

# From noise in jets & wind turbines to relativity

Dr Sam Sinayoko

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# Objectives

- Two applications
  - Jet noise sources
  - Wind turbine noise

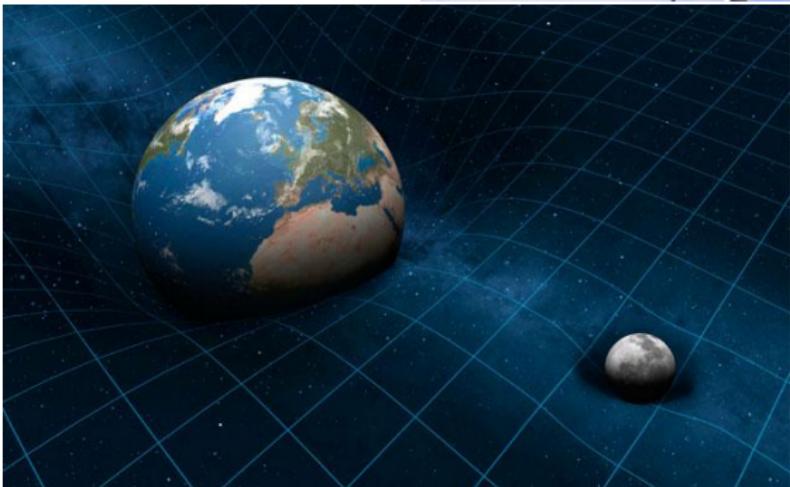
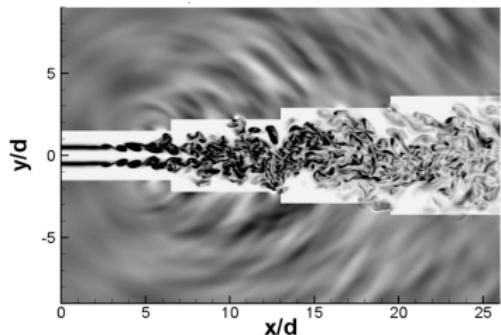
# Objectives

- Two applications
  - Jet noise sources
  - Wind turbine noise
- Two major problems
  - Noise sources / fluctuations are hidden in the flow.
  - Existing mathematical tools are limited: confusing and error prone.

# Objectives

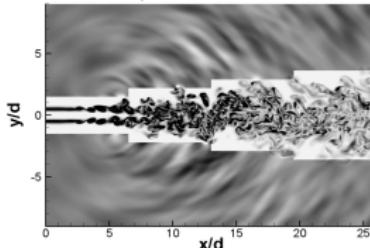
- Two applications
  - Jet noise sources
  - Wind turbine noise
- Two major problems
  - Noise sources / fluctuations are hidden in the flow.
  - Existing mathematical tools are limited: confusing and error prone.
- Possible solutions
  - silent base flow analogy
  - acoustic space-time

# Outline



# Outline

## True sources of jet noise



Engineering and Physical Sciences  
Research Council



Rolls-Royce

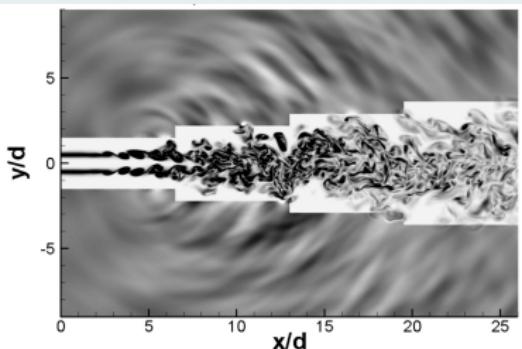
UNIVERSITY OF  
Southampton  
Institute of Sound and  
Vibration Research

## Acknowledgements

- Anurag Agarwal
- Chris Morfey
- Zhiwei Hu
- Victoria Suponitsky
- Neil Sandham
- Peter Jordan
- Richard Sandberg

# Lighthill's Acoustic Analogy

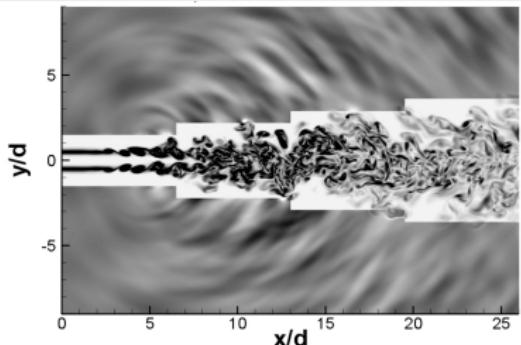
Complex turbulent flow



# Source definition

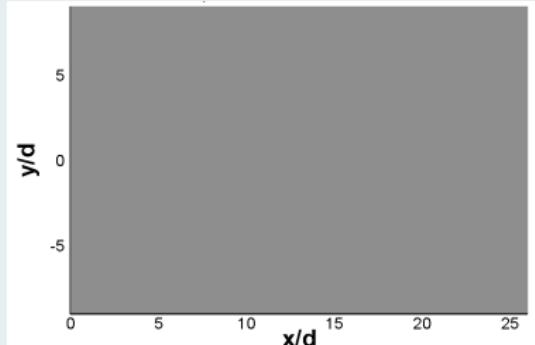
Lighthill's acoustic analogy

Turbulent flow



Complex propagation

Quiescent medium

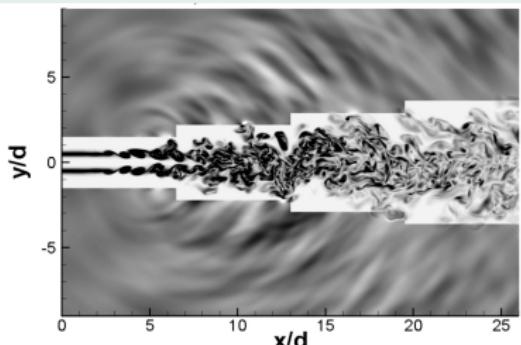


Simple propagation

# Source definition

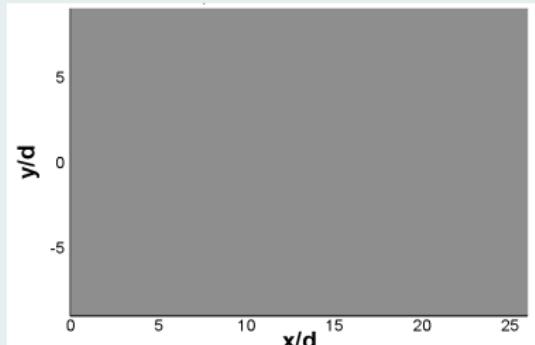
Lighthill's acoustic analogy

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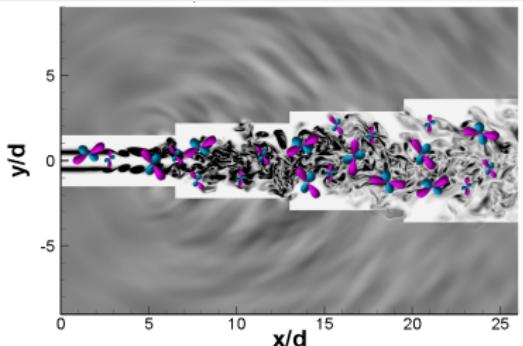
Simple propagation

⇒ What are the equivalent sound sources?

