

ascending order. Before the start of the next iteration  $i$  updates to  $(i+1)$  and it's easy to see that the loop invariant is preserved.

**Termination:** The outer loop terminates when  $i = a[0].col$ . We already know that  $a[0].col$  stores the no. of columns in  $a[]$ .

By the loop invariant, the transpose of all non-zero elements in columns 0 to  $a[0].col-1$  (i.e. all the columns of matrix  $a$ ) have been correctly placed in  $b[]$  as triples  $\langle row, col, value \rangle$ , where  $row = a[i].col$ ,  $col = a[i].row$ , and  $value = a[i].value$ . These entries occupies the first  $currentb$  posns. of  $b$  and are arranged such that: 1) The row fields in  $b[i]$  to  $b[currentb-1]$  are in ascending order. 2) For entries with the same row, the col fields are in ascending order.

$\therefore$  matrix  $b[]$  stores the transpose of matrix  $a[]$ , follows the criterion of sparse matrix representation. Hence, the function is correct  $\square$

**Time Complexity:**  $O(\text{columns} \times \text{elements})$  (Easy to see)

• This time is a little disturbing since we know that if we represented our matrices as two-dimensional arrays of size  $rows \times columns$ , we could obtain the transpose in  $O(rows \cdot columns)$  time. The algorithm to accomplish this has the simple form:

```
for (j = 0; j < columns; j++)  
    for (i = 0; i < rows; i++)  
        b[j][i] = a[i][j];
```

The  $O(\text{columns} \cdot \text{elements})$  time for our transpose function becomes  $O(\text{columns}^2 \cdot row)$  when the number of elements is of the order  $columns \cdot rows$ .