

We decrypted the binary text using online tools and used 43MKB as ASCII key and got the problem.

question reduces to:

A is a  $4 \times 4$  matrix is composed of elements 0, 1, and 2. Both A and  $A^T$  have an eigen vector  $[1, 1, 1, 1]$  corresponding to the same eigen value. Find number of such matrices.

from definition of eigen value,

$$AX = \lambda X$$

$$\begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} = \lambda \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

$$\Rightarrow \begin{aligned} a+b+c+d &= \lambda & - (1) \\ e+f+g+h &= \lambda & - (2) \\ i+j+k+l &= \lambda & - (3) \\ m+n+o+p &= \lambda & - (4) \end{aligned}$$

where  $\lambda \in [0, 8]$  since  $a, b, c, d$  can take values only from 0, 1, 2.

So essentially we have to solve

$$a+b+c+d = x$$

where  $x \in [0, 8]$ .

Since all the cases (1) to (4) are mutually independent so total cases can be calculated by (no. of ways of any one case).  
Since all are identical.

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now, to find the answer to the  
code is the above code using python.

In the loop, we have taken value of  
a, b, c, d ranging in the loop.