

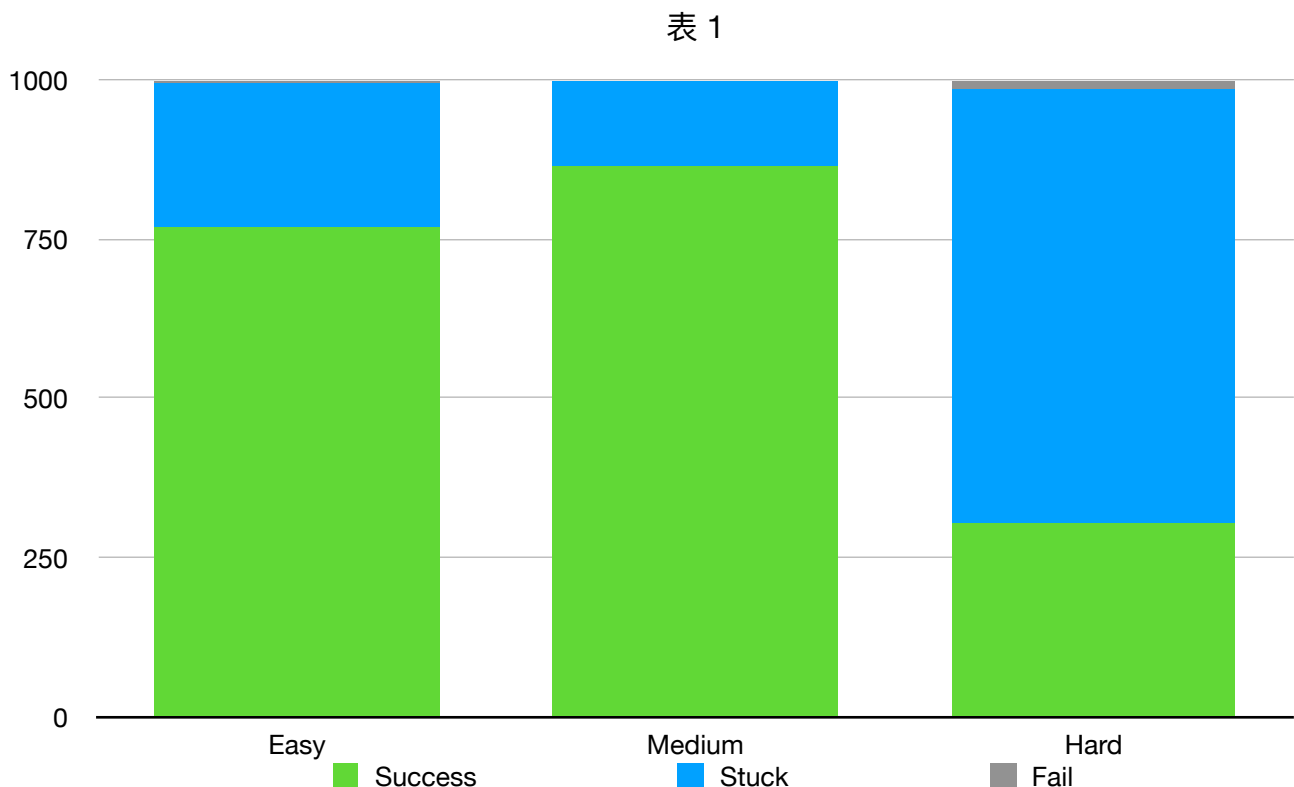
# Introduction to AI

## Programming Assignment #3

### 實驗與結果

#### 盤面難易度與結果比較

表 1 為使用 3 種不同難易程度（Easy、Medium、Hard）的盤面，測試每種盤面難易度時，均隨機產生 1000 組盤面進行測試，進行遊戲後統計 Success、Stuck、Fail 的結果紀錄，表 1 Y 軸為場數，使用線性刻度。



遊戲開始時，均給定  $\text{round}(\sqrt{\# \text{cells}})$  個初始安全位置，Easy 盤面大小為  $9 \times 9$ ，有 10 個地雷；Medium 盤面大小為  $16 \times 16$ ，有 25 個地雷；Hard 盤面大小為  $30 \times 16$ ，有 75 個地雷（因使用 Spec 的要求而放置 99 個地雷時，遊戲實在太容易 Stuck，故改為 75 個地雷進行測試）。

從表 1 可以看出，遊戲在難易程度為 Medium 時，最容易成功解出，其 Success 比率約為 0.86，在難易程度為 Easy 時，其 Success 比率約為 0.76，難易程度為 Hard 時，最容易 Stuck，其 Success 比率僅約為 0.3。

