WebAssembly library construction for investment portfolio optimization using genetic algorithms

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Abstract

Constructing a WebAssembly library in C++20, clang and Rational Unified Process to choose an investment portfolio since Modern Portfolio Theory (MPT) using genetic algorithms.

Keywords: multi-objective problems, optimization algorithms, C++20, software library, evolutionary computation, investment portfolio optimization

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Because time is the difference between feasible and unfeasible multi-objective constrained optimization problems in high-dimension and their solution is highly esteemed to cast aside (especially when there is money as in this project or another key resource allocation), whichever extra performance is a step forward to do it as in a software library construction used in production.

To get roses and perform an excel work running in the Web (a real-time production environment), I'd chosen C++20, clang and Rational Unified Process to solve a constrained investment portfolio optimization problem (CPOP) from the state-of-the-art and compare my API suggesting improvements to the algorithms provided by Coello et al. (2006) bringing into play (Aranha & Iba, 2008; Liagkouras & Metaxiotis, 2015; Turcas et al., 2017) assessing by Apipie and Georgescu (2019) metrics e.g. we'll select same 20 Bucharest Stock Exchange assets and after 500 stocks from S&P500.

So, it's an applied project driven by a quantitative method whose intended readers are developers in the finance industry, investors, stock market speculator, managers, and other researchers concerned about portfolio optimization.

In following sections, you'll read about how to choose a portfolio on Modern Portfolio Theory (MPT) introduced by (Markowitz, 1952; Roy, 1952) and find it a solution on Multiobjective Evolutionary Algorithm (MOEA), and constructing a solution with C++20 who works real-time in the Web from scratch.

Problem Description and Statement

Allocate a fixed amount of capital among n assets such as stocks, funds, bonds, and so forth in order to find the best Sharpe Ratio: maximizing the expected return and minimizing the risk -the covariance matrix of returns- from real-time data in the Web. So, it's constrained multi-objective optimization.

Goals

The project aims at constructing an open-source software library in C++20 running in the Web for constrained multi-objective optimization by new evolutionary algorithms based on Coello's work to solve a Markowitz's portfolio optimization problem. It includes objectives like implementing the algorithms, benchmarking the results obtained, and suggesting improvements in space, time, and clarity about them.

Why matters?

Financial institutions are relentless maximize their returns at an up-to-scratch level of risk, so choosing the best portfolio is an essential asset of fund management.

Since Sefiane and Benbouziane (2012) confirms evolutionary algorithms' validity and efficiency, better techniques will have better-applied results as pretends to do this project.

Background

Although the industry has unlike solver packages to optimize a portfolio involving evolutionary algorithms, quadratic programming, and so forth, none runs in the Web from a client (table 1 summarizes the packages). So the leading knowledge fields are evolutionary algorithms in the Web browsers in order to choose an investment portfolio in real time.

We know which are the most frequently used multiobjective evolutionary algorithm (MOEAs) and their performance metrics for solving the portfolio optimization problem by (Apipie & Georgescu, 2019; Coello et al., 2006; Liagkouras & Metaxiotis, 2015). See table 2.

Because realistic constraints become CPOP to a quadratic mixed-integer problem (QMIP) that is discrete NP-hard (Liagkouras & Metaxiotis, 2015), even though "there ain't no such thing as a free lunch" exists (Wolpert & Macready, 1997) choosing a right algorithm in order to perform better than each other (Apipie & Georgescu, 2019) is critical.

Theory

Optimization and Genetic Algorithms

Optimization dates back millennia, from Plato (427-347 BCE) and Aristotle (384-322 BCE) used to find the best society to most recently it used to allocate resources in World War II with George Dantzig (1914-2005). We'll focus on multi-objective optimization problems in a numerical sense and ending up analyzing a solution approach —genetic algorithms.

First off, we deal with present the basic optimization problem that is

$$\text{minimize } f(\mathbf{x}) \tag{1}$$

$$\text{subject to } \mathbf{x} \in \chi \tag{2}$$

where x is a design point, χ is the feasible set and it can be discrete or continuous, and f is the objective function. Among all points in the feasible set χ, the $\mathbf{x}$ that minimizes the objective function is called a solution or minimizer. A particular solution is denoted as $\mathbf{x}^*$. As we work with n-dimensional space, x is a vector and it's written as usual:

$$\mathbf{x} = [x_1, x_2, x_3, ..., x_i, ..., x_n] \tag{3}$$

where x_i is called decision variable or design variable.

