INF385T_ML_Project_Prototype_updated

April 17, 2018

```
In [1]: # import required packages
        import numpy as np
        import pandas as pd
        import math
        import sklearn
        import sklearn.preprocessing
        import datetime
        import os
        import matplotlib.pyplot as plt
        import tensorflow as tf
In [2]: # display parent directory and working directory
        print(os.path.dirname(os.getcwd())+':', os.listdir(os.path.dirname(os.getcwd())));
        print(os.getcwd()+':', os.listdir(os.getcwd()));
/home/nbuser: ['.bash_logout', '.profile', '.bashrc', '.local', '.cache', '.nb.setup.log', 'anac
/home/nbuser/library: ['lab5.ipynb', 'Lab Assignment 3.ipynb', 'testing.ipynb', 'prices split ad
In [3]: # split data in 80%/10%/10% train/validation/test sets
        valid_set_size_percentage = 10
       test_set_size_percentage = 10
In [4]: # import stock prices data
        df = pd.read_csv("prices-split-adjusted.csv", index_col = 0)
       df.info()
        # number of different stocks
        print('\nnumber of different stocks: ', len(list(set(df.symbol))))
        print(list(set(df.symbol))[:10])
<class 'pandas.core.frame.DataFrame'>
Index: 851264 entries, 2016-01-05 to 2016-12-30
```

```
Data columns (total 6 columns):
          851264 non-null object
symbol
open
          851264 non-null float64
close
          851264 non-null float64
          851264 non-null float64
low
          851264 non-null float64
high
volume
          851264 non-null float64
dtypes: float64(5), object(1)
memory usage: 45.5+ MB
number of different stocks: 501
['LLY', 'SCG', 'PRU', 'PAYX', 'HD', 'RAI', 'MAR', 'XRX', 'GWW', 'SYK']
In [5]: df.head()
Out[5]:
                    symbol
                                             close
                                                            low
                                                                       high
                                                                                 volume
                                  open
        date
                                                                 126.250000
        2016-01-05
                     WLTW
                            123.430000
                                        125.839996
                                                     122.309998
                                                                              2163600.0
        2016-01-06
                     WLTW
                            125.239998
                                        119.980003
                                                     119.940002
                                                                 125.540001
                                                                              2386400.0
        2016-01-07
                     WLTW 116.379997
                                        114.949997
                                                     114.930000
                                                                 119.739998
                                                                              2489500.0
        2016-01-08
                     WLTW 115.480003 116.620003
                                                     113.500000
                                                                 117.440002
                                                                              2006300.0
        2016-01-11
                     WLTW 117.010002 114.970001
                                                     114.089996
                                                                117.330002 1408600.0
In [6]: df.tail()
Out [6]:
                    symbol
                                  open
                                             close
                                                            low
                                                                       high
                                                                                 volume
        date
        2016-12-30
                      ZBH
                            103.309998
                                        103.199997
                                                     102.849998
                                                                 103.930000
                                                                               973800.0
        2016-12-30
                     ZION
                             43.070000
                                         43.040001
                                                      42.689999
                                                                  43.310001
                                                                              1938100.0
        2016-12-30
                      ZTS
                             53.639999
                                         53.529999
                                                      53.270000
                                                                  53.740002
                                                                              1701200.0
        2016-12-30
                       AIV
                             44.730000
                                         45.450001
                                                      44.410000
                                                                  45.590000
                                                                              1380900.0
        2016-12-30
                      FTV
                             54.200001
                                         53.630001
                                                      53.389999
                                                                  54.480000
                                                                               705100.0
In [7]: df.describe()
Out [7]:
                         open
                                       close
                                                         low
                                                                       high \
               851264.000000
                              851264.000000
                                              851264.000000
                                                              851264.000000
        count
        mean
                   64.993618
                                   65.011913
                                                   64.336541
                                                                  65.639748
        std
                   75.203893
                                   75.201216
                                                   74.459518
                                                                  75.906861
                    1.660000
                                                    1.500000
        min
                                    1.590000
                                                                   1.810000
        25%
                   31.270000
                                   31.292776
                                                   30.940001
                                                                  31.620001
        50%
                                                   47.970001
                    48.459999
                                   48.480000
                                                                  48.959999
        75%
                   75.120003
                                   75.139999
                                                   74.400002
                                                                  75.849998
                                                 1549.939941
        max
                 1584.439941
                                 1578.130005
                                                                1600.930054
                     volume
               8.512640e+05
        count
```

