

b)  $n \log n = \Theta(n^2)$ . Suppose, it is true.  $\therefore$  There exists <sup>ve</sup> constants  $c_1, c_2$ , no s.t.  
 $\boxed{c_1 n^2 \leq n \log n \leq c_2 n^2, \text{ for } n \geq n_0}$   $n \log n \leq c_2 n^2 \Rightarrow \log n \leq c_2 \Rightarrow \sqrt[n]{n} \leq 2^{c_2}$   
 There is no upper bound on  $n$ .  $\therefore$  Contradiction

c)  $\frac{n^2}{\log n} = \Theta(n^2)$ . Suppose it is true.  $\therefore$  There exists +ve constants  $c_1, c_2$ , no s.t.  
 $\boxed{c_1 n^2 \leq \frac{n^2}{\log n} \leq c_2 n^2, \text{ for } n \geq n_0}$   $c_1 n^2 \leq \frac{n^2}{\log n} \Rightarrow \log n \leq \frac{1}{c_1}$   
 $\Rightarrow \sqrt[n]{n} \leq 2^{1/c_1}$

There is no upper bound on  $n$ .  $\therefore$  Contradiction

d)  $n^2 \cdot 2^n + 6n^2 3^n = O(n^2 \cdot 2^n)$ . Suppose it is true.  $\therefore$  There exists +ve constants  $c$ , no s.t.  
 $\boxed{n^2 \cdot 2^n + 6n^2 3^n \leq c n^2 \cdot 2^n \text{ for } n \geq n_0}$

$$6n^2 3^n \leq c n^2 \cdot 2^n \Rightarrow 6 \cdot 3^n \leq 2^n (c - n) \Rightarrow [6 \cdot (1.5)^n + n \leq c]$$

If  $n \rightarrow \infty$ ,  $6(1.5)^n + n \rightarrow \infty$   $\therefore$  Contradiction

e)  $3^n = O(2^n)$ . Suppose it is true.  $\therefore$  There exists +ve constants  $c$ , no s.t.  
 $\boxed{3^n \leq c \cdot 2^n \text{ for } n \geq n_0}$   $\therefore \left(\frac{3}{2}\right)^n \leq c \Rightarrow (1.5)^n \leq c$   
 As  $n \rightarrow \infty$ ,  $(1.5)^n \rightarrow \infty$   $\therefore$  Contradiction

Statement	Asymptotic Analysis
5) void printMatrix(int matrix[][MAX_SIZE], int rows, int cols)	$\Theta(1)$
int i;	$\Theta(1)$
for(i=0; i<rows; i++)	$\Theta(1)$
{ for(j=0; j<cols; j++)	$\Theta(\text{rows})$
printf("%d", matrix[i][j]);	$\Theta(1)$
printf("\n");	$\Theta(\text{rows} \cdot \text{cols})$
}	$\Theta(\text{rows} \cdot \text{cols})$
	$\Theta(\text{rows})$
	$\Theta(1)$
	$\Theta(1)$
Total:	$\Theta(\text{rows} \cdot \text{cols})$