



Claim: For all $n \in \mathbb{N}$, $0 \leq \text{begin} \leq n$, the function `all_comb` on the ~~leaf~~ parameters $(\text{tval}, \text{begin}, n)$ is called 2^{begin} times.

Proof: First, we show that for a fixed n , and $\forall \text{begin} \leq n$, $\text{begin} \geq 0$, the function `all_comb` on the parameters $(\text{tval}, \text{begin}, n)$ is called 2^{begin} times. The proof is by mathematical induction on begin .

Base Case: $\text{begin} = 0$. If $n = 0$, the if condn. on line 4 would be satisfied. It's easy to see then that only the newline on line 9 will be printed then, and the function would return ~~not~~ ~~no~~ void.

• If $n > 0$, then the else block on lines 11-18 will execute. The function is called twice by lines 15, 17. On both cases, the function parameters are $(\text{tval}, \text{begin}+1=1, n)$. It's easy to see that the value of begin can never again be 0, because otherwise, when the function