

**Claim:** Lines 6-9 and lines 16-18 will be executed ~~multiple times~~  $(n+1)$  and  $n$  times respectively

**Proof:** The proof will be by mathematical induction on the degree  $n$  of the polynomial.

**Base Case:**  $n=0$ . Here  $A(x) = x^0$  and  $B(x) = x^1$ .  $\text{startA} = \text{finishA} = 0$  and  $\text{startB} = \text{finishB} = 1$ . (Initially)

• The while loop condn. on line 4 holds. By correctness of compare function on line 5 inside the switch conditional,  $\because \text{OK}1, -1$  is returned and lines 6-9 will be evaluated. On line 8, we update value of  $\text{startB}$  to 2 and break out from the switch block on line 9. Now on line 4, the while condn. fails because  $\text{startB} = 2 > \text{finishB} = 1$ .  
 $\therefore$  Lines 6-9 gets executed  $(n+1=1)$  time and lines 16-18 will be executed  $n=0$  time.

**Induction hypothesis:**  $n=K$ .  $A(x) = x^{2K} + x^{2(K-1)} + \dots + x^2 + x^0$  and  $B(x) = x^{2K+1} + x^{2K-1} + \dots + x^3 + x$ .  $\text{startA} = 0$ ,  $\text{finishA} = K$  and  $\text{startB} = K+1$ ,  $\text{finishB} = 2K+1$  (Initially).

• We assume that lines 6-9 will be executed  $(K+1)$  times and lines 16-18 will be executed  $K$  times.

**Induction Step:**  $n=K+1$ .  $A(x) = x^{2K+2} + x^{2K} + x^{2K-2} + \dots + x^2 + x^0$  and  $B(x) = x^{2K+3} + x^{2K+1} + \dots + x^3 + x$ .  $\text{startA} = 0$ ,  $\text{finishA} = K+1$  and  $\text{startB} = K+2$ ,  $\text{finishB} = 2K+3$  (Initially).

• The while loop condition holds (line 4). On line 5, by correctness of the compare function in the switch condn, since  $2K+2 < 2K+3$ ,  $-1$  is returned and lines 6-9 is evaluated. On line 8, we update  $\text{startB}$  to  $K+2$  and on line 9 we break out from the switch condition.

• The while loop condition again holds (line 4). On line 5, by correctness of the