

$$\begin{aligned}
1. a^2+b^2+c^2 &= (6K_1)^2 + (6K_2)^2 + (6K_3)^2 = 6(36K_1^2 + 36K_2^2 + 36K_3^2) \\
2. a^2+b^2+c^2 &= (6K_1)^2 + (6K_2+1)^2 + (6K_3+5)^2 = 216K_1^2 + 216K_2^2 + 108K_2^2 + 18K_2 + 1 \\
&\quad + 216K_3^2 + 540K_3^2 + 750K_3 + 25 \\
&= 6(36K_1^2 + 36K_2^2 + 36K_3^2 + 18K_2^2 + 3K_2 + 90K_3^2 + 125K_3 + 21) \\
3. a^2+b^2+c^2 &= (6K_1)^2 + (6K_2+2)^2 + (6K_3+4)^2 = 216K_1^2 + 216K_2^2 + 216K_2^2 + 72K_2 + 8 \\
&\quad + 216K_3^2 + 12 \times 36K_3^2 + 48 \times 6K_3 + 64 \\
&= 6(36K_1^2 + 36K_2^2 + 36K_2^2 + 12K_2 + 36K_3^2 + 72K_3^2 + 48K_3 + 12) \\
4. a^2+b^2+c^2 &= (6K_1)^2 + (6K_2+3)^2 + (6K_3+3)^2 = 216K_1^2 + 216K_2^2 + 3 \cdot 36K_2^2 \cdot 3 \\
&\quad + 3 \cdot 6K_2 \cdot 9 + 27 + 216K_3^2 + 3 \cdot 36K_3^2 \cdot 3 + 3 \cdot 6K_3 \cdot 9 + 27 \\
&= 6(36K_1^2 + 36K_2^2 + 54K_2^2 + 27K_2 + 36K_3^2 + 54K_3^2 + 27K_3 + 9) \\
5. a^2+b^2+c^2 &= (6K_1+1)^2 + (6K_2+1)^2 + (6K_3+4)^2 = 216K_1^2 + 108K_1^2 + 18K_1 + 1 \\
&\quad + 216K_2^2 + 108K_2^2 + 18K_2 + 1 + 216K_3^2 + 12 \cdot 36K_3^2 + 48 \cdot 6K_3 + 64 \\
&= 6(36K_1^2 + 18K_1^2 + 3K_1 + 36K_2^2 + 18K_2^2 + 3K_2 + 36K_3^2 + 72K_3^2 + 48K_3 + 11) \\
6. a^2+b^2+c^2 &= (6K_1+1)^2 + (6K_2+2)^2 + (6K_3+3)^2 = 216K_1^2 + 108K_1^2 + 18K_1 + 1 \\
&\quad + 216K_2^2 + 216K_2^2 + 72K_2 + 8 + 216K_3^2 + 9 \cdot 36K_3^2 + 18 \cdot 9K_3 + 9 \\
&= 6(36K_1^2 + 18K_1^2 + 3K_1 + 36K_2^2 + 36K_2^2 + 12K_2 + 36K_3^2 + 54K_3^2 + 27K_3 + 3) \\
7. a^2+b^2+c^2 &= (6K_1+2)^2 + (6K_2+2)^2 + (6K_3+2)^2 = 6(36K_1^2 + 36K_1^2 + 12K_1 \\
&\quad + 36K_2^2 + 36K_2^2 + 12K_2 + 36K_3^2 + 36K_3^2 + 12K_3 + 4)
\end{aligned}$$

Prob 27: The sum of the squares of three natural numbers is divisible by 9. Prove that we can choose two of these ^{no.s} ~~no.s~~ such that their difference is div by 9. (Wrong question)

By division algorithm, $\forall x \in \mathbb{N}, x = 9p$ or $x = 9p+1$ or $x = 9p+2$ for some $p \in \mathbb{N}$.

Let, $a, b, c \in \mathbb{N}$. ~~Let~~ $a = 9p, 9p+1$ or $9p+2$; $b = 9q, 9q+1, 9q+2$,
 $c = 9r, 9r+1, 9r+2$ for some $p, q, r \in \mathbb{Z}$