

**Theorem 1.1:** Function  $\text{sort}(\text{list}, n)$  correctly sorts a set of  $n \geq 1$  integers.

The result remains in  $\text{list}[0], \dots, \text{list}[n-1]$  s.t.  $\text{list}[0] \leq \text{list}[1] \leq \dots \leq \text{list}[n-1]$

**Proof:** We first prove the correctness of the inner loop the 1st ~~iteration~~ <sup>iteration</sup> having

**Claim:** The loop in lines 7-9 always finds out ~~the min~~ <sup>the 1st</sup> index having the min. value in the range  $[\text{list}[i], \text{list}[n-1]]$ .

**Proof:** In line 6, initially, the min value index is initialized to  $i$ .

The proof is by induction on  $m$ , where  $m = (n-1) - i$ .

**Base Case:**  $m=0 \therefore i=(n-1)$ . On line 7,  $j$  is initialized to  $(n-1)+1=n$  which is not less than  $n$ .  $\therefore$  The loop doesn't proceed further and min index is  $i$ , which is correct (Easy to see)

**Induction Step:** Let, our claim holds for the value  $m$ .  $\therefore$  ~~then~~  
The loop returns the 1st min index in the range  $[\text{list}[n-1-m], \text{list}[n-1]]$ .

Now, let's check for the value  $m+1$ .  $(m+1) = (n-1) - i$ ,  $i = (n-1-m) - 1$

**Claim:** Before the ~~current~~ <sup>next</sup> iteration of the loop, the 1st index having the min. value in the range  $[\text{list}[i], \text{list}[i]]$  has been found.

**Proof:** The proof is by induction on  $j$ , where  $i \leq j < n$ .

**Base Case:**  $j=i+1$ . In lines 8-9, we compare  $\text{list}[i]$  and  $\text{list}[j]$  and store the index of the min. value in  $\text{min}$ .

**Induction Step:** Let our claim hold for an arbitrary  $j$ .

$\therefore$   $\text{min}$  stores the 1st index having the min. value in the range  $[\text{list}[i], \text{list}[j]]$ .