Department of Mathematics, Bennett University Engineering Calculus (EMAT101L) Tutorial Sheet 4 (Limit)

1. Evaluate:

(a)
$$\lim_{x \to -1} \frac{(x+2)(3x-1)}{x^2+3x-2}$$

(b)
$$\lim_{x\to 0} \frac{\sqrt{4+x}-2}{x}$$

(c)
$$\lim_{x \to 1} \frac{x^2 - 1}{x - 1}$$

(d)
$$\lim_{x \to 2} \frac{(4-x^2)}{3-\sqrt{x^2+5}}$$

(e)
$$\lim_{x \to 0} \frac{\sin 2x + \sin 6x}{\sin 5x - \sin 3x}$$

(f)
$$\lim_{x \to a} \frac{\sin x - \sin}{x - a}$$

(g)
$$\lim_{x \to 0} \frac{\sec x - 1}{\tan^2 x}$$

(h)
$$\lim_{x \to \frac{\pi}{2}} \sec x - \tan x$$

Evaluate:
(a)
$$\lim_{x \to -1} \frac{(x+2)(3x-1)}{x^2+3x-2}$$
 (b) $\lim_{x \to 0} \frac{\sqrt{4+x}-2}{x}$ (c) $\lim_{x \to 1} \frac{x^2-1}{x-1}$ (d) $\lim_{x \to 2} \frac{(4-x^2)}{3-\sqrt{x^2+5}}$ (e) $\lim_{x \to 0} \frac{\sin 2x + \sin 6x}{\sin 5x - \sin 3x}$ (f) $\lim_{x \to a} \frac{\sin x - \sin a}{x-a}$ (g) $\lim_{x \to 0} \frac{\sec x - 1}{\tan^2 x}$ (h) $\lim_{x \to \frac{\pi}{2}} \sec x - \tan x$ (i) $\lim_{x \to 1} f(x)$ where $f(x) = \begin{cases} 4 - 2x & x < 1 \\ 6x - 4 & x \ge 1 \end{cases}$

$$(k) \lim_{x \to 0} \frac{\tan 3x}{\sin 8x}$$

2. Show that each of the following limits does not exist:

$$(a) \lim_{x \to 1} \frac{x-1}{|x-1|}$$

(a)
$$\lim_{x \to 1} \frac{x-1}{|x-1|}$$
 (b) $\lim_{x \to 2} f(x)$ where $f(x) = \begin{cases} x+3 & x \le 2 \\ -2x+5 & x > 2 \end{cases}$

$$(c) \lim_{x \to 0} e^{\frac{1}{x}}$$

$$(c) \lim_{x \to 0} e^{\frac{1}{x}} \qquad (d) \lim_{x \to 0} x + \operatorname{sgn}(x)$$

$$(e) \lim_{x \to 0} \frac{\sin x}{|x|}$$

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3. For what values of a, $\lim_{x\to 2^-} f(x) = \lim_{x\to 2^+} f(x)$ where

$$f(x) = \begin{cases} a^2x - 2a & x \ge 2\\ 12 & x < 2 \end{cases}$$

4. For what values of a, $\lim_{x\to 3^-} f(x) = \lim_{x\to 3^+} f(x)$ where

$$f(x) = \begin{cases} x^2 - 1 & x < 3\\ 2ax & x \ge 3 \end{cases}$$

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