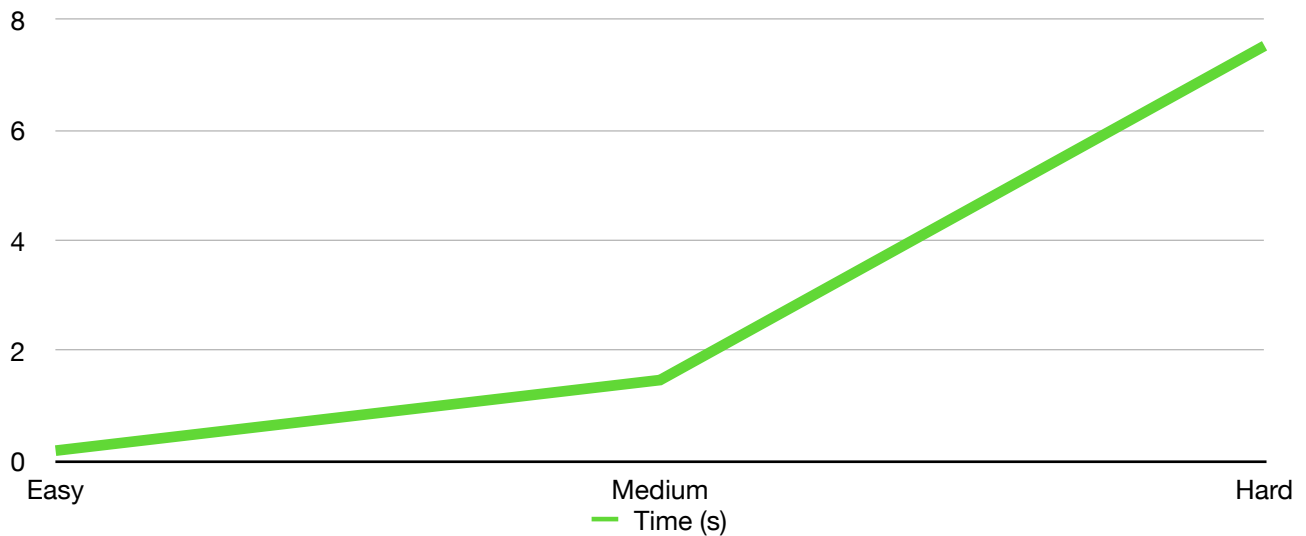
表 1 實驗中，若遞迴 3 次仍無法產生新的步數，即判定為 Stuck，另外，其所發生的極少數 Fail，大都是因一些並排的地雷相鄰圍繞行成一個封閉區域，使得遊戲時無法探索封閉區域內的 Hints，也無法對封閉區域中的位置產生相關的 Clause，導致即便 KB 內已無任何 Clause 時，遊戲仍尚未完成。