5.415113e+06

mean

```
      std
      1.249468e+07

      min
      0.000000e+00

      25%
      1.221500e+06

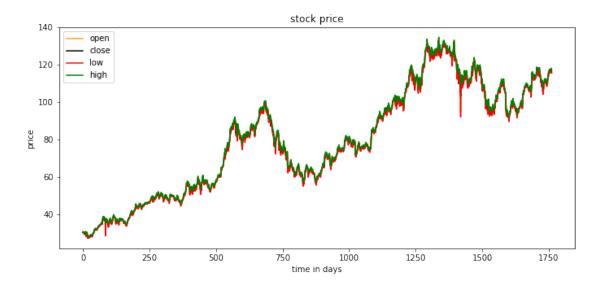
      50%
      2.476250e+06

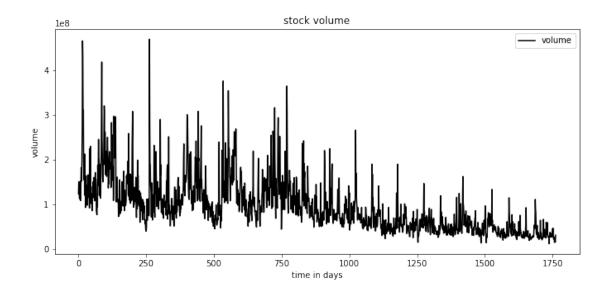
      75%
      5.222500e+06

      max
      8.596434e+08
```

