Department of Mathematics, Bennett University Engineering Calculus (EMAT101L) Tutorial Sheet 3

1. Determine which of the following series converges/diverges:

$$(a)\sum_{n=1}^{\infty} \frac{4}{n^2 + 3n + 2}$$

$$(a) \sum_{n=1}^{\infty} \frac{4}{n^2 + 3n + 2}$$
 $(b) \sum_{n=1}^{\infty} \left(\sin^2 \frac{1}{n} - \sin^2 \frac{1}{n+2} \right).$

2. Determine which of the following series converges/diverges:

$$(a) \sum_{n=1}^{\infty} 5^{\frac{1}{n}}$$

$$(b) \sum_{n=1}^{\infty} \left(1 + \frac{x}{n}\right)^n$$

$$(c)$$
 $\sum_{n=1}^{\infty} \log\left(\frac{n+1}{n}\right)$

(a)
$$\sum_{n=1}^{\infty} 5^{\frac{1}{n}}$$
 (b) $\sum_{n=1}^{\infty} \left(1 + \frac{x}{n}\right)^n$ (c) $\sum_{n=1}^{\infty} \log\left(\frac{n+1}{n}\right)$ (d) $\sum_{n=1}^{\infty} (a + (n-1)b)$

3. Determine which of the following series converges/diverges:

(a)
$$\sum_{n=1}^{\infty} \frac{1}{n \sqrt[n]{n}}$$

$$(b)\sum_{n=1}^{\infty}\frac{\sqrt[n]{n}}{n^2}$$

$$(c)$$
 $\sum_{n=0}^{\infty} \sin\left(\frac{\pi}{2^n}\right)$

(a)
$$\sum_{n=1}^{\infty} \frac{1}{n\sqrt[n]{n}}$$
 (b) $\sum_{n=1}^{\infty} \frac{\sqrt[n]{n}}{n^2}$ (c) $\sum_{n=0}^{\infty} \sin\left(\frac{\pi}{2^n}\right)$ (d) $\sum_{n=1}^{\infty} \frac{1}{n} \sin\left(\frac{1}{\sqrt{n}}\right)$.

4. Determine which of the following series converges/diverges:

$$(a) \sum_{n=1}^{\infty} \frac{n^{\sqrt{2}}}{2^n}$$

$$(b) \sum_{n=1}^{\infty} \frac{n!}{10^n}$$

(a)
$$\sum_{n=1}^{\infty} \frac{n^{\sqrt{2}}}{2^n}$$
 (b) $\sum_{n=1}^{\infty} \frac{n!}{10^n}$ (c) $\sum_{n=1}^{\infty} \frac{n!}{(2n+1)!}$.

5. Determine which of the following series converges absolutely/conditionally:

(a)
$$\sum_{n=1}^{\infty} (-1)^n \frac{1}{n}$$

$$(b) \sum_{n=1}^{\infty} (-1)^n \frac{\sin nx}{n^2}$$

(a)
$$\sum_{n=1}^{\infty} (-1)^n \frac{1}{n}$$
 (b) $\sum_{n=1}^{\infty} (-1)^n \frac{\sin nx}{n^2}$ (c) $\sum_{n=2}^{\infty} (-1)^n \frac{1}{\log n}$.

6. Find the value of x for which the following series converges:

$$(a) \sum_{n=0}^{\infty} (n+1+2^n) x^n$$

$$(b) \sum_{n=0}^{\infty} \frac{n! x^n}{n^n}$$

(a)
$$\sum_{n=0}^{\infty} (n+1+2^n)x^n$$
 (b) $\sum_{n=0}^{\infty} \frac{n!x^n}{n^n}$ (c) $\sum_{n=1}^{\infty} \frac{n^{n^2}}{(n+1)^{n^2}}(x-1)^n$.

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