determined that the total sum of squares (**SST**) was **76**, the sum of squares regression (**SSR**) was **54.850**, and the sum of squares due to error (**SSE**) was **21.150**. Calculate **R<sup>2</sup>** and determine its meaning. Round your answer to four decimal places?

Great work! That's correct.

R<sup>2</sup>=0.3856

Therefore, **38.56%** of the variation in the observed y-values can be explained by the estimated regression equation.



R<sup>2</sup>=0.7217

Therefore, **72.17%** of the variation in the observed y-values can be explained by the estimated regression equation.



R<sub>2</sub>=1.3856

Therefore, 13.856% of the variation in the observed y-values can be explained by the estimated regression equation.



R<sub>2</sub>=0.2783

Therefore, 27.83% of the variation in the observed y-values can be explained by the estimated regression equation.

## Answer Explanation

**Correct answer:**

R<sub>2</sub>=0.7217

Therefore, 72.17% of the variation in the observed y-values can be explained by the estimated regression equation.

R<sub>2</sub>=SSRSST

R<sub>2</sub>=54.86176.012

R<sub>2</sub>=0.7217

R<sub>2</sub>=72.17%

## Correlation and Causation

True or False: The more mangoes you eat, the more rashes you get.

**Correct! You nailed it.**



True



False

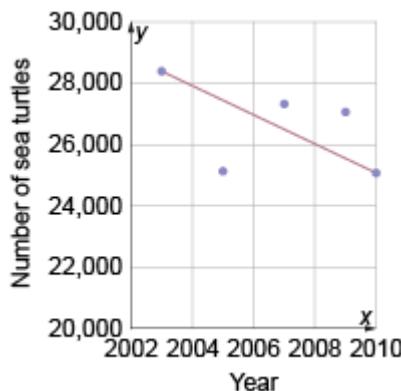
## Answer Explanation

**Correct answer:**

False

Many things can cause an increase or decrease in rashes: diet, exercise, hormones, medication, etc. There are too many other confounding variables that it can not be determined that Mango's are the cause of a rash.

The scatter plot below shows data for the number of sea turtles ( $y$ ) tagged by scientists in a given year, where  $X$  is the year. The least squares regression line is given by  $\hat{y} = 917,234 - 444x$ .



A coordinate plane has a horizontal x-axis labeled Year from 2002 to 2010 in increments of 2 and a vertical y-axis labeled Number of sea turtles from 20,000 to 30,000 in increments of 2000. The following points are plotted: left-parenthesis 2003 comma 28,500 right-parenthesis, left-parenthesis 2005 comma 25,000 right-parenthesis, left-parenthesis 2007 comma 27,500 right-parenthesis, left-parenthesis 2009 comma 27,000 right-parenthesis, and left-parenthesis 2010 comma 25,000 right-parenthesis. A line falls from left to right, passing through left-parenthesis 2003 comma 28,500 right-parenthesis and left-parenthesis 2010 comma 25,000 right-parenthesis. All coordinate are approximate.

Interpret the  $y$ -intercept of the least squares regression line.

**Perfect. Your hard work is paying off 😊**



The predicted number of sea turtles tagged by scientists in the year 0 is 917,234.



- The predicted number of sea turtles tagged by scientists in the year 2000 is **-444**.
- 
- The predicted number of sea turtles tagged by scientists in the year **2002** is **917,234**.
- 
- The **y**-intercept should not be interpreted.

## Answer Explanation

**Correct answer:**

The **y**-intercept should not be interpreted.

Scientists did not tag sea turtles in the year **2000**, so it is not appropriate to interpret the **y**-intercept

Suppose that data collected from police reports of motor vehicle crashes show a moderate positive correlation between the speed of the motor vehicle at the time of the crash and the severity of injuries to the driver. Answer the following question based only on this information.

True or false: It can be concluded that the faster a motor vehicle is traveling at the time of a crash, the more severe the injuries to the driver are.

**Correct! You nailed it.**

- 
- True
- 

**False**

## Answer Explanation

**Correct answer:**

False

Correlation does not prove causation. The provided information shows that there is a positive association between speed and severity of injuries, but that information alone is not sufficient to conclude that greater speed causes more severe injuries. Based only

on this information, there could be a third variable associated with speed that causes more severe injuries in crashes.

That said, the statement "the faster a motor vehicle is traveling at the time of a crash, the more severe the injuries to the driver are" does not imply a causal relationship between speed and severity of injuries.

Which of the following data sets or plots could have a regression line with a negative slope? Select all that apply.

