

PRF is a efficient and deterministic function that is:

- Easy to compute
- Computationally indistinguishable from a random function

PRF is based on PRG with the only exception that in addition to the internal state they can accept any input data.

Let  $G$  be a secure PRG, which on input  $\{0,1\}^s$ , outputs  $\{0,1\}^{2s}$ , i.e. double the length of the input. Let  $G_0$  and  $G_1$  be the left and right halves of  $G$ , respectively such that  $G(x) = G_0(x) \parallel G_1(x)$ . For any  $K$  belonging to  $\{0,1\}^s$ , define  $F_K: \{0,1\}^n \rightarrow \{0,1\}^s$  by

$$F_K(x_1 \dots x_n) = G_{x_n}(G_{x_{n-1}}(\dots G_{x_1}(K) \dots))$$

If the PRG  $G$  is secure then the function  $F$  is also secure.