以下其他實驗若無特別說明，則其盤面大小及地雷數量皆與表 1 中的實驗配置相同。

## 盤面難易度與時間比較

表 2 為在表 1 實驗中，成功解出盤面後，統計其時間，取其結果之平均時間紀錄。表 2 Y 軸為時間，使用線性刻度，單位為秒。

表 2

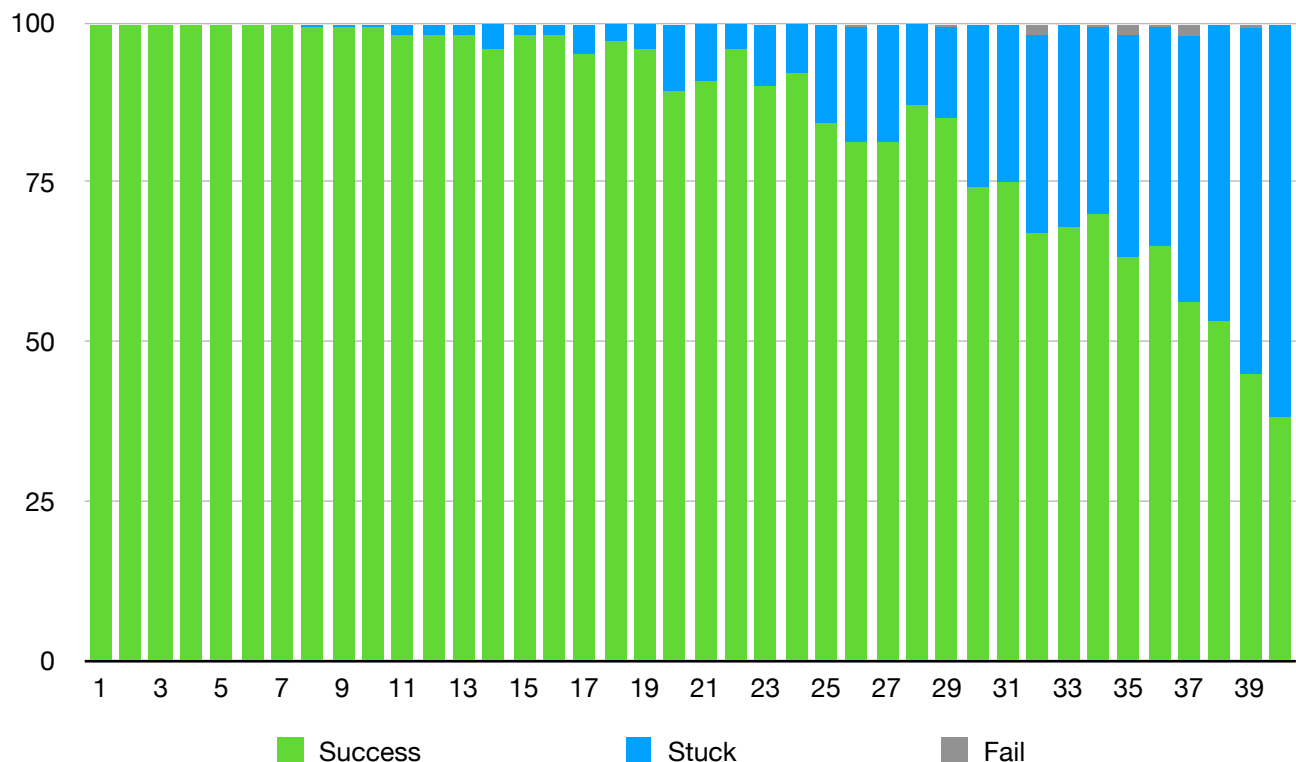


由表 2 可以看出，盤面難易度增加時，所需時間亦增加。

## 地雷數量與結果比較

表 3 為使用 16\*16 的盤面大小，分別測試在盤面上放置 1 個至 40 個地雷，觀察其解出所需時間。測試每個地雷數量時，均隨機產生 100 組盤面進行測試，進行遊戲後統計 Success、Stuck、Fail 的結果紀錄，表 3 X 軸為地雷數量，Y 軸為場數，使用線性刻度。

