

62. $(-1) \cdot ((-1) \cdot x) = ((-1) \cdot (-1)) \cdot x$ (Symmetry of eq 57)
63. $(-1) \cdot ((-1) \cdot x) = 1 \cdot x$ (Transitivity of eq 62, 59)
64. $(-1) \cdot ((-1) \cdot x + (-1) \cdot x) = 1 \cdot x + 1 \cdot x$ (Substitute eq 63 in 56)
65. $1 \cdot x + 1 \cdot x = (-1) \cdot ((-1) \cdot x + (-1) \cdot x)$ (Symmetry of eq 64)
66. $(1 \cdot x + 1 \cdot x) + 1 = (-1) \cdot ((-1) \cdot x + (-1) \cdot x) + 1$ (Substitute eq 65)
67. $(1 \cdot x + 1 \cdot x) + 1 = (-2x) + 1$ (Transitivity of eq 66, 55)
55. $(-1) \cdot (2x) + 1 = ((-1) \cdot x + (-1) \cdot x) + 1$ (Substitute eq 53)
56. $((-1) \cdot x + (-1) \cdot x) + 1 = (-1) \cdot x + ((-1) \cdot x + 1)$ (A2)
57. $(-1) \cdot (2x) + 1 = (-1) \cdot x + ((-1) \cdot x + 1)$ (Transitivity of eq on 55, 56)
58. $(-2x) + 1 = (-1) \cdot (2x) + 1$ (Symmetry of eq 54)
59. $(-2x) + 1 = (-1) \cdot x + ((-1) \cdot x + 1)$ (Transitivity of eq on 58, 57)
60. $x^2 + ((-2x) + 1) = x^2 + ((-1) \cdot x + ((-1) \cdot x + 1))$ (Substitute eq 59)
61. $(x^2 + (-1) \cdot x) + ((-1) \cdot x + 1) = x^2 + ((-1) \cdot x + ((-1) \cdot x + 1))$ (A2)
62. $x^2 + ((-1) \cdot x + ((-1) \cdot x + 1)) = (x^2 + (-1) \cdot x) + ((-1) \cdot x + 1)$ (Symmetry of eq 61)
63. $x^2 + ((-2x) + 1) = (x^2 + (-1) \cdot x) + ((-1) \cdot x + 1)$ (Transitivity of eq 60, 62)
64. $x^2 = x \cdot x$ (By defn.) 65. $x^2 + (-1) \cdot x = x \cdot x + (-1) \cdot x$ (Substitute eq 64)
66. ~~$x^2 + (-1) \cdot x = (x + (-1)) \cdot x$~~ (Symmetry of eq 66)
67. $x \cdot x + (-1) \cdot x = (x + (-1)) \cdot x$ (Transitivity of eq 65, 67)
68. $x^2 + (-1) \cdot x = (x + (-1)) \cdot x$ (Symmetry of eq 67)
69. ~~$x^2 + (-1) \cdot x + ((-1) \cdot x + 1) = (x + (-1)) \cdot x + ((-1) \cdot x + 1)$~~ (Substitute eq 68 in RHS of 62)

70. $(-1) \cdot (-1) = 1$ (Ex 2.1, 1(d))
71. $(-1) \cdot x + (-1) \cdot (-1) = (-1) \cdot x + 1$ (Substitute eq 70)
72. $(-1) \cdot (x + (-1)) = (-1) \cdot x + (-1) \cdot (-1)$ (D)
73. $(-1) \cdot (x + (-1)) = (-1) \cdot x + 1$ (Transitivity of eq 72, 71)
74. $(x + (-1)) \cdot (-1) = (-1) \cdot (x + (-1))$ (M1)
75. $(x + (-1)) \cdot (-1) = (-1) \cdot x + 1$ (Transitivity of eq 74, 73)