

\therefore Loop invariant holds.

Maintenance: Let, the loop invariant hold just before the start of the iteration when $i = x$, where $1 \leq x \leq \text{numTerms}$. For all indices K where $1 \leq K \leq x$, the no. of elements corresponding to each column j where $0 \leq j < a[0].\text{col}$ has been

\therefore For every column index j in the range $0 \leq j < a[0].\text{col}$, the value $\text{rowTerms}[j]$ is equal to the no. of times $a[K].\text{col} = j \quad \forall K, 1 \leq K \leq x$.

Now, $a[x].\text{col}$ returns the column no. y of the ~~the~~ non-zero element $a[x].\text{value}$. We know, $0 \leq y < a[0].\text{col}$. Since, now we have encountered one more non-zero element of column y , we must increase the count by 1, i.e. $\text{rowTerms}[y]++ \Leftrightarrow \text{rowTerms}[a[x].\text{col}]++$. We are doing just that on Line 11.

Just before the start of the ^{next} iteration, i updates to $(x+1)$. We can easily see that $\forall K', 1 \leq K' \leq x$, when $a[K']. \text{col} \neq y$, $\text{rowTerms}[a[K']. \text{col}]$ has not been updated when $i = x$.

\therefore It's clear that the loop invariant still holds.

Termination: The loop terminates when $i = \text{numTerms} + 1$. By the loop invariant, for every column index j in the range $0 \leq j < a[0].\text{col}$, the value $\text{rowTerms}[j]$ is equal to the no. of times $a[K].\text{col} = j \quad \forall K$ s.t. $1 \leq K \leq \text{numTerms}$.

\therefore For matrix $a[]$, $\text{rowTerms}[j]$ holds the no. of non-zero elements of $a[]$ having column index j , where $0 \leq j < a[0].\text{col}$. We can conclude this because by line 4, numTerms holds the no. of non-zero elements of $a[]$ and they ~~are~~ are stored in $a[]$ starting from index 1 to numTerms .

□