## October Circuits '18

Oct 26, 2018, 09:00 PM IST - Nov 04, 2018, 10:00 PM IST

INSTRUCTIONS PROBLEMS SUBMISSIONS LEADERBOARD ANALYTICS

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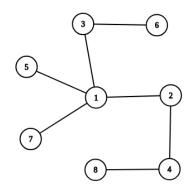
# ← Problems / Divide the tree Divide the tree Max. Marks: 100 This is an approximate problem.

Let's define tree  $T_{K}$  in the following way:

1.  $T_1$  is a tree with just one vertrex.

2. If K>1 then let D be the biggest integer such that D|K and  $1 \leq D < K$ . The tree  $T_K$  will be the union of  $T_{K-1}$  with vertex  $\{K\}$  and edge (D,K).

The image below represents the tree  $T_8$ .



Two graphs  $G_1=(\{A_1,A_2,\ldots,A_M\},E_1)$  &  $G_2=(\{B_1,B_2,\ldots,B_M\},E_2)$  are isomorphic if there exists a permutation P of length M such that  $\forall (i,j), (A_i,A_j) \in E_1 \iff (B_{P_i},B_{P_j}) \in E_2$ .

Given a tree F with N vertices. Let E be the set of edges. You need to delete some edges from the tree, such for every disjoint tree U in the remaining forest there exists an integer i such that U is isomorphic to  $T_i$ .

#### Input

The first line contains two integers -  $N,\,W.$ 

The following N-1 lines contain two integers - U,V, meaning there is edge (U,V) in tree F.

#### Scoring

Suppose the sizes of the trees in the remaining forest are  $S_1, S_2, \ldots, S_L$ . Let  $R = \frac{\sum_{i=1}^L S_i^4}{W}$ , then your score will be equal to  $10000^{\min(1.25,R)} + max(0,R-1.25) \cdot 10$ . You want to maximize this score.

#### Output

The first line contains one integer - L.

The  $(i+1)^{th}$  line has the following format -  $S_i,P_1,P_2,\ldots,P_{S_i}$ . P is a set of vertices, representing a tree in the remaining forest. The condition  $\forall (x,y), (x,y) \in T_{S_i} \iff (P_x,P_y) \in E$  must be satisfied.

We must have that  $\sum_{i=1}^L S_i = N$ . Every vertex must appear exactly once.

#### **Test Generation**

For the first 10 tests. At first, an array  $\emph{V}$  of length  $\emph{K}$  is generated uniformly under the conditions attached below. Then, we generate a forest containing trees  $T_{V_1},T_{V_2},\ldots,T_{V_K}$  with indices from 1 to N. After this, random edges are added in order to transform the forest into tree F. W will be assigned value  $\sum_{i=1}^K V_i^3$ .

The rest of the tests have random trees. W will be assigned value 21N.

| Test | N      | $V_i \le$ | $V_i \ge$ | Special Conditions   |
|------|--------|-----------|-----------|--|
| 1    | 100    | 4         | 1         | No   |
| 2    | 100000 | 4         | 1         | No   |
| 3    | 100000 | 10        | 1         | No   |
| 4    | 100000 | 20        | 10        | No   |
| 5    | 100000 | 10000     | 10        | There exists only one $i$ with $V_i=10000$ , for the rest of $j\neq i$ $V_j\leq 20$ is satisfied |
| 6    | 100000 | 10000     | 1         | There evicte only  |

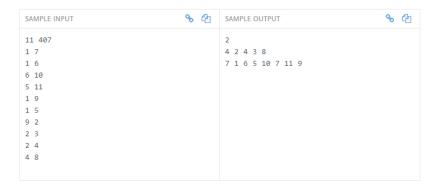




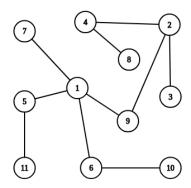
| Ŭ  | 100000 | 10000 | •   | one $i$ with $V_i = 10000$ , for the rest of $j \neq i$ $V_j \leq 5$ is satisfied                  |
|----|--------|-------|-----|--|
| 7  | 1000   | 100   | 10  | There exists only one $i$ with $V_i = 100$ , for the rest of $j \neq i$ $V_j \leq 20$ is satisfied |
| 8  | 1000   | 100   | 1   | There exists only one $i$ with $V_i = 100$ , for the rest of $j \neq i$ $V_j \leq 5$ is satisfied  |
| 9  | 100000 | 1000  | 1   | No   |
| 10 | 100000 | 1000  | 100 | No   |
| 11 | 10     | -     | -   | No   |
| 12 | 100    | -     | -   | No   |
| 13 | 1000   | -     | -   | No   |
| 14 | 10000  | -     | -   | No   |
| 15 | 100000 | -     | -   | No   |

Note that the tests are ordered in the same way as presented in the table above.

Test data will be regenerated with different seeds after the contest.



#### Explanation



Suppose that  $K=2,V_1=7,V_2=4$ , then  $W=7^3+4^3=407$ . We created trees  $T_7$  with indices  $\{1,5,6,7,10,11\}$  and  $T_4$  with indices  $\{2,3,4,8\}$ . Next, to connect both trees, we add edge (9,2).

Note that we can also delete edges  $\{(3,2),(2,4),(4,8)\}$ , but then we would obtain a smaller cost equal to  $7^3+4\cdot 1^3=347$  compared to  $7^3+4^3=407$ .

| 5.0 sec(s) for each input file.   |  |  |  |
|---|--|--|--|
| 256 MB  |  |  |  |
| 1024 KB   |  |  |  |
| Marks are awarded if any testcase passes.   |  |  |  |
| Bash, C, C++, C++14, Clojure, C#, D, Erlang, F#, Go, Groovy, Haskell, Java, Java 8, JavaScript(Rhino), JavaScript(Node.js), Julia, Kotlin, Lisp, Lisp (SBCL), Lua, Objective-C, OCaml, Octave, Pascal, Perl, PHP, Python, Python 3, Racket, Ruby, Rust, Scala, Swift, Swift-4.1, Visual Basic |  |  |  |
|   |  |  |  |

### **CODE EDITOR**