In [8]: #Plotting volume and price of a specific stock versus time

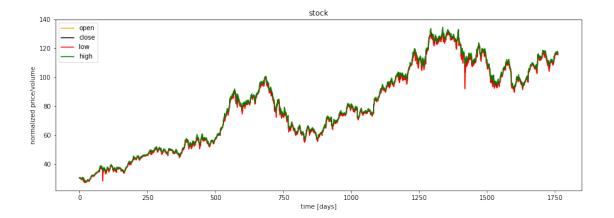
```
plt.figure(figsize=(25, 5));
plt.subplot(1,2,1);
plt.plot(df[df.symbol == 'AAPL'].open.values, color='orange', label='open')
plt.plot(df[df.symbol == 'AAPL'].close.values, color='black', label='close')
plt.plot(df[df.symbol == 'AAPL'].low.values, color='red', label='low')
plt.plot(df[df.symbol == 'AAPL'].high.values, color='green', label='high')
plt.title('stock price')
plt.xlabel('time in days')
plt.ylabel('price')
plt.legend(loc='best')
# plt.show()
plt.figure(figsize=(25, 5));
plt.subplot(1,2,2);
plt.plot(df[df.symbol == 'AAPL'].volume.values, color='black', label='volume')
plt.title('stock volume')
plt.xlabel('time in days')
plt.ylabel('volume')
plt.legend(loc='best');
plt.show()
```





```
In [9]: # function for min-max normalization of stock
        def normalize_data(df):
            min_max_scaler = sklearn.preprocessing.MinMaxScaler()
            df['open'] = min_max_scaler.fit_transform(df.open.values.reshape(-1,1))
            df['high'] = min_max_scaler.fit_transform(df.high.values.reshape(-1,1))
            df['low'] = min_max_scaler.fit_transform(df.low.values.reshape(-1,1))
            df['close'] = min_max_scaler.fit_transform(df['close'].values.reshape(-1,1))
            return df
        # function to create train, validation, test data given stock data and sequence length
        def load_data(stock, seq_len):
            raw_data = stock.as_matrix() # convert to numpy array
            data = []
            # create all possible sequences of length seq_len
            for index in range(len(raw_data) - seq_len):
                data.append(raw_data[index: index + seq_len])
            data = np.array(data);
            valid_set_size = int(np.round(valid_set_size_percentage/100*data.shape[0]));
            test_set_size = int(np.round(test_set_size_percentage/100*data.shape[0]));
            train_set_size = data.shape[0] - (valid_set_size + test_set_size);
            x_train = data[:train_set_size,:-1,:]
            y_train = data[:train_set_size,-1,:]
            x_valid = data[train_set_size:train_set_size+valid_set_size,:-1,:]
            y_valid = data[train_set_size:train_set_size+valid_set_size,-1,:]
```

```
x_test = data[train_set_size+valid_set_size:,:-1,:]
            y_test = data[train_set_size+valid_set_size:,-1,:]
            return [x_train, y_train, x_valid, y_valid, x_test, y_test]
        # choose one stock
        df_stock = df[df.symbol == 'AAPL'].copy()
        df_stock.drop(['symbol'],1,inplace=True)
        df_stock.drop(['volume'],1,inplace=True)
        cols = list(df_stock.columns.values)
        print('df_stock.columns.values = ', cols)
        # normalize stock
        df_stock_norm = df_stock.copy()
        df_stock_norm = normalize_data(df_stock_norm)
        # create train, test data
        seq_len = 20 # choose sequence length
        x_train, y_train, x_valid, y_valid, x_test, y_test = load_data(df_stock_norm, seq_len)
        print('x_train.shape = ',x_train.shape)
        print('y_train.shape = ', y_train.shape)
        print('x_valid.shape = ',x_valid.shape)
        print('y_valid.shape = ', y_valid.shape)
        print('x_test.shape = ', x_test.shape)
        print('y_test.shape = ',y_test.shape)
df_stock.columns.values = ['open', 'close', 'low', 'high']
x_{train.shape} = (1394, 19, 4)
y_{train.shape} = (1394, 4)
x_{valid.shape} = (174, 19, 4)
y_valid.shape = (174, 4)
x_{test.shape} = (174, 19, 4)
y_{test.shape} = (174, 4)
In [10]: plt.figure(figsize=(15, 5));
         plt.plot(df[df.symbol == 'AAPL'].open.values, color='orange', label='open')
         plt.plot(df[df.symbol == 'AAPL'].close.values, color='black', label='close')
         plt.plot(df[df.symbol == 'AAPL'].low.values, color='red', label='low')
         plt.plot(df[df.symbol == 'AAPL'].high.values, color='green', label='high')
         #plt.plot(df_stock_norm.volume.values, color='gray', label='volume')
         plt.title('stock')
         plt.xlabel('time [days]')
         plt.ylabel('normalized price/volume')
         plt.legend(loc='best')
         plt.show()
```



```
In [11]: # prepare batches
         index_in_epoch = 0;
         permutation_array = np.arange(x_train.shape[0])
         np.random.shuffle(permutation_array)
         # function to get the next batch
         def get_next_batch(batch_size):
             global index_in_epoch, x_train, perm_array
             start = index_in_epoch
             index_in_epoch += batch_size
             if index_in_epoch > x_train.shape[0]:
                 np.random.shuffle(permutation_array) # shuffle permutation array
                 start = 0 # start next epoch
                 index_in_epoch = batch_size
             end = index_in_epoch
             return x_train[permutation_array[start:end]], y_train[permutation_array[start:end]]
In [12]: ## Model Run w/ Basic RNN
         # parameters
```

```
n_steps = seq_len-1
n_inputs = 4
n_neurons = 200
n_outputs = 4
n_layers = 2
learning_rate = 0.001
batch_size = 50
n_epochs = 100
train_set_size = x_train.shape[0]
```

```
tf.reset_default_graph()
         X = tf.placeholder(tf.float32, [None, n_steps, n_inputs])
         y = tf.placeholder(tf.float32, [None, n_outputs])
         # use Basic RNN Cell
         layers = [tf.contrib.rnn.BasicRNNCell(num_units=n_neurons, activation=tf.nn.elu)
                   for layer in range(n_layers)]
         multi_layer_cell = tf.contrib.rnn.MultiRNNCell(layers)
         rnn_outputs, states = tf.nn.dynamic_rnn(multi_layer_cell, X, dtype=tf.float32)
         stacked_rnn_outputs = tf.reshape(rnn_outputs, [-1, n_neurons])
         stacked_outputs = tf.layers.dense(stacked_rnn_outputs, n_outputs)
         outputs = tf.reshape(stacked_outputs, [-1, n_steps, n_outputs])
         outputs = outputs[:,n_steps-1,:] # keep only last output of sequence
         loss = tf.reduce_mean(tf.square(outputs - y)) # loss function = mean squared error
         optimizer = tf.train.AdamOptimizer(learning_rate=learning_rate)
         training_op = optimizer.minimize(loss)
         # run model
         with tf.Session() as sess:
             sess.run(tf.global_variables_initializer())
             for iteration in range(int(n_epochs*train_set_size/batch_size)):
                 x_batch, y_batch = get_next_batch(batch_size) # fetch the next training batch
                 sess.run(training_op, feed_dict={X: x_batch, y: y_batch})
                 if iteration % int(5*train_set_size/batch_size) == 0:
                     mse_train = loss.eval(feed_dict={X: x_train, y: y_train})
                     mse_valid = loss.eval(feed_dict={X: x_valid, y: y_valid})
                     print('%.2f epochs: MSE train/valid = %.6f/%.6f'%(
                         iteration*batch_size/train_set_size, mse_train, mse_valid))
             y_train_pred = sess.run(outputs, feed_dict={X: x_train})
             y_valid_pred = sess.run(outputs, feed_dict={X: x_valid})
             y_test_pred = sess.run(outputs, feed_dict={X: x_test})
0.00 \text{ epochs}: MSE \text{ train/valid} = 0.077708/0.139151
4.99 epochs: MSE train/valid = 0.000588/0.001505
9.97 epochs: MSE train/valid = 0.000238/0.000627
14.96 epochs: MSE train/valid = 0.000234/0.000552
19.94 epochs: MSE train/valid = 0.000230/0.000630
24.93 epochs: MSE train/valid = 0.000212/0.000523
29.91 epochs: MSE train/valid = 0.000142/0.000408
34.90 epochs: MSE train/valid = 0.000144/0.000402
39.89 epochs: MSE train/valid = 0.000162/0.000431
```

