

1. Introduction

Hybrid video coding is an advanced coding technique which is derived from both predictive coding and transform coding. Hybrid video coding framework is commonly used in modern video coding standards, e.g., H.26x, MPEG2/4, AVS, HEVC, etc. Objective of this project is to develop simplified version of Video coding system using tools like discrete cosine transformation, quantization, prediction, Intra coding and entropy coding.

During this project, block based image compression which can also be used in compressing I frames of video and motion-compensated frame prediction using block matching by evaluating motion vector was studied.

In image compression, DCT (Discrete Cosine Transform) for image transformation and entropy coding techniques; Huffman coding and Run Length coding was implemented. Furthermore, quality of image with different quantization levels also studied.

Then, in video coding, inter coding of P frames using block matching was implemented. Matlab 2015a version was used for coding and implementation purpose.

2. Basic concepts in image compression System

Simplified version of image compression flow chart is given below.

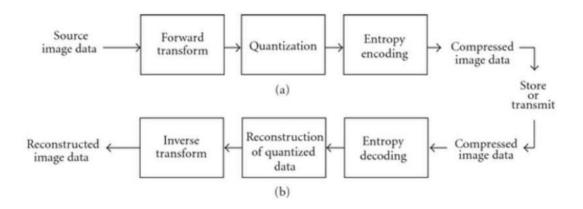


Fig 01: Block diagram of simplified version of image compression

Theory behind techniques corresponding to each part of image compression which is used during the project is discussed below.

2.1 Discrete Cosine Transform (DCT)

The Discrete Cosine transform (DCT) represents an image as a sum of sinusoids of varying magnitudes and frequencies. DCT is derived from extracting real part of corresponding Discrete fourier transform. Since coefficients of DCT are real instead of complex, hardware implementation of DCT is much easier compared to DFT.

The DCT has the property that, for typical image, most of the visually significant imformation about the image is concentrated in just a few coefficients of the DCT. This property is known as Energy Compaction property.

2D Forward DCT is given below.

The two-dimensional DCT of an $M \times N$ image f(x, y) is defined as follows.

$$F(p,q) = \alpha_p \alpha_q \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x,y) \cos \left[\frac{\pi (2x+1)p}{2M} \right] \cos \left[\frac{\pi (2y+1)q}{2N} \right]$$
 (1)

Where, $0 \le p \le M-1$ and $0 \le q \le N-1$ and

$$\alpha_p = \begin{cases} \frac{1}{\sqrt{M}}, & p = 0 \\ \sqrt{\frac{2}{M}}, & 1 \le p \le M - 1 \end{cases} \qquad \alpha_q = \begin{cases} \frac{1}{\sqrt{N}}, & q = 0 \\ \sqrt{\frac{2}{N}}, & 1 \le q \le N - 1 \\ \sqrt{\frac{2}{N}}, & 1 \le q \le N - 1 \end{cases}$$

2.2 Quantization

Quantization is the most elementary form of lossy data compression. When a number x is quantized to L levels, we mean that its value is replaced by (or quantized to) the nearest member of a set of L quantization levels. Here, we consider uniform quantization.

For the uniform quantization used here:

- We define a quantizer range defined by values xmin and xmax
- We divide this range into L equally sized segments, each with size $\Delta = (xmax-xmin)/L$.
 - We place the quantization level for a given segment in the middle of that segment.

For 8 levels of uniform quantized levels above explanation can be depicted as follows.

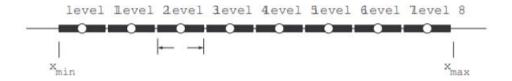
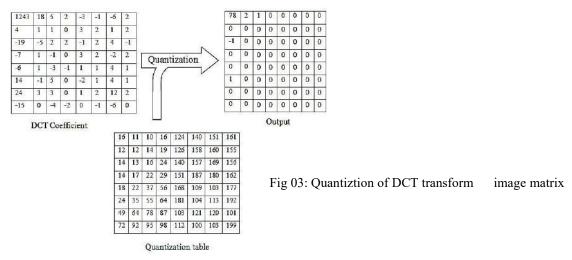


Fig 02: Quantizaton using 8 levels

A typical image compression works by breaking the picture into discrete blocks (8×8 pixels blocks also known as marco blocks). These blocks can then be subjected to discrete cosine transform (DCT) to calculate the frequency components, both horizontally and vertically. The resulting block (the same size as the original block) is then pre-multiplied by the quantization scale code and divided element-wise by the quantization matrix, and rounding each resultant element.