Easily a minimization problem can be replaced by maximization problem and vice versa. From

$$\text{maximize } f(\mathbf{x}) \text{ subject to } \mathbf{x} \in \chi \tag{4}$$

to

$$\text{minimize } -f(\mathbf{x}) \text{ subject to } \mathbf{x} \in \chi \tag{5}$$

Kochenderfer and Wheeler (2019)

But, what is a feasible set? A feasible set is defined by the whole constraints where each constraint restricts of possible solutions. They are written with $\leq$, $\geq$, or $=$ since we work with numerical optimization. So, our problem follows the General Multiobjective Optimization Problem definition by Coello et al. (2006) that is

$$F(\mathbf{x}) = (f_1(\mathbf{x}), ..., f_k(\mathbf{x})) \tag{6}$$

subject to

$$g_i(\mathbf{x}) \leq 0, i = 1, ..., p \tag{7}$$

$$h_j(\mathbf{x}) = 0, j = 1, ..., q \tag{8}$$

and our goal is to find global minimizer, a particular $\mathbf{x}^*$ such that $f(\mathbf{x}^*) \leq f(\mathbf{x})$.

But some multi-objective problems are a tradeoff between costs, performance, and time, and it is unclear how to prioritize constraints, so when we search them a solution, we use Pareto optimality that is a design of equilibrium between tradeoff objectives. Then, we will describe domination, a criterion that compares two solutions.

Domination's definition. Domination is a relationship such that $\mathbf{x}$ dominates $\mathbf{x}'$ iff $f_i(\mathbf{x}) \leq f_i(\mathbf{x}')$ for all $i \in \{1, ..., m\}$ and $f_i(\mathbf{x}) < f_i(\mathbf{x}')$ for some i.

Also we say $\mathbf{x}$ is better than $\mathbf{x}'$. The non-dominated set is one that no point dominates its elements in criterionhttps://www.overleaf.com/project/6273e1b2a24f0f9cca6cb8bc space, which is called the Pareto frontier where criterion space is the image of χ through f, and it's written Υ. Criterion space is sometimes called objective function space.

Non-dominated set generator

A subproblem is how we can generate a non-dominated set but no criterion space in order to shed light on algorithm behavior. You can check out on https://github.com/sanchezcarlosjr/non-dominated-set-generator-cli/

Simplex and monotonic decreasing functions are non-dominated set. For instance 1 2 3 4 5.

How can we solve multi-objective problems?

We can solve multi-objective problems with enumerative, deterministic, or stochastic techniques, where genetic algorithms are the last ones, those heuristic algorithms are our object of study. A non-exhaustive list can be found on 6 and MOEA types and their score to solve CPOP is on 2.

We measure technique's solution with performance metrics 3, but most popular is hypervolume. Hernández Gómez (2018) made a fast unpublished C framework to calculate those metrics.

A genetic algorithm is defined by Coello et al. (2006), in short, it's a bio-inspired algorithm using evolution as a metaphor. I show you an outline below.

A foundational concept is population that is the generalized composite data structure on evolutionary algorithms 7.

Algorithm genetic do the following with population:

INITIALIZE-POPULATION makes a random population from design space and encodes it to binary, real, permutation, or tree.

THE TERMINATION CRITERION IS NOT TRUE uses it to determine when the algorithm ends. Perhaps, the easiest way is a generation limit.

SELECT-PARENTS-FOR-THE-NEXT-GENERATION evaluates a decoding population on the objective function, after that procedure applies a fitness function, and then it makes a mating pool with parents by the canonical selection, roulette wheel selection, or other. When the procedure always pass the best parent is called elitism.

CROSSOVER combines parents from mate pool to make offsprings. Some crossover schemes are single-point crossover, two-point crossover, uniform crossover.

MUTATE allows new traits exploration. Some mutation schemes over offsprings are flipping each bit with small rate for bit-valued chromosomes and Gaussian mutation for real-valued chromosomes.

Worked example

A worked example is useful to understand optimization problems and genetic algorithms. In genetic algorithms with elitism, each generation is closer to global minimum than previous generations how you can appreciate on 8.

$$F(x, y) = min(x^2 + y^2) \tag{9}$$

subject to

$$-5.14 \leq x \leq 5.14 \tag{10}$$

$$-5.14 \leq y \leq 5.14 \tag{11}$$

You can check out a genetic algorithm implementation on https://gist.github.com/sanchezcarlosjr/dc500b87169f1f0be17158ecb376e377. Another worked example is the path finder problem on https://graph-theory.sanchezcarlosjr.com/.