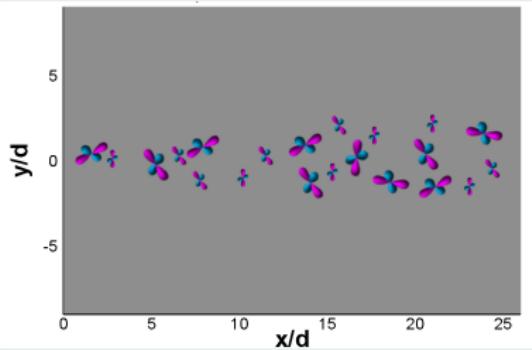
# Source definition

## Lighthill's acoustic analogy

### Complex turbulent flow



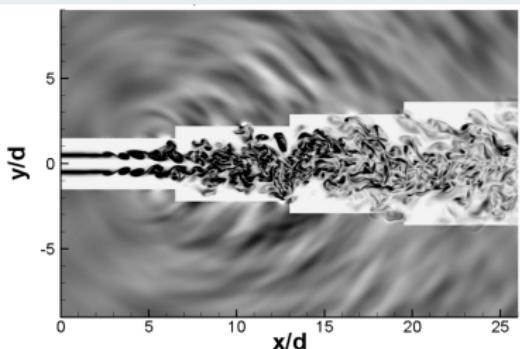
### Simple quiescent medium



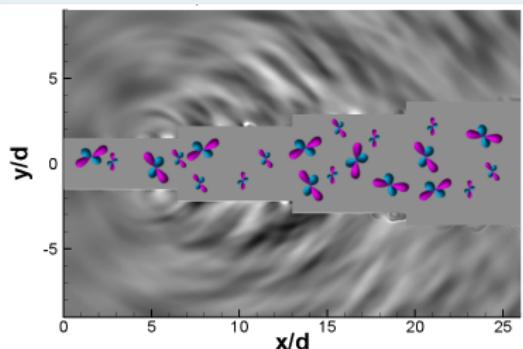
# Source definition

## Lighthill's acoustic analogy

### Complex turbulent flow



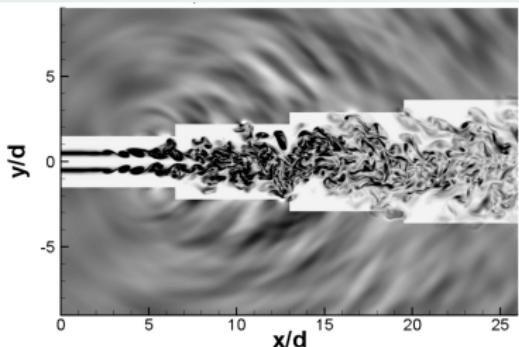
### Simple quiescent medium



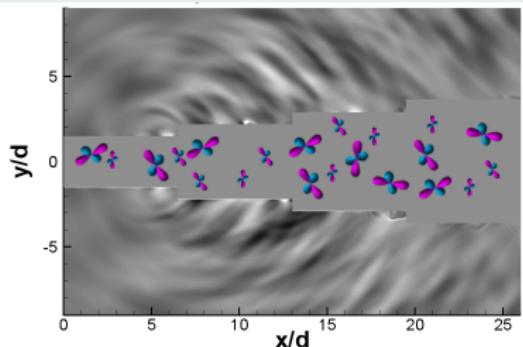
# Source definition

## Lighthill's acoustic analogy

### Complex turbulent flow



### Simple quiescent medium



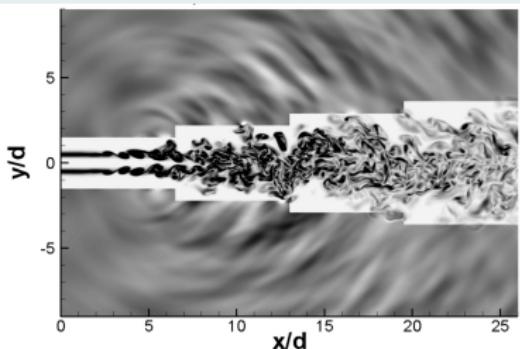
Great but...

These are **equivalent sources**, not true sources!