表 3

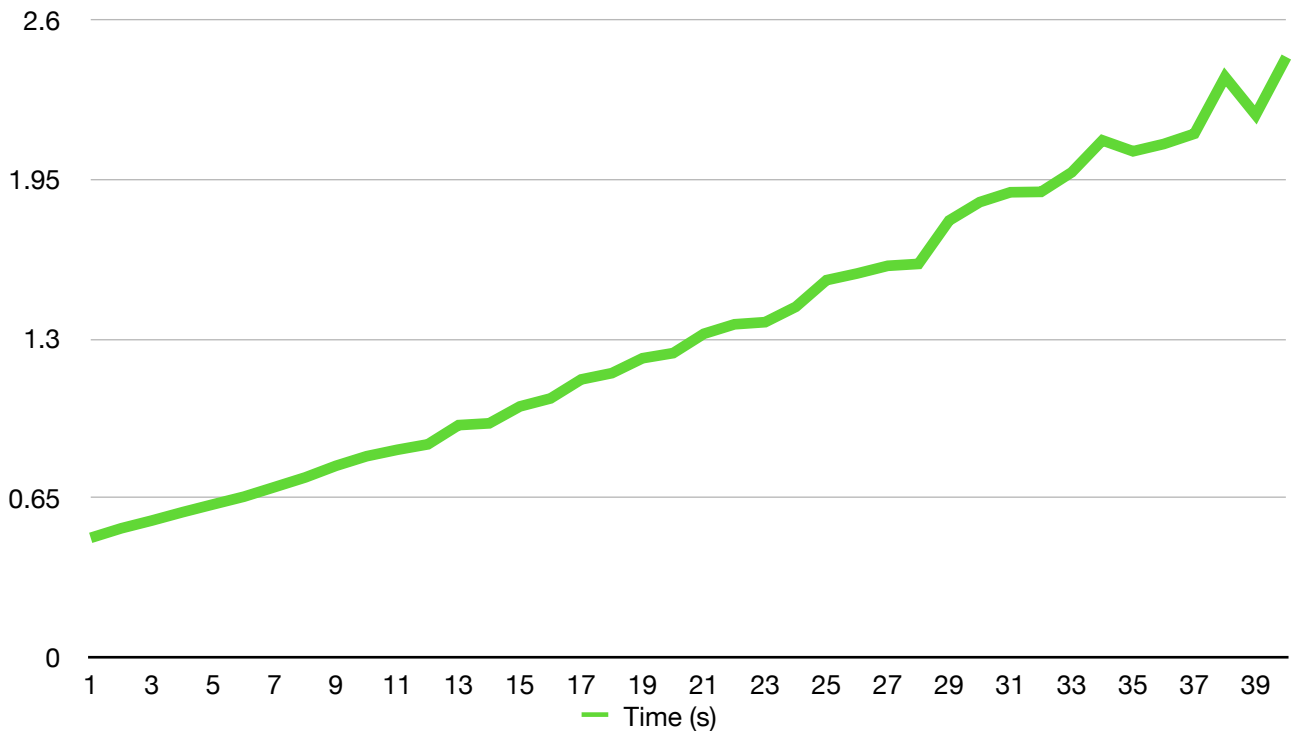


在表 3 實驗中，最初均給定  $\text{round}(\sqrt{\# \text{cells}})$  個初始安全位置，從表 3 可以看出，當地雷數量增加時，遊戲越來越容易發生 Stuck 的情形，我認為這是由於在確定是地雷的位置上，無法得知該位置的 Hints 值，也就是說，當地雷數量越多，所能取得的 Hints 數量就越少，導致越來越容易 Stuck。

## 地雷數量與時間比較

表 4 為在表 3 實驗中，成功解出盤面後，統計其時間，取其結果之平均時間紀錄。表 3 X 軸為地雷數量，Y 軸為時間，使用線性刻度，單位為秒。

表 4



從表 4 可以看出，即便是盤面大小皆相同，當地雷數量越來越多時，所需時間仍成線性成長。我認為這是由於地雷數量越多，所能取得的 Hints 數量就越少，使得需要做更多的 Pairwise matching 才能產生 Single literal 的原因所導致。

## 所學

透過本次實驗我所學以下幾點：

1. 利用物件導向程式設計，以 Python 實作互動遊戲之 Framework。
2. 了解 Propositional logic、Resolution、Matching 等等技巧的運作原理、特性以及優缺點。
3. 透過比較不同的盤面難易程度來體會時間及空間複雜度對於 Propositional logic 的影響。
4. 將實驗結果整理、列表並使人易於閱讀。

## 討論

### 使用 First order logic

定義 Relations :  $\text{hint\_eq\_around\_mines}(x)$  表示  $x$  的 Hints 和周圍已知的地雷數量相同、 $\text{adjacent}(x, y)$  表示  $x$ 、 $y$  相鄰、 $\text{mine}(x)$ ,  $\text{safe}(x)$ ,  $\text{unmarked}(x)$  表示  $x$  的狀態。

1. 對於所有安全的位置  $x$ ，若其 Hints 和周圍已知的地雷數量相同，則與  $x$  相鄰的所有未知位置為安全。

$$\forall x \forall y \text{ safe}(x) \wedge \text{hint\_eq\_around\_mines}(x) \wedge \text{adjacent}(x, y) \wedge \text{unmarked}(y) \Rightarrow \text{safe}(y)$$

2. 對於所有安全的位置  $x$ ，若其 Hints 和周圍已知的地雷數量不相同，則與  $x$  相鄰的未知位置中存在地雷。

$$\forall x \exists y \text{ safe}(x) \wedge \neg \text{hint\_eq\_around\_mines}(x) \wedge \text{adjacent}(x, y) \wedge \text{unmarked}(y) \Rightarrow \text{mine}(y)$$

以上為兩個使用 First order logic 的 Sentence 實例，若 Sentence 完整，我推測使用 First order logic 會比使用 Propositional logic 更有效率。

### Forward chaining 與 Backward chaining

使用 Forward chaining 時，先將 KB 做成圖，其中每個節點都是一個 Implication，遞迴計算每個節點當中已被證實的 Fact，當布標節點被標示為 1 時，即代表目標亦成為 Fact 了，整個過程即為 Horn clause implication 的拆除。

使用從目標節點出發，遞迴檢視可以 Imply 目標的 Horn clause，直到沒有 Horn clause 之後，再檢查實際是否能推到目標。

Backward chaining 中的 Goal-driven 特性使得其與 Forward chaining 相比更有效率。

### Stuck 時的猜測

如果剩餘未解位置不多，可以嘗試加入 Global constraint 進入 KB，使用地雷數量與剩餘為標記的位置來增加線索。

若無法使用 Global constraint 或使用後無效，可使用表決機制，即用 KB 中的 Clause 裡每個 Literal 來投票，假如一個 Literal 指出位置 A 為安全，則 A 加 1 票，若不安全則減 1 票，最後統計票高者進行猜測並選擇。

### 使用 Search

我認為邏輯和搜尋可以同時並進，也就是每次遞回時先使用邏輯標示出已經確定的位置，然後避開這些位置進行搜尋。如此一來，搜尋時會減少搜索不必要的、已被推定為安全或是地雷的位置，可以減少搜尋所需的時間和空間，同時也可避免在遊戲初始時，無意義的產生很多 Clause 進行無用的 Matching。