**Great work! That's correct.**



- the difference in the number of ships launched by competing ship builders as a function of the number of months since the start of last year



- the number of hawks sighted per day as a function of the number of days since the two-week study started



- 

~~the total number of ships launched by a ship builder as a function of the number of months since the start of last year~~



- the average number of hawks sighted per day in a series of studies as a function of the number of days since the ten-week study started

## Answer Explanation

**Correct answer:**

the difference in the number of ships launched by competing ship builders as a function of the number of months since the start of last year

the number of hawks sighted per day as a function of the number of days since the two-week study started

the average number of hawks sighted per day in a series of studies as a function of the number of days since the ten-week study started

The slope is related to the increase or decrease of the dependent variable as a function of the independent variable. If the dependent variable can decrease, then the slope can be negative, such as with the difference in the number of ships launched.

Suppose that a large controlled experiment tests whether caffeine improves reaction times. A very large number of randomly selected participants are randomly given identical-seeming pills with varying doses of caffeine (including none) and then given tests of reaction times under the same conditions. The experiment finds a strong negative correlation between caffeine dose and reaction time. (Note that lower reaction times are better.)

Identify what can be concluded based on this information.

**Great work! That's correct.**

- There is evidence that caffeine causes lower (better) reaction times.
- People with lower (better) reaction times generally choose to consume more caffeine.
- Lower reaction times are associated with higher caffeine doses, but this study provides no evidence that caffeine causes lower reaction times.
- There is no relationship between reaction time and caffeine.

## Answer Explanation

**Correct answer:**

There is evidence that caffeine causes lower (better) reaction times.

Correlation alone does not prove causation, but this scenario provides more evidence than just correlation between two variables. Since the data were obtained from an appropriately randomized controlled experiment, a correlation can be used as evidence of a causal relationship. Since all other variables were controlled, there is no third variable that could be associated with caffeine that actually causes differences in reaction times.

## Question

A non-profit finds that donations decrease when the economy measured by GDP decreases.

Identify the relation between donations and GDP.

**Great work! That's correct.**

- Donations and GDP are positively correlated.
- Donations and GDP are negatively correlated.
- A decrease in donations causes a decrease in GDP.
- A decrease in GDP causes a decrease in donations.

## Answer Explanation

**Correct answer:**

Donations and GDP are positively correlated.

A decrease in donations is associated with a decrease in GDP, which implies a positive relationship. There would need to be more evidence to prove causation.

## Question

Which of the following data sets or plots could have a regression line with a negative slope.

## Answer Explanation

**Correct answer:**

the number of miles a ship has traveled each year as a function of the number of years since it was launched

the number of cats living in an abandoned lot as a function of the number of years since the building was torn down

the number of cats born each year in an abandoned lot as a function of the number of years since the building was torn down

The slope is related to the increase or decrease of the dependent variable as a function of the independent variable. If the dependent variable can decrease, then the slope can be negative, such as with the number of cats born each year.

**Your answer:**

the number of miles a ship has traveled as a function of the number of years since it was launched

The distance a ship has traveled can only increase, so the slope of the line can only be positive.

the number of miles a ship has traveled each year as a function of the number of years since it was launched

the number of cats born each year in an abandoned lot as a function of the number of years since the building was torn down

Which of the following data sets or plots could have a regression line with a negative slope? Select all that apply.

**Perfect. Your hard work is paying off 😊**



the number of tons of trash a dump truck has hauled as a function of the number of years since it was built



the number of people who work on a dump truck as a function of the number of years since it was built

- - the number of people who have worked on a dump truck as a function of the number of years since it was built
  - 
  -
- the highest number of tons of trash any dump truck has hauled during the year as a function of the number of years since 1955
- 

## Answer Explanation

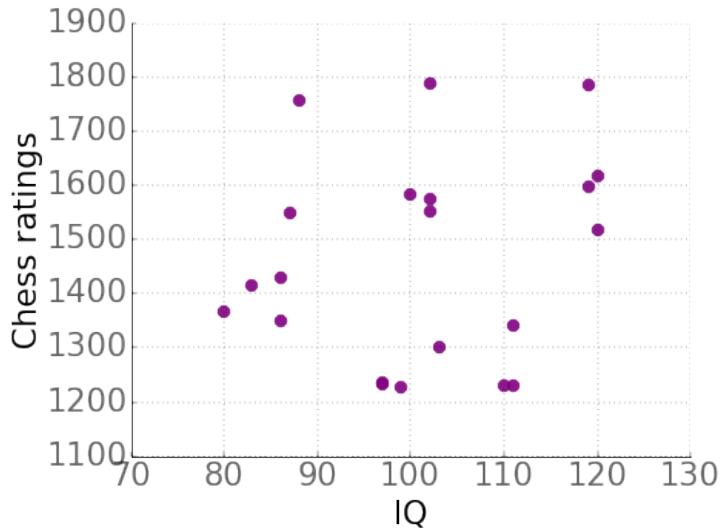
**Correct answer:**

- 2. the number of people who work on a dump truck as a function of the number of years since it was built
- 4. the highest number of tons of trash any dump truck has hauled during the year as a function of the number of years since 1955

