

- With this mapping, we can retrieve an item, replace an item, or find the length of a list in constant time
- We also can read the items in the list, from either direction, by simply changing subscripts in a controlled way.
- Insertion and deletion pose problems since we must move the items to preserve sequential mapping. This is the reason non-sequential mapping is needed.

Problem: Build a set of functions that allow for the manipulation of symbolic polynomials. $A(x) = \sum a_i x^i$ $B(x) = \sum b_i x^i$, then $A(x) + B(x) = \sum (a_i + b_i) x^i$ and $A(x) \cdot B(x) = \sum (a_i x^i \cdot \sum (b_j x^j))$. Similarly we can define subtraction and division on polynomials, as well as many other operations.

Abstract data type Polynomial

ADT Polynomial is

Objects: $p(x) = a_1 x^{e_1} + \dots + a_n x^{e_n}$; a set of ordered pairs of $\langle e_i, a_i \rangle$ where a_i in Coefficients and e_i in Exponents, e_i are integers ≥ 0 .

Functions: for all $\text{poly}, \text{poly1}, \text{poly2} \in \text{Polynomial}$, $\text{coef} \in \text{Coefficients}$, $\text{expon} \in \text{Exponents}$

- Polynomial $\text{Zero}() ::=$ return the polynomial, $p(x) = 0$
- Boolean $\text{IsZero}(\text{poly}) ::=$ if (poly) return FALSE
else return TRUE
- Coefficient $\text{Coef}(\text{poly}, \text{expon}) ::=$ if $(\text{expon} \in \text{poly})$ return its coefficient
else return Zero
- Exponent $\text{LeadExp}(\text{poly}) ::=$ return the largest exponent in poly
- Polynomial $\text{Attach}(\text{poly}, \text{coef}, \text{expon}) ::=$ if $(\text{expon} \in \text{poly})$ return error
else return the polynomial poly
with the term $\langle \text{coef}, \text{expon} \rangle$ inserted.
- Polynomial $\text{Remove}(\text{poly}, \text{expon}) ::=$ if $(\text{expon} \in \text{poly})$
return the polynomial poly with the term
whose exponent is expon deleted else return error