# AntMan: Dynamic Scaling on GPU Clusters for Deep Learning

Authors: Wencong Xiao, Shiru Ren, Yong Li, Yang Zhang, Pengyang Hou,
Zhi Li, Yihui Feng, Wei Lin, Yangqing Jia
Alibaba Group

Presenters: Shi Pu, Jianbin Zhang

# Deep Learning Training

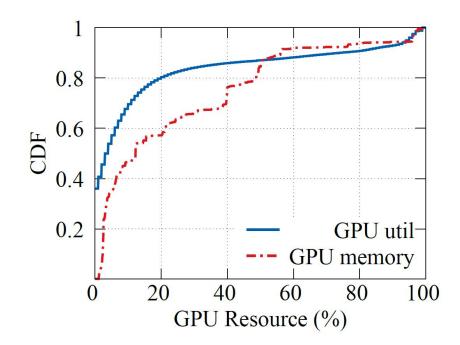
#### Deep learning

- Spans across multiple fields
  - Computer vision
  - Language understanding
  - Speech recognition
  - Advertisement
  - o ...
- Adopts data parallelism in multiple GPUs to speed up training
- Large companies use multi-tenant clusters to improve hardware

#### Characteristics of Production DL Clusters

#### Low utilization of in-use GPUs

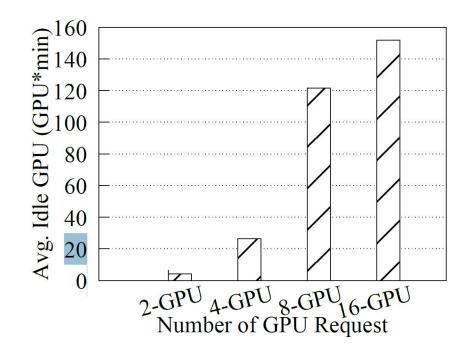
- 20% of the GPUs are consuming more than half of the GPU memory
- 10% of the GPUs achieve higher than 80% utilization



# Characteristics of Production DL Clusters (cont.)

#### Idle waiting for gang-schedule

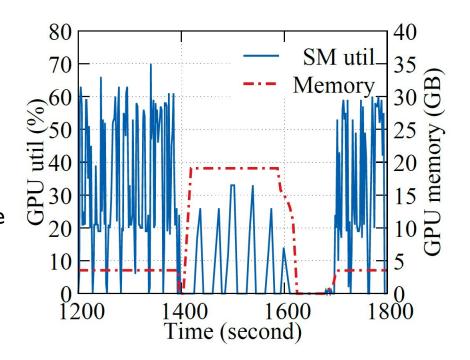
- A job will not start until all required GPUs are simultaneously available
- Wasted GPU cycles



# Characteristics of Production DL Clusters (cont.)

#### Dynamic resource demand

- Training pipeline contains several different phases
- Each phase has different resource requirements
- Hardware is underutilized because jobs request resources according to their peak usage

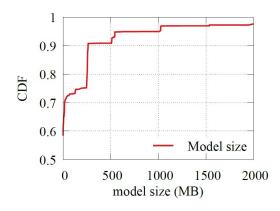


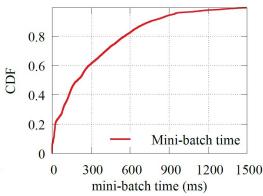
### Solution: Resource Sharing!

#### Challenges of GPU resource sharing:

- Achieve performance isolation for important jobs (resource-guarantee jobs)
  - Ensure Job performance as same as dedicated GPU execution
- Prevent potential failure from GPU memory contention
  - Dynamic resource demand happens

### Opportunities in DL Uniqueness





#### Small models

90% of DL models occupy only 500 MB

#### Short mini-batch

80% of tasks consume a minibatch with
 600 ms

#### Similar mini-batch

Allows performance profiling

## AntMan: Dynamic Scaling on GPU Clusters

- Improves GPU utilization
  - While providing performance guarantee on resource-guarantee jobs
- Utilizes spare GPU resources to co-execute multiple jobs
  - Dispatches opportunistic jobs to best-effort utilize GPU resources

## Design

#### AntMan co-designs:

- DL framework
  - Dynamic memory management
  - Dynamic computation management
- Cluster scheduler
  - Global scheduler
  - Local coordinator

### Dynamic Scaling Mechanism

#### Challenge: Executing jobs

- Satisfying minimal requirements
- Preventing GPU memory usage outbreak failures
- Adapting to the fluctuation in computation unit usage

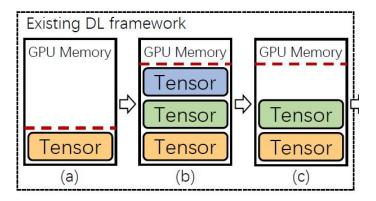
#### Dynamic scaling mechanism:

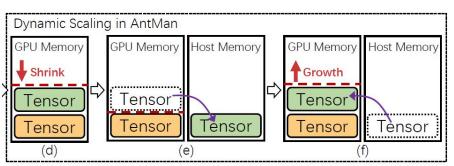
- Fine-grained dynamic control
- GPU memory
- Computation unit

# Memory Management

#### Universal Memory

- Use host memory to prevent failure
- Dynamically adjust cached memory
- Thanks to unique pattern of DL
  - Avoids tensor copy
  - Negligible performance overhead

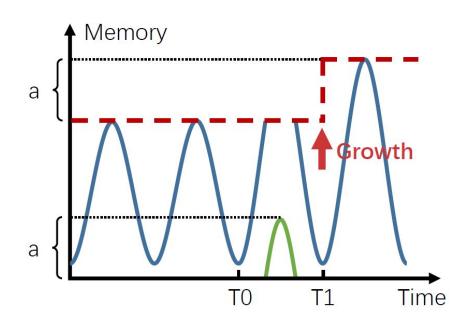




# Memory Management Example

#### To handle burst demand:

- T0: Memory requirement increases
- TI:AntMan raises GPU memory's upper limit according to the usage of the host memory

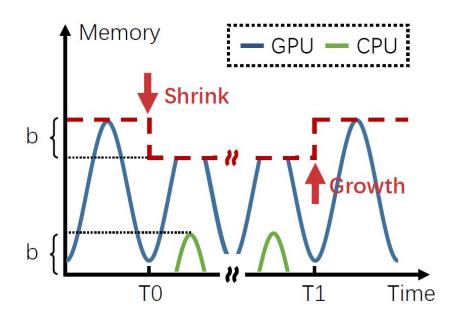


(a) Scaling for memory burst up.