## 疑問與探討

1. 在盤面難易度為 Hard 時，Spec 所要求的地雷數量為 99，但當我使用這項配置時，遊戲非常容易進入 Stuck 狀態，雖然不排除是我的程式有錯誤，但我有將盤面狀態印出並逐一比對，也確認真的是 Stuck，因此很疑惑為何會有這樣的狀況發生。此外，即便是將原本 99 個地雷的配置修改為 75 個地雷，成功率依然只有如表 1 所標示的三成左右，遠遠不如難易度 Medium 近九成的成功率。
2. 在 Spec 中有提到可以將  $\text{round}(\sqrt{\#cells})$  個初始安全位置的數量加以改變，觀察遊戲成功機率的變化。而我認為：其實初始位置最重要的是要有 0 的 Hints，如果初始位置完全沒有 Hints 為 0，則遊戲有極高的可能性會一開局就進入 Stuck 狀態。然而， $\text{round}(\sqrt{\#cells})$  因涉及根號，因此不好改變與掌握，所以我稍作變形，改做了表 3 和表 4 的實驗，我認為其原理相當，都是在於探討為 0 的 Hints 在初始安全位置中出現的機率，機率越大，越不容易 Stuck，反之就越容易。

## 未來發想

在實驗的過程中，如果印出 KB 來做觀察，會發現單純使用 Propositional logic 時，其所產生的很多 Clause 其實是無用的，但是這個 Clause 會一直存在 KB 當中，不斷的與其他 Clause 進行毫無用處的 Matching，最後才被移除。而這樣的狀況往往是因為有一個不為 0 的 Hints，其位置的周圍完全沒有其他 Hints 或已被標示為地雷的位置，則此 Hints 在這樣的情形之下，對於整個遊戲來說是毫無用處的。因此，為來可考慮先暫時排除將這樣的 Hints 所產生的 Clause 列入 KB，直到其周圍有位置被解出，如此一來可以免去很多不必要的 Matching，我認為或許可以增加遊戲的效率。

# Appendix

## Structure

- minesweeper.py
- agent.py
- logic.py
- board.py
- test.py

### minesweeper.py

```
import time
from board import Board, Action
from logic import Literal, Clause
from agent import Agent

class Result():
    def __init__(self, status, stuck, play_time):
        self.status = status
        self.stuck = stuck
        self.play_time = play_time

class MineSweeper():
    def __init__(self, difficulty, mines = None):
        self.board = Board(difficulty, mines)
        self.agent = Agent()
        self.debug = False

    def play(self, debug = None):
        if debug is not None:
            self.debug = debug
        start_time = time.time()
        stucked = False
        status = ''

        # Initial game
        for pos in self.board.init_safe_pos:
            new_clause = Clause( [-Literal(pos)] )
            self.agent.add_clause_to_KB(new_clause)

        while True:
            # Print current board
            if self.debug:
                self.board.print_current_board()
                print()

            # Take action
            action = self.agent.take_action(self.board)
```

```

# Game flow
if 'query' == action.action:
    new_hint = self.board.query(action.position)
    if new_hint == -3:
        if self.debug:
            print('Fail on', action.position)
            break
    self.agent.new_hint(action.position, new_hint,
self.board)
elif 'mark_mine' == action.action:
    self.board.mark_mine(action.position)
elif 'done' == action.action:
    break
elif 'give_up' == action.action:
    stucked = True
    if self.debug:
        print(self.agent.KB0)
        for c in self.agent.KB:
            print(c)
        print('Stucked')
    break

# Statistics
play_time = (time.time() - start_time)
if self.board.check_success():
    status = 'Success'
else:
    status = 'Fail'

if self.debug:
    # Results
    print('====Result====')
    self.board.print_current_board()
    print()
    print('====Answer====')
    self.board.print_answer_board()
    print('====Status====')
    print(status)
    print('Duration:', play_time, 'sec')

return Result(status, stucked, play_time)

if __name__ == '__main__':
    # Examples
    game = MineSweeper('easy')
    game.play(debug = True)

```

**agent.py**

```

import time
import copy, itertools
from board import Action, Board
from logic import Literal, Clause

class Agent():
    def __init__(self):
        self.KB0 = []
        self.KB = []

    def add_clause_to_KB(self, new_clause):
        if not new_clause.is_empty():
            # Do resolution of the new clause with all the clauses
            in KB0
            for c in self.KB0:
                tmp_clause, co_literal_count =
self.resolution(new_clause, c)
                if tmp_clause > new_clause:
                    new_clause = tmp_clause

            # Check for identification and subsumption with all the
            clauses in KB
            is_useable = not (new_clause.is_empty())
            reduntents = []
            for c in self.KB:
                if not is_useable:
                    break
                if new_clause <= c:
                    is_useable = False
                if new_clause > c:
                    reduntents.append(c)
            if is_useable:
                self.KB.append(new_clause)

            for r in reduntents:
                self.remove_clause_from_KB(r)

    def remove_clause_from_KB(self, clause):
        try:
            self.KB.remove(clause)
        except:
            pass

    def global_constraint(self, b):
        unmarked, marked_mine = b.global_constraint_check()
        self.gen_clause(unmarked, marked_mine, b.mines)

    def new_hint(self, position, hint, b):
        around_unmarked = b.around_unmarked_position(position)

