

**Termination:** The loop terminates when  $i = \text{MAX\_SIZE}$   
 $\therefore$  By loop invariant and by correctness of Loop(K),

$\forall x, x \in \mathbb{N}, 0 \leq x < \text{MAX\_SIZE}$ , the element  $c[x][x]$  is computed correctly.

$\therefore$  For row  $i$ , <sup>all</sup> the elements of the product matrix  $c$  has been computed correctly.  $\square$

### Outer Loop Invariant

Just before the start of the iteration when  $i = n$ , the matrix  $c$  has been correctly computed for all rows from 0 to  $(n-1)$ .

**Initialization:** ~~when~~  $i = 0$ .  $\therefore n = 0$ , the indexes from 0 to -1 doesn't make sense.  $\therefore$  The outer loop invariant trivially holds

**Maintenance:** Let, just before the start of the iteration when  $i = n$ , the loop invariant ~~holds~~ holds.  $\therefore \forall x, x \in \mathbb{N}, 0 \leq x < n-1$ , the corresponding matrix elements for row  $c[x]$  has been computed correctly. Now,  $i = n$ . By correctness of the two inner loops,  $\forall y, y \in \mathbb{N}, 0 \leq y < \text{MAX\_SIZE}$ ,  $c[x][y]$  has been computed correctly.  $\therefore$  Row ~~n~~  $n$  is also computed correctly.

The variable  $i$  gets updated to  $(n+1)$ . We see,  $\forall x, x \in \mathbb{N}, 0 \leq x < (n+1)-1$ , the corresponding matrix elements for row  $c[x]$  has been correctly computed.  $\therefore$  Loop invariant still holds.

**Termination:** The loop terminates when  $i = \text{MAX\_SIZE}$ .  $\therefore$  By Loop invariant, the matrix  $c$  has been correctly computed for all rows from 0 to  $(\text{MAX\_SIZE}-1)$ . By using correctness of the two inner loops,  $\forall x, y, 0 \leq x, y < \text{MAX\_SIZE}$

$$c[x][y] = \sum_{k=0}^{\text{MAX\_SIZE}-1} a[x][k] * b[k][y], \therefore \text{The product matrix is correctly computed } \square$$