

5. $(-1)a - (-a) = (-1)a + (-(-a))$ (Defn. of subtraction)
6. $(-1)a + (-(-a)) = (-1)a - (-a)$ (Symmetry of eq on 5)
7. $(-1)a + (-(-a)) = c$ (Transitivity of eq 6, 4)
8. $-(-a) = a$ (Part b) 9. $(-1)a + (-(-a)) = (-1)a + a$ (Substitution of eq on 8)
10. $(-1)a + a = (-1)a + (-(-a))$ (Symmetry of eq on 9)
11. $(-1)a + a = c$ (Transitivity of eq on 10, 7)
12. $1 \cdot a = a$ (M3) 13. $(-1)a + 1 \cdot a = (-1)a + a$ (Substitution of eq on 12)
14. $(-1)a + 1 \cdot a = c$ (Transitivity of eq on 13, 11)
15. $((-1) + 1) \cdot a = (-1) \cdot a + 1 \cdot a$ (D) 16. $((-1) + 1) \cdot a = c$ (Transitivity of eq on 15, 14)
17. $(-1) + 1 = 0$ (A4) 18. $((-1) + 1) \cdot a = 0 \cdot a$ (Substitution of eq on 17)
19. $0 \cdot a = a \cdot 0$ (M1) 20. $((-1) + 1) \cdot a = a \cdot 0$ (Transitivity of eq on 18, 19)
21. $a \cdot 0 = 0$ (Thm 2.1.2(c)) 22. $((-1) + 1) \cdot a = 0$ (Transitivity of eq on 20, 21)
23. $c = ((-1) + 1) \cdot a$ (Symmetry of eq on 16) 24. $c = 0$ (Transitivity of eq on 23, 22)

But, csp. \therefore This is a contradiction

Similarly, we will again arrive at $c=0$ if we assume $(-1)a \neq -a$. (Contradiction)

$$\boxed{\therefore (-1)a = -a} \text{ (Proved)}$$

25. Let $-a \rightarrow (-1)a$ 26. $(-a) - (-1)a \in P$ (Defn. 2.1.6(a) on 25)
27. $\therefore P$ is non-empty, $\exists a, b$ s.t. $(-a) - (-1)a = c_1$
28. ~~$(-a) - (-1)a = (-a) + (-(-1)a)$~~ (Defn. of subtraction)
29. $(-a) + (-(-1)a) = (-a) - (-1)a$ (Symmetry of eq) 30. $(-a) + (-(-1)a) = c_1$ (Transitivity of eq on 29, 27)
31. $a + ((-a) + (-(-1)a)) = a + c_1$ (Substitution of eq on 30)
32. $(a + (-a)) + (-(-1)a) = a + ((-a) + (-(-1)a))$ (A2)
33. $(a + (-a)) + (-(-1)a) = a + c_1$ (Transitivity of eq on 32, 31)
34. $a + (-a) = 0$ (A4) 35. $(a + (-a)) + (-(-1)a) = 0 + (-(-1)a)$ (Substitution of eq on 34)
36. $0 + (-(-1)a) = (-(-1)a)$ (A3) 37. $(a + (-a)) + (-(-1)a) = (-(-1)a)$ (Transitivity of eq on 35, 36)