

is empty. Any claim on an empty set is vacuously true. \therefore Loop invariant holds \square .

1) a **Maintenance:** Let, the loop invariant hold just before the start of the iteration when $i = x$, where $0 \leq x < \text{numCols}$. $\therefore \forall K, 0 \leq K < x$, ~~rowTerms[K] = 0~~.
rowTerms[K] = 0. Line 9 implies rowTerms[x] = 0. Before the start of the next iteration, i updates to $(x+1)$ and it's easy to see that the loop invariant still holds.

Termination: The loop terminates when $i = \text{numCols}$. By the loop invariant, $a[0].\text{col}$
 $\forall K, 0 \leq K < \text{numCols} - 1$, rowTerms[K] = 0. We know, by line 4 $\text{numCols} = a[0].\text{col}$
 \therefore For each column of $a[]$, the array holding the respective no. of non-zero elements has been initially initialized to 0. \square

Loop invariant of lines 10-11: ~~Just~~ Just before the start of the i th iteration of the loop, for all indices K where $1 \leq K \leq i$, the no. of elements corresponding to each column j where $0 \leq j < a[0].\text{col}$ has been correctly computed and stored in rowTerms[j] for all the terms $a[K].\text{value}$. \rightarrow bit vague.

Suggested Refinement (ChatGPT): At the beginning of the i th iteration (where $1 \leq i \leq \text{numTerms}$), for every column index j in the range ~~$0 \leq j < a[0].\text{col}$~~ $0 \leq j < a[0].\text{col}$, the value rowTerms[j] is equal to the number of times $a[K].\text{col} == j$ for all K such that $1 \leq K \leq i$.

Initialization: At the start of the 1st iteration of the loop, $i = 1$.

Just before the start of this iteration, the term indices of $a[]$ $1 \leq K < i = 1$ is empty. Any claim on an empty set is vacuously true.