Solutions of Tut-3

Q-1

Electric field due to
$$+Q$$

$$\vec{E}^{\dagger} = \frac{1}{(n-a)^{n} + y^{n} + z^{n}}$$
Total field $\vec{E} = \vec{E}^{\dagger} + \vec{E}$
Calculate divergence of the field. when

Q-2

Both hours become

Horrizon tal' components

cancel each other.

Add ($\lambda = \text{line} - \text{charge denity} = \frac{Q}{2\sqrt{x}}$

Therefore the electric field at P is just the

restical confinent (000 component):

 $\frac{1}{E} = \frac{1}{4\pi \epsilon} \int \frac{\lambda dl}{8^2} \cos \theta \stackrel{?}{=} \frac{(\hat{z} = unif-vector)}{vector} down$ direction)

 $\Lambda^2 = \Lambda^2 + R^2$ $Go 0 = \frac{a}{5}$ and $\Lambda = \frac{Q}{2\pi R}$

 $\vec{e} = \frac{\lambda}{4\pi\epsilon} \int \frac{dl}{\vec{a} + R^2} \cdot \frac{a}{\sqrt{\vec{a} + R^2}} \cdot d\vec{a}$

 $= \frac{\lambda_0}{4\kappa t_0} \cdot \frac{\alpha}{(\alpha^{\nu} + R^{\nu})^3/2} \int du \hat{z}$

= \frac{\lambda \cdot 2 \times \frac{\lambda}{\lambda^{\sigma} + \rangle^{\sigma}} \frac{2}{\lambda^{\sigma} + \rangle^{\sigma}} \frac{3}{2}^2

 $= \frac{\alpha}{9 \times 60} \cdot \frac{\alpha}{(\alpha^{r} + R^{r})^{3/2}} z^{2}$

Break it into the rings of radius's' and thickness dr, and use the previous problem's rounds.

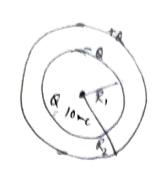
Total charge of a ring = 8.227 dr

(6 = surface charge density of circular disk = $\frac{Q}{AR^2}$)

Electric field at a distance 'z' due to the ring = $\frac{6.2x r dr}{4\pi \ell_0} \cdot \frac{z}{(r^2 + z^2)^{3/2}}$

Therefore electric field for the disk at a distant $Z = \frac{2\pi 6Z}{4\pi \epsilon_0} \cdot \int_{\kappa}^{\kappa} \frac{\gamma dr}{(\tilde{r}^2 + Z^2)^3 h}$

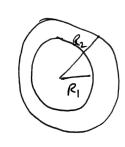
 $= \frac{2 \times 2}{4 \times \epsilon_0} \cdot \frac{Q}{\times R^2} \left[\frac{1}{Z} - \sqrt{\frac{R^2 + 2^2}{R^2 + 2^2}} \right] \hat{z}$ $= \frac{Q^2}{2 \times \epsilon_0 R^2} \left[\frac{1}{Z} - \sqrt{\frac{R^2 + 2^2}{R^2 + 2^2}} \right] \hat{z}$



(a) Total charges indicad the at the inner surface = -Q = -10 mc

Total charges induced at the outer surface = + i0 = +10mc

6) Uniform



vol. charge density = P.

Those regions -

Regin 1 \rightarrow 0 $\langle \sigma \leq R_1 \rangle$ Regin 2 \rightarrow $R_1 \leq \tau \leq R_2$ From the Centre.

Regin 3 \rightarrow $\tau > R_2$

There is no charge in Region -1,

Hence electric field $\vec{E}_1 = 0$ OKTKR, $\vec{a} \cdot \vec{E}_1 = 0$

Que = P.
$$\frac{4}{3}$$
 = $\left(\sigma^{3} - R_{1}^{3}\right)$

Huc
$$\vec{\xi} = \frac{4\pi P}{3\epsilon_0} \cdot \frac{1}{4\pi r^2} \left(r^3 - R_1^3\right) \hat{\tau}$$

$$\vec{\nabla} \cdot \vec{E_2} = P/\epsilon_0 \qquad = \left(\frac{Pr}{3\epsilon_0} - \frac{PR_1^3}{3\epsilon_0 r^2}\right) \hat{\tau}$$

$$\vec{\sigma} = \frac{regin - 3}{r^3} \left(r > R_2\right)$$

$$Q_{exc} = \rho. \frac{4\pi}{3} \left(\mathcal{R}_2^3 - \mathcal{R}_1^3 \right)$$

$$\vec{E}_{3} = \frac{4 \kappa \rho}{3 \epsilon_{0}} \cdot \frac{1}{4 \pi^{2}} \left(R_{2}^{3} - R_{1}^{3} \right)$$

$$= \frac{\rho}{3 \epsilon_{0} r^{2}} \left(R_{2}^{3} - R_{1}^{3} \right) \hat{r}$$

$$\overline{\varphi}.\overline{\underline{\epsilon}_3} = 0$$

Q-6

- C

TYR.