# Memory Management Example (cont.)

To secure memory for other jobs:

- T0: Memory requirement decreases
- T1: Memory requirement grows back after other jobs are finished



(b) Scaling to secure memory.

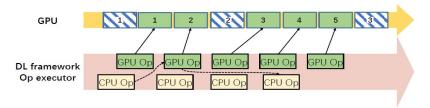
## Computation Management

#### **GpuOpManager**

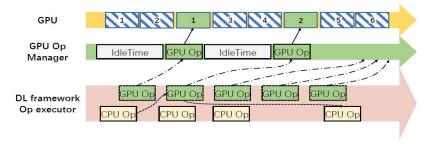
- Controls launching frequency
- Profiles GPU execution time
- Distributes idle time slots



(a) Job-A executes in a GPU exclusively despite some idle cycles.

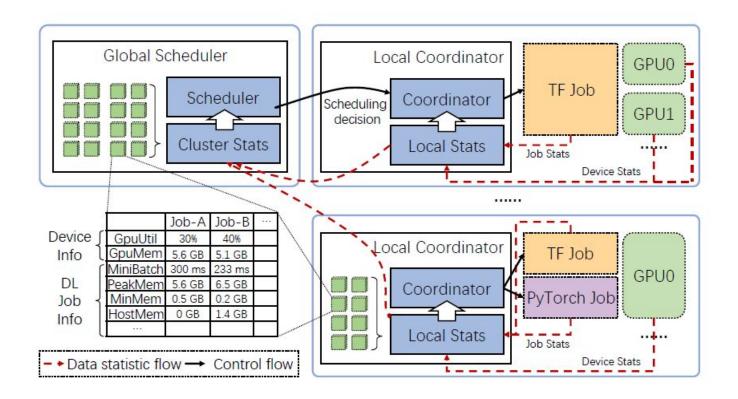


(b) Job-A significantly interfered by Job-B.



(c) GpuOpManager of Job-B controls the interference.

#### Collaborative Scheduler



## Scheduling Policy

#### Goals:

- Primary: Multi-tenant fairness
- Secondary: Improve cluster efficiency
  - Opportunities jobs to steal idle cycles in GPUs

# Scheduling Policy (cont.)

#### Global scheduler

- Resource-guaranteed jobs are given sufficient GPU resources
- Execute long queueing delay jobs as opportunistic jobs
- Allocate opportunistic jobs on the freest candidates

#### **Algorithm 1** scheduleJob(in job, out nodes)

```
    nodes0 ← findNodes(job.gpu, constraints ← job.topo)
    nodes1 ← findNodes(job.gpu, constraints ← M)
    nodes2 ← minLoadNodes(nodes1, job.gpu)
    if job.isResourceGuarantee:
    if numGPUs(nodes0) >= job.gpu:
    return nodes0
    else:
    reserve(nodes0)
    else:
    return nodes2
```

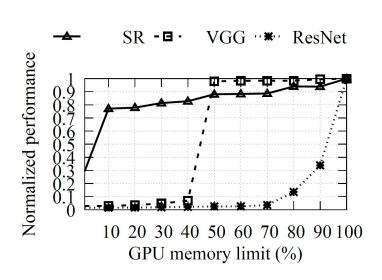
# Scheduling Policy (cont.)

#### Local Coordinator

- Limit the usage of GPU resources of opportunistic jobs
- Optimizes aggregated job performance when there exists multiple opportunistic jobs

#### Job Upgrade

 Upgrade opportunistic jobs when resources permit



### Implementation

- TensorFlow and PyTorch frameworks
  - Modification mainly in memory allocator, GPU executor and interfaces
- Prototype in Kubernetes
  - o 2000 LOC in Python
- Implementation in Fuxi (Alibaba's internal cluster scheduler)
  - o 10,000 LOC in C++
  - Including failover support and testing

### **Evaluation**

# Dynamic GPU memory scaling

- Preempt killed Job-A.
- FIFO introduces 17.1 minutes queuing delay.
- Pack failed Job-B due to insufficient memory.
- UMem used host memory when needed.
- AntMan showed great results.

	Model	Arrival	GpuMem	BS	Quota
Job-A	GCN	0 min	3.5 GB	1400	No
Job-B	ResNet	26 min	30.0 GB	360	Yes

Table 1: Setup and information of two jobs.

	Preempt	FIFO	Pack	UMem	AntMan
Job-A	Failed	43.0	43.1	43.4	43.9
Job-B	91.1	108.2	Failed	541.6	91.8

Table 2: Job status and JCT (min) of two jobs executing in different configurations.

## Cluster Experiment

- Job queueing delay reduces by 2x on average
- Almost 99% jobs suffer zero job interference

	Avg.	90% tile	95% tile
Dec. 2019	1132	1978	5960
Apr. 2020	550	124	489

Table 4: One-week queuing delay statistic in seconds.

Interference	0%	0~1%	1~2%	2~3%	3~4%
# of jobs	9895	26	30	20	29

Table 5: Interference analysis on mini-batch time for 10K production jobs

#### Other Benchmarks

- Efficient memory shrinkage and growth
- Dynamic GPU computation unit scaling
- Prototype trace experiment
- Omitted for brevity

#### Conclusion

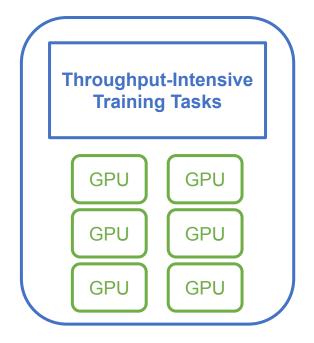
- Implementation deployed on DL infrastructure at Alibaba
- Provides dynamic scaling primitives for DL jobs
- GPU utilization maximized for opportunistic jobs while avoiding job interference
- 42% improvement in GPU memory utilization
- 34% improvement in GPU computation resources utilization

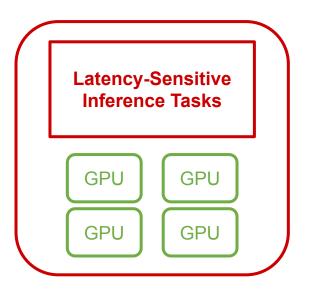
# PipeSwitch: Fast Pipelined Context Switching for Deep Learning Applications

Authors: Zhihao Bai, Zhen Zhang, Yibo Zhu, Xin Jin John Hopkins University ByteDance Inc.