Modern Portfolio Theory (MPT)

In spite of (Buffett, 1997; Hathaway, 1996) said the MPT is twaddle and has no utility since its risk definition and its tendency to diversify are wrong incluiding it is precisely wrong than approximately right —value investing, MPT is the current paradigm. The constrained portfolio optimization problem (CPOP) is formulated as

$$f_i : \Omega \to R^m, \Omega \subset R^m, \Omega : \text{search space} \tag{12}$$

$$\text{Optimize objetive functions } f(w.) = (f_1(w), f_2(w)) \tag{13}$$

$$\text{Maximize portfolio return } f_1(w) = \sum_{i=1}^{m} w_i r_i \tag{14}$$

$$\text{Minimize portfolio return } f_2(w) = \sum_{i=1}^{m} \sum_{j=1}^{m} w_i w_j \sigma_i \sigma_j \rho_{ij} \tag{15}$$

where

$$m \equiv \text{number of stocks}, i, j \in [1, m]. \tag{16}$$

$$w_i \equiv i \text{ decision variable, } w_i \subset \Omega. \tag{17}$$

$$r_i \equiv \text{rate of return of asset } i. \tag{18}$$

$$\rho_{ij} \equiv \text{correlation between assets } i,\ j \text{ such as } -1 \leq \rho_{ij} \leq 1. \tag{19}$$

$$\sigma_i, \sigma_j \equiv \text{standard deviation of stocks returns } i \text{ and } j. \tag{20}$$

subject to

$$\sum_{i=1}^{m} w_i = 1 \tag{21}$$

$$0 \leq w_i \leq 1 \tag{22}$$

C++ library construction in the Web

Since web development no installation is required, it's free local ecosystem —operating system, local software, and so on, and now it's possible run better performance languages for instance C++, Rust to the client side by WebAssembly than JavaScript, safe, fast and portable client side web was chosen —Sletten, 2021. Of course, we may be limited to local hardware capabilities.

WebAssembly are the assembly set instructions running in the web and it executes a particular chip's instructions. Hence, you may compile C++ using the clang with backend wasm-ld. We made a toy project as proof of concept —calculator intrepreter, it's on https://calculator.sanchezcarlosjr.com/.

Methods

It is an applied project in computer science which means implementing state-of-the-art software —their efficiency and accuracy are our objects of study. Reliability concerns the robustness of the construction —free of "bugs" and crashes, and since the Rational Unified Process guarantees it —Jacobson et al. (1999), I chose it. You can see RUP phases and disciplines to 9, hence we'll use UML and develop iteratively.

On the other hand, validity is the accuracy between our MOEA output and Apipie and Georgescu (2019) performance metrics and experimental design, which means 3.

We'll choose same 20 Bucharest Stock Exchange assets as Apipie and Georgescu (2019) and after 500 stocks from S&P500 with real time data provided by Yahoo Finance API.

Even though our method can be reliable and valid, it can be twaddle and don't reflect the best portfolio investment.

Schedule

Following the Rational Unified Process, this is the schedule 10.

Conclusion

Since my current results, we can deduce it is possible to run efficiently on web genetic algorithms in order to solve CPOP.

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Table 1

Multi-objective optimization software packages

Name
Pymoo
MOSEK
Excel Solver Function
TOMLAB
NAG Numerical Library

Table 2

MOEA types and their score to solve CPOP

MOEA type	Research Percentage (%)	Score
MOPSO		70
NSGAII	29.17	47
SPEA2	25.00	51
PESA	16.67	
SPEA	8.33	
PAES	8.33	
MOGA	4.17	
NPGA2	4.17	
IBEA	4.17	
SPEA2SDE		56
MOEADDRA		54

Table 3

Performance metrics

Metric
Hypervolume (HV)
Generational distance (GD)
Inverted generational distance (IGD)
Averaged Hausdorff distance (Δp)
Spread metric Δ
Spacing metric (S)
Coverage of two sets (C)
Riesz s-energy

