

In DLP we deal with Z_p^* , but for building collision resistant hash function we will deal with prime order sub-group of Z_p^* . Let's assume G_q is a q -order sub-group of Z_p^* , where q is of n -bits and a generator g . Select uniformly at random an element h from G_q . Select x_1, x_2 (both in the range 0 to $q-1$). The hash function h^s can be defined as:

$$h^s(x_1, x_2) = g^{x_1} h^{x_2} \bmod p, \text{ where } s = (G_q, q, g, h)$$

In order to choose p, q , and g , we can choose a prime p such that $q=(p-1)/2$ is also a prime and $p \equiv 7 \pmod{8}$. In this case 2 is guaranteed to be a generator of order q .