

SMOOTHING USING BIAGRAM

Problems with simple MLE estimates :zero

Zero probability n-gram problem.

We can not compute perplexity and chain rule for the sentences.

so we a use the Laplace smoothing(Add-one estimation)

Just add one to all the count!

$$P(w_i | w_{i-1}) = \text{count}(w_{i-1}w_i) + 1 / \text{count}(w_{i-1}) + v$$

<S> JOHN READ MOBY DICK </S>

<S> MARY READ A DIFFERENT BOOK </S>

<S> SHE READ A BOOK BY CHER </S>

V=11 (total number of different word present in corpus)

Using smopthing the probability of bigram is...

$$P(w_i | w_{i-1}) = \text{count}(w_{i-1}w_i) + 1 / \text{count}(w_{i-1}) + v$$

$$P(\text{JOHN} | \text{<S>}) = \text{count}(\text{<S>}, \text{JOHN}) + 1 / \text{count}(\text{<S>}) + V$$

$$= (1+1) / (3+11) = 2/14$$

$$P(\text{READ} | \text{JOHN}) = \text{count}(\text{JOHN}, \text{READ}) + 1 / \text{count}(\text{JOHN}) + V$$

$$= (1 + 1) / (1+11) = 2/12$$

$$P(A \mid \text{READ}) = (2 + 1)/(3 + 11) = 3/14$$

$$P(\text{BOOK} \mid A) = (1 + 1)/(2 + 11) = 2/13$$

$$P(</S> \mid \text{BOOK}) = (1 + 1)/(2 + 11) = 2/13$$

$$P(\text{CHER} \mid <S>) = (0 + 1)/(3 + 11) = 1/14$$

$$P(\text{READ} \mid \text{CHER}) = (0 + 1)/(1 + 11) = 1/12$$

$$\begin{aligned} P(\text{JOHN READ A BOOK}) &= P(\text{JOHN} \mid <S>) * P(\text{READ} \mid \text{JOHN}) * \\ &\quad P(A \mid \text{READ}) * P(\text{BOOK} \mid A) * P(</S> \mid \text{BOOK}) \\ &= 2/14 * 2/12 * 3/14 * 2/13 * 2/13 \\ &= 0.0001 \end{aligned}$$

$$\begin{aligned} P(\text{CHER READ A BOOK}) &= P(\text{CHER} \mid <S>) * P(\text{READ} \mid \text{CHER}) * \\ &\quad P(A \mid \text{READ}) * P(\text{BOOK} \mid A) * P(</S> \mid \text{BOOK}) \\ &= 1/14 * 1/12 * 3/14 * 2/13 * 2/13 \\ &= 0.00003 \end{aligned}$$

SMOOTHING USING TRIAGRAM

<S> JOHN READ MOBY DICK </S>

<S> MARY READ A DIFFERENT BOOK </S>

<S> SHE READ A BOOK BY CHER </S>

$$P(\text{JOHN} \mid \langle S \rangle) = \text{count}(\langle S \rangle, \text{JOHN}) + 1 / \text{count}(\langle S \rangle) + V$$

$$= (1+1) / (3+11) = 2/14$$

$$P(\text{READ} \mid \text{JOHN}, \langle S \rangle) = \text{count}(\langle S \rangle, \text{JOHN}, \text{READ}) + 1 / \text{count}(\langle S \rangle, \text{JOHN}) + V$$

$$= (1+1) / (1+11) = 2/12$$

$$P(A \mid \text{JOHN}, \text{READ}) = \text{count}(\text{JOHN}, \text{READ}, A) + 1 / \text{count}(\text{JOHN}, \text{READ}) + V$$

$$= (0 + 1) / (1+11) = 1/12$$

$$P(\text{BOOK} \mid \text{READ}, A) = \text{count}(\text{READ}, A, \text{BOOK}) + 1 / \text{count}(\text{READ}, A) + V$$

$$= (1+1) / (2+11) = 2/13$$

$$P(\langle /S \rangle \mid A, \text{BOOK}) = \text{count}(A, \text{BOOK}, \langle /S \rangle) + 1 / \text{count}(A, \text{BOOK}) + V$$

$$= (0+1) / (1+11) = 1/12$$

$$P(\text{CHER} \mid \langle S \rangle) = \text{count}(\langle S \rangle, \text{CHER}) + 1 / \text{count}(\langle S \rangle) + V$$

$$= (0+1) / (3+11) = 1/14$$

$$P(\text{READ} \mid \text{CHER}, \langle S \rangle) = \text{count}(\langle S \rangle, \text{CHER}, \text{READ}) + 1 / \text{count}(\langle S \rangle, \text{CHER}) + V$$

$$= (0+1) / (0+11) = 1/11$$

$$P(A \mid \text{CHER}, \text{READ}) = \text{count}(\text{CHER}, \text{READ}, A) + 1 / \text{count}(\text{CHER}, \text{READ}) + V$$

$$= (0 + 1) / (0+11) = 1/11$$

$$P(\text{JOHN READ A BOOK}) = P(\text{JOHN} \mid \langle S \rangle) * P(\text{READ} \mid \text{JOHN}, \langle S \rangle) * \\ P(A \mid \text{JOHN}, \text{READ}) * P(\text{BOOK} \mid \text{READ}, A) * P(\langle /S \rangle \mid A, \text{BOOK})$$

$$= 2/14 * 2/12 * 1/12 * 2/13 * 1/12$$

$$= 0.00002543752$$

$$\begin{aligned}
P(\text{CHER READ A BOOK}) &= P(\text{CHER} \mid \langle S \rangle) * P(\text{READ} \mid \text{CHER}, \langle S \rangle) * \\
&P(A \mid \text{CHER}, \text{READ}) * P(\text{BOOK} \mid \text{READ}, A) * P(\langle /S \rangle \mid A, \text{BOOK}) \\
&= 1/14 * 1/11 * 1/11 * 2/13 * 1/12 \\
&= 0.00000756818
\end{aligned}$$