test_set_size = x_test.shape[0]

```
44.87 epochs: MSE train/valid = 0.000122/0.000353
49.86 epochs: MSE train/valid = 0.000137/0.000386
54.84 epochs: MSE train/valid = 0.000120/0.000346
59.83 epochs: MSE train/valid = 0.000156/0.000432
64.81 epochs: MSE train/valid = 0.000149/0.000398
69.80 epochs: MSE train/valid = 0.000169/0.000464
74.78 epochs: MSE train/valid = 0.000158/0.000441
79.77 epochs: MSE train/valid = 0.000113/0.000311
84.76 epochs: MSE train/valid = 0.000107/0.000295
89.74 epochs: MSE train/valid = 0.000101/0.000289
94.73 epochs: MSE train/valid = 0.000108/0.000294
99.71 epochs: MSE train/valid = 0.000117/0.000336
In [13]: print(y_train.shape[0])
         print(y_test.shape[0])
1394
174
In [14]: var = 0 # 0 = open, 1 = close, 2 = highest, 3 = lowest
         ## show predictions
         plt.figure(figsize=(15, 5));
         plt.subplot(1,2,1);
         plt.plot(np.arange(y_train.shape[0]), y_train[:,var], color='blue', label='train target
         plt.plot(np.arange(y_train.shape[0], y_train.shape[0]+y_valid.shape[0]), y_valid[:,var]
                  color='gray', label='valid target')
         plt.plot(np.arange(y_train.shape[0]+y_valid.shape[0],
                            y_train.shape[0]+y_test.shape[0]+y_test.shape[0]),
                  y_test[:,var], color='black', label='test target')
         plt.plot(np.arange(y_train_pred.shape[0]),y_train_pred[:,var], color='red',
                  label='train prediction')
         plt.plot(np.arange(y_train_pred.shape[0], y_train_pred.shape[0]+y_valid_pred.shape[0]),
                  y_valid_pred[:,var], color='orange', label='valid prediction')
         plt.plot(np.arange(y_train_pred.shape[0]+y_valid_pred.shape[0],
                            y_train_pred.shape[0]+y_valid_pred.shape[0]+y_test_pred.shape[0]),
                  y_test_pred[:,var], color='green', label='test prediction')
         plt.title('past and future stock prices')
         plt.xlabel('time in days')
```

```
plt.ylabel('normalized price')
     plt.legend(loc='best');
     plt.subplot(1,2,2);
     plt.plot(np.arange(y_train.shape[0], y_train.shape[0]+y_test.shape[0]),
                 y_test[:,var], color='black', label='test target')
     plt.plot(np.arange(y_train_pred.shape[0], y_train_pred.shape[0]+y_test_pred.shape[0]),
                 y_test_pred[:,var], color='blue', label='test prediction')
     plt.title('future stock prices')
     plt.xlabel('time in days')
     plt.ylabel('normalized price')
     plt.legend(loc='best');
     plt.show()
               past and future stock prices
                                                                  future stock prices
      train target

    test target

       valid target
                                                        test prediction
       test target
       train prediction
 0.8
                                                 0.80
       valid prediction
       test prediction
normalized price
                                                 0.75
                                               nalized
                                                 0.70
 0.4
                                                 0.65
 0.2
 0.0
```

corr_price_development_train, corr_price_development_valid, corr_price_development_