du is spherical polar coordinate

Total charge inside the sphere of radius R

den = ((Po + dr) 2 sin 8 de d d dr

$$= \frac{4 \pi \ell_0}{3} R_{/3}^3 + \frac{4 \pi \ell_0}{60 \pi^{1/3}} \frac{R^4}{4}$$

$$= \frac{4\pi R^3}{3} \left(e_0 + \frac{3\alpha}{4} R \right)$$

$$\frac{F_{\text{r}} \quad O < r < R}{\text{Denc}} = \frac{4 \pi^3}{3} \left(\rho_{\text{o}} + \frac{3 \times \sigma}{4} \right)$$

Hence
$$\vec{E} = \frac{1}{417^2} \cdot \frac{4\pi \gamma^3}{3\epsilon_0} \left(\rho_0 + \frac{3\alpha \gamma}{4} \right)$$

$$= \frac{7}{3\epsilon_0} \left(\rho_0 + \frac{3\alpha \gamma}{4} \right)$$

$$\vec{F} = \frac{1}{4\pi^2} \frac{4\pi R^3}{3\epsilon_0} \left(P_0 + \frac{3\alpha R}{4} \right)$$

$$= \frac{R^3}{3\epsilon_0 r} \left(P_0 + \frac{3 \times R}{4} \right)$$

$$\vec{\nabla} \cdot \vec{E} = \frac{P}{f_0} \quad \text{for} \quad OCTCR$$

$$\vec{\nabla} \cdot \vec{E} = 0 \quad \text{for} \quad \tau > R$$

$$z=5m$$
. On $\lambda = 1$ time change dens. My $\lambda = \frac{50 \times 10^{-9}}{2 \times 2}$ Coulon/m

$$\frac{\partial V(1)}{\partial x} = \frac{\lambda d}{4\pi \epsilon_0 \Re}$$

$$= \sqrt{2^{2} + 5^{2}}$$

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$$= \sqrt{29}$$

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= 2x7.2 4x Eo \29

9 Find the pitchtial at
$$z=0$$
 (V₁) and at $z=5$ in (V₂)

Work done =
$$Q(V_2-V_1)$$
, Lere $Q=10 \text{ nc}$.

priential at
$$z=5$$
 and $z=-5$ is same.
Hence in this cone $V_1=V_L$

work done = 0.

Q-8
$$\vec{E} = 2 (n+4y)^{\frac{1}{1}} + 8n^{\frac{1}{3}}$$

$$\vec{d} = dn^{\frac{1}{1}} + dy^{\frac{2}{3}} + dz^{\frac{2}{3}}$$

$$(0,0) (4,0)$$

 $\vec{E} \cdot \vec{u} = 2(x+4y)dx + 8x dy$

potential difference =
$$\int \mathcal{E} \cdot dI$$

= $\int_{0}^{4} (2(2+48)) dx + \int_{0}^{2} (22 dy) dx$
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printed due to a print change of (26

Q-9 pitertral at (x, y, z) due to a print charge at (x0, y, z0) can be expressed as

$$V(x_1,z) = \frac{9}{4\pi(19)}$$
 (x_0, y_0, z_0)

 $\frac{1}{2} = (x - x_0)^{\frac{1}{2}} + (y - y_0)^{\frac{1}{2}} + (z - z_0)^{\frac{1}{2}}$

 $|\vec{y}| = \sqrt{(x-x_0)^2 + (y-x_0)^2} + (z-z_0)^2$

prefertial at (2,2,3) where

 $/\bar{A}_{1}^{\prime} = \sqrt{(2-2)^{2} + (2-3)^{2} + (3-3)^{2}}$

9 1·2×10-1 4×6×1

Similarly (91) for (-2,3,3) is

 $|\tilde{\chi}_2| = \sqrt{(-2-2)^2 + (3-3)^2 + (3-3)^2}$

potential difference. = $\left(V_1 - V_2\right)$.