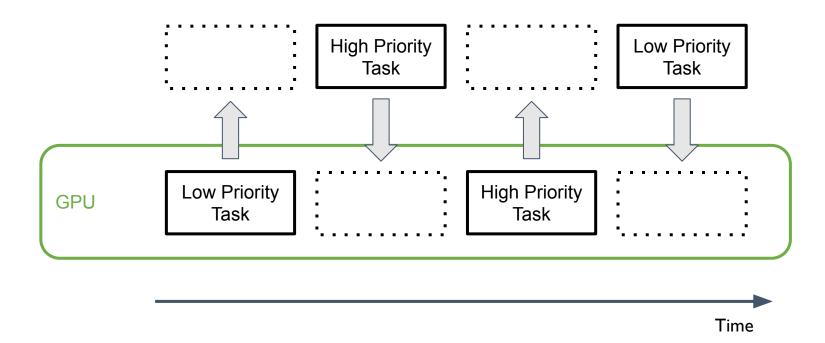
Presenters: Wenqi Zhu, Jianbin Zhang

### Training and Inference Tasks





### What if we can time-share GPU tasks?



## GPU Task Switching Overhead

- Four components
  - Task cleaning
  - Task initialization
  - Memory allocation
  - Model transmission
- SLA violated

Instance Type	g4dn.2xlarge NVIDIA T4	p3.2xlarge NVIDIA V100	
GPU Type	NVIDIA 14	NVIDIA VI00	
Task Cleaning	155 ms	165 ms	
Task Initialization	5530 ms	7290 ms	
Memory Allocation	10 ms	13 ms	
Model Transmission	91 ms	81 ms	
Total Overhead	5787 ms	7551 ms	
Inference Time	105 ms	32 ms	

### **GPU Task Switching Problems**

- Training BERT to Inference ResNet on Nvidia T4: 6 seconds
- GPU memory is limited
- DL models are large and getting larger
- GPU memory isolation

#### Solutions

#### Current:

- Nvidia MPS: high overhead due to contention between tasks
- Salus: allows fast job switching only if all models are preloaded in GPU memory

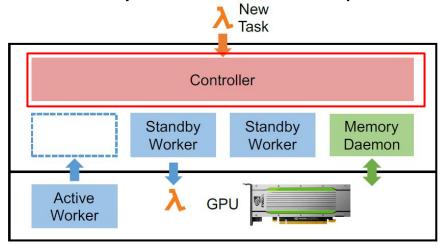
#### Proposed:

PipeSwitch!

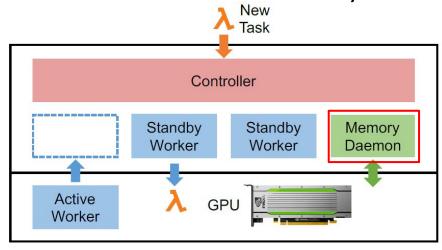
## PipeSwitch: Fast Pipelined Context Switch

- Enable GPU-efficient multiplexing of multiple DL applications with fine-grained time-sharing.
- Achieve millisecond-scale task switching overhead to satisfy SLOs requirements.

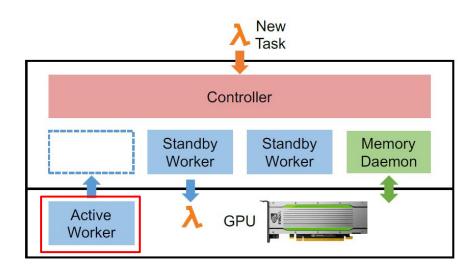
- Controller
  - Central Component.
  - Receives task from clients.
  - Controls the memory daemon and worker processes.



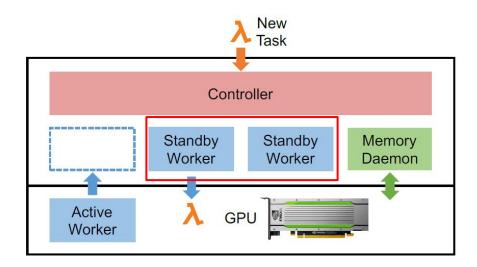
- Memory Daemon
  - A customized memory manager between GPU driver and worker process.
  - Allocates the GPU memory for worker.
  - Transfers the model from CPU host memory to GPU memory.



- Active Worker
  - The worker process that is currently executing the task.



- Standby Worker
  - The worker process that is idle/task initializing/task cleaning.
  - A server has one or more standby workers.



### How to reduce context switching overhead?

Model Transmission → Pipelined Model Transmission

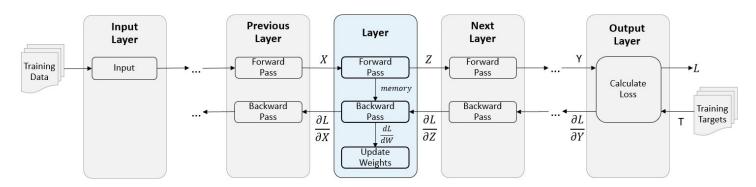
Memory Allocation

Task Initialization

Task Cleaning

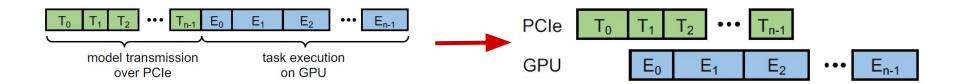
#### Pipelined Model Transmission: Basic Idea

- Insight: DL workloads have well-defined layered structures.
  - Computation takes place layer by layer.
  - To compute current layer, we only need
    - Output from earlier layers
    - Parameters of the current layer



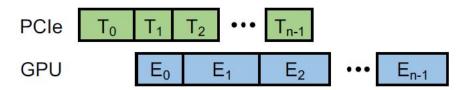
#### Pipelined Model Transmission: Basic Idea

- Model is transmitted via PCle from CPU to GPU.
  - Overhead is bounded by PCle bandwidth!
- Leverage layered structure of DL model,
  - We can pipeline model transmission and task execution!
  - Model transmission overhead can be hidden.