# Source definition

Silent base flow analogy

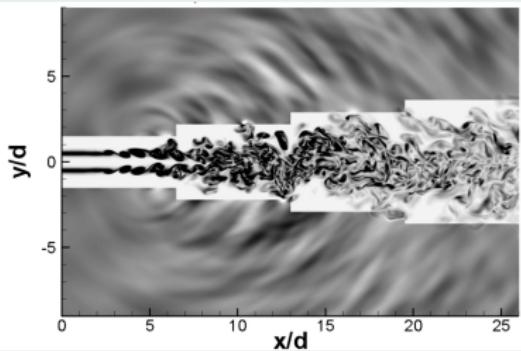
Jet



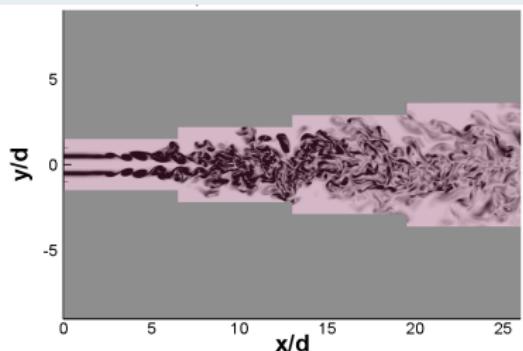
# Source definition

Silent base flow analogy

Jet



Silent jet

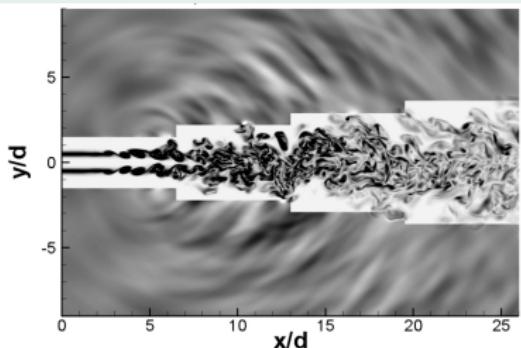


⇒ Filter removing acoustic components

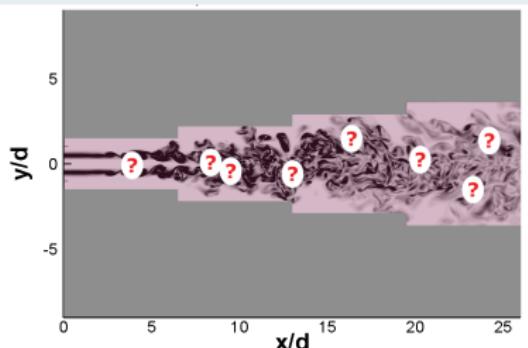
# Source definition

Silent base flow analogy

Jet



Filtered jet

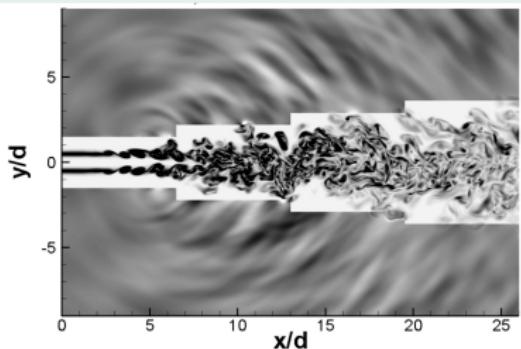


⇒ Source calculation

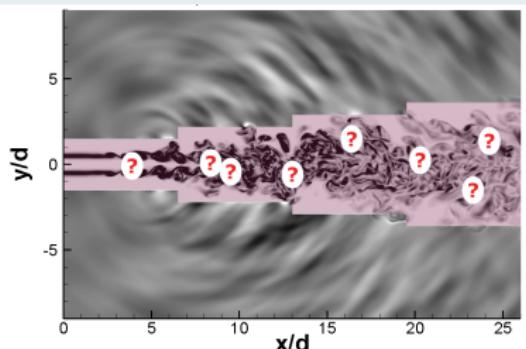
# Source definition

Silent base flow analogy

Jet



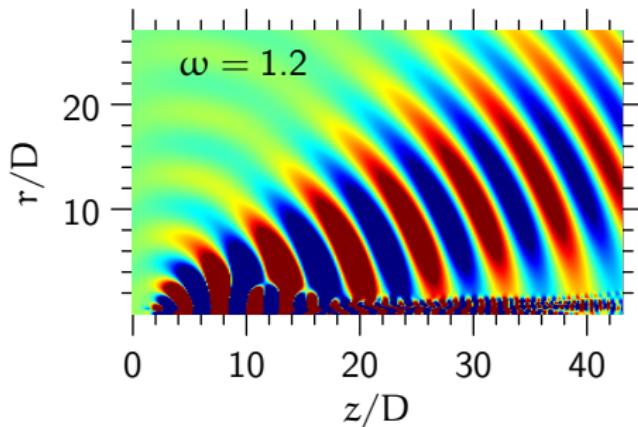
Filtered jet



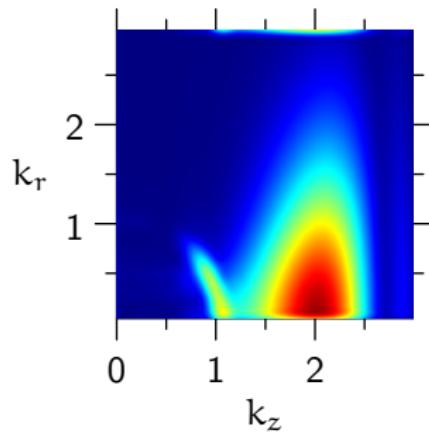
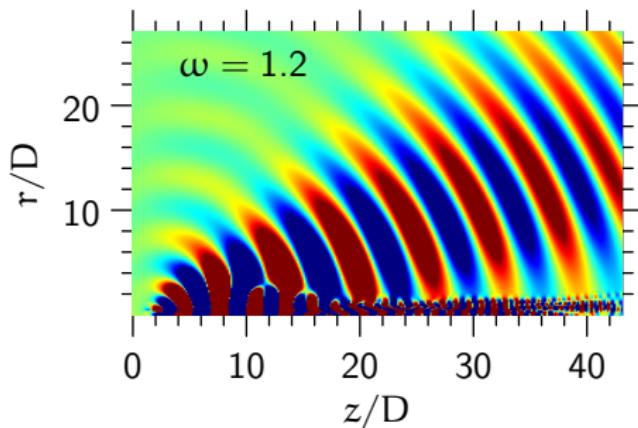
⇒ Sound propagation

Sources are close to the **true sources** of sound.

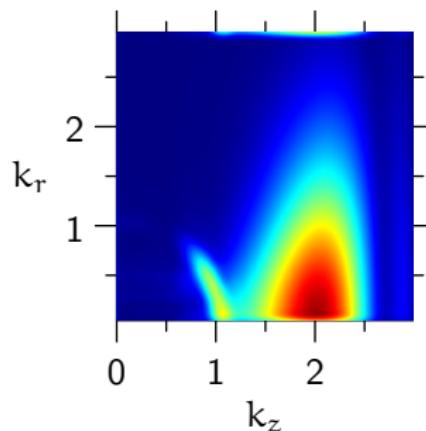
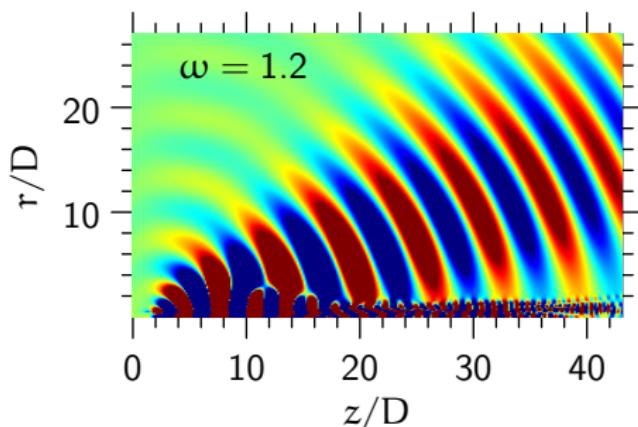
# Flow filtering



# Flow filtering



# Flow filtering



Filtering criterion for “acoustic” waves

Radiating components satisfy  $k = \omega/c_\infty$  in the frequency domain

# Sound sources in a simplified jet

## References

-  S. Sinayoko, A. Agarwal, and Hu Z.  
Flow decomposition and aerodynamic noise generation.  
*Journal of Fluid Mechanics*, 668:335–350, 2011.
-  S. Sinayoko and A. Agarwal.  
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# Sound sources in a simplified jet

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## Achievements

- ① Computed silent base flow
- ② Computed sound sources

# Sound sources in a simplified jet

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- ③ Validated sound sources

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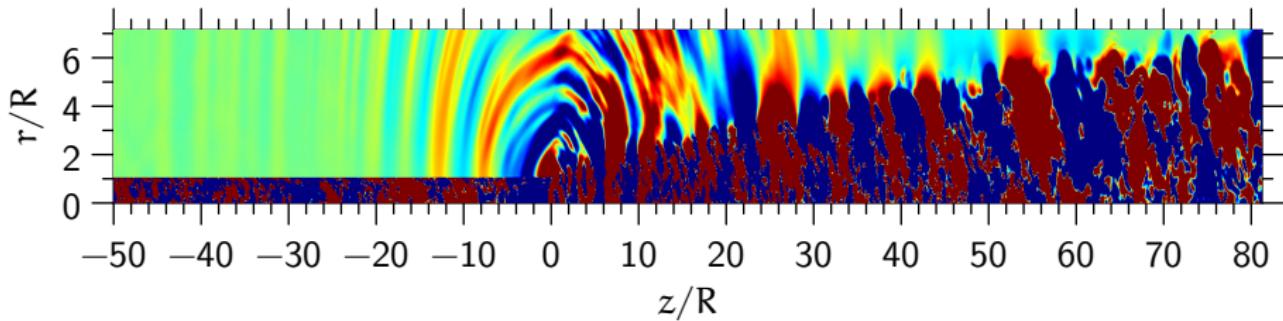
*Journal of the Acoustical Society of America*, 131:1959–1968, 2012.

## Achievements

- ① Computed silent base flow
- ② Computed sound sources
- ③ Validated sound sources
- ④ Dominant source:  $\rho \bar{u}_0 \bar{u}'_z$