A common quantization process behaves like following



2.3 Huffman coding

Huffman coding is a lossless coding technique which was proposed by Dr. David A. Huffman in 1952. It is method for the construction of minimum redundancy code. Huffman code is a technique for compressing data. Huffman's greedy algorithm looks at the occurrence of each character and it as a binary string in an optimal way.

Huffman algorithm accomplish it's data compression by allowing shorter code words for frequently occurring characters/data. Therefore, code word lengths are no longer fixed like in ASCII.

Huffman Coding Algorithm

- 1. Initialization: Put all symbols on a list sorted according to their frequency counts.
- 2. Repeat until the list has only one symbol left:
 - From the list pick two symbols with the lowest frequency counts
 - 2. Form a Huffman sub-tree that has these two symbols as child nodes and create a parent node.
 - Assign the sum of the children's frequency counts to the parent and insert it into the list such that the order is maintained.
 - 4. Delete the children from the list.
- Assign a codeword for each leaf based on the path from the root.

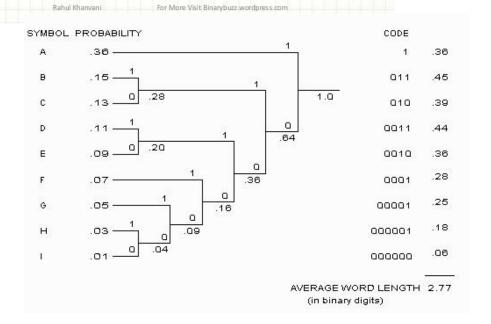


Fig 04: Huffman Coding

2.4 Motion Estimation and Motion Vector

Adjacent frames in a video are quite similar and differ due to the motion of object or camera. Hence, this property of similarity is called as "Temporal correlation". Due to the above characteristics, when coding adjacent frames, we can use these temporal redundancies to compress frames. In real video scenes, motion can be a complex combination of translation and rotation. Such motion is difficult to estimate and may require large amounts of processing. However, translational motion is easily estimated and has been used successfully for motion compensated coding.

Block matching algorithm is used to obtain motion vector.

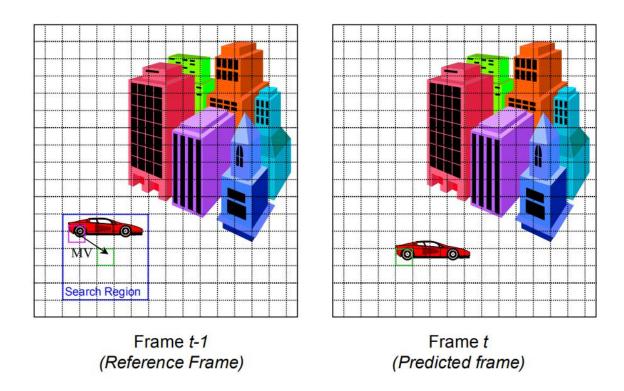


Fig 05 Motion Vector and motion estimation

2.5 Block matching Algorithm

Objective of block matching is to find the best matching marco block for a given frame (Target frame) using reference frame. This algorithm able to calculate Motion Vector generation by calculating x axis and y axis displacement between current marco block and best matched marco block. Current marco block of target frame is replaced with best matched marco block. By continue this for every marco block, motion - compensated image is obtain. Difference between motion-compensated image and current frame is calculated as residue. Using reference frame, motion vector and residue, target frame can be reconstructed.

Criteria to find best matched marco block.

- Mean Square error
- Mean Absolute error
- Sum of absolute error

During this project, Sum of absolute error criteria is used to find best matching marco block.