#### Per-Layer vs Per-Group Granularity

- Basic way for pipelining: on per-layer granularity
- Introduce large pipelining overhead!
  - A PCle call is invoked per layer.
  - Synchronization overhead between transmission and computation.
- Group multiple layers, perform pipelining on *per-group* granularity.
  - Still need to pay pipelining overhead, but once a group!



#### Per-Group Granularity

- Trade-off between pipelining efficiency and pipelining overhead.
- Small groups
  - Per-layer in the extreme case
  - Huge pipelining overhead
- Big groups
  - Entire model in one group in the extreme case
  - Low pipelining efficiency
- PipeSwitch's solution to find optimal grouping strategy efficiently
  - Optimal Model-Aware Grouping algorithm

#### Formulate the optimal grouping question

```
n = number of total layers in a model
```

F(B, i):

B = already formed groups, from layer 0 to i-I

i = the first layer that have not formed a group

return total time of the optimal grouping strategy from layer i to n-1, given B.

We have the following recursive formula:

$$F(\{\},0) = \min_{i} \left[ F(\{group(0,i)\}, i+1) \right]$$

To find the optimal grouping strategy for the entire model,

we divide all possible combinations into n cases based on how the first group is formed.

F( {group(0,i)}, i+1 ) can be recursively computed using this formula.

## Pruning opportunity I

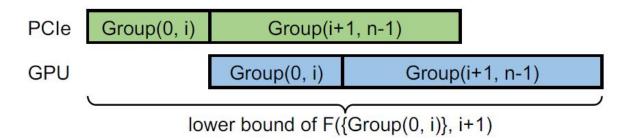
$$F(\{\},0) = \min_{i} F(\{group(0,i)\}, i+1)$$

Considering a best scenario:

- Given formed Group(0,i), all the remaining layers are combined in one group.
- Computation of Group(i+1, n-1) can happen right after the computation of Group(0,i) finishes.

The total time of case i in this scenario is considered as lower bound.

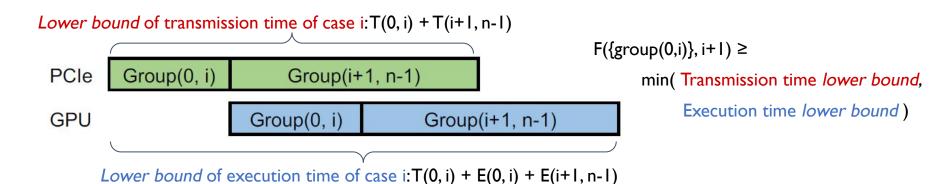
If the lower bound of case i is already larger than current optimal time, we can prune this case i.



#### Pruning opportunity 1: Compute Lower-bound

T(i,j) = Transmission times for a group from layer i to j, including overhead of invoking multiple PCles. Calculated based on the size of layer i to j and PCle bandwidth.

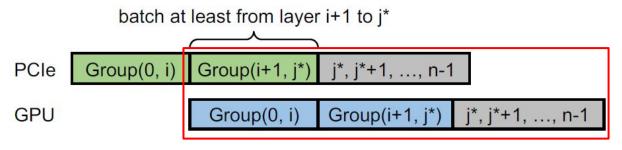
E(i,j) = Execution times for a group from layer i to j. Profiled on the GPU



#### Pruning opportunity 2

$$F(\{\},0) = \min_{i} F(\{group(0,i)\}, i+1)$$

We can safely pack multiple layers in a group without affecting pipeline efficiency. But which layers?



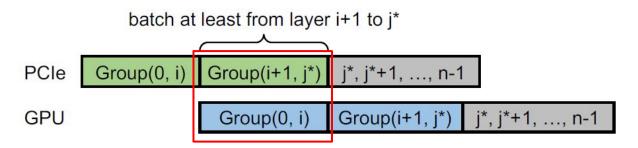
Group(0,i) already fixed.

We are applying the recursion equation to find the second group [i+1,j]. We want to pick a best j in range (i+1,n-1)

#### Pruning opportunity 2

$$F(\{\},0) = \min_{i} F(\{group(0,i)\}, i+1)$$

We can safely pack multiple layers in a group without affecting pipeline efficiency. But which layers?



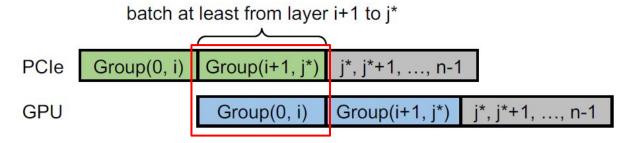
Find a max  $j^*$  in [i+1, n-1]. s.t.Transmission overhead of  $Group(i+1, j^*)$  is hidden behind computation of Group(0,i)Which means  $T(i+1, j^*) \le E(0,i)$ 

#### Pruning opportunity 2

$$F(\{\},0) = \min_{i} F(\{group(0,i)\}, i+1)$$

We can safely pack multiple layers in a group without affecting pipeline efficiency.

Layers [i+1, j\*] can be packed in a group directly. We only need to search for  $j \ge j^*$ .