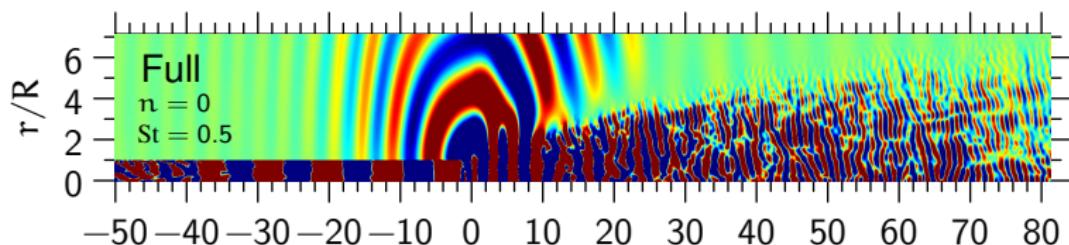
# Sound sources in turbulent jet

Density fluctuations



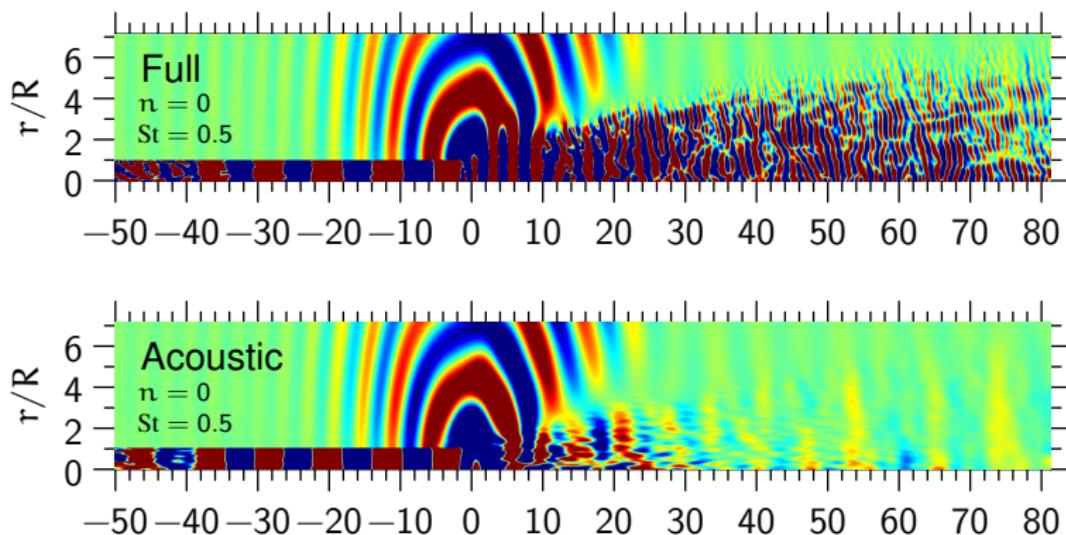
# Sound sources in turbulent jet

Flow decomposition  $n = 0$   $St_D = 0.5$



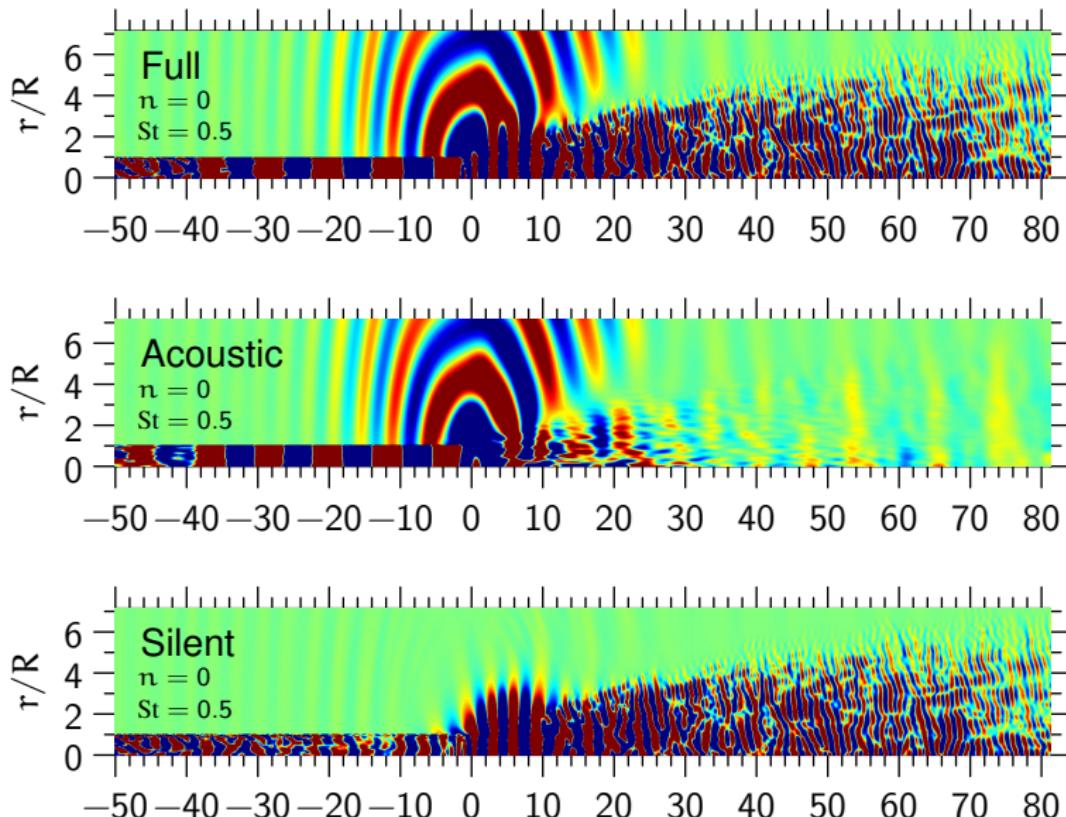
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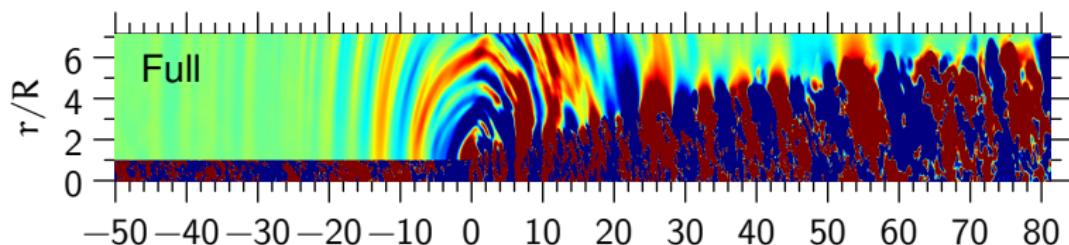
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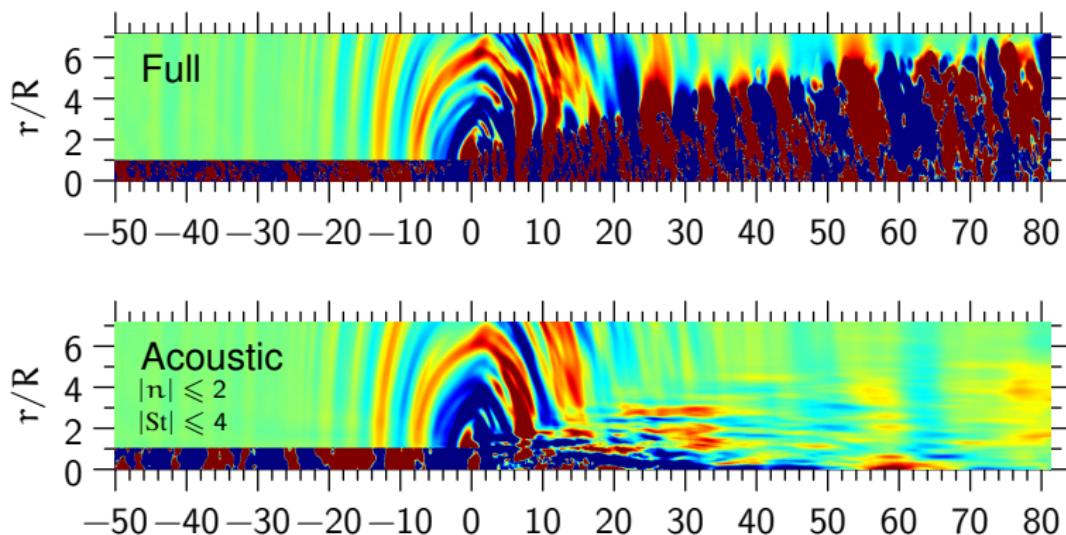
# Sound sources in turbulent jet

