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STAT2203 - Probability Models and Data Analysis for Engineering

STAT2203 Assignment 1

Question 1

Let S be the event the system succeeds Let A be the event that a joint is successful Let L_i^l be the event that an O-ring is successful $\mathbb{P}(L_i) = 1 - \mathbb{P}(L_i^c)$

$$\mathbb{P}(L_i) = 1 - \mathbb{P}(L_i^c)$$

$$= 1 - 0.1 \qquad \text{(From question)}$$

$$= 0.9$$

$$\mathbb{P}(A_i^c) = \mathbb{P}(L_i \cap L_i)$$

$$= \mathbb{P}(L_i^c)\mathbb{P}(L_i^c)$$

$$= 2 \times 0.1$$

$$= 0.01$$

$$\mathbb{P}(A_i) = 0.99$$

$$\mathbb{P}(S) = \mathbb{P}(A_i \cap A_i \cap A_i \cap A_i \cap A_i \cap A_i)$$

$$= \mathbb{P}(A_i)^6$$

$$= 0.99^6$$

$$= 0.9415$$

$$\mathbb{P}(S^c) = 1 - \mathbb{P}(S)$$

$$\approx 0.0585$$

Therefore the probability that the system will fail is 5.85%

Question 2

Let R_i be the event that i is received Let S_i be the event that i is sent From the question:

$$\mathbb{P}(S_0) = 0.5$$

$$\mathbb{P}(S_1) = 0.5$$

$$\mathbb{P}(R_1 \mid S_1) = 0.9$$

$$\mathbb{P}(R_0 \mid S_0) = 0.95$$

Using Baynes rule:

$$\mathbb{P}(S_0 \mid R_1) = \frac{\mathbb{P}(R_1 \mid S_0) \mathbb{P}(S_0)}{\mathbb{P}(R_1 \mid S_0) \mathbb{P}(S_0) + \mathbb{P}(R_1 \mid S_1) \mathbb{P}(S_1)}$$
$$= \frac{(1 - 0.95) \times 0.5}{(1 - 0.95) \times 0.5 + 0.9 \times 0.5}$$
$$= \frac{1}{19} \approx 0.0526$$

Therefore, given we receive a 1 it is 5.26% likely that a 0 was sent

Question 3

Let A be the event that the sum of numbers is 1

$$\Omega = \{-1, 0, 1\}$$

Assume that the each number is draw at equal probability

Without Replacement

$$(1,0),$$
 $(1,-1),$ $(0,1),$ $(0,-1),$ $(-1,0),$ $(1,1)$
 1 0 1 -1 0

Therefore:

$$\mathbb{P}(A) = \frac{|A|}{|\Omega|}$$
$$= \frac{2}{6} = \frac{1}{3}$$

With Replacement

Therefore:

$$\mathbb{P}(A) = \frac{|A|}{|\Omega|}$$
$$= \frac{2}{9}$$

Question 4

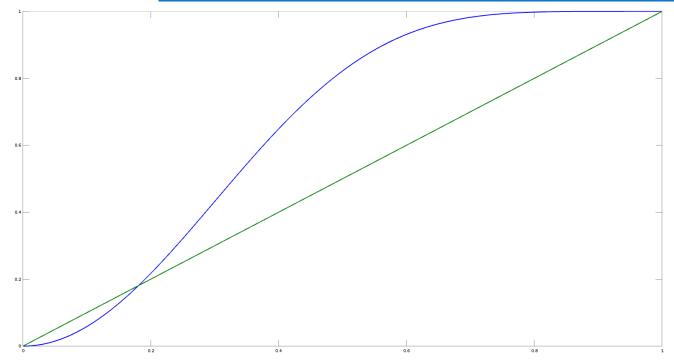


Figure 1: Question 4 Answer

```
function result = ass1
 2
     N = 1e3;
     x = linspace(0, 1, N);
      y = [1:N];
 5
      for i = 1:N
 6
       y(i) = systemFailure(x(i));
 7
8
      plot(x, y, "linewidth", 2, x, x, "linewidth", 2);
9
    endfunction
10
11
   function result = linkSuccess(p)
      result = 1 - p;
12
13
    endfunction
14
15 function result = sealSuccess(p)
16
     result = 1 - (1 - linkSuccess(p))^2;
17
   endfunction
18
   function result = systemSuccess(p)
19
20
      result = sealSuccess(p)^6;
21
22
    endfunction
23
   function result = systemFailure(p)
24
      result = 1 - systemSuccess(p);
    endfunction
```

Question 5

```
function result = ass1q5
     N = 1e4;
 2
 3
      received = 0;
      sent0 = 0;
 5
      for i = 1:N
 6
        [s, r] = get_receive_bit();
 7
        if r == 1
 8
         received += 1;
 9
          if s == 0
10
            sent0 += 1;
11
          endif
12
        endif
13
      end
      printf("%d:%d\n", received, sent0);
14
15
    endfunction
16
17
   function [sent, received] = get_receive_bit
      bit = get_sent_bit();
18
      if bit == 1
19
20
        if rand >= 0.9
21
          received = bit;
22
        else
23
         received = 0;
24
        endif
25
      else
26
        if rand >= 0.95
27
         received = bit;
28
        else
29
          received = 1;
30
        endif
31
      endif
32
      sent = bit;
33
    endfunction
34
35
   function result = get_sent_bit
      if rand >= 0.5
36
37
       result = 1;
38
39
        result = 0;
40
      endif
   endfunction
```

Based on the code above, the output by running ass1q5, we can expect an answer close to 5241:4728