Find a max  $j^*$  in [i+1, n-1]. s.t.Transmission overhead of  $Group(i+1, j^*)$  is hidden behind computation of Group(0,i)Which means  $T(i+1, j^*) \leq E(0,i)$ 

#### Algorithm 1 Optimal Model-Aware Grouping

```
1: function FINDOPTGROUPING(B, x)
        opt\_groups \leftarrow \emptyset, opt\_groups.time \leftarrow \infty
        // find first group from layer i to j^*
        i^* \leftarrow x
 5:
        for layer i from x to n-1 do
 6:
            if T(x,i) \leq B.delay then
                i^* \leftarrow i
            else
 9:
                break
        // recursively find the optimal grouping
10:
11:
        for layer i from j^* to n-1 do
12:
            if opt_groups \neq \emptyset then
13:
                // compute lower bound
14:
                trans\_time \leftarrow T(x,i) + T(i+1,n-1)
                exec\ time \leftarrow max(T(x,i),B.delay)
15:
                           +E(x,i)+E(i+1,n-1)
16:
                lower\ bound \leftarrow min(trans\ time, exec\ time)
17:
18:
                if lower bound > opt groups.time then
19:
                    continue
20:
            // recursively find rest groups
21:
            first group \leftarrow Group(x,i)
            rest\_groups \leftarrow FindOptGrouping(
23:
                          B + first\_group, i + 1)
24:
            cur\ groups \leftarrow first\ group + rest\ groups
25:
            if cur_groups.time < opt_groups.time then
26:
                opt_groups ← cur_groups
        return opt_groups
```

- Given n layers
  - Worst case time complexity: O(2^n)
  - But pruning techniques work really well in practice
- The algorithm finds the optimal grouping strategy that minimizes the total time for the pipeline.
  - Proved with induction.
- The algorithm is applicable to the general case.
  - Work for DAGs model like ResNet.

#### How to reduce context switching overhead?

Model Transmission → Pipelined Model Transmission

Memory Allocation

Task Initialization

Task Cleaning

#### How to reduce context switching overhead?

Model Transmission

Pipelined Model Transmission

Memory Allocation

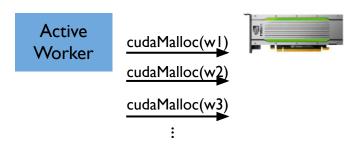
Unified Memory Management

Task Initialization

Task Cleaning

## Unified Memory Management: Basic Idea

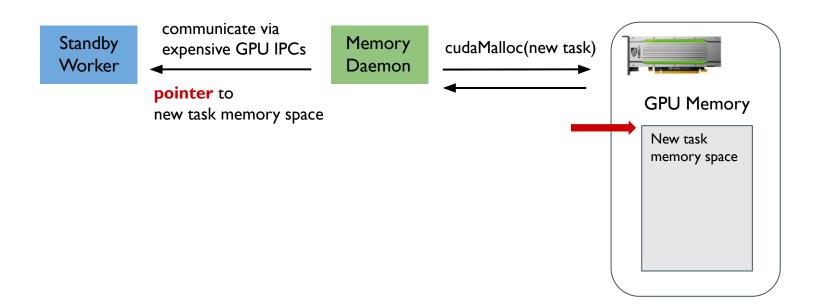
- Worker calls malloc function (e.g., cudaMalloc for NVIDIA GPUs) to request
   GPU memory
  - Many function calls introduce large overhead!
- Native GPU memory management is designed for general-purpose apps.
  - Very heavy-weight!



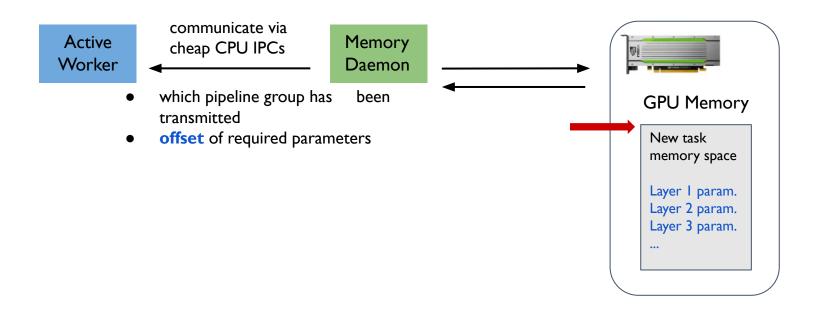
#### Unified Memory Management: Basic Idea

- Insight I: For DNN models in GPU memory
  - o the amount of memory it needs is fixed.
- Insight 2: For intermediate results in GPU memory
  - they change in a simple and deterministic pattern.
- Leverage DL characteristics, PipeSwitch customizes a memory daemon
  - to request a large amount of GPU memory at the beginning.
  - to handle memory allocation/release using light-weight stack-like mechanism.

