

Data Structures and Algorithms

Submission Report: Priority-Driven Ticketing

1. Problem-Solution Fit: The Need for Prioritization

Problem Statement

In high-volume customer support environments, critical issues (e.g., system outages) often get buried beneath numerous routine or low-priority requests. Staff require a dynamic, real-time queue that eliminates manual sorting and guarantees that the most urgent tasks are presented first, thereby minimizing business risk and meeting service level agreements (SLAs).

Solution: Justification of Priority Queue (PQ)

The **Priority Queue** data structure is the optimal choice for this problem as it inherently maintains a collection of elements prioritized by a key metric (ticket severity).

- **Justification:** The PQ ensures $O(1)$ access to the highest-priority element (the next ticket the staff should process). This contrasts sharply with simple list structures which would require $O(n)$ search time or $O(n\log n)$ sorting every time a new element is added.

2. Priority Queue Implementation Details

The Priority Queue logic is implemented in **JavaScript** on the Staff Dashboard to process data fetched from Firebase Firestore.

Sorting Logic

The prioritization utilizes a two-tiered comparison to ensure both urgency and fairness (First-In, First-Out).

Tier	Priority Metric	Rule	Data Source
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Primary	Ticket Severity	Highest priority is addressed first.	<code>priority</code> field (Mapped: High (3) > Medium (2) > Low (1)).
Secondary	Submission Time (FIFO)	If priorities are equal, the oldest ticket is addressed first.	<code>created_at</code> field (Timestamp).

Pseudocode for Ticket Comparison

The core sorting algorithm utilizes an array sort with a custom comparator function that implements the PQ logic:

```
// Comparator Function (A - B)
function compareTickets(A, B) {
  // 1. Primary Sort: Priority (Descending Order: High (3) is greater than Low (1))
  if (A.priorityValue !== B.priorityValue) {
    return B.priorityValue - A.priorityValue;
  }
  // 2. Secondary Sort: Timestamp (Ascending Order: Older time is smaller value)
  return A.created_at.seconds - B.created_at.seconds;
}
```

3. Efficiency & Optimization

Time and Space Complexity

The implementation currently uses the built-in JavaScript `Array.prototype.sort()` method on the collection of tickets fetched from Firestore, effectively simulating the PQ output.

Operation	Implementation	Time Complexity	Notes on Efficiency
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Enqueue	<code>array.push()</code> followed by <code>array.sort()</code> .	$O(n \log n)$	While $O(1)$ for simple insertion, the full sort dominates the complexity.
Dequeue	<code>array[0]</code> access.	$O(1)$	Retrieval of the most urgent ticket is instantaneous.
Space Complexity	Array storage for all fetched tickets.	$O(n)$	Space requirement scales linearly with the number of tickets.

Note on Optimality

While the current approach (Array + Sort) provides correct prioritization, for very large datasets ($n \gg 1000$), a pure heap-based Priority Queue implementation would yield $O(\log n)$ for Enqueue, offering better performance scalability than $O(n \log n)$.

4. Implementation Accuracy and Innovation

Implementation Accuracy

- **Correctness:** The custom comparison function accurately applies both priority and FIFO rules to generate a valid priority-sorted queue.
- **Data Integrity:** The use of Firebase `Timestamp` for `created_at` ensures high-precision, non-client-manipulable data necessary for the accurate FIFO tie-breaker logic.

Innovation

- **Real-World Application:** The project demonstrates the practical application of the Priority Queue to a ubiquitous business problem—resource allocation and urgent task management—thereby optimizing staff operational flow in a real-time environment.
- **Integration with Web Services:** The seamless integration of a DSA concept (PQ) with a real-time database (Firestore) illustrates a modern, service-oriented approach to data processing and display.

5. Summary of Deliverables

The **Data Structures and Algorithms** component is delivered via:

1. **Code:** JavaScript implementation of the `sortTickets` function on the `staff_dashboard.html` file, demonstrating the PQ logic.
2. **Report:** This document provides the formal explanation and complexity analysis.
3. **Demo:** A running demo showcasing the automatic reordering of the staff queue when tickets of varying priorities are submitted in quick succession.