SAD = sum(sum(abs(f1(i:i+N-1,j:j+N-1)-f2(i+k:i+k+N-1,j+l:j+l+N-1))))

Techniques for searching best matched marco block.

- Full / Sequential search
- Logarithmic search
- Hierachial search

During this project, sequential search technique is used.

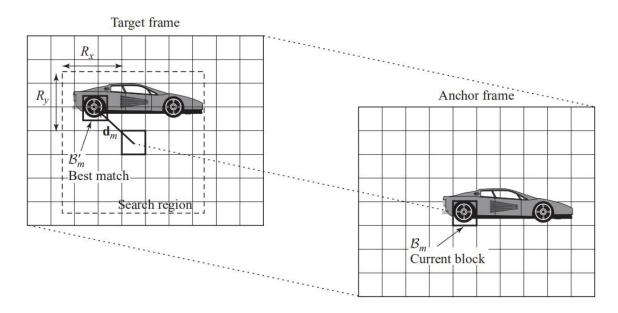
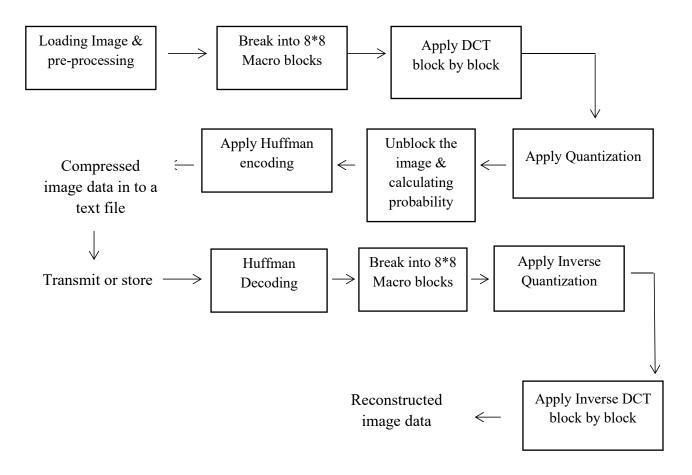


Fig 06: Block matching

3. Image Compression System

3.1 Flow Chart



3.2 Results



Original Image



Gray scaled Image



Compressed Image Q_level 1



Compressed Image Q_level 2

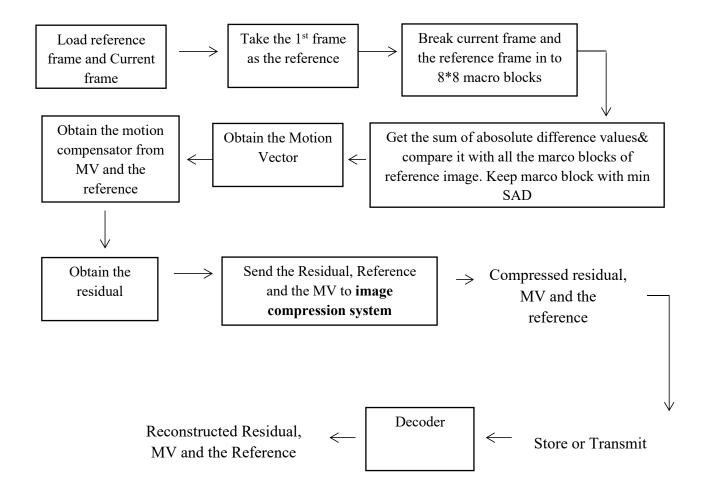


Compressed Image Q_level 3

Video Compression System

This video compression system consists of concepts like Motion Vectors, Motion estimation, Intra prediction frame coding, macro block based coding and etc

Flow Chart



Results



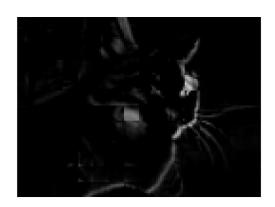
Reference Frame (I Frame)



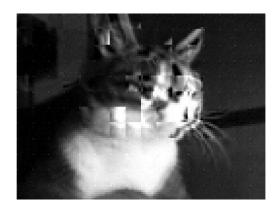
Target Frame (P Frame)