#### At initialization stage



#### At execution stage



#### How to reduce context switching overhead?

Model Transmission

Pipelined Model Transmission

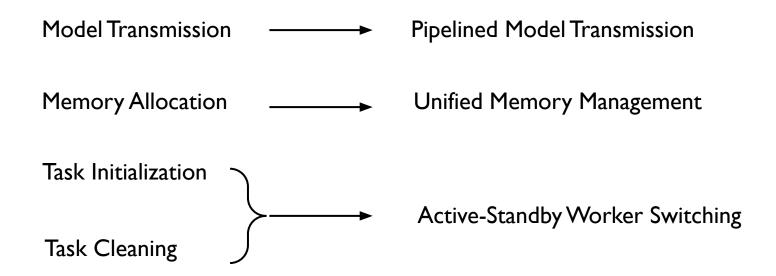
Memory Allocation

Unified Memory Management

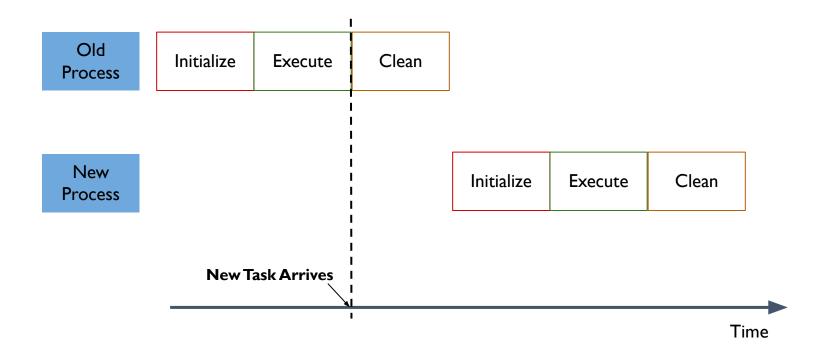
Task Initialization

Task Cleaning

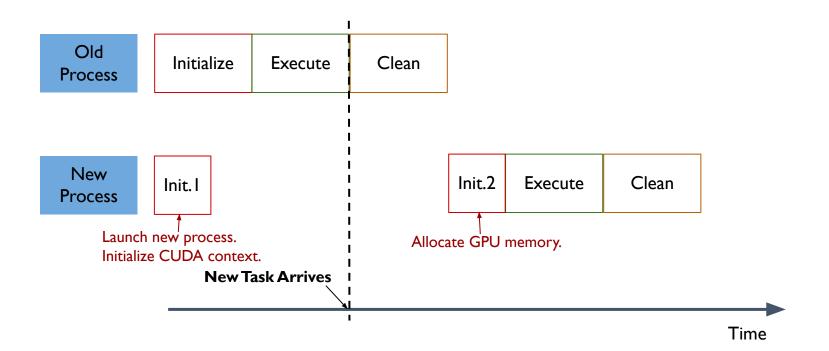
#### How to reduce context switching overhead?



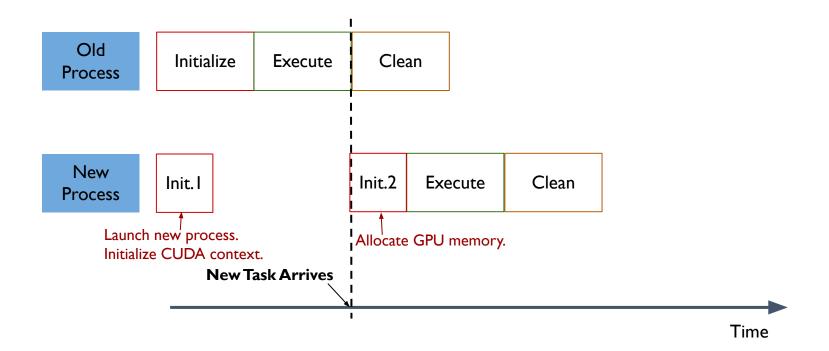
## Sequential Initialization and Cleaning



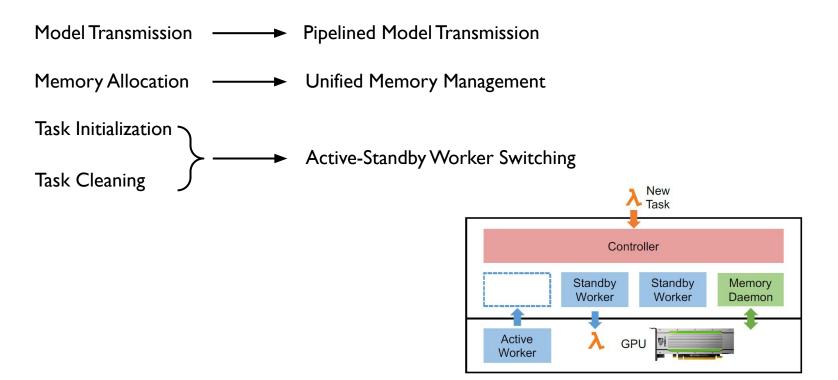
## Active-Standby Worker Switching



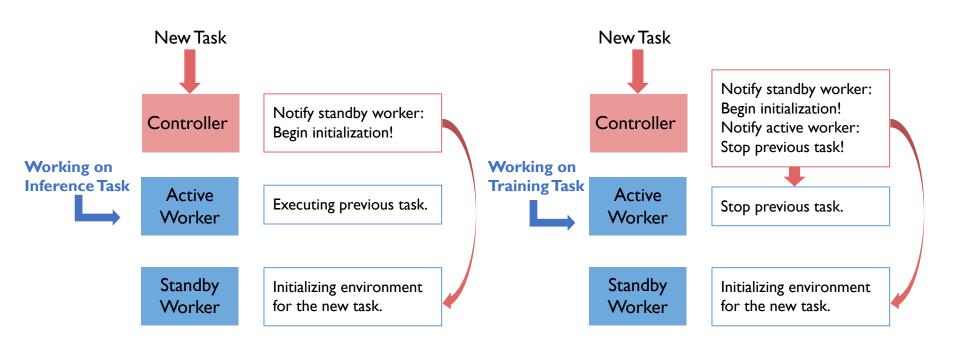
## Active-Standby Worker Switching



#### How is a task executed?



#### Controller starts a new task.



## System executes new task.

Notify memory daemon and worker: Controller Begin execution! Active Previous work Cleaning environment for the previous completes/stops Worker task. Standby **Finish** Becomes the new active worker. Worker initialization Executes the new task. Allocates the GPU memory for new Memory active worker to execute task. Daemon Transmits the new task model from host memory to GPU memory.

#### Implementation

- PyTorch framework plugins
  - Modification mainly in allocating GPU memory, sharing the GPU memory through CUDA IPC API, and getting the shared GPU memory
- Prototype in C++ and Python
  - 3600 LOC

#### **Evaluation**

#### **End-to-End Experiments**

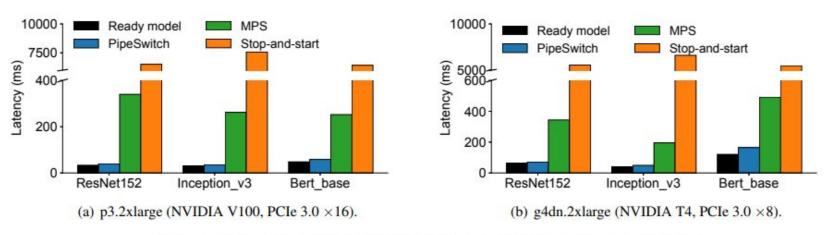


Figure 5: Total latency experienced by the client for different mechanisms.