Flow decomposition



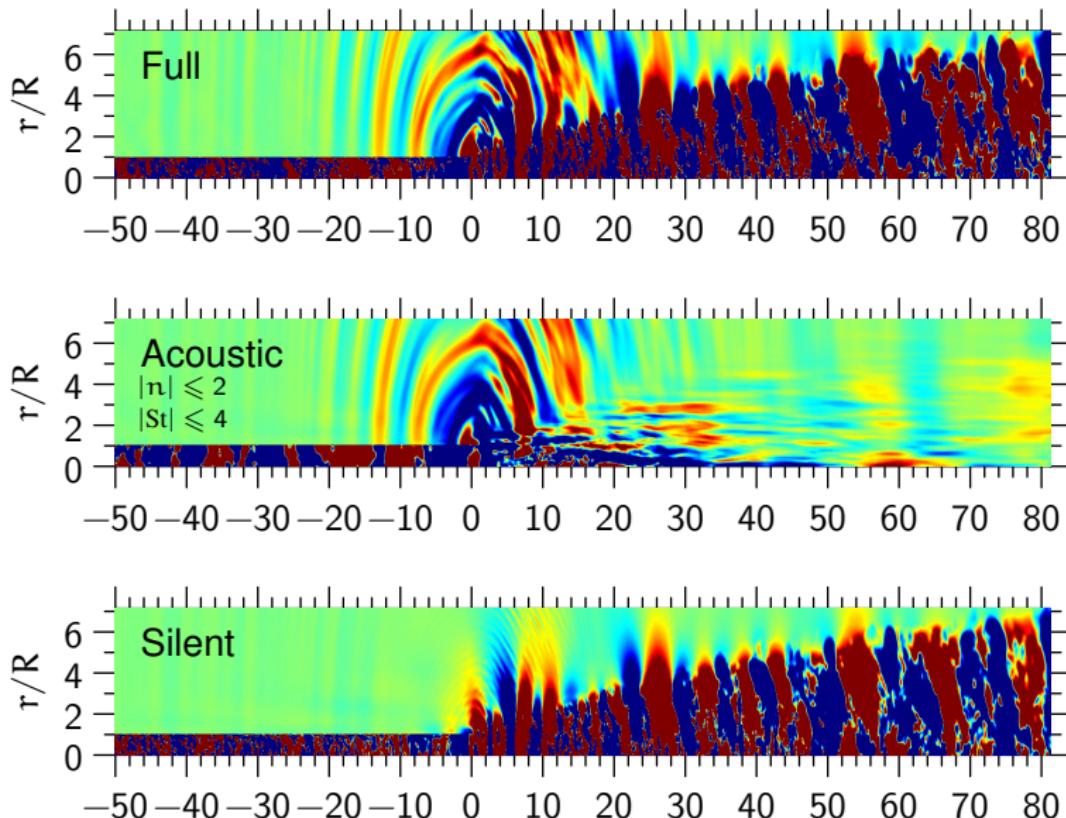
# Sound sources in turbulent jet

Flow decomposition



# Sound sources in turbulent jet

Flow decomposition

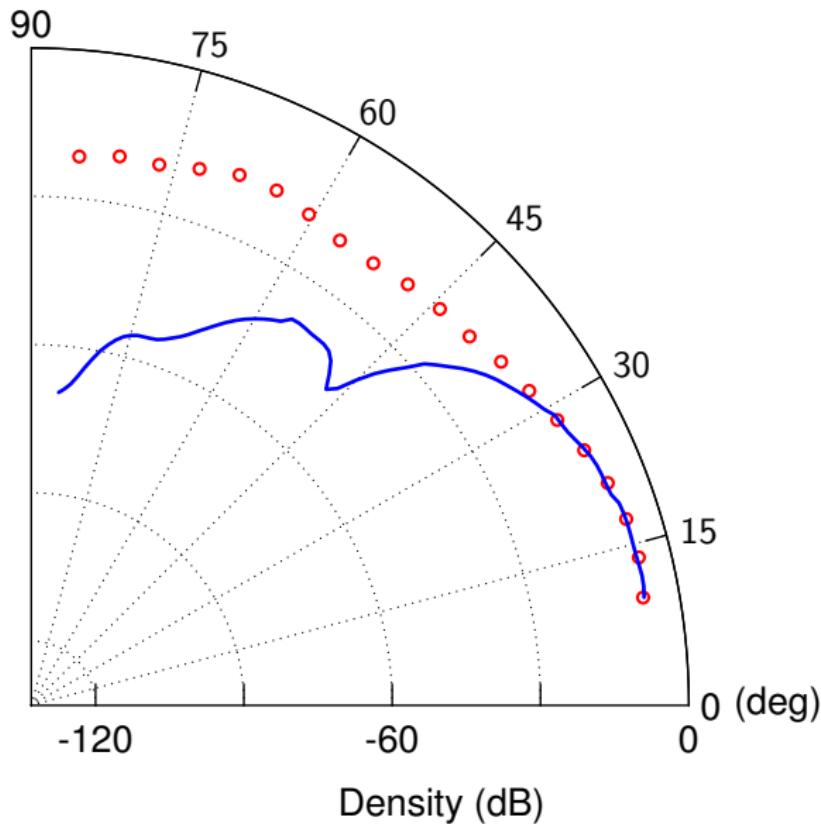


# Sound sources in turbulent jet

Axial source     $n = 0$      $St_D = 0.3$

# Sound sources in turbulent jet

Validation  $n = 0$   $St_D = 0.3$



# Sound sources in turbulent jet

## Reference



S. Sinayoko, A. Agarwal, and R. Sandberg.

Physical sources of sound in laminar andturbulent jets.

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## Achievements

- Silent base flow
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- Validated  $n = 0$     $St = 0.3$

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## Achievements

- Silent base flow
- Computed sound sources
- Validated  $n = 0$     $St = 0.3$

## Future

- $n > 0$     $St \neq 0.3$
- Apply to LES data
- Improve filtering criterion

# Outline

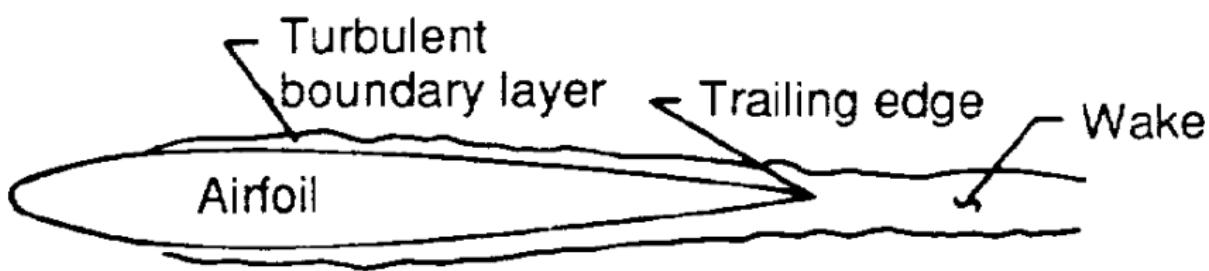
## Trailing edge noise



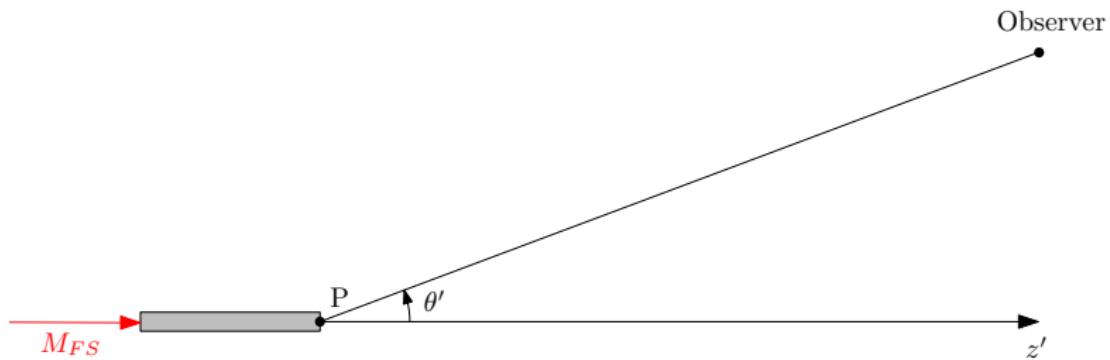
## Acknowledgements

- Mike Kingan
- Anurag Agarwal
- Graham Pullan
- Phil Joseph
- Michel Roger
- Ann Dowling

