

36. $(-a) \cdot (-a) = a \cdot a$ (Transitivity of eq on 21, 35)
 37. $a^2 = a \cdot a$ (By defn.) 38. $a \cdot a = a^2$ (Symmetry of eq 37)
 39. $(-a) \cdot (-a) = a^2$ (Transitivity of eq on 37, 38)
 40. $a^2 > 0$ (Substitution of eq 39 on 18)

\therefore Square of any non-zero real no. is positive

- b) 1. $1 \in \mathbb{R}$ (Given) 2. $1 \neq 0$ (M3) 3. $1^2 > 0$ (By part a)
 4. ~~1~~ $1^2 = 1 \cdot 1$ (By defn.) 5. $1 \cdot 1 = 1$ (M3) 6. $1^2 = 1$ (Transitivity of eq ^{on} 4, 5)
 7. $1 > 0$ (Substitution of eq 6 in 3)

- c) 1. The proof will be by mathematical induction on n .
 2. Base Case: $1 > 0$ (holds by part b), or $1 \in P$ (by defn.)
 3. Inductive Step: Let $n > 0$ hold, for some $n \in \mathbb{N}$, i.e. $n \in P$ (by defn.)
 $\therefore n+1 \in P$ (Prop 2.1.5(i)), or $(n+1) > 0$ (By defn.)

\therefore The assertion is true for all natural no.s