## End-to-End Experiments (Cont'd)

	p3.2xlarge (NVIDIA V100, PCIe 3.0 ×16)			g4dn.2xlarge (NVIDIA T4, PCIe $3.0 \times 8$ )		
	ResNet152	Inception_v3	Bert_base	ResNet152	Inception_v3	Bert_base
Stop-and-start	6475.40 ms	7536.07 ms	6371.32 ms	5486.74 ms	6558.76 ms	5355.95 ms
NVIDIA MPS	307.02 ms	232.25 ms	204.52 ms	259.20 ms	193.05 ms	338.25 ms
PipeSwitch	6.01 ms	5.40 ms	10.27 ms	5.57 ms	7.66 ms	34.56 ms

Table 3: Total overhead, i.e., the difference on total latency between different mechanisms and ready model.

## Does Pruning Work? YES!

	ResNet152	Inception_v3	Bert_base
# of Layers	464	189	139
Algorithm 1	1.33 s	0.18 s	0.34 s
Only Pruning 1	2.09 s	0.30 s	0.88 s
Only Pruning 2	3.44 h	5.07 s	> 24 h
No Pruning	> 24 h	> 24 h	> 24 h

Table 5: Effectiveness of two pruning techniques.

#### Other Benchmarks

- Pipelined model transmission
- Unified memory management
- Active-standby worker switching
- Omitted for brevity

#### Conclusion

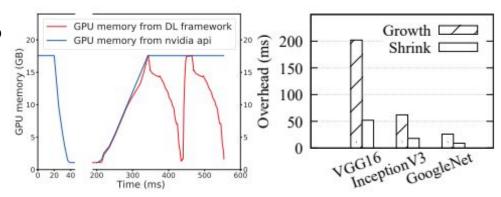
- Introduces pipelined context switching
- Total overhead of 5.4-34.6 ms
- GPU utilization near 100%

# Backup Slides

#### AntMan

#### Efficient memory shrinkage and growth

- Memory shrinkage from 17.6 GB to 1.3 GB took 17 ms.
- Memory growth from 1.3 GB to 17.6 GB took 143 ms.
- Largest overhead is negligible 0.4%.



(a) A shrink-growth profiling on (b) Overhead of GPU memory ResNet-50. scaling for typical models.

Figure 11: Efficiency of GPU memory scaling in AntMan.

#### Dynamic GPU computation unit scaling

- Naive packing is unfair to ESPnet because ResNet-50 launches more kernels.
- AntMan ensures the performance of ESPnet adaptively.

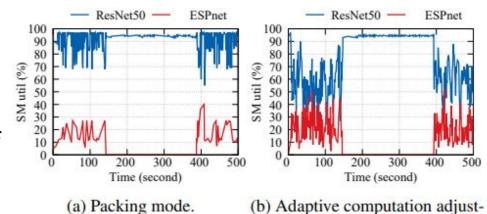
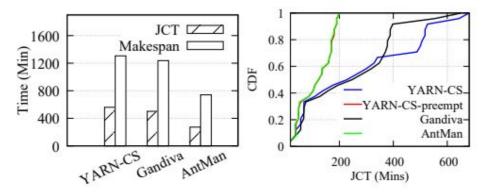


Figure 12: The SM utilization rates of packing mode in Gandiva [48] and an adaptive computation adjustment mode in AntMan for a 500s segment of execution of ESP-net and ResNet-50.

ment mode.

#### Trace Experiment

- AntMan improves
  - $\circ$  average JCT by 2.05x and 1.84x.
  - o makespan by 1.76x and 1.67x.
- AntMan achieves similar JCT as YARN-CS-preempt with a much lower job preemption rates



(a) Comparison of YARN-CS, (b) Job completion time of Gandiva, and AntMan. resource-guarantee jobs.

Figure 13: Trace experiment on 64 V100 GPUs.

# PipeSwtich

#### Algorithm 1 Optimal Model-Aware Grouping

```
1: function FINDOPTGROUPING(B, x)
        opt\_groups \leftarrow \emptyset, opt\_groups.time \leftarrow \infty
        // find first group from layer i to j^*
        i^* \leftarrow x
 5:
        for layer i from x to n-1 do
 6:
            if T(x,i) \leq B.delay then
                j^* \leftarrow i
            else
 9:
                break
        // recursively find the optimal grouping
10:
11:
        for layer i from j^* to n-1 do
12:
            if opt_groups \neq \emptyset then
13:
                // compute lower bound
14:
                trans\_time \leftarrow T(x,i) + T(i+1,n-1)
                exec\ time \leftarrow max(T(x,i),B.delay)
15:
16:
                           +E(x,i)+E(i+1,n-1)
                lower\_bound \leftarrow min(trans\_time, exec\_time)
17:
18:
                if lower bound > opt groups.time then
19:
                    continue
20:
            // recursively find rest groups
21:
            first group \leftarrow Group(x,i)
            rest\_groups \leftarrow FindOptGrouping(
23:
                          B + first\_group, i + 1)
24:
            cur\ groups \leftarrow first\ group + rest\ groups
25:
            if cur_groups.time < opt_groups.time then
26:
                opt_groups ← cur_groups
        return opt_groups
```

B = groups that have already formed from layer 0 to x-1.

x = the first layer that have not formed a group

#### Goal:

Recursively finds the optimal grouping strategy based on the equation.

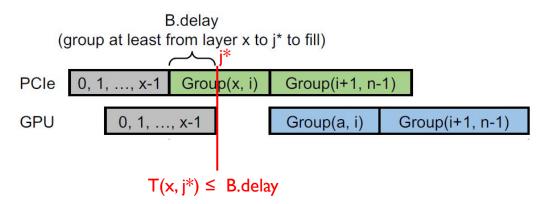
$$F(\{\},0) = \min_{i} F(\{group(0,i)\}, i+1)$$

```
Algorithm 1 Optimal Model-Aware Grouping
 1: function FINDOPTGROUPING(B, x)
        opt\_groups \leftarrow \emptyset, opt\_groups.time \leftarrow \infty
       // find first group from layer i to j^*
 4:
        i^* \leftarrow x
 5:
        for layer i from x to n-1 do
 6:
            if T(x,i) \leq B.delay then
                i^* \leftarrow i
 8:
            else
 9:
                break
        // recursively find the optimal grouping
10:
11:
        for layer i from j^* to n-1 do
12:
            if opt_groups \neq \emptyset then
13:
                // compute lower bound
14:
                trans\_time \leftarrow T(x,i) + T(i+1,n-1)
                exec\ time \leftarrow max(T(x,i),B.delay)
15:
16:
                           +E(x,i)+E(i+1,n-1)
17:
                lower\_bound \leftarrow min(trans\_time, exec\_time)
18:
                if lower bound > opt groups.time then
19:
                    continue
20:
            // recursively find rest groups
21:
            first group \leftarrow Group(x,i)
            rest\_groups \leftarrow FindOptGrouping(
23:
                         B + first\_group, i + 1)
24:
            cur\ groups \leftarrow first\ group + rest\ groups
25:
            if cur_groups.time < opt_groups.time then
26:
                opt_groups ← cur_groups
```