```



```

        around_marked_mine =
b.around_marked_mine_position(position)
        self.gen_clause(around_unmarked, around_marked_mine, hint)

def gen_clause(self, unmarked, marked_mine, hint):
    m = len(unmarked)
    n = hint - len(marked_mine)

    if n == m:
        # Insert the m single-literal positive clauses to KB
        for au in unmarked:
            new_clause = Clause( [Literal(au)] )
            self.add_clause_to_KB(new_clause)
    elif n == 0:
        # Insert the m single-literal negative clauses to KB
        for au in unmarked:
            new_clause = Clause( [-Literal(au)] )
            self.add_clause_to_KB(new_clause)
    elif m > n > 0:
        # General cases
        # Generate CNF clauses and add them to the KB
        all_positive = list(itertools.combinations(unmarked,
m-n+1))
        all_negative = list(itertools.combinations(unmarked,
n+1))

        for comb in all_positive:
            literals = []
            for au in comb:
                literals.append(Literal(au))
            new_clause = Clause(literals)
            self.add_clause_to_KB(new_clause)

        for comb in all_negative:
            literals = []
            for au in comb:
                literals.append(-Literal(au))
            new_clause = Clause(literals)
            self.add_clause_to_KB(new_clause)

    else:
        # For debugging
        # print('Something is wrong')
        # print(position, hint, m, n, len(unmarked),
len(marked_mine))
        pass

def resolution(self, clause_a, clause_b):
    co_literal_count = 0
    new_clause = Clause([])
    for l in clause_a.literals:
        literal = l

```

```

        new_clause.literals.append(literal)
    for l in clause_b.literals:
        literal = l
        co_literal = -l
        if co_literal in new_clause.literals:
            new_clause.literals.remove(co_literal)
            co_literal_count += 1
        elif literal not in new_clause.literals:
            new_clause.literals.append(literal)
    return new_clause, co_literal_count

def remain_literals_matching(self, moved_clause,
remain_clause):
    redundant_clause = None
    add_clause = None

    literal = moved_clause.literals[0]
    co_literal = -moved_clause.literals[0]

    if co_literal in remain_clause.literals:
        new_clause = copy.deepcopy(remain_clause)
        redundant_clause = remain_clause
        new_clause.literals.remove(co_literal)
        add_clause = new_clause
    elif literal in remain_clause.literals:
        redundant_clause = remain_clause

    return redundant_clause, add_clause

def pairwise_matching(self, clause_a, clause_b):
    # Check for duplication or subsumption first
    # Keep only the more strict clause.
    if len(clause_a.literals) > 2 and len(clause_b.literals) >
2:
        return
    if not (clause_a in self.KB and clause_b in self.KB):
        return

    if clause_a <= clause_b:
        self.remove_clause_from_KB(clause_a)
        return
    elif clause_a >= clause_b:
        self.remove_clause_from_KB(clause_b)
        return

    # Do resolution
    new_clause, co_literal_count = self.resolution(clause_a,
clause_b)

    if co_literal_count == 1:
        # Only one pair of complementary literals:
        self.remove_clause_from_KB(clause_a)

```

```

        self.remove_clause_from_KB(clause_b)
        self.add_clause_to_KB(new_clause)
    else:
        # No or more than one pairs of complementary literals
        # Do nothing
        pass

def take_action(self, b):
    # Make a query
    no_action_count = 0

    while len(self.KB):
        if no_action_count == 3:
            return Action('give_up')
        has_single_literal = False

        for c in self.KB:
            if c.is_single_literal():
                # Single-lateral clause in the KB
                # Mark this cell as safe or mined
                clause = c

                # Move that clause to KB0
                self.remove_clause_from_KB(clause)
                self.KB0.append(clause)

                # Process the matching of that clause to all
the remaining clauses in the KB
                reduntents = []
                adds = []
                for remain_c in self.KB:
                    redundant_clause, add_clause =
self.remain_literals_matching(clause, remain_c)
                    if redundant_clause:
                        reduntents.append(redundent_clause)
                    if add_clause:
                        adds.append(add_clause)
                for r in reduntents:
                    self.remove_clause_from_KB(r)
                for a in adds:
                    self.add_clause_to_KB(a)

                if clause.is_safe():
                    return Action('query',
clause.literals[0].position)
                    no_action_count = 0
                else:
                    return Action('mark_mine',
clause.literals[0].position)
                    no_action_count = 0

