

invariant, ~~the row x~~ $\forall x \in N, 0 \leq x < \text{MAX_SIZE}-2$, row x has been interchanged with column x .

• Now, what about the last row, i.e. when $x = \text{MAX_SIZE}-1$? By loop invariant, $\forall y \in N, 0 \leq y < \text{MAX_SIZE}-1$, ~~the row~~ $a[\text{MAX_SIZE}-1][y]$ is already interchanged with $a[y][\text{MAX_SIZE}-1]$. There is no need to interchange the bottom rightmost element, i.e. $a[\text{MAX_SIZE}-1][\text{MAX_SIZE}-1]$.

\therefore The original matrix a has been transposed in-place \square

The matrix transpose function using dynamically allocated arrays has the exact same function body.