# Trailing Edge Noise

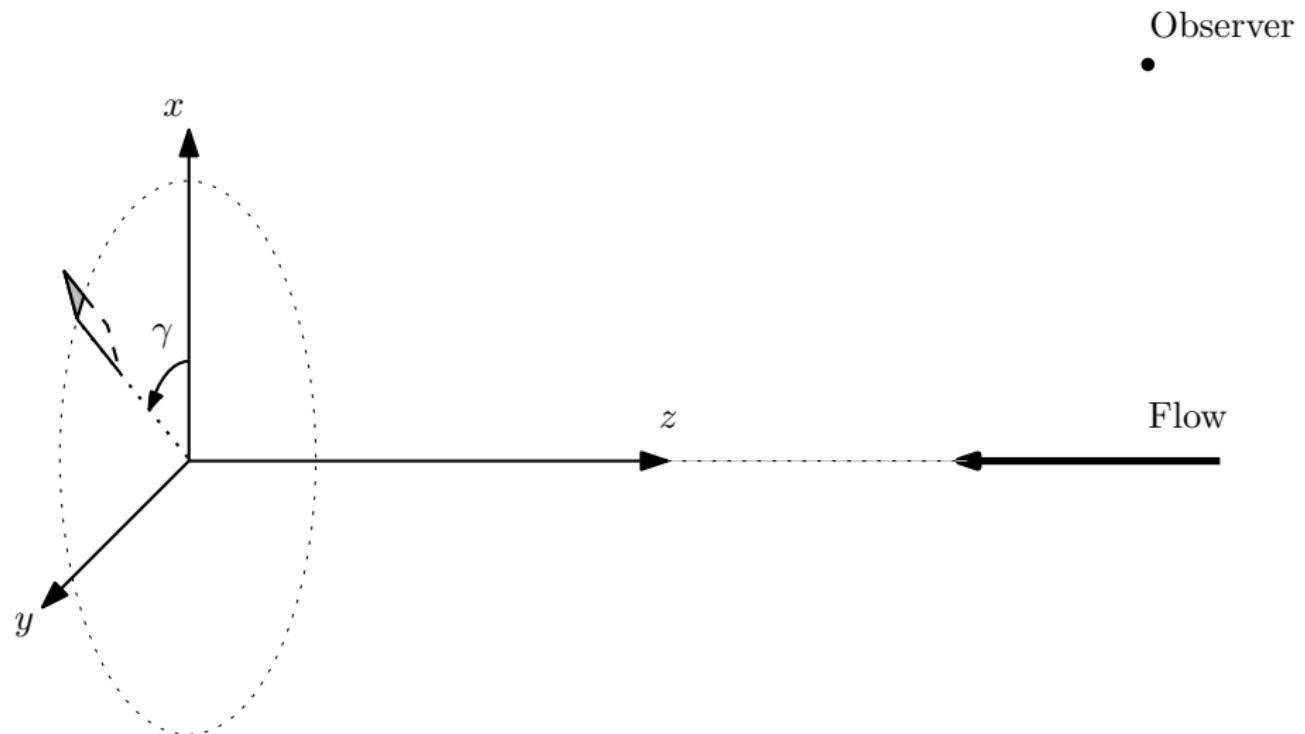


# Isolated airfoil



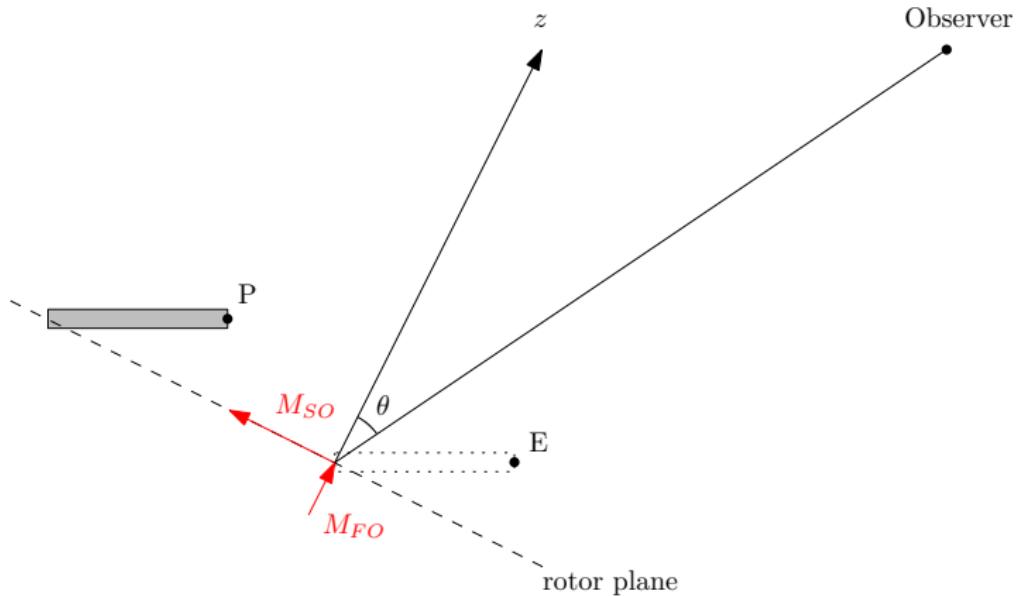
Amiet's (1976) theory predicts noise radiating to observer.