The slope is related to the increase or decrease of the dependent variable as a function of the independent variable. If the dependent variable can decrease, then the slope can be negative, such as with the number of people who work on a dump truck or the amount of trash a dump truck hauls.

## Linear Regression Equations

The scatter plot below shows data relating competitive chess players' ratings and their IQ. Which of the following patterns does the scatter plot show?



Correct! You nailed it.

- positive linear pattern
- positive linear pattern with deviations
- negative linear pattern
- negative linear pattern with deviations
- no pattern

## Answer Explanation

Correct answer:

no pattern

Here, there is no visible pattern or relationship between the X-values (IQ) and Y-values (chess ratings).

Jamie owns a house painting service. For each house, she charges **\$70** plus **\$40** per hour of work. A linear equation that expresses the total amount of money Jamie earns per house is **y=70+40x**. What are the independent and dependent variables? What is the **y**-intercept and the slope?

Well done! You got it right.



The independent variable ( $x$ ) is the amount, in dollars, Jamie earns for a house. The dependent variable ( $y$ ) is the amount of time Jamie paints a house.

Jamie charges a one-time fee of \$40 (this is when  $x=0$ ), so the  $y$ -intercept is 40. Jamie earns \$70 for each hour she works, so the slope is 70.



The independent variable ( $x$ ) is the amount, in dollars, Jamie earns for a house. The dependent variable ( $y$ ) is the amount of time Jamie paints a house.

Jamie charges a one-time fee of \$70 (this is when  $x=0$ ), so the  $y$ -intercept is 70. Jamie earns \$40 for each hour she works, so the slope is 40.



The independent variable ( $x$ ) is the amount of time Jamie paints a house. The dependent variable ( $y$ ) is the amount, in dollars, Jamie earns for a house.

Jamie charges a one-time fee of \$40 (this is when  $x=0$ ), so the  $y$ -intercept is 40. Jamie earns \$70 for each hour she works, so the slope is 70.



**The independent variable ( $x$ ) is the amount of time Jamie paints a house. The dependent variable ( $y$ ) is the amount, in dollars, Jamie earns for a house.**

**Jamie charges a one-time fee of \$70 (this is when  $x=0$ ), so the  $y$ -intercept is 70. Jamie earns \$40 for each hour she works, so the slope is 40.**

## Answer Explanation

### Correct answer:

The independent variable ( $X$ ) is the amount of time Jamie paints a house. The dependent variable ( $y$ ) is the amount, in dollars, Jamie earns for a house.

Jamie charges a one-time fee of \$70 (this is when  $x=0$ ), so the  $y$ -intercept is 70. Jamie earns \$40 for each hour she works, so the slope is 40.

The independent variable ( $X$ ) is the amount of time Jamie paints a house because it is the value that changes. She may work different amounts per house, and her earnings are dependent on how many hours she works. This is why the amount, in dollars, Jamie earns for a house is the dependent variable ( $y$ ).

The  $y$ -intercept is 70 ( $b=70$ ). This is her one-time fee. The slope is 40 ( $a=40$ ). This is the increase for each hour she works.

George is an avid plant lover and is concerned about the lack of daffodils that grow in his backyard. He finds the growth of the daffodils,  $G$ , is dependent on the percent of aluminum measured in the soil,  $X$ , and can be modeled by the function

$$G(x)=16-4x.$$

Draw the graph of the growth function by plotting its  $G$ -intercept and another point.

Correct! You nailed it.

0, 16  
4, 0

### Answer Explanation

\$\$0, 16  
\$\$7, -12

The function  $G(x)=16-4x$  is a linear equation, so its graph is a straight line that can be drawn by plotting 2 points and connecting them.

Its  $G$  intercept occurs when  $x=0$ , so

$$G(0)=16,$$

and  $(0, 16)$  is the  $G$ -intercept.