Figure 1

Cos

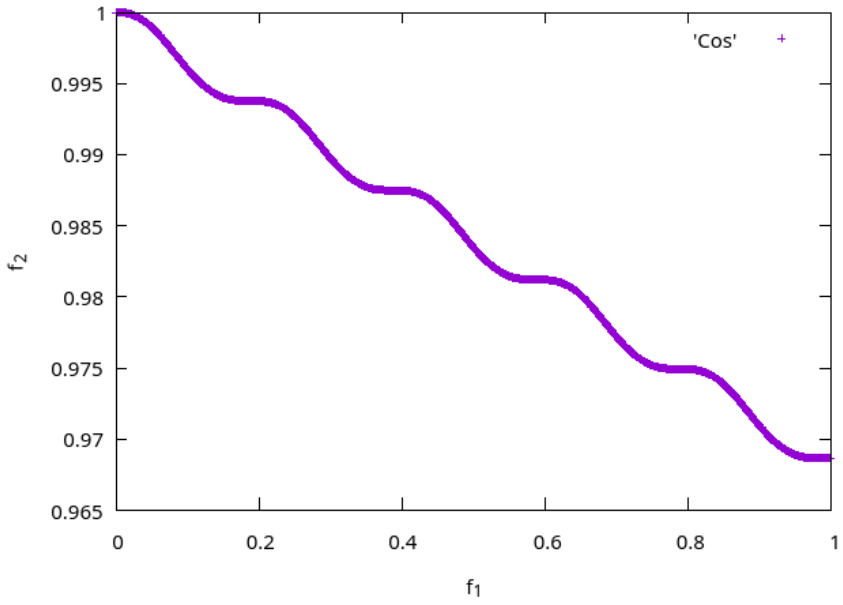

Figure 2

Exponential

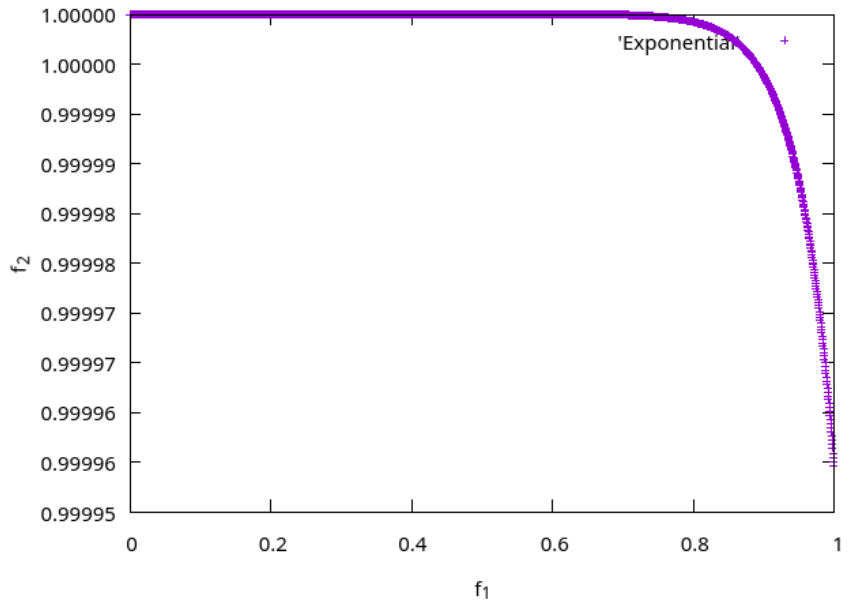

Figure 3

Simplex