Motion - Compensated Image



Residue



Reconstructed Image

Appendix

1 .Image Compression

```
I=imread('download.jpg');
Gray_I= rgb2gray(I); %converted into gray scaled image
Gray I = im2double(Gray I);
%imshow(itg)
imhist(Gray I);hold on;
%representing discrete cosine transform using 8 by 8 blocks
B = blkproc(Gray I, [8 8], 'dct2');
B = ceil(B*1000);
응응
응응
%quantization values for each quality level
q low = 8;
q medium = 16;
q high = 8;
%performing quantization
Blow = B/(2*q low);
Blow = ceil(Blow);
응응
%calculate frequency and its probability for each quantized value
[glow,~,intensity_val] = grp2idx(Blow(:));
Frequency = accumarray(glow,1);
probability = Frequency./(225*225);
T = table(intensity val ,Frequency,probability);
%perform huffman coding
dict=huffmandict(intensity val,probability);
encode I = huffmanenco(Blow(:), dict);
```

```
응응
```

```
%perform huffman decoding
decode I = huffmandeco(encode I, dict);
re img = reshape(decode I,[225 225]); %reshaping the image
%dequantization
Blow2 = re img*q low*2;
Blow2 = Blow2/1000;
I_decoded = blkproc(Blow2,[8 8],'idct2'); %performing inverse dct
imshow(Gray I),figure,imshow(I decoded);
imhist(I decoded);
응응
%perform run length coding
[d, c] = my RLE(Blow(:));
decode_I2 = rl_dec(d,c);
re img2 = reshape(decode I2,[225 225]);
imshow(re img2);
응응
%dequantization
Blow3 = re img2*q medium*2;
Blow3 = Blow3/1000;
I_decoded2 = blkproc(Blow2,[8 8],'idct2'); %performing inverse dct
imshow(Gray I),figure,imshow(I decoded2);
```

2. Run length Encoding

```
function [d,c]=my RLE(x);
% This function performs Run Length Encoding to a strem of data x.
% [d,c]=rl enc(x) returns the element values in d and their number of
% apperance in c. All number formats are accepted for the elements of x.
if nargin~=1
   error('A single 1-D stream must be used as an input')
end
ind=1;
d(ind) = x(1);
c(ind)=1;
for i=2 :length(x)
   if x(i-1) == x(i)
      c(ind) = c(ind) + 1;
   else ind=ind+1;
       d(ind) = x(i);
       c(ind)=1;
   end
end
```

