



**EMAT101L**  
**Engineering Calculus**  
**Quiz Test 1**

Total marks: 10

Time: 10 minutes

Each question carries 2 marks.

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1. Find the supremum and infimum of  $S = \left\{ (-1)^n \left( \frac{1}{6} - \frac{6}{n} \right) : n \in \mathbb{N} \right\}$ .

- (a)  $\sup(S) = \frac{1}{6}, \quad \inf(S) = -\frac{1}{6}$
- (b)  $\sup(S) = \frac{1}{6}, \quad \inf(S) = -\frac{17}{6}$
- (c)  $\sup(S) = \frac{35}{6}, \quad \inf(S) = -\frac{1}{6}$
- (d)  $\sup(S) = \frac{35}{6}, \quad \inf(S) = -\frac{17}{6}$

2. Which of the following sequences converge? Select all that apply.

I. 100, 80, 60, 40, ...

II. 0, 5, 0, 5, 0, ...

III.  $a_n = 5 \left( \frac{3}{2} \right)^n$

IV.  $a_1 = 4, a_n = \frac{1}{2}a_{n-1}$

- (a) I., III., IV.      (b) IV.      (c) III.      (d) all of the above

3. Choose the sequence for which  $\lim_{n \rightarrow \infty} a_n = e$ .

- (a)  $a_n = 1 + \frac{1}{n^n}$
- (b)  $a_n = \left( 1 + \frac{1}{n} \right)^n$
- (c)  $a_n = \left( n + \frac{1}{n} \right)^n$

- (d) None of them
4. Find the supremum and infimum values of  $S = \{x \in \mathbb{Q} : |x - 2| < 1\}$ .
- (a)  $\sup(S) = 1$  and  $\inf(S) = -1$ .
  - (b)  $\sup(S) = 3$  and  $\inf(S) = -1$ .
  - (c)  $\sup(S) = 3$  and  $\inf(S) = 1$ .
  - (d)  $\sup(S) = 2$  and  $\inf(S) = -1$ .
5. Let  $A$  be a set and  $L$  be a real number. If  $\sup(A) = L$ , this means that
- (a)  $a \leq L$ , for every  $a \in A$ .
  - (b)  $L$  lies in  $A$  and  $L$  is larger than every other element of  $A$ .
  - (c) Every number less than  $L$  lies in  $A$ , and every number greater than  $L$  does not lie in  $A$ .
  - (d)  $\inf(A) \neq \sup(A)$ .