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# Problem 1

```
function f = ffunctgravgradsc02(t,x,IMoIbody,norbit)
%
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%
% This function implements a nonlinear dynamic model
% of a rigid-body spacecraft that includes the
% gravity-gradient torques produced by a  $1/r^2$ 
% gravity field for a spacecraft that is flying
% in a circular orbit. This particular model
% uses quaternion to parameterize the transformation
% from local-level orbit following coordinates
% to the body-fixed coordinates in which
% the moment-of-inertia matrix IMoIbody is
% defined so that the transformation from
% local-level coordinates to body-fixed coordinates
% is defined by the orthonormal rotation matrix:
%
%  $R = R(q)$ 
%
% Inputs:
%
% t The time, in seconds, at which f is
% to be computed.
%
% x = [q1;q2;q3;q4;omegabody1;omegabody2;
% omegabody3], the 7-by-1 state
% vector of this system. The first four
% elements give the non-dimensional unit-
% normalized attitude quaternion for the
% rotation from local-level coordinates
% to spacecraft body coordinates. The last
% three elements give the body rotation rate
% vector relative to inertial coordinates
% in radians/second and expressed in
% the same body-fixed axes in which
% IMoIbody is defined.
%
% IMoIbody The 3-by-3 symmetric spacecraft
% moment-of-inertia matrix about the
% spacecraft center of mass and given
% in body-fixed coordinates in units
% of  $\text{kg}\cdot\text{m}^2$ .
%
% norbit The orbital motion rate in
% radians/sec. This is known as
% the mean motion in Keplerian
% orbital dynamics parlance.
%
% Outputs:
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%
%      f      =
%      [q1dot;q2dot;q3dot;q4dot;omegabody1dot;...
%              omegabody2dot;omegabody3dot],
%              the 7-by-1 vector that contains the
%              computed time derivatives of the state
%              from the kinematics and dynamics models
%              of the spacecraft.  f(1:4,1) is given
%              in 1/second units.  f(5:7,1) is given in
%              radians/second^2.
%

%
% Determine the rotation matrix from local-level coordinates
% to body-fixed coordinates.
%
q = x(1:4);
qnorm = q*(1/sqrt(sum(q.^2)));
R = rotmatquaternion(qnorm);
%
% Determine the rotation rate of the body-fixed coordinates
% relative to local-level coordinates and given along
% body axes.
%
omegavec = x(5:7);
deltaomegavec = omegavec - R*[0;-norbit;0];
%
% Determine the quaternion time rate of change from
% the quaternion kinematics model.
%
Omegamat = [0 deltaomegavec(3) -deltaomegavec(2)
deltaomegavec(1);...
            -deltaomegavec(3) 0 deltaomegavec(1)
deltaomegavec(2);...
            deltaomegavec(2) -deltaomegavec(1) 0
deltaomegavec(3);...
            -deltaomegavec(1) -deltaomegavec(2) -deltaomegavec(3)
0];
qdot = 0.5*Omegamat*q;
%
% Compute the unit direction vector from the Earth to
% the spacecraft and given in spacecraft body coordinates:
%
rhaticmvec = R*[0 0 -1]';
%
% Compute the gravity-gradient torque in body coordinates.
%
IMoI_rhaticmvec = IMoIbody*rhaticmvec;
Tgravgradvec = 3*(norbit^2)*cross(rhaticmvec,IMoI_rhaticmvec);
%
% Compute the angular velocity rate using Euler's equation.
%
hvec = IMoIbody*omegavec;
omegavecdot = IMoIbody\((cross(-omegavec,hvec)+Tgravgradvec);

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%  
% Assemble the computed state time derivative elements  
% into the output vector.  
%  
f = [qdot;omegavecdot];
```

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