# Winter 2022, CSE342/542

## Assignment 1

Deadline: 11:59PM Monday, 7th Feb

#### Instructions:

- You are required to submit a .py file necessarily for each coding question (you may or may not submit .ipynb files)
- Questions where you need to plot indicate coding questions. Others do not.

#### Q1:

You are given P(w1)=¼ , P(w2)=¾ and P(x|w1)=N(2,1) , P(x|w2)=N(5,1) where N(a,b) is normal distribution with mean a and variance b .

Plot 
$$P(x|w1)$$
 vs x,  $P(x|w2)$  vs x,  $P(x|w1)/P(x|w2)$  vs x. [1]

Also, find the decision boundary which minimizes the error in case of:

ii) 
$$\lambda_{12}=2, \lambda_{21}=3, \lambda_{11}=0, \lambda_{22}=0.$$
 [1]

(where  $\lambda_{ij}$  denotes predicting class "i" when the true class is "j")

Would you prefer using the zero-one loss for a task like cancer prediction on a real world dataset? Why, or why not?

#### Q2:

X = [X1, X2, X3] be a random vector with u = [5, -5, 6] being the mean vector. The covariance matrix is given by :-

Calculate the mean of

$$Y = A^{T}X + B$$
  
where  $A = (2, -1, 2)^{T}$  and  $B = 5$ 

[1]

### Q3:

Let the conditional densities for two-category one dimensional problem given the following distribution (Cauchy' pdf).

$$Px|w_i)=rac{1}{\pi b}.rac{1}{1+\left(rac{x-a_i}{b}
ight)^2},\,i=1,2$$

- A) Compute the optimal or minimum error rate decision boundary for zero one loss.
- B) Plot p(w1|x) for a1 = 3, a2= 5 and b= 1 [1]
- C) What is the overall error rate? [1]
- Q4. a. Find the pdf of  $x = [a \ b]$  a 2-d vector, where a is a Bernoulli random variable and b is a Gaussian random variable. Assume,  $\theta$  is the parameter for Bernoulli which gives the probability of a = 1, that is  $p(a=1) = \theta$ . Assume, b follows a Gaussian distribution with mean m and variance  $\sigma^2$ . The covariance of x is [1] [ $\theta(1-\theta)$  0; 0  $\sigma^2$ ]

b. Let the pdf of part (a) be p(x). Now assume that there are N iid samples drawn from this pdf. Find  $\theta$  that maximizes the joint probability q(x) of these N samples. Once you determine q(x), use In q(x) for computing  $\theta$ . [2]