# Rotating airfoil



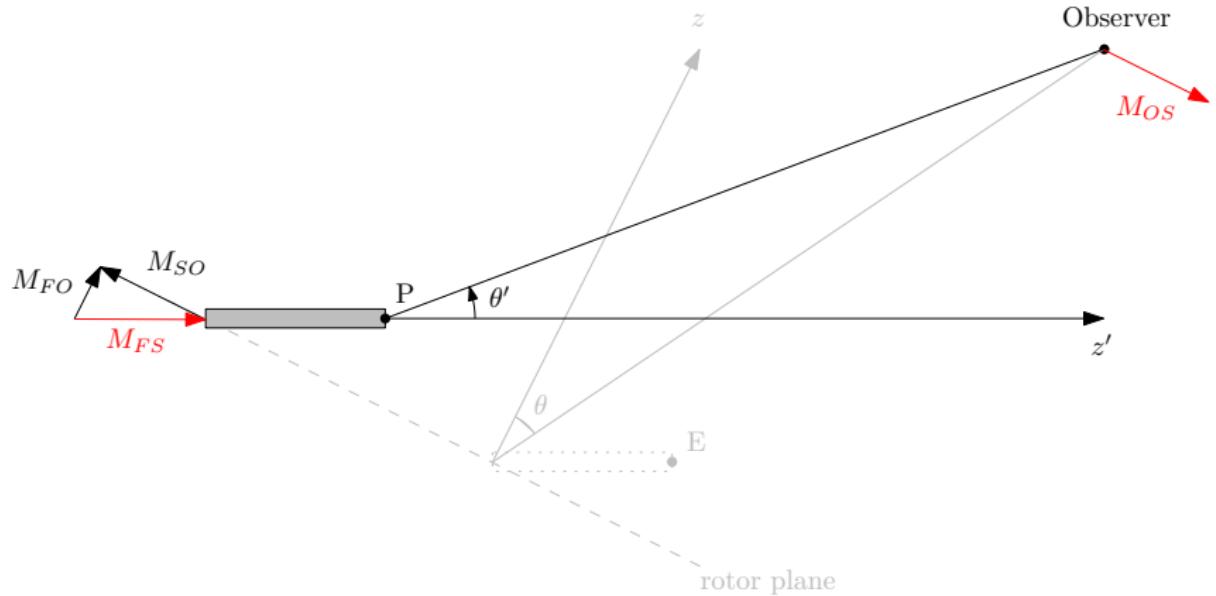
# Change of reference frame

Observer frame



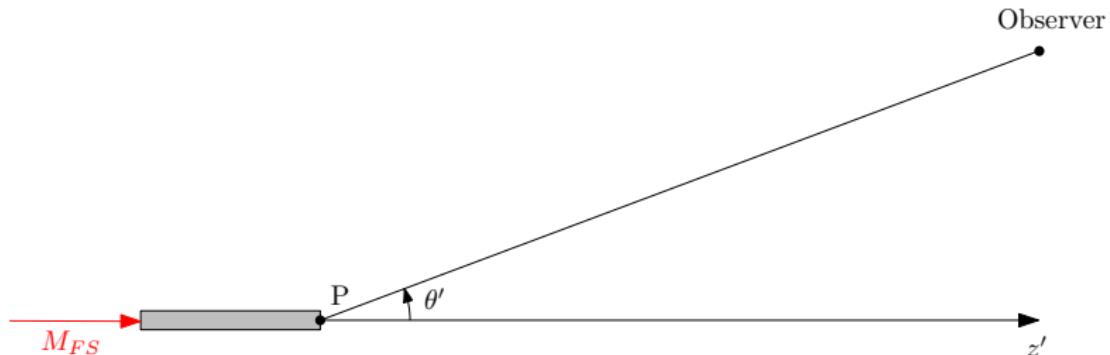
# Change of reference frame

Source frame



# Change of reference frame

Wind tunnel case



## Amiet's formulation(s)

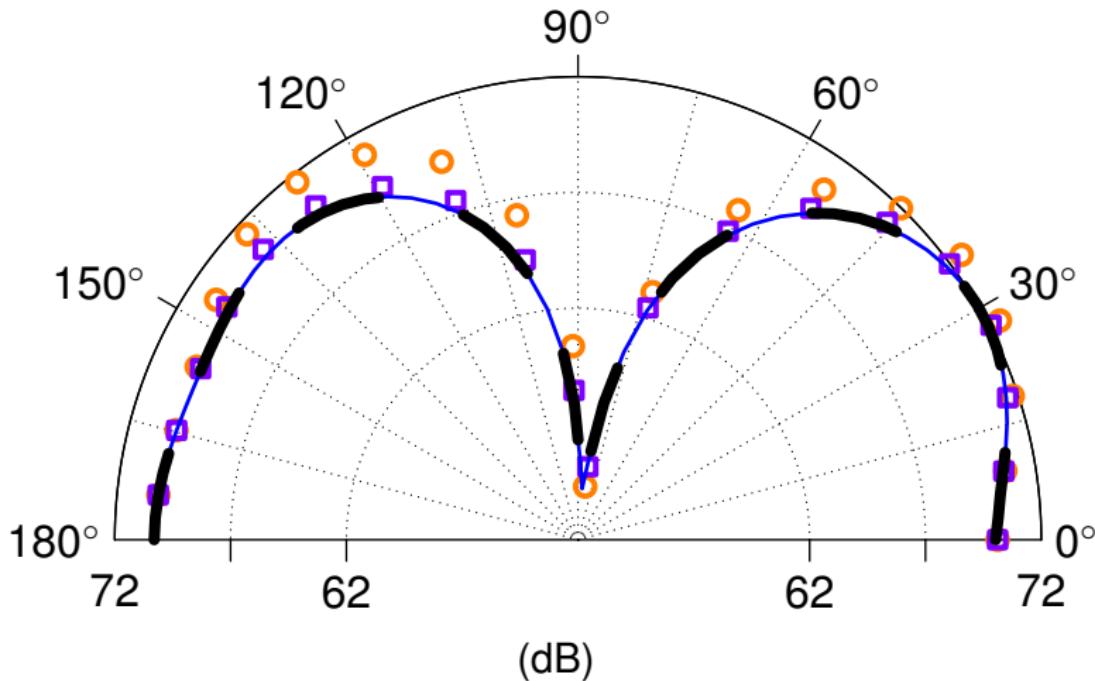
$$S_{\text{pp}}(\omega) = \frac{1}{2\pi} \int_0^{2\pi} \left( \frac{\omega'}{\omega} \right)^e S'_{\text{pp}}(\omega', \gamma) d\gamma$$

Source	Exponent $e$
Amiet (1976)	1
Rozenberg et al (2010)	1
Schlinker and Amiet (1981)	2
Blandeau and Joseph (2011)	-2

Which value of the exponent is correct?

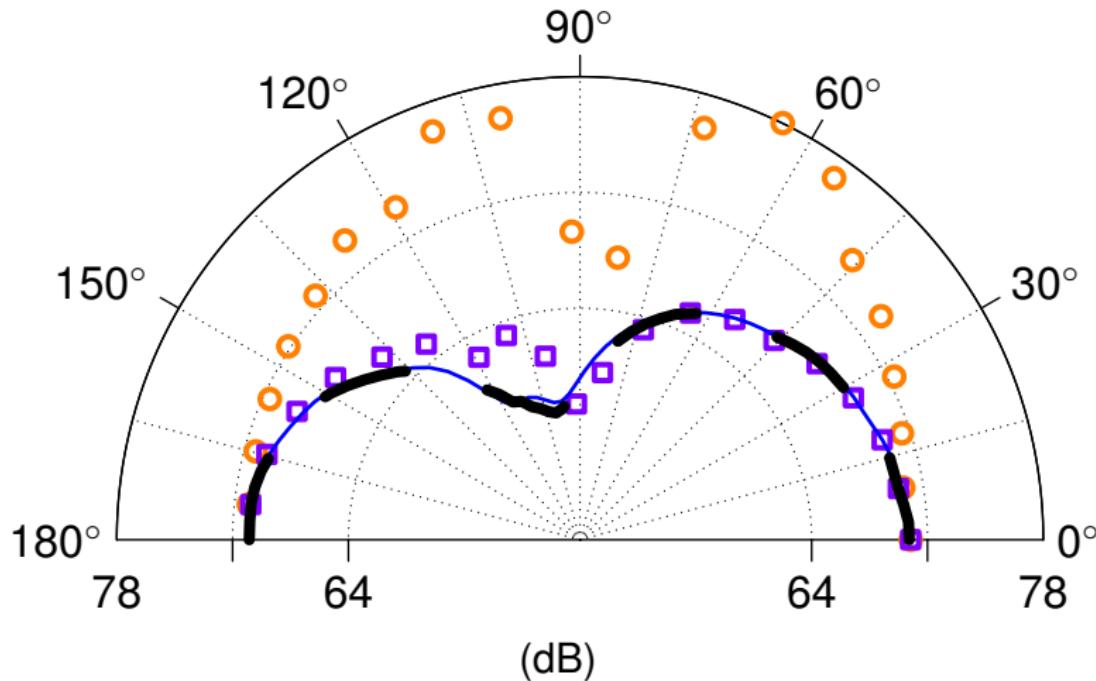
# Wind turbine $k_c = 5$

Sinayoko et al, Amiet  $\alpha = -2$ , Amiet  $\alpha = 1$ , Amiet  $\alpha = 2$



# Open propellor takeoff $k_c = 5$

Sinayoko et al, Amiet  $\alpha = -2$ , Amiet  $\alpha = 1$ , Amiet  $\alpha = 2$



# Trailing edge noise

## Reference

 S. Sinayoko, M. Kingan, and A. Agarwal.  
Trailing edge noise for rotating blades in uniform flow  
*Proc. R. Soc. A*, 2013 469