```

```

        has_single_literal = True

    if not has_single_literal:
        no_action_count += 1
        # tmp_KB = list(self.KB)

        # Apply pairwise matching of the clauses in the KB
        # Only match clause pairs where one clause has
        only at most two literals
        for comb in list(itertools.combinations(self.KB,
2)):
            if comb[0] in self.KB and comb[1] in self.KB:
                self.pairwise_matching(comb[0], comb[1])

            # if tmp_KB == self.KB:
            #     # self.global_constraint(b)
            #     if tmp_KB == self.KB:
            #         return Action('give_up')

        # if len(self.KB) == 0:
        #     unmarked, marked_mine = global_constraint_check
        #     if len(unmarked):
        #         self.global_constraint(b)

    return Action('done')

```

## logic.py

```

class Literal():
    def __init__(self, position, positive = True):
        self.positive = positive
        self.position = position

    def __neg__(self):
        return Literal(self.position, not self.positive)

    def __eq__(self, other):
        return self.positive == other.positive and self.position
== other.position

    def __ne__(self, other):
        return not self.__eq__(other)

    def __repr__(self):
        return ('' if self.positive else '-') + str(self.position)

class Clause():
    def __init__(self, literals):
        self.literals = literals

```

```

def __eq__(self, other):
    if not len(self.literals) == len(other.literals):
        return False
    for l in self.literals:
        if l not in other.literals:
            return False
    return True

def __gt__(self, other):
    # Return True when self is stricter than other
    if not len(self.literals) < len(other.literals):
        return False
    for l in self.literals:
        if l not in other.literals:
            return False
    return True

def __ge__(self, other):
    if not len(self.literals) <= len(other.literals):
        return False
    for l in self.literals:
        if l not in other.literals:
            return False
    return True

def __lt__(self, other):
    if not len(other.literals) < len(self.literals):
        return False
    for l in other.literals:
        if l not in self.literals:
            return False
    return True

def __le__(self, other):
    if not len(other.literals) <= len(self.literals):
        return False
    for l in other.literals:
        if l not in self.literals:
            return False
    return True

def __repr__(self):
    ret = ''
    for l in self.literals:
        ret += (' v ' + str(l)) if ret else str(l)
    return '(' + ret + ')'

def is_empty(self):
    return len(self.literals) == 0

def is_single_literal(self):
    if len(self.literals) == 1:

```

```

        return True
    return False

def is_safe(self):
    if len(self.literals) == 1:
        return not self.literals[0].positive
    return False

if __name__ == '__main__':
    # Examples
    a = Literal((5, 3))
    b = -Literal((2, 4))
    c = Literal((6, 13))
    d = -Literal((2, 1))
    e = Literal((7, 0))

    clause1 = Clause([a, b, c])
    clause2 = Clause([a, b, c, d])
    clause3 = Clause([a, b, c, d, e])
    clause4 = Clause([a, b, c, d, e])

    print(clause1 < clause2)
    print(clause3 < clause1)
    print(clause1 < clause2)
    print(clause1 < clause4)
    print(clause1 > clause4)

```

## board.py

```

import copy, math, random

class Action:
    def __init__(self, action, position = None):
        self.action = action
        self.position = position

class Board():
    def __init__(self, difficulty, mines = None):
        init_param = {}
        if 'easy' == difficulty:
            init_param = {'size': (9, 9), 'mines': mines if mines
else 10}
            elif 'medium' == difficulty:
                init_param = {'size': (16, 16), 'mines': mines if
mines else 25}
            elif 'hard' == difficulty:
                init_param = {'size': (30, 16), 'mines': mines if
mines else 75}

```

```

self.x = init_param['size'][0]
self.y = init_param['size'][1]
self.mines = init_param['mines']
self.hints = []
self.marked = []

# Randomly generate a new board
positions = []
for j in range(self.y):
    for i in range(self.x):
        positions.append((i, j))

# Select mine and initial safe positions
init_safe_cells = round(math.sqrt(self.x * self.y))
sltd_pos = random.sample(positions, self.mines +
init_safe_cells)
mine_pos = sltd_pos[0:self.mines]
self.init_safe_pos = sltd_pos[self.mines:]
# print(mine_pos)
# print(self.init_safe_pos)

# Generate hints
for i in range(self.x):
    for j in range(self.y):
        if j == 0:
            self.hints.append([])
            self.marked.append([])
        if (i, j) in mine_pos:
            self.hints[i].append(-3)
        else:
            around = self.around_position((i, j))
            mines_count = 0
            for a in around:
                if a in mine_pos:
                    mines_count += 1
            self.hints[i].append(mines_count)
            self.marked[i].append(0)

def query(self, position):
    x = position[0]
    y = position[1]
    self.marked[x][y] = -2
    return self.hints[x][y]

def mark_mine(self, position):
    x = position[0]
    y = position[1]
    self.marked[x][y] = -3

def available_position(self, position):