3. Run Length Decoding

응응

```
function x=rl dec(d,c);
% This function performs Run Length Dencoding to the elements of the strem
% of data d according to their number of apperance given in c. There is no
% restriction on the format of the elements of d, while the elements of c
% must all be integers.
if nargin<2</pre>
   error('not enough number of inputs')
end
x=[];
for i=1:length(d)
x=[x d(i) * ones(1,c(i))];
end
4. Motion Vecotor and residue Calculaton
응응
%f1: anchor frame; f2: target frame, fp: predicted image;
%mvx,mvy: store the MV image
%widthxheight: image size; N: block size, R: search range
function [vector, residue] = motionVector(f1, f2, N)
S = size(f1);
height = S(1);
width = S(2);
%N = 8;
%R = -50:50;
vectors = zeros(2,floor(height/N)*floor(width/N));
blk count = 1;
```

```
for i=1:N:height-N+1
for j=1:N:width-N+1 %for every block in the anchor frame
MAD min=256*N*N;
mvx=0;
mvy=0;
for k= 1:1:height-N+1
for l= 1:1:width-N+1 %for every search candidate
refBlkVer = i + k; % row/Vert co-ordinate for ref block
refBlkHor = j + 1; % col/Horizontal co-ordinate
if ( refBlkVer < 1 || refBlkVer+N-1 > height || refBlkHor < 1 || refBlkHor+N-1 >
width)
continue;
end
MAD = sum (sum (abs (f1(i:i+N-1,j:j+N-1)-f2(i+k:i+k+N-1,j+l:j+l+N-1))));
% calculate MAD for this candidate
if MAD<MAD min</pre>
MAD min=MAD; dy=k; dx=l;
end;
end;
end;
fp(i:i+N-1,j:j+N-1) = f2(i+dy:i+dy+N-1,j+dx:j+dx+N-1);
%put the best matching block in the predicted image
vectors(1,blk_count) = dy; % row co-ordinate for the vector
vectors(2,blk_count) = dx; % col co-ordinate for the vector
blk count = blk count+1;
end;
```

```
end;
vector = vectors;
S2 = size(fp);
residue = f2(1:S2(1),1:S2(2)) - fp;
5. Motion compensated image contruction
% Computes motion compensated image using the given motion vectors
% Input
% I : The reference image
% motionVect : The motion vectors
% block size : Size of the macroblock
% Ouput
응
function imgComp = Motion_Compensated_Image(I, motionVect, N)
[height width] = size(I);
block Count = 1;
for i = 1:N:height-N+1
for j = 1:N:width-N+1
% dy is row(vertical) index
% dx is col(horizontal) index
% this means we are scanning in order
dy = motionVect(1,block Count);
dx = motionVect(2,block_Count);
refBlkVer = i + dy;
refBlkHor = j + dx;
imageComp(i:i+N-1,j:j+N-1) =
I(refBlkVer:refBlkVer+N-1, refBlkHor:refBlkHor+N-1);
```

```
block Count = block Count + 1;
end
end
imgComp = imageComp
6. Video Compression
응응
f1 = imread('cat1.jpg');
f2 = imread('cat2.jpg');
f1= rgb2gray(f1); %converted into gray scaled image
f1 = im2double(f1);
f1 = imresize(f1, [100 130]);
f2= rgb2gray(f2);
f2 = im2double(f2);
f2 = imresize(f2, [100 130]);
응응
[Motion_vector, residue] = motionVector(f1, f2, 8); %Calculating Motion vector
응응
S = size(residue);
응응
B = blkproc(residue,[8 8],'dct2');
B = ceil(B*1000);
응응
%quantization values for each quality level
q low = 32;
q medium = 8;
q high = 8;
```

```
%performing quantization
Blow = B/(2*q medium);
Blow = ceil(Blow);
응응
%calculate frequency and its probability for each quantized value
[glow,~,intensity val] = grp2idx(Blow(:));
Frequency = accumarray(glow,1);
probability = Frequency./(S(1)*S(2));
T = table(intensity val ,Frequency,probability);
응응
%perform huffman coding
dict=huffmandict(intensity val,probability);
encode I = huffmanenco(Blow(:), dict);
응응
[d,c] = my_RLE(Blow(:));
응응
$$$$$$$$$$$$$$$$$$$$$
응응
compensated_img = Motion_Compensated_Image(f1,Motion_vector,8);
응응
decode I = huffmandeco(encode I, dict);
re img = reshape(decode_I,[S(1) S(2)]); %reshaping the image
```

```
응응
re_img = RLE_dec(d,c);
re_img = reshape(re_img,[S(1) S(2)]);
응응
%dequantization
Blow2 = re_img*q_medium*2;
Blow2 = Blow2/1000;
I_decoded = blkproc(Blow2,[8 8],'idct2'); %performing inverse dct
응응
I_decode_dash = I_decoded(1:96,1:128);
%Residue_dash = Residue(1:96,1:128);
compensated_img = im2double(compensated_img);
%Residue_dash = im2double(Residue_dash);
Recontruct img = compensated img + I decode dash;
%Recontruct img2 = compensated img + Residue dash;
```

Refferences:

- 1. EE4414: Motion Estimation Basics, Yao Wang, 2003
- 2. STILL IMAGE AND VIDEO COMPRESSION WITH MATLAB, K. S. Thyagarajan, John willey & sons Publications 2011
- 3. Aroh Barjatya (2020). Block Matching Algorithms for Motion Estimation (https://www.mathworks.com/matlabcentral/fileexchange/8761-block-matching-algorithms -for-motion-estimation), MATLAB Central File Exchange. Retrieved December 9, 2020.