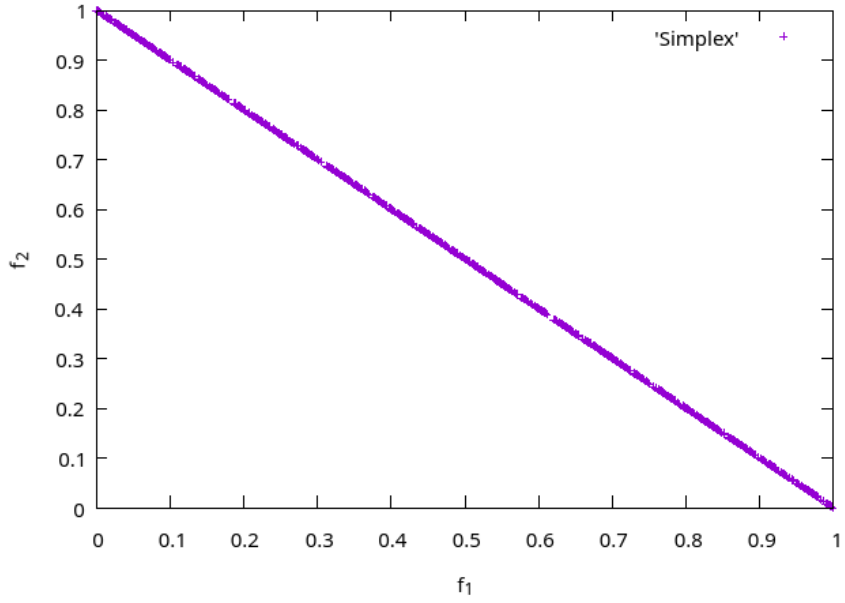

Figure 4

Polynomial

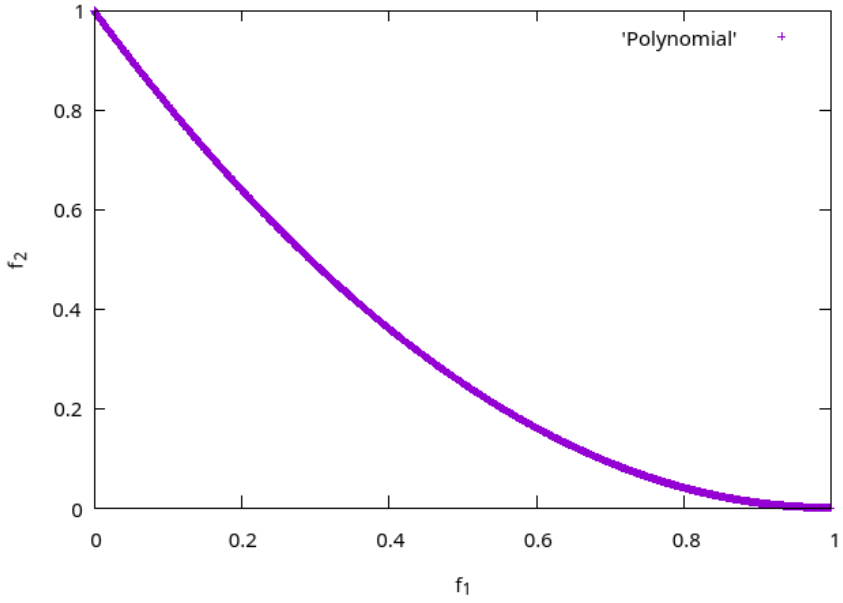

Figure 5

Sqrt

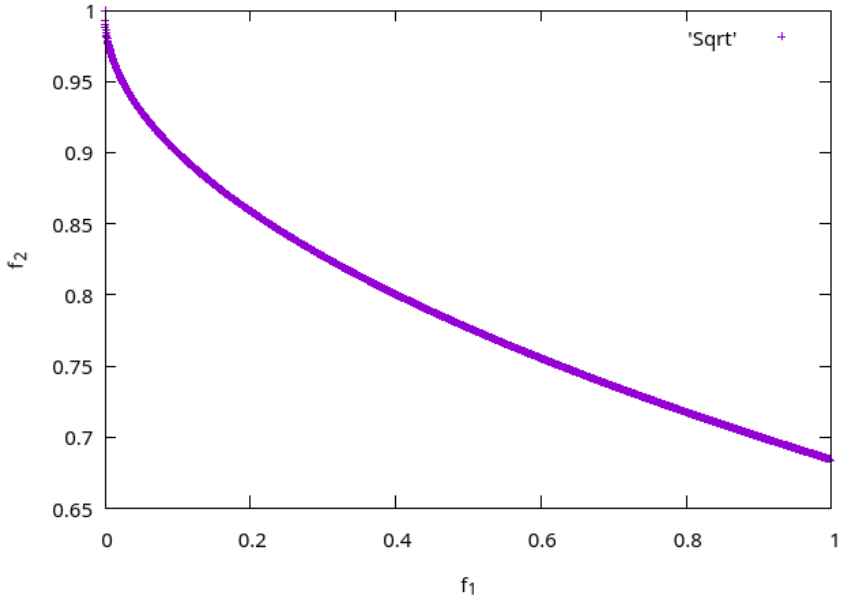