```

```

        # Returns true if the given position is available on this
board
        return 0 <= position[0] < self.x and 0 <= position[1] <
self.y

    def around_position(self, position):
        # Returns a list of available postions around the given
position
        x = position[0]
        y = position[1]
        psb_pos = [(x-1, y-1), (x, y-1), (x+1, y-1),
                    (x-1, y), (x+1, y),
                    (x-1, y+1), (x, y+1), (x+1, y+1)]
        around = []
        for pos in psb_pos:
            if self.available_position(pos):
                around.append(pos)
        return around

    def around_unmarked_position(self, position):
        # Returns a list of unmarked postions around the given
position
        around = self.around_position(position)
        around_unmarked = []
        for a in around:
            if self.marked[a[0]][a[1]] == 0:
                around_unmarked.append(a)
        return around_unmarked

    def around_marked_mine_position(self, position):
        # Returns a list of marked mine postions around the given
position
        around = self.around_position(position)
        around_marked_mine = []
        for a in around:
            if self.marked[a[0]][a[1]] == -3:
                around_marked_mine.append(a)
        return around_marked_mine

    def check_success(self):
        marked_count = 0
        marked_mine_count = 0
        current = copy.deepcopy(self.marked)
        for j in range(self.y):
            for i in range(self.x):
                if current[i][j] != 0:
                    marked_count += 1
                if current[i][j] == -3:
                    marked_mine_count += 1
        return marked_count == self.x*self.y and marked_mine_count
== self.mines

```



```

def global_constraint_check(self):
    unmarked = []
    marked_mine = []
    current = copy.deepcopy(self.marked)
    for j in range(self.y):
        for i in range(self.x):
            if current[i][j] == 0:
                unmarked.append((i, j))
            elif current[i][j] == -3:
                marked_mine.append((i, j))
    return unmarked, marked_mine

def print_current_board(self):
    # Print the current board status
    # _ : Unassigned
    # | : Assigned no mine
    # * : Assigned mine
    # [0-8] : Hint
    current = copy.deepcopy(self.marked)
    for j in range(self.y):
        for i in range(self.x):
            current[i][j] = '_' if current[i][j] == 0 else
current[i][j]
            current[i][j] = self.hints[i][j] if current[i][j]
== -2 else current[i][j]
            current[i][j] = '*' if current[i][j] == -3 else
current[i][j]
            print(current[i][j], end=" ")
        print()

def print_answer_board(self):
    # Print the answer board
    # * : Mine
    # [0-8] : Hint
    board = copy.deepcopy(self.hints)
    for j in range(self.y):
        for i in range(self.x):
            board[i][j] = '*' if board[i][j] == -3 else
board[i][j]
            print(board[i][j], end=" ")
        print()

if __name__ == '__main__':
    # Examples
    b = Board('easy')
    b.print_answer_board()

```

## test.py

```

from minesweeper import MineSweeper, Result

```

```

def simple_test(rounds, difficulty, show = False):
    success = 0
    fail = 0
    stuck = 0
    success_duration = 0

    for i in range(rounds):
        game = Minesweeper(difficulty)
        result = game.play(show)
        if result.status == 'Success':
            success += 1
            success_duration += result.play_time
        elif result.status == 'Fail':
            fail += 1
        if result.stuck:
            stuck += 1

    print()
    print('=====')
    print('Tested:\t\t\t', rounds, difficulty, 'games')
    print('Success:\t\t\t', success, 'games')
    print('Success duration:\t\t', success_duration/success, 'sec
per game')
    print('Fail (Stuck):\t\t\t {} ({} ) games'.format(fail, stuck))

def mines_count_test(rounds, difficulty, mines, show = False):
    print('=====')
    print('Tested:', rounds, difficulty, 'games per mines_counts')
    print('Mines\tSuccess\tStuck\tFail\tFail-Stuck\tSuccess
duration')
    for m in range(1, mines+1):
        success = 0
        fail = 0
        stuck = 0
        success_duration = 0

        for i in range(rounds):
            game = Minesweeper(difficulty, m)
            result = game.play(show)
            if result.status == 'Success':
                success += 1
                success_duration += result.play_time
            elif result.status == 'Fail':
                fail += 1
            if result.stuck:
                stuck += 1

        print('{}\t{}\t{}\t{}\t{}\t{}\t{}'.format(m, success, stuck,
fail, fail-stuck, success_duration/success))

```

```
if __name__ == '__main__':  
    simple_test(1000, 'easy')  
    simple_test(1000, 'medium')  
    simple_test(1000, 'hard')  
    mines_count_test(100, 'medium', 40)
```