

To obtain a solⁿ of rectangular game, it is feasible to find out:

- 1.) The best strategy for player A
- 2.) The best strategy for player B
- 3.) The value of the game

Ex: Player A can choose his strategy from (A_1, A_2, A_3) only while B can choose from the set (B_1, B_2) . The rules of the game state that, the payments should be made in accordance with the set of the strategies.

Strategy Pair selected	Payment to be made
(A_1, B_1)	Player A pays £1 to player B.
(A_1, B_2)	Player B pays £6 to player A.
(A_2, B_1)	Player B pays £2 to player A.
(A_2, B_2)	Player B pays £4 to player A.
(A_3, B_1)	Player A pays £2 to player B.
(A_3, B_2)	Player A pays £6 to player B.

Q1. What strategies A and B play in order to get the optimum benefit of the play?

		B1	B2	Player B.
		-1	6	-1
		2	4	2
Player A	A1	-1	6	-1
	A2	2	4	2
	A3	-2	-6	-6

↙ ↓

Payoff matrix for player A

minmax

Value of the game is $\frac{1}{2}$ for A & $-\frac{1}{2}$ for Player B

Optimum solⁿ is: Player A - A₂ & Player B - B₁

1.) Optimum strategy for player A - A₂

2.) Optimum strategy for player B - B₁

The value of the game is $\frac{1}{2}$

As $V \neq 0$ the game is not a fair game.

As $V = U = \frac{1}{2}$, it is a strictly determinable game.

Q2. The payoff matrix of the game is given. Find the solⁿ.

		I	II	III	IV	V
		-2	0	0	5	3
		3	2	11	2	2
A	I	-2	0	0	5	3
	II	3	2	11	2	2
	III	4	-3	0	-2	6
	IV	5	3	-4	2	-6

P: solⁿ

-A - 17

B - 17

S' 3 1 5 6

minmax - 1.

Value of the game is $\frac{1}{2}$ for A & $-\frac{1}{2}$ for player B.

Q3.

	I	II	III
I	-2	15	$ -2 $
II	-5	$ -6 $	-4
III	-5	20	$ -8 $

 $\boxed{-2}$

20

-2

20

 $|-8|$

X marks

There are several methods for determining for optimal strategies & the value of the game. Like arithmetic or analytical method, graphical method or simplex method.

1. ARITHMETIC METHOD.

A 2×2 matrix where there is no saddle pt can be solved by AM as follows:

Consider the foll.

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$$

Value of the game is

$$V = a_{11}a_{22} - a_{21}a_{12}$$

$$\frac{(a_{11} + a_{22}) - (a_{12} + a_{21})}{2}$$

With the coordinates,

$$x_1 = \frac{a_{22} - a_{21}}{(a_{11} + a_{22}) - (a_{12} + a_{21})}$$

$$x_2 = \frac{a_{11} - a_{12}}{(a_{11} + a_{22}) - (a_{12} + a_{21})}$$

$$(x_1) + (x_2) = 1$$

$$y_1 = \frac{a_{22} - (a_{12})}{(a_{11} + a_{22}) - (a_{12} + a_{21})}$$

$$y_2 = \frac{a_{11} - a_{21}}{(a_{11} + a_{22}) - (a_{12} + a_{21})}$$

Optimal strategy for player A is s_A

$$(x_1, x_2) = s_A$$

" for player B is s_B

The vector $(x_1, x_2), \dots, (x_m)$ of non-negative no's satisfying $x_1 + x_2 + \dots + x_m = 1$ is called mixed strategy of player A.

The vector $y = (y_1, y_2)$ of non-negative no's satisfying $y_1 + y_2 = 1$ is called mixed strategy of player B.

Q. Solve the foll. payoff matrix for player A.

$$\begin{bmatrix} 5 & 1 \\ 3 & 4 \end{bmatrix} \quad | \quad 3.$$

5 4

This problem does not have SP, \therefore AM is used to solve the problem.

Value of the game is,

$$V = \frac{(5 \times 4) - (3 \times 1)}{(5+4) - (3+1)}$$

$$\Rightarrow \frac{20 - 3}{8 - 4} \Rightarrow \frac{17}{4}$$

$$x_1 = \frac{1}{5} \quad x_2 = \frac{4}{5} \quad y_1 = \frac{3}{5} \quad y_2 = \frac{2}{5}$$

$$S_A = \left(\frac{1}{5}, \frac{4}{5} \right) \quad S_B = \left(\frac{3}{5}, \frac{2}{5} \right)$$

Arithmetically the method consists of the foll. steps:

- 1.) Find the difference of 2 nos in col 1 & enter the resultant in col 2. Neglect the -ve sign if it occurs.
- 2.) Find the difference b/w 2 nos in col 2 & enter the resultant in col 1. Neglect the -ve sign if it occurs.
- 3.) Repeat the same procedure for 2 rows. solve the.

Q. solve the foll:-

Growing complexities of modern projects required

to optimise the efficiency of executing the project.

This Project management has evout evolved as a new field as a development too - tech niques for planning, scheduling & control -ing for proj.

- 1.) CPM - critical path management.
- 2.) Project evaluation & review technique (PERT)

* APPLICATIONS OF PERT- CPM.

1.) They are applied to a variety of problems that include :

- (i.) construction of dam or renal system.
- (ii.) construction of a building or a highway.
- (iii.) Maintenance of flights or oil refineries.
- (iv.) space flights
- (v.) cost control of a project.
- (vi.) Designing a prototype of m/c.
- (vii.) Development of supersonic A/a plane.
- (viii.) Designing & developing s/w projects.

~~X~~ * BASIC STEPS IN PERT- CPM TECHNIQUES.

1) Project Scheduling by PERT- CPM consists of 4 main steps :

(a) PLANNING

(i) It starts with by splitting total project into smaller sub-projects.

(ii) These sub-projects are further divided into activities.

(iii) The relationship b/w activities is established.

(iv) Responsibilities & authorities are also taken.

Planning reduces the possibility of overlooking any important task.

< b. > SCHEDULING

(i) It involves preparing a timing chart showing the start & finish time for each activity as well as its relationship to other activities of the project.

(ii) It finds the critical path activity which requires a special attention if the project has to be completed on time.

(iii) For non-critical activity, the schedule must show the amount of slack or float type

which can be used when such activities are delayed or when limited resources are available.

(c) ALLOCATION OF RESOURCES.

- (i) A resource is a variable such as labour, finance, equipment & space which will impose a limitation on completion time of the project.
- (ii) When resources are limited & conflicting a systematic method allocation for resources become very essential.

(d) CONTROLLING.

- (i) By while having progress report from time to time & updating the now continuously, a better control over the project is exercised.
- (ii) Arrow diagram & time charts are used for making periodic progress reports.