Figure 6

Global optimization approaches

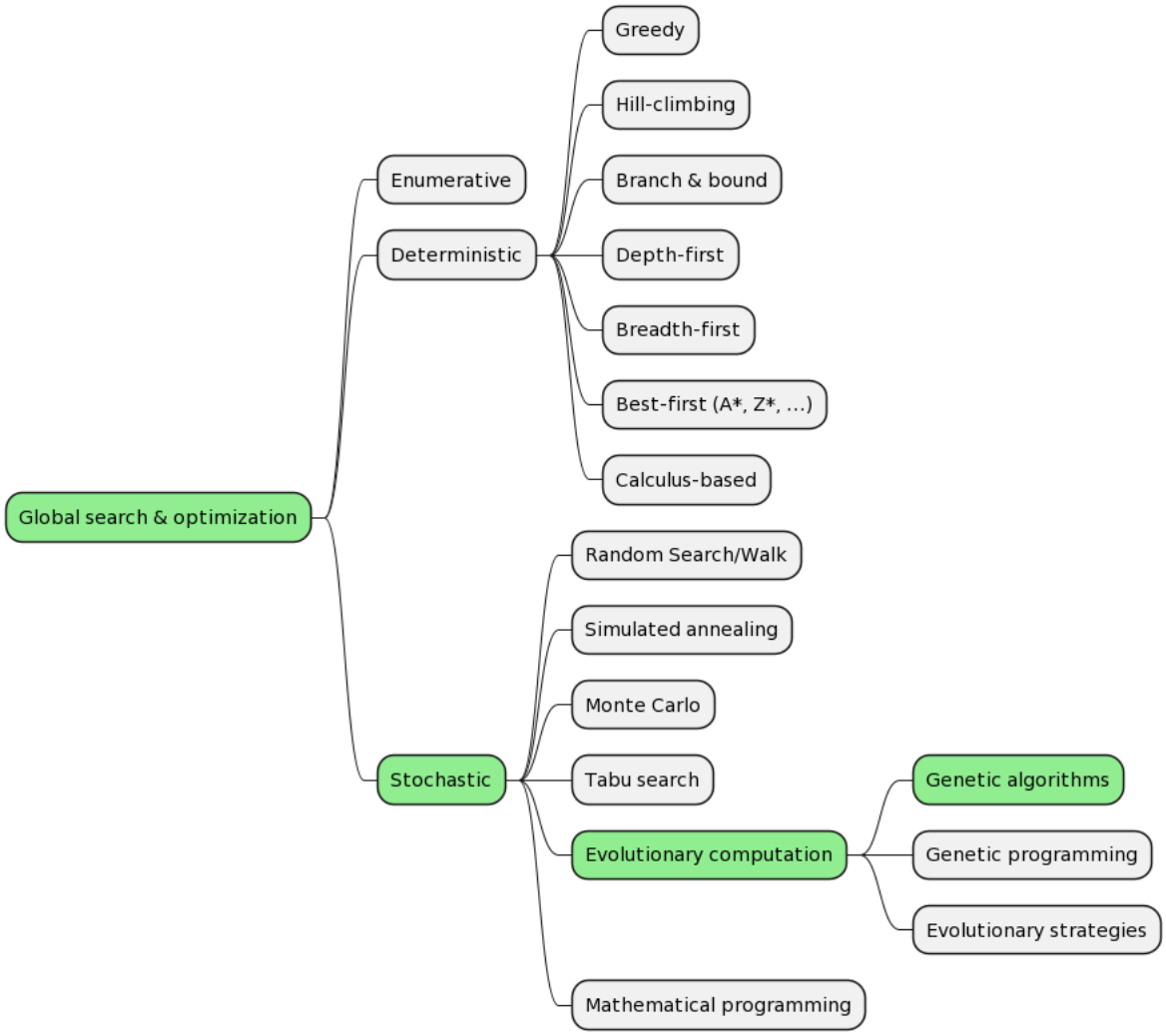

Figure 7

Population

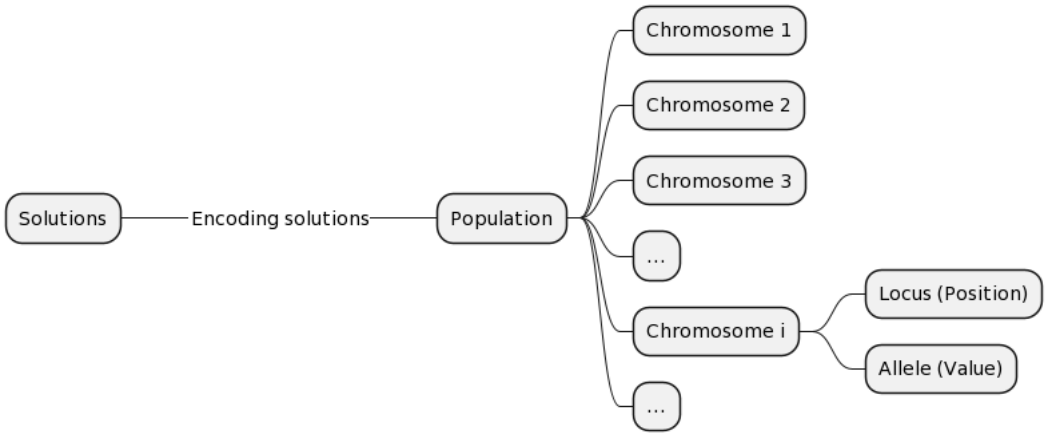

Figure 8

