

2. Each exponent is unique within a polynomial. There are no duplicate exponents (eg: no two terms like $3x^2 + 4x^2$ — these would already be combined during construction).

While Loop Invariant

• At the beginning of each loop iteration, for all exponents $\text{exp} > \max(\text{terms}[\text{startA}], \text{terms}[\text{startB}].\text{expon})$ s.t. $\exists i, j$ where $(0 \leq i < \text{startA}$ and $\text{exp} = \text{terms}[i].\text{expon})$ or $(\text{finishA} + 1 \leq j < \text{startB}$ and $\text{exp} = \text{terms}[j].\text{expon})$, we have already calculated the correct corresponding coefficient for x^{exp} in the polynomial D.

Initialization: At the beginning of the 1st iteration, $\text{startA} = 0$, $\text{startB} = \text{finishA} + 1$. This is according to our original representation where polynomial B is just after polynomial A. The index $0 \leq i < \text{startA} = 0$ and $\text{finishA} + 1 \leq j < \text{finishA} + 1$ doesn't logically make sense. \therefore The Loop invariant automatically holds.

Maintenance: Let, $\text{startA} = x$ and $\text{startB} = y$. $0 \leq x < \text{finishA}$ and $\text{startB} = \text{finishA} + 1 \leq y < \text{finishB}$. Let, the loop invariant hold just before the start of this iteration.

\therefore For all exponents $\text{exp} > \max(\text{terms}[x].\text{expon}, \text{terms}[y].\text{expon})$ s.t. $\exists i, j$ where $(0 \leq i < x$ and $\text{exp} = \text{terms}[i].\text{expon})$ or $(\text{finishA} + 1 \leq j < y$ and $\text{exp} = \text{terms}[j].\text{expon})$, we have already calculated the corresponding coefficient for x^{exp} in the polynomial D.

• From lines 5-19, we can see that we have a switch block. In the switch condn. on line 5 we compare $\text{terms}[x].\text{expon}$ and $\text{terms}[y].\text{expon}$. Suppose, wlog, $\text{terms}[x].\text{expon} < \text{terms}[y].\text{expon}$. \therefore COMPARE will return -1 and lines 6-9 will be evaluated. By correctness of attach function, the coefficient of $\text{terms}[y]$ along with the respective