Homework Project 2

Given 10/12/2011, Due 10/26/2010

Implement the simplex algorithm to compute the maximum of a linear objective function under a set of linear inequalities.

You should write a function

which has as parameters the number of variables d, the number of inequalities n, the coefficient matrix A and right-hand side b, the coefficients of the objective function c, as well as the result vector result, which contains the optimum values for the d variables x_0, \ldots, x_{d-1} . It returns an integer, which is the number of simplex steps taken by the algorithm to reach the optimum.

Your function should solve the LP problem

$$\begin{aligned} \max \mathbf{c}[\mathbf{0}] x_0 + \dots + \mathbf{c}[\mathbf{d} - 1] x_{d-1} \\ \mathbf{A}[\mathbf{0}][\mathbf{0}] x_0 + \dots + \mathbf{A}[\mathbf{0}][\mathbf{d} - 1] x_{d-1} &\leq \mathbf{b}[\mathbf{0}] \\ \mathbf{A}[\mathbf{1}][\mathbf{0}] x_0 + \dots + \mathbf{A}[\mathbf{1}][\mathbf{d} - 1] x_{d-1} &\leq \mathbf{b}[\mathbf{1}] \\ & & \vdots \\ \mathbf{A}[\mathbf{n} - 1][\mathbf{0}] x_0 + \dots + \mathbf{A}[\mathbf{n} - 1][\mathbf{d} - 1] x_{d-1} &\leq \mathbf{b}[\mathbf{n} - 1] \\ x_0 &\geq 0, x_1 \geq 0, \dots, x_{d-1} \geq 0 \end{aligned}$$

Do not make any assumptions on the size of the matrix; any additional storage you need should be allocated dynamically. The programming language is C or C++; test your code before submission using the gcc or g++ compiler. Submit your source code (the function) by mail to peter@cs.ccny.cuny.edu.