1400

1425

1450

1475

time in days

1500

1525

1550

1575

250

500

750

time in days

1000

1250

1500

1750

```
In [16]: ## Model Run w/ Gated RNN, LSTM
         # parameters
         n_{steps} = seq_{len-1}
         n_{inputs} = 4
         n_neurons = 200
         n_{outputs} = 4
         n_{ayers} = 2
         learning_rate = 0.001
         batch_size = 50
         n_{epochs} = 100
         train_set_size = x_train.shape[0]
         test_set_size = x_test.shape[0]
         tf.reset_default_graph()
         X = tf.placeholder(tf.float32, [None, n_steps, n_inputs])
         y = tf.placeholder(tf.float32, [None, n_outputs])
         # use LSTM Cell
         layers = [tf.contrib.rnn.BasicLSTMCell(num_units=n_neurons, activation=tf.nn.elu)
                  for layer in range(n_layers)]
         multi_layer_cell = tf.contrib.rnn.MultiRNNCell(layers)
         rnn_outputs, states = tf.nn.dynamic_rnn(multi_layer_cell, X, dtype=tf.float32)
         stacked_rnn_outputs = tf.reshape(rnn_outputs, [-1, n_neurons])
         stacked_outputs = tf.layers.dense(stacked_rnn_outputs, n_outputs)
         outputs = tf.reshape(stacked_outputs, [-1, n_steps, n_outputs])
         outputs = outputs[:,n_steps-1,:] # keep only last output of sequence
         loss = tf.reduce_mean(tf.square(outputs - y)) # loss function = mean squared error
         optimizer = tf.train.AdamOptimizer(learning_rate=learning_rate)
         training_op = optimizer.minimize(loss)
         # run model
         with tf.Session() as sess:
             sess.run(tf.global_variables_initializer())
             for iteration in range(int(n_epochs*train_set_size/batch_size)):
                 x_batch, y_batch = get_next_batch(batch_size) # fetch the next training batch
                 sess.run(training_op, feed_dict={X: x_batch, y: y_batch})
                 if iteration % int(5*train_set_size/batch_size) == 0:
                     mse_train = loss.eval(feed_dict={X: x_train, y: y_train})
                     mse_valid = loss.eval(feed_dict={X: x_valid, y: y_valid})
                     print('%.2f epochs: MSE train/valid = %.6f/%.6f'%(
```

```
iteration*batch_size/train_set_size, mse_train, mse_valid))
             y_train_pred = sess.run(outputs, feed_dict={X: x_train})
             y_valid_pred = sess.run(outputs, feed_dict={X: x_valid})
             y_test_pred = sess.run(outputs, feed_dict={X: x_test})
         # classify into binary classes based on Close-Open predictions (gainers= +, lossers= -)
        corr_price_development_train = np.sum(np.equal(np.sign(y_train[:,1]-y_train[:,0]),
                     np.sign(y_train_pred[:,1]-y_train_pred[:,0])).astype(int)) / y_train.shape[
         corr_price_development_valid = np.sum(np.equal(np.sign(y_valid[:,1]-y_valid[:,0]),
                     np.sign(y_valid_pred[:,1]-y_valid_pred[:,0])).astype(int)) / y_valid.shape[
         corr_price_development_test = np.sum(np.equal(np.sign(y_test[:,1]-y_test[:,0]),
                     np.sign(y_test_pred[:,1]-y_test_pred[:,0])).astype(int)) / y_test.shape[0]
        print('correct classifiation of close - open price for train/valid/test: %.2f/%.2f/%.2f
             corr_price_development_train, corr_price_development_valid, corr_price_development_
0.00 \text{ epochs}: MSE train/valid = 0.134898/0.319776
4.99 epochs: MSE train/valid = 0.000780/0.001395
9.97 epochs: MSE train/valid = 0.000527/0.001028
14.96 epochs: MSE train/valid = 0.000496/0.001112
19.94 epochs: MSE train/valid = 0.000697/0.001356
24.93 epochs: MSE train/valid = 0.000489/0.000936
29.91 epochs: MSE train/valid = 0.000302/0.000622
34.90 epochs: MSE train/valid = 0.000273/0.000660
39.89 epochs: MSE train/valid = 0.000238/0.000553
44.87 epochs: MSE train/valid = 0.000233/0.000518
49.86 epochs: MSE train/valid = 0.000197/0.000475
54.84 epochs: MSE train/valid = 0.000174/0.000410
59.83 epochs: MSE train/valid = 0.000173/0.000388
64.81 epochs: MSE train/valid = 0.000157/0.000388
69.80 epochs: MSE train/valid = 0.000138/0.000333
74.78 epochs: MSE train/valid = 0.000197/0.000498
79.77 epochs: MSE train/valid = 0.000128/0.000328
84.76 epochs: MSE train/valid = 0.000127/0.000313
89.74 epochs: MSE train/valid = 0.000112/0.000285
94.73 epochs: MSE train/valid = 0.000111/0.000292
99.71 epochs: MSE train/valid = 0.000142/0.000358
correct classifiation of close - open price for train/valid/test: 0.75/0.78/0.89
In [17]: # Optimize Hyper-paramters of Model
In [ ]: ## Model Run w/ Gated RNN, LSTM w/ Varying Number of Neurons
```

```
number_neurons=[]
best_neurons=[]
for x in range(1,501,100):
    # parameters
   n_{steps} = seq_{len-1}