return opt groups

```
B.delay = time to which new group can be formed T(x,i) = \text{transmission time of group } [x,i] j^* = \text{prune } i \in [x,j^*-1] \text{ from searching}
```

#### Leverage pruning opportunity 2



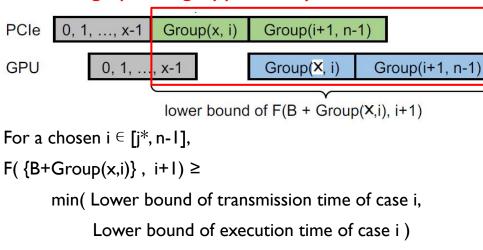
#### Algorithm 1 Optimal Model-Aware Grouping

```
1: function FINDOPTGROUPING(B, x)
        opt\_groups \leftarrow \emptyset, opt\_groups.time \leftarrow \infty
        // find first group from layer i to j^*
        i^* \leftarrow x
 5:
        for layer i from x to n-1 do
 6:
            if T(x,i) \leq B.delay then
                i^* \leftarrow i
            else
 9:
                 break
        // recursively find the optimal grouping
10:
                                                       For case i
11:
        for layer i from j^* to n-1 do
12:
             if opt\_groups \neq \emptyset then
13:
                // compute lower bound
14:
                trans\_time \leftarrow T(x,i) + T(i+1,n-1)
                exec\ time \leftarrow max(T(x,i),B.delay)
15:
                            +E(x,i)+E(i+1,n-1)
16:
                lower\_bound \leftarrow min(trans\_time, exec\_time)
17:
18:
                if lower bound > opt groups.time then
19:
                    continue
20:
            // recursively find rest groups
21:
             first group \leftarrow Group(x,i)
            rest\_groups \leftarrow FindOptGrouping(
23:
                          B + first\_group, i + 1)
24:
            cur\ groups \leftarrow first\ group + rest\ groups
25:
            if cur_groups.time < opt_groups.time then
26:
                opt_groups ← cur_groups
```

**return** opt\_groups

B.delay = time to which new group can be formed T(x, i) = transmission time of group [x,i] E(x, i) = execution time of group [x,i]

#### Leverage pruning opportunity I



#### Algorithm 1 Optimal Model-Aware Grouping

```
1: function FINDOPTGROUPING(B, x)
        opt\_groups \leftarrow \emptyset, opt\_groups.time \leftarrow \infty
        // find first group from layer i to j^*
        i^* \leftarrow x
 5:
        for layer i from x to n-1 do
 6:
            if T(x,i) \leq B.delay then
                i^* \leftarrow i
            else
 9:
                 break
        // recursively find the optimal grouping
10:
11:
         for layer i from j^* to n-1 do
12:
            if opt_groups \neq \emptyset then
13:
                // compute lower bound
14:
                trans\_time \leftarrow T(x,i) + T(i+1,n-1)
                exec\ time \leftarrow max(T(x,i),B.delay)
15:
                            +E(x,i)+E(i+1,n-1)
16:
                lower\ bound \leftarrow min(trans\ time, exec\ time)
17:
18:
                if lower bound > opt groups.time then
19:
                     continue
20:
            // recursively find rest groups
21:
             first group \leftarrow Group(x,i)
            rest\_groups \leftarrow FindOptGrouping(
23:
                          B + first\_group, i + 1)
24:
            cur\ groups \leftarrow first\ group + rest\ groups
25:
            if cur_groups.time < opt_groups.time then
26:
                opt\_groups \leftarrow cur\_groups
```

return opt groups

Line 21:

Given that group[x,i] is formed.

Line 22-23:

The function recursively applies itself to find the optimal groups in layers [i+1, n-1].

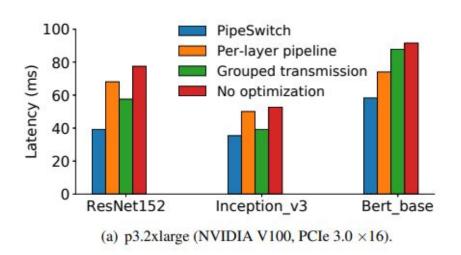
Line 24-26:

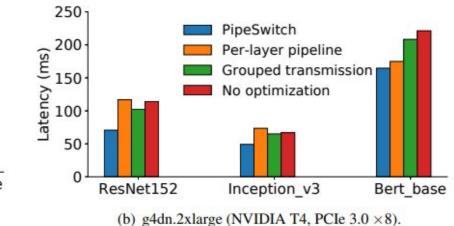
Update opt groups if current strategy is better.

Given:

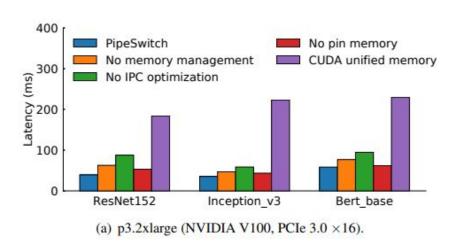
group [x, i] is formed!

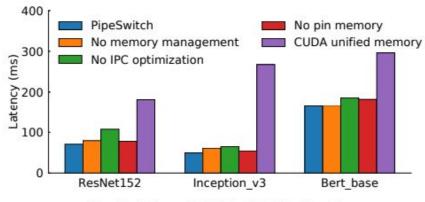
#### Pipelined Model Transmission





## Unified Memory Management





## Active-Standby Worker Switching