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## Achievements

- ➊ New exact theory

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## Achievements

- ① New exact theory
- ② Correct value:  $\alpha = 2$

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## Achievements

- ① New exact theory
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- ③ Clarified  $dt' = (\omega/\omega')dt$

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## Achievements

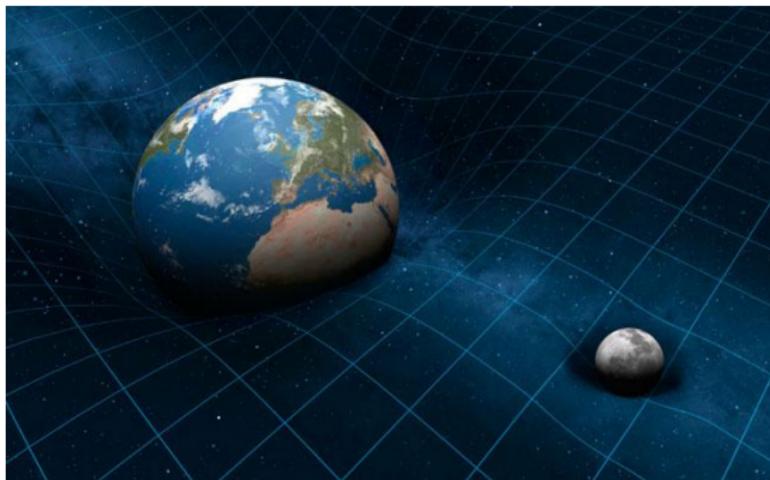
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## Future

- Acceleration effects high Mach
- Wake-vortex interaction

# Outline

## Aeroacoustics and relativity



## Acknowledgements

- Alastair Gregory
- Anurag Agarwal
- Joan Lasenby

# Motivation

## Unanswered questions

- Lorentz transformation comes from relativity (Einsten et al)
- "Lorentz transformation" common in aeroacoustics
- They are not the same thing...?
- More questions: Chapman (2001) and the frequency factor...?
- How about the Prandtl-Glauert transformation?

# Outline

- ① Principle of relativity
- ② Lorentz transform in physics
- ③ Lorentz transform in aeroacoustics
- ④ Acoustic space-time

# Special relativity

Galilean invariance

## Principle of Relativity

Governing equations must independent of the observer frame.

## Example

### Wave Equation

- Stationary frame ( $x, t$ ):

$$\left\{ \nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right\} p = 0$$

# Special relativity

## Galilean invariance

### Principle of Relativity

Governing equations must independent of the observer frame.

### Example

#### Wave Equation

- Stationary frame ( $x, t$ ):  
$$\left\{ \nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right\} p = 0$$
- Moving frame ( $x' = x + Ut, t' = t$ ) (Galilean Transformation):  
$$\left\{ \nabla^2 - \frac{1}{c^2} \left( \frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla \right)^2 \right\} p = 0$$

The convected wave equation violates the principle of relativity!

# Special relativity

Galilean invariance

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### Example

#### Wave Equation

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The convected wave equation violates the principle of relativity!

→ The wave operator is not Galilean invariant.

# Special relativity

Lorentzian invariance

## Principle of Relativity

Governing equations must independent of the observer frame.

# Special relativity

## Lorentzian invariance

### Principle of Relativity

Governing equations must independent of the observer frame.

### Example

#### Wave Equation (revisited)

- Stationary frame ( $x, t$ ):  
$$\left\{ \nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right\} p = 0$$
- Moving frame ( $x'', t''$ ) (Lorentz Transformation):  
$$\left\{ \nabla''^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t''^2} \right\} p = 0$$

# Special relativity

## Lorentzian invariance

### Principle of Relativity

Governing equations must independent of the observer frame.

### Example

#### Wave Equation (revisited)

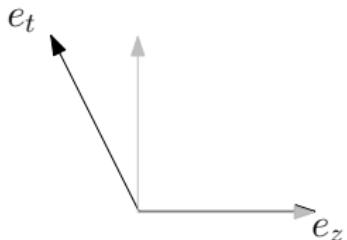
- Stationary frame ( $x, t$ ):  
$$\left\{ \nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right\} p = 0$$
- Moving frame ( $x'', t''$ ) (Lorentz Transformation):  
$$\left\{ \nabla''^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t''^2} \right\} p = 0$$

→ The wave equation is Lorentz-invariant.

# Acoustic space-time

Observer frame

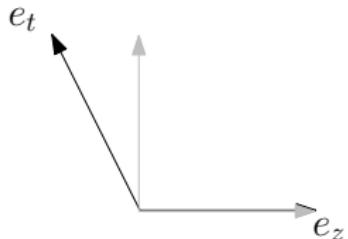
$$\nabla^2 - \frac{1}{c^2} \left( \frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla \right)^2$$



# Acoustic space-time

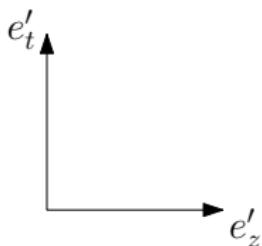
Observer frame

$$\nabla^2 - \frac{1}{c^2} \left( \frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla \right)^2$$



Fluid frame

$$\nabla'^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t'^2}$$



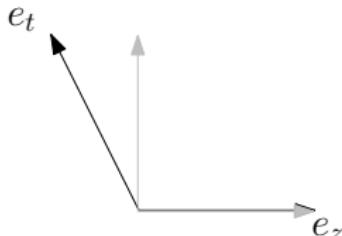
Galilean transformation



# Acoustic space-time

Observer frame

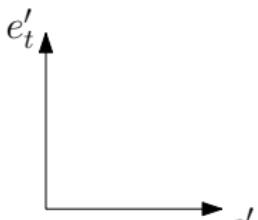
$$\nabla^2 - \frac{1}{c^2} \left( \frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla \right)^2$$



Galilean transformation

Fluid frame

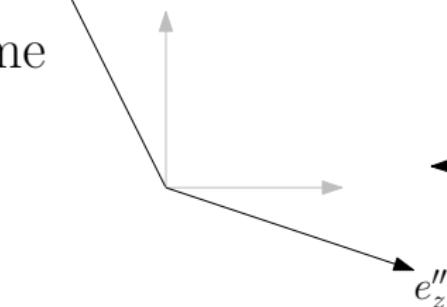
$$\nabla'^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t'^2}$$



Lorentz transformation

Lorentzian frame

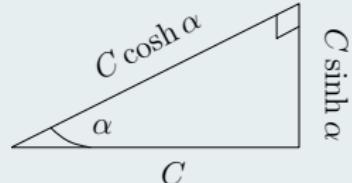
$$\nabla''^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t''^2}$$



# Acoustic space-time

## Cons

- Unfamiliar world

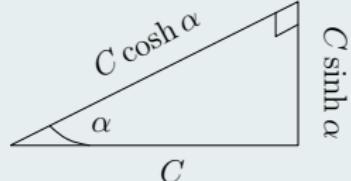


- Need time

# Acoustic space-time

## Cons

- Unfamiliar world



- Need time

## Pros

- Explains the physics (no longer need to be a genius!)
- Geometric interpretation: new intuition and insights ( $dt' = (\omega/\omega')dt$ , Fourier transform)
- Very powerful:
  - Doppler shift
  - Green's function
  - Dispersion relation and null vectors ( $\kappa^2 = 0$ )
  - Scales to more complex flows (e.g. potential)

→ Highly recommended!

# Aeroacoustics and relativity

## Reference

 A. Gregory, S. Sinayoko, A. Agarwal, and J. Lasenby.

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aeroacoustics.

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## Future

- Deal with non-uniform flows
- Find better definition for acoustic waves than  $k = \omega/c_\infty$

# Thank you!

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