   n_{inputs} = 4
    n_neurons = x
   n_{outputs} = 4
    n_{layers} = 2
    learning_rate = 0.001
    batch_size = 50
    n_{epochs} = 100
    train_set_size = x_train.shape[0]
    test_set_size = x_test.shape[0]
    tf.reset_default_graph()
    X = tf.placeholder(tf.float32, [None, n_steps, n_inputs])
    y = tf.placeholder(tf.float32, [None, n_outputs])
    # use LSTM Cell
    layers = [tf.contrib.rnn.BasicLSTMCell(num_units=n_neurons, activation=tf.nn.elu)
             for layer in range(n_layers)]
    multi_layer_cell = tf.contrib.rnn.MultiRNNCell(layers)
    rnn_outputs, states = tf.nn.dynamic_rnn(multi_layer_cell, X, dtype=tf.float32)
    stacked_rnn_outputs = tf.reshape(rnn_outputs, [-1, n_neurons])
    stacked_outputs = tf.layers.dense(stacked_rnn_outputs, n_outputs)
    outputs = tf.reshape(stacked_outputs, [-1, n_steps, n_outputs])
    outputs = outputs[:,n_steps-1,:] # keep only last output of sequence
    loss = tf.reduce_mean(tf.square(outputs - y)) # loss function = mean squared error
    optimizer = tf.train.AdamOptimizer(learning_rate=learning_rate)
    training_op = optimizer.minimize(loss)
    # run model
    with tf.Session() as sess:
        sess.run(tf.global_variables_initializer())
        for iteration in range(int(n_epochs*train_set_size/batch_size)):
            x_batch, y_batch = get_next_batch(batch_size) # fetch the next training batch
            sess.run(training_op, feed_dict={X: x_batch, y: y_batch})
            if iteration % int(5*train_set_size/batch_size) == 0:
                mse_train = loss.eval(feed_dict={X: x_train, y: y_train})
                mse_valid = loss.eval(feed_dict={X: x_valid, y: y_valid})
        y_train_pred = sess.run(outputs, feed_dict={X: x_train})
```

```
y_valid_pred = sess.run(outputs, feed_dict={X: x_valid})
                y_test_pred = sess.run(outputs, feed_dict={X: x_test})
            # classify into binary classes based on Close-Open predictions (gainers= +, lossers=
            corr_price_development_test = np.sum(np.equal(np.sign(y_test[:,1]-y_test[:,0]),
                        np.sign(y_test_pred[:,1]-y_test_pred[:,0])).astype(int)) / y_test.shape[
            number_neurons.append(x)
            best_neurons.append(corr_price_development_test)
        # evaluate results
        plt.plot(x=number_neurons,y=best_neurons,color='black')
        plt.title('Optimizing Number of Neurons')
        plt.xlabel('Number of Neurons')
        plt.ylabel('Correct Classifications')
        plt.show()
        selected_value_neurons = max(best_neurons)
        selected_index = best_neurons.index(selected_value_neurons)
        selected_neurons = number_neurons[selected_index]
        print('Optimal Number of Neurons: %1f'%(selected_neurons))
        print('Highest correct classifiation of close - open price for test set: %.15f'%(selecte
In [20]: ## Model Run w/ Gated RNN, LSTM w/ Varying Number of Layers
         number_layers=[]
         best_layers=[]
         for x in range(1,6,1):
             # parameters
             n_{steps} = seq_{len-1}
             n_{inputs} = 4
             n_neurons = selected_value_neurons
             n_{outputs} = 4
             n_{ayers} = x
             learning_rate = 0.001
             batch_size = 50
             n_{epochs} = 100
             train_set_size = x_train.shape[0]
             test_set_size = x_test.shape[0]
             tf.reset_default_graph()
             X = tf.placeholder(tf.float32, [None, n_steps, n_inputs])
```

```
y = tf.placeholder(tf.float32, [None, n_outputs])
    # use LSTM Cell
    layers = [tf.contrib.rnn.BasicLSTMCell(num_units=n_neurons, activation=tf.nn.elu)
             for layer in range(n_layers)]
    multi_layer_cell = tf.contrib.rnn.MultiRNNCell(layers)
    rnn_outputs, states = tf.nn.dynamic_rnn(multi_layer_cell, X, dtype=tf.float32)
    stacked_rnn_outputs = tf.reshape(rnn_outputs, [-1, n_neurons])
    stacked_outputs = tf.layers.dense(stacked_rnn_outputs, n_outputs)
    outputs = tf.reshape(stacked_outputs, [-1, n_steps, n_outputs])
    outputs = outputs[:,n_steps-1,:] # keep only last output of sequence
    loss = tf.reduce_mean(tf.square(outputs - y)) # loss function = mean squared error
    optimizer = tf.train.AdamOptimizer(learning_rate=learning_rate)
    training_op = optimizer.minimize(loss)
    # run model
    with tf.Session() as sess:
        sess.run(tf.global_variables_initializer())
        for iteration in range(int(n_epochs*train_set_size/batch_size)):
            x_batch, y_batch = get_next_batch(batch_size) # fetch the next training bat