To find another point, plug in another  $X$  value into the function  $G(x)$ . For example, when  $X=7$ , we have

$$G(7)=16-4(7)=-12.$$

So,  $(7, -12)$  is another point on the graph of  $G(x)$ .

**What percent of aluminum in the soil must there be for the daffodils to grow only by 5 centimeters?**

- Round your final answer to the nearest whole number.

**Great work! That's correct.**

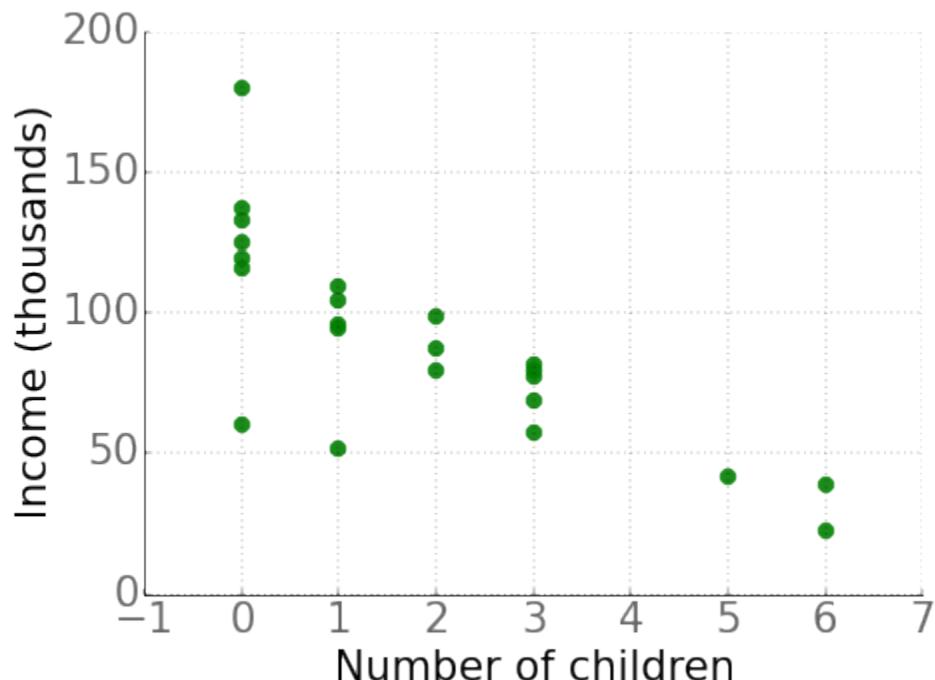
3 percent

## Answer Explanation

For the daffodils to grow only by 5 centimeters, the growth must be 5. So, we must find the percent of aluminum in the soil,  $X$ , so that  $G(x)=5$ .

For  $G(x)=5$ , we have  $16-4x=5$ ,  $-4x=-11$ ,  $x=-11/-4$ ,  $x=2.75$ ,  $x\approx 3$ .

The scatter plot below shows data relating total income and the number of children a family has. Which of the following patterns does the scatter plot show?



A scatterplot has a horizontal axis labeled "Number of children" from negative 1 to 7 in increments of 1 and a vertical axis labeled "Income (in thousands)" from 0 to 200 in increments of 50. A series of plotted points loosely forms a line that falls from left to right and passes through the points (0, 180) and (6, 25). All coordinates are approximate.

**Perfect. Your hard work is paying off 😊**

- Positive linear pattern
- Positive linear pattern with deviations
- Negative linear pattern
- Negative linear pattern with deviations
- No pattern

## Answer Explanation

**Correct answer:**

Negative linear pattern with deviations

We can see that as the **X**-values (number of children) increase, the **Y**-values (income) decrease.

So it is a negative relationship. But there are points that deviate from the negative linear pattern, so it is a weaker pattern, instead of a strong one.

## Question

A gym teacher finds that the distance students run in miles per week in gym class, **D**, is dependent on the time students warm-up beforehand in minutes per week, **X**, and can be modeled by the function

$$D(x)=2+0.5x.$$

Draw the graph of the distance function by plotting its **D**-intercept and another point.

**Answer 1:**

**That's not right - let's review the answer.**

**\$\$0, 14**

**\$\$11, 3**

**Answer 2:**

**Not quite - review the answer explanation to help get the next one.**

0, 14  
11, 3

## Answer Explanation

0, 2  
6, 5

The function  $D(x)=2+0.5x$  is a linear equation, so its graph is a straight line that can be drawn by plotting 2 points and connecting them.

