#### Differential Equations

# Part I Introduction

Differential Equations model the rate of change in a system

# Part II History

# Part III

# Method

# **Basics**

# Differential Equations

### 3.1 Notation

First order differential of y w.r.t x

$$\frac{dy}{dx} \tag{3.1}$$

Second order differential of y w.r.t x

$$\frac{d^2y}{dx^2} \tag{3.2}$$

## Differentiation

The derivative of a function is defined as

$$\frac{df}{dx} = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h} \tag{4.1}$$

#### 4.1 Chain Rule

Given

$$f(x) = F(g(x)) \tag{4.2}$$

Then

$$\frac{df}{dx} = \frac{dF}{dg} \cdot \frac{dg}{dx} \tag{4.3}$$

#### 4.2 Product Rule

Given

$$f(x) = u(x)v(x) \tag{4.4}$$

Then

$$\frac{df}{dx} = \frac{du}{dx}(x) \cdot v(x) + u(x) \cdot \frac{dv}{dx}$$
 (4.5)

### 4.3 Trigonometric Functions