            sess.run(training_op, feed_dict={X: x_batch, y: y_batch})
            if iteration % int(5*train_set_size/batch_size) == 0:
                mse_train = loss.eval(feed_dict={X: x_train, y: y_train})
                mse_valid = loss.eval(feed_dict={X: x_valid, y: y_valid})
        y_train_pred = sess.run(outputs, feed_dict={X: x_train})
        y_valid_pred = sess.run(outputs, feed_dict={X: x_valid})
        y_test_pred = sess.run(outputs, feed_dict={X: x_test})
    # classify into binary classes based on Close-Open predictions (gainers= +, lossers
    corr_price_development_test = np.sum(np.equal(np.sign(y_test[:,1]-y_test[:,0]),
                np.sign(y_test_pred[:,1]-y_test_pred[:,0])).astype(int)) / y_test.shape
    number_layers.append(x)
    best_layers.append(corr_price_development_test)
# evaluate results
plt.plot(x=number_layers,y=best_layers,color='black')
plt.title('Optimizing Number of Layers')
plt.xlabel('Number of Layers')
plt.ylabel('Correct Classifications')
plt.show()
```

```
selected_value = max(best_layers)
     selected_index = best_layers.index(selected_value)
     selected_layers = number_layers[selected_index]
     print('Optimal Number of Layers: %1f'%(selected_layers))
     print('Highest correct classifiation of close - open price for test set: %.15f'%(select
                                              Traceback (most recent call last)
    TypeError
    ~\Anaconda3\lib\site-packages\tensorflow\python\framework\tensor_shape.py in __init__(se
    427
--> 428
                dims_iter = iter(dims)
    429
              except TypeError:
    TypeError: 'numpy.float64' object is not iterable
During handling of the above exception, another exception occurred:
                                              Traceback (most recent call last)
    ValueError
    <ipython-input-20-07813d3618f8> in <module>()
     27
     28
            multi_layer_cell = tf.contrib.rnn.MultiRNNCell(layers)
---> 29
            rnn_outputs, states = tf.nn.dynamic_rnn(multi_layer_cell, X, dtype=tf.float32)
     30
     31
            stacked_rnn_outputs = tf.reshape(rnn_outputs, [-1, n_neurons])
    ~\Anaconda3\lib\site-packages\tensorflow\python\ops\rnn.py in dynamic_rnn(cell, inputs,
    546
              if not dtype:
    547
                raise ValueError("If there is no initial_state, you must give a dtype.")
--> 548
              state = cell.zero_state(batch_size, dtype)
    549
    550
            def _assert_has_shape(x, shape):
    ~\Anaconda3\lib\site-packages\tensorflow\python\ops\rnn_cell_impl.py in zero_state(self,
            with ops.name_scope(type(self).__name__ + "ZeroState", values=[batch_size]):
    891
              if self._state_is_tuple:
    892
--> 893
                return tuple(cell.zero_state(batch_size, dtype) for cell in self._cells)
    894
              else:
```

```
~\Anaconda3\lib\site-packages\tensorflow\python\ops\rnn_cell_impl.py in <genexpr>(.0)
            with ops.name_scope(type(self).__name__ + "ZeroState", values=[batch_size]):
   891
   892
              if self._state_is_tuple:
--> 893
                return tuple(cell.zero_state(batch_size, dtype) for cell in self._cells)
   894
              else:
   895
                # We know here that state_size of each cell is not a tuple and
   ~\Anaconda3\lib\site-packages\tensorflow\python\ops\rnn_cell_impl.py in zero_state(self,
            with ops.name_scope(type(self).__name__ + "ZeroState", values=[batch_size]):
   227
   228
              state_size = self.state_size
--> 229
              return _zero_state_tensors(state_size, batch_size, dtype)
    230
    231
    ~\Anaconda3\lib\site-packages\tensorflow\python\ops\rnn_cell_impl.py in _zero_state_tens
            size.set_shape(c_static)
   128
   129
            return size
--> 130
         return nest.map_structure(get_state_shape, state_size)
   131
   132
   ~\Anaconda3\lib\site-packages\tensorflow\python\util\nest.py in map_structure(func, *str
   323
   324
         return pack_sequence_as(
              structure[0], [func(*x) for x in entries])
--> 325
   326
   327
   ~\Anaconda3\lib\site-packages\tensorflow\python\util\nest.py in <listcomp>(.0)
   323
   324
         return pack_sequence_as(
              structure[0], [func(*x) for x in entries])
--> 325
   326
   327
   ~\Anaconda3\lib\site-packages\tensorflow\python\ops\rnn_cell_impl.py in get_state_shape(
         def get_state_shape(s):
   123
            """Combine s with batch_size to get a proper tensor shape."""
   124
--> 125
            c = _concat(batch_size, s)
   126
            c_static = _concat(batch_size, s, static=True)
```

