

Q) How do we really know if n is sufficiently large?

• If Program P actually runs in $10^6 n$ milliseconds while program Q runs in n^2 milliseconds and if we always have $n \leq 10^6$, then, other factors being equal, program Q is faster

$\log n$	n	$n \log n$	n^2	n^3	$\frac{2^n}{2}$
0	1	0	1	1	4
1	2	2	4	8	16
2	4	8	16	64	256
3	8	24	64	512	65,536
4	16	64	256	4096	4,294,967,296
5	32	160	1024	32,768	

• If a program needs 2^n steps for execution, then when $n=40$, the number of steps needed is approximately 1.1×10^{12} . On a computer performing 1 billion steps per second, this would require about 18.3 minutes. If $n=50$, the same program would run for about 13 days on this computer. When $n=60$, about 310.56 years will be required to execute the program and when $n=100$, about 4×10^{13} years will be needed. \therefore For exp programs, utility - ($n \leq 40$).

• Programs that have a complexity that is a polynomial of high degree are also of limited utility. For ex, if a program needs n^{10} steps, then using our 1 billion steps per second computer we will need 10 seconds when $n=10$; 3171 years when $n=100$; and 3.17×10^{13} years when $n=1000$.

• From a practical standpoint, it is evident for reasonably large n (say $n > 100$), only programs of small complexity (such as $n, n \log n, n^2, n^3$) are feasible.

• 4×10^{13} years is about 2900 times the current age of the universe. It is longer than any star will live.

• If $n=10^9$, $2^n = 32 \times 10^{283}$ y on a 1-billion steps per-second computer.

10^{283} > all known physical timescales

Black hole evaporation (supermassive)
max 10^{110} .