

## 2.5.3 Transposing a Matrix

• To transpose a matrix we must interchange the rows and columns. This means that each element  $a[i][j]$  in the original matrix becomes element  $b[j][i]$  in the transpose matrix.

### First algorithm

for each row  $i$

take element  $\langle i, j, \text{value} \rangle$   
and store it as element  $\langle j, i, \text{value} \rangle$   
of the transpose;

	row	col	value
$b[0]$	6	6	8
$[1]$	0	0	15
$[2]$	0	4	91
$[3]$	1	1	11
$[4]$	2	1	3
$[5]$	2	5	28
$[6]$	3	0	22
$[7]$	3	2	-6
$[8]$	5	0	-15

**Problem:** If we process the original matrix by the row indices we will not know exactly where to place element  $\langle j, i, \text{value} \rangle$  in the transpose matrix until we have processed all the elements that precede it.

Eq:  $(0, 0, 15)$  becomes  $(0, 0, 15)$ ;  $(0, 3, 22)$  becomes  $(3, 0, 22)$ ;  $(0, 5, -15)$  becomes  $(5, 0, -15)$ .

- If we place these triples consecutively in the transpose matrix, then, as we insert new triples, we must move elements to maintain the correct order.
- We can avoid this data movement by using the column indices to determine the placement of elements in the transpose matrix.

### Second algorithm

for all elements in column  $j$   
place element  $\langle i, j, \text{value} \rangle$  in element  $\langle j, i, \text{value} \rangle$

### Transpose of example matrix