We know here that state_size of each cell is not a tuple and

895

```
127
            size = array_ops.zeros(c, dtype=dtype)
    ~\Anaconda3\lib\site-packages\tensorflow\python\ops\rnn_cell_impl.py in _concat(prefix,
                               "but saw tensor: %s" % s)
   103
   104
          else:
--> 105
            s = tensor_shape.as_shape(suffix)
            s_static = s.as_list() if s.ndims is not None else None
   106
   107
            s = (constant_op.constant(s.as_list(), dtype=dtypes.int32)
   ~\Anaconda3\lib\site-packages\tensorflow\python\framework\tensor_shape.py in as_shape(sh
   796
   797
          else:
--> 798
            return TensorShape(shape)
   799
   800
   ~\Anaconda3\lib\site-packages\tensorflow\python\framework\tensor_shape.py in __init__(se
   429
              except TypeError:
   430
                # Treat as a singleton dimension
                self._dims = [as_dimension(dims)]
--> 431
   432
              else:
   433
                # Got a list of dimensions
   ~\Anaconda3\lib\site-packages\tensorflow\python\framework\tensor_shape.py in as_dimension
   374
            return value
   375
          else:
--> 376
            return Dimension(value)
   377
   378
    ~\Anaconda3\lib\site-packages\tensorflow\python\framework\tensor_shape.py in __init__(se
              if (not isinstance(value, compat.bytes_or_text_types) and
    33
    34
                  self._value != value):
---> 35
                raise ValueError("Ambiguous dimension: %s" % value)
              if self._value < 0:</pre>
    36
                raise ValueError("Dimension %d must be >= 0" % self._value)
    37
   ValueError: Ambiguous dimension: 0.896551724138
```

In []: ## Model Run w/ Gated RNN, LSTM w/ Varying Batch Sizes

```
number batch=[]
best_batch=[]
for x in range(1,101,10):
    # parameters
   n_{steps} = seq_{len-1}
   n_{inputs} = 4
    n_neurons = selected_value_neurons
    n_{outputs} = 4
    n_layers = selected_layers
    learning_rate = 0.001
    batch\_size = x
    n_{epochs} = 100
    train_set_size = x_train.shape[0]
    test_set_size = x_test.shape[0]
    tf.reset_default_graph()
    X = tf.placeholder(tf.float32, [None, n_steps, n_inputs])
    y = tf.placeholder(tf.float32, [None, n_outputs])
    # use LSTM Cell
    layers = [tf.contrib.rnn.BasicLSTMCell(num_units=n_neurons, activation=tf.nn.elu)
             for layer in range(n_layers)]
    multi_layer_cell = tf.contrib.rnn.MultiRNNCell(layers)
    rnn_outputs, states = tf.nn.dynamic_rnn(multi_layer_cell, X, dtype=tf.float32)
    stacked_rnn_outputs = tf.reshape(rnn_outputs, [-1, n_neurons])
    stacked_outputs = tf.layers.dense(stacked_rnn_outputs, n_outputs)
    outputs = tf.reshape(stacked_outputs, [-1, n_steps, n_outputs])
    outputs = outputs[:,n_steps-1,:] # keep only last output of sequence
    loss = tf.reduce_mean(tf.square(outputs - y)) # loss function = mean squared error
    optimizer = tf.train.AdamOptimizer(learning_rate=learning_rate)
    training_op = optimizer.minimize(loss)
    # run model
    with tf.Session() as sess:
        sess.run(tf.global_variables_initializer())
        for iteration in range(int(n_epochs*train_set_size/batch_size)):
            x_batch, y_batch = get_next_batch(batch_size) # fetch the next training batch
            sess.run(training_op, feed_dict={X: x_batch, y: y_batch})
            if iteration % int(5*train_set_size/batch_size) == 0:
                mse_train = loss.eval(feed_dict={X: x_train, y: y_train})
                mse_valid = loss.eval(feed_dict={X: x_valid, y: y_valid})
        y_train_pred = sess.run(outputs, feed_dict={X: x_train})
```

```
y_valid_pred = sess.run(outputs, feed_dict={X: x_valid})
        y_test_pred = sess.run(outputs, feed_dict={X: x_test})
    # classify into binary classes based on Close-Open predictions (gainers= +, lossers=
    corr_price_development_test = np.sum(np.equal(np.sign(y_test[:,1]-y_test[:,0]),
                np.sign(y_test_pred[:,1]-y_test_pred[:,0])).astype(int)) / y_test.shape[
    number_batch.append(x)
    best_batch.append(corr_price_development_test)
# evaluate results
plt.plot(x=number_batch,y=best_batch,color='black')
plt.title('Optimizing Number of Batches')
plt.xlabel('Number of Batches')
plt.ylabel('Correct Classifications')
plt.show()
selected_value = max(best_batch)
selected_index = best_batch.index(selected_value)
selected_batch = number_batch[selected_index]
print('Optimal Number of Batches: %1f'%(selected_batch))
print('Highest correct classifiation of close - open price for test set: %.15f'%(selected)
```