

Enrolment No: _____ Name of Student: _____
 Department/ School: _____

END TERM EXAMINATION EVEN SEMESTER 2022-23

COURSE CODE	CSET106	MAX. DURATION	2 HR 30 MIN
COURSE TITLE	Discrete Mathematical Structures		
COURSE CREDIT	4	TOTAL MARKS	50

GENERAL INSTRUCTIONS: -

1. Attempt all the questions. All the questions are compulsory.
2. Do not write anything on the question paper except name, enrolment number and department/school.
3. Carrying mobile phone, smart watch and any other non-permissible materials in the examination hall is an act of UFM.

Q1. Answer the following questions

(1*5)

- i. If $6 + 2 = 5$, then the milk is white. Determine the truth value of this statement.
- ii. $[p \rightarrow (q \wedge r)] \vee [(p \rightarrow q) \wedge (p \rightarrow r)] \vee 1$. Determine the value of this logical equivalence.
- iii. Give an example of a relation which is both symmetric and anti-symmetric.
- iv. Find the smallest number of colours you need to properly colour the vertices of $K_{4,5}$ graph.
- v. In a word jumble, there are 8 consonants and 5 vowels given. Find out in how many ways can we form a 5-letter word having 3 consonants and 2 vowels?

Q2. Answer the following questions

- i. Solve the logical equivalence using the truth table. (3)

$$[\neg (p \wedge q)] \rightarrow r$$
- ii. Determine whether the following expression is a tautology, a contingency, or a contradiction (3)

$$[\neg (A \vee q)] \wedge (A \wedge q)$$
- iii. For each of these relations on the set $\{1, 2, 3, 4\}$, decide whether it is reflexive, irreflexive, symmetric, antisymmetric, asymmetric, and transitive. (5)
 - a. $\{(2, 2), (2, 3), (2, 4), (3, 2), (3, 3), (3, 4)\}$
 - b. $\{(1, 1), (1, 2), (2, 1), (2, 2), (3, 3), (4, 4)\}$
 - c. $\{(2, 4), (4, 2)\}$
 - d. $\{(1, 1), (2, 2), (3, 3), (4, 4)\}$
 - e. $\{(1, 3), (1, 4), (2, 3), (2, 4), (3, 1), (3, 4)\}$
- iv. Determine the number of edges in a graph with 6 vertices, 2 of degree 4 and 4 of degree 2. Draw two such graphs. (3)

P	q	$\neg p$
0	0	1
0	1	1
1	0	0
1	1	0

- v. If $f(x) = x^2 + 5$ and $g(x) = x^3 - 2$. Find $f \circ g(x)$ and $g \circ f(x)$. (2)

Q3. Answer the following questions

- Give a proof by contradiction of the theorem "If $3n+2$ is odd, then n is odd." (3)
- Let $f: \mathbb{Z} \rightarrow \mathbb{Z}$ be the function defined by $f(x) = 3x^2 + 1$. Prove that $f(x)$ is not a bijective function. (3)
- Let us assume that R is a relation on the set of integers defined by aRb if and only if $a - b$ is an integer. Prove that R is an equivalence relation? (3)
- The set $L = \{1, 2, 3, 4, 5, 6, 12\}$ of factors of 12 under divisibility forms a lattice. ~~Prove it using~~ Hasse diagram. *Check with +* (3)
- Find the maximum number of edges in a bipartite graph of 12 vertices. Justify your answer. (2)

Q4. Answer the following questions

- Consider the set $S = \{1, -1, i, -i\}$. If $*$ denotes the multiplication operation then prove that structure $\{S, *\}$ forms a cyclic group. Find the generator/(s) of this set. (4+1)
- Determine the GCD of 1288 and 333 using Euclidian algorithm. Express the greatest common divisor of the given pair of integers as a linear combination of these integers. (3+2)
- Using Chinese remainder theorem, determine the value of x : (5)

$$x \equiv 2 \pmod{3}$$

$$x \equiv 1 \pmod{4}$$

$$x \equiv 7 \pmod{11}$$

$$m_1 = 3$$

$$m_2 = 4$$

$$m_3 = 11$$

$$M = m_1 \times$$

$$M_i = \frac{M}{m_i}$$

$$(a_1 m_1 m_1^{-1} + \dots)$$

$$\frac{m_1 m_1^{-1} - 1}{m_1}$$