Polynomial

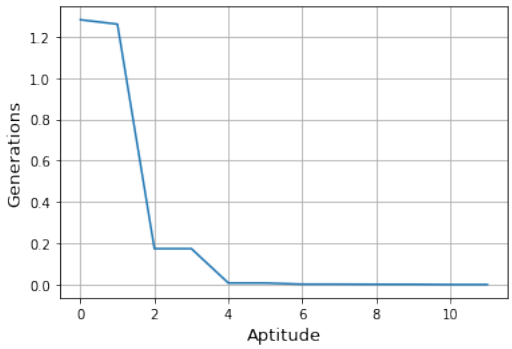

Figure 9

RUP phases and disciplines

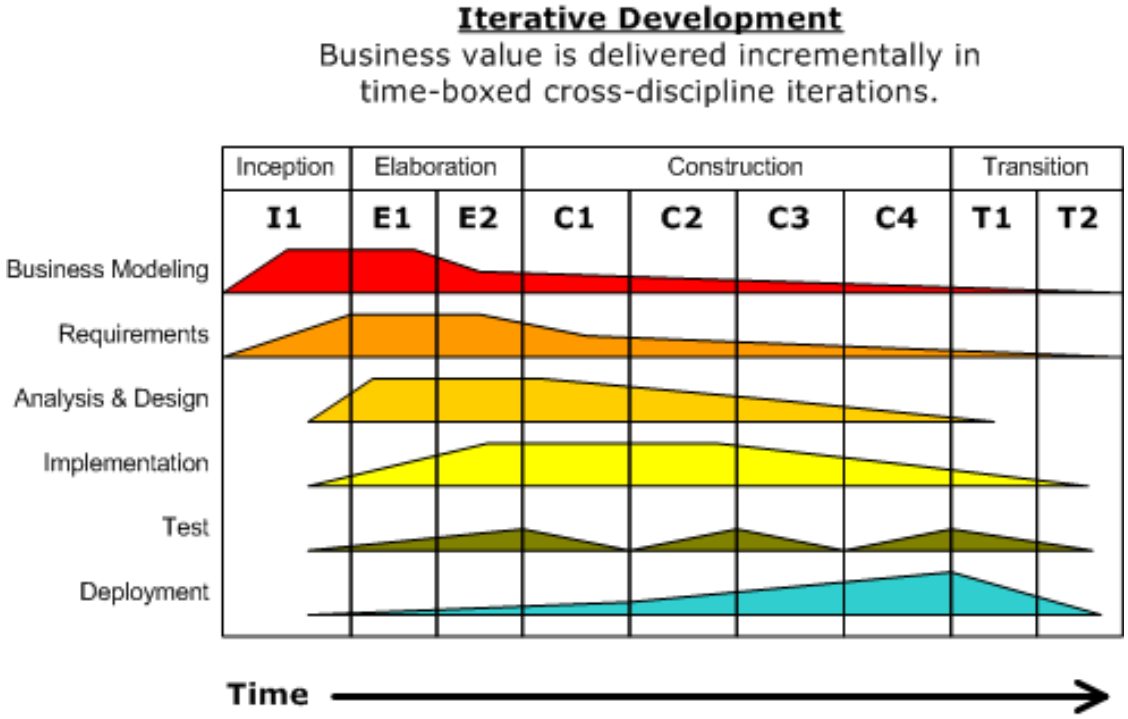

Figure 10

Schedule