Its  $D$  intercept occurs when  $x=0$ , so  $D(0)=2$ , and  $(0,2)$  is the  $D$ -intercept.

To find another point, plug in another  $X$  value into the function  $D(x)$ . For example, when  $x=6$ , we have

$$D(6)=2+0.5(6)=5.$$

So,  $(6,5)$  is another point on the graph of  $D(x)$

How long did a student warm-up in order for them to run 10 miles per week in gym class?

**Great work! That's correct.**

16 minutes

## Answer Explanation

**Correct answers:**

- 16 minutes

For a student to run 10 miles per week in gym class, the distance must be 10. So, we must find the amount of warm-up time,  $X$ , so that  $D(x)=10$ .

For  $D(x)=10$ , we have,  $2+0.5x=10$ ,  $0.5x=8$ ,  $x=8/0.5=16$ .

An owner of multiple online clothing stores explored the relationship between the percent of on-call service representatives and the percent of purchases over \$75 at

the same stores. The owner collects information from 6 of their online stores, shown in the table below.

Use the graph below to plot the points and develop a linear relationship between the percent of on-call service representatives and the percent of purchases over \$75.

Store Number	% of On-call service reps	% of purchase over \$75
1	20	20
2	35	25
3	50	40
4	55	35
5	60	40

6, 75, 34

**Yes that's right. Keep it up!**

The percent of on-call service representatives is the X-coordinate, while the percent of purchases over \$75 is the Y-coordinate. So, the table of values corresponds to the points

(20,20), (35,25), (50,40), (55,35), (60,40), (75,54).

**ON THIS QUESTION, IT'S ASKING YOU TO GRAPH THE %OF ONCALL SRVC WITH %OF PURCHASE**

Using the linear relationship graphed above, estimate the percent of over \$75 purchases if there are 40% on-call service representatives.

**Answer 1:**

**Not quite - review the answer explanation to help get the next one.**

\$\$60%

**Answer 2:**

**That's not right - let's review the answer.**

\$\$67.5%

## Answer Explanation

**Correct answers:**

- 30%

Based on the linear relationship that is graphed, when the percent of on-call service representatives is **40%**, the line has a value between **25** and **35**.

A government agency explored the relationship between the percent of companies that are technology related and the percent of higher paying jobs. The researchers collects information from **5** states, shown in the table below.

Use the graph below to plot the points and develop a linear relationship between the percent of technology companies and the percent of higher paying jobs.

State number	% of tech com.	% of higher paying jobs
1	20	25
2	35	30
3	50	45
4	55	65
5	60	70

**Answer 2:**

**Great work! That's correct.**

## Answer Explanation

The percent of tech companies is the **X**-coordinate, while the percent of higher paying jobs is the **Y**-coordinate. So, the table of values corresponds to the points

$$(20,25), (35,30), (50,45), (55,65), (60,70).$$

Using the linear relationship graphed above, estimate the percent of higher paying jobs if there are **30%** technology companies.

**Well done! You got it right.**

32.5%

## Answer Explanation

**Correct answers:**

- 30%

Based on the linear relationship that is graphed, when the percent of technology companies is **30%**, the line has a value between **25** and **35**.

Question:

A random sample of 11 employees produced the following data where  $x$  is the number of shifts worked in 8 weeks, and  $y$  is the number of breaks taken.

$X$  = explanatory variable      $Y$  = outcome of the study # of breaks taken per shifts worked

$x$	$y$
27	15
29	19
30	19

32	17
33	20
35	22
36	20
37	23
39	22
21	24
43	20

What is the equation of the regression line?

$$y = 0.381z + 6.9$$

Question:

A random sample of 11 university students produced the following data where x is the minutes spent studying per day, and y is the first exam score (out a maximum of 100 points).

x	y
11	39
13	55
14	43
17	46
19	69

22	75
24	77
25	78
28	77
31	93
34	92

What is the value of the intercept of the regression line, b rounded to one decimal place.

**Answer:** 16.4

Independent (x)	Dependent (y)	Slope ( $\beta_1$ )	2.369324
11	39	y-Intercept ( $\beta_0$ )	16.372817
13	55	Correlation Coefficient (r)	0.940900
14	43	Coefficient of Determination ( $r^2$ )	0.885293
17	46	Standard Error	6.802371
19	69		
22	75		
24	77		
25	78		
28	77		
31	93		
34	92		

**Question:**

Which of the following data sets or plots could have a regression line with a negative y-intercept?

Answer: The difference in height between two twins plotted as a function of age.

