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```
clc;
clear;
```

Some Functions

```
Weighting_func = @(m_vec,x_vec) (x_vec*m_vec')./sum(m_vec);

AngMom_func = @(m_vec,r_vec,v_vec,rcom) ...
    [ ((r_vec(2,:)-rcom(2)).*v_vec(3,:) - (r_vec(3,:)-
rcom(3)).*v_vec(2,:)) *m_vec' ; ...
      ((r_vec(3,:)-rcom(3)).*v_vec(1,:) - (r_vec(1,:)-
rcom(1)).*v_vec(3,:)) *m_vec' ; ...
      ((r_vec(1,:)-rcom(1)).*v_vec(2,:) - (r_vec(2,:)-
rcom(2)).*v_vec(1,:)) *m_vec' ];
```

Checking with data set at time t0

```
load mrvdata0_2019

Mtot = sum(mvec);
rcm0 = Weighting_func(mvec,rmat0);
vcm0 = Weighting_func(mvec,vmat0);
ptot0 = vcm0.*Mtot;
h0 = AngMom_func(mvec,rmat0,vmat0,rcm0);

rcm0_c =[ 4.135068659460397; 4.232438883625573; -2.649670988093459];
ptot0_c =[ -3.304955397587092; 2.615681258483552;
-12.378512402556995];
vcm0_c =[ -0.448630861116144; 0.355065407616567; -1.680320007510681];
h0_c =[ 0.158538578051034; -0.117644152647727; -0.423922316388524];

format long
disp('Errors are:')
disp('Center of mass')
disp(norm(rcm0-rcm0_c))
disp('Total momentum')
disp(norm(ptot0-ptot0_c))
disp('Velocity of center of mass')
disp(norm(vcm0-vcm0_c))
disp('Angular velocity about center of mass')
```

```

disp(norm(h0-h0_c))

Errors are:
Center of mass
    1.256073966947020e-15

Total momentum
    1.831026719408895e-15

Velocity of center of mass
    5.926969055564841e-16

Angular velocity about center of mass
    1.509301780344530e-14

```

Solution for data set at time t1

```

load mrvdata1_2019

rcm1 = Weighting_func(mvec,rmatl);
vcml = Weighting_func(mvec,vmatl);
ptotl = vcml.*Mtot;
hl = AngMom_func(mvec,rmatl,vmatl,rcml);

disp('Solution for Data set at t1:')
disp('Center of mass')
disp(rcml')
disp('Total momentum')
disp(vcml')
disp('Velocity of center of mass')
disp(ptotl')
disp('Angular velocity about center of mass')
disp(hl')

Solution for Data set at t1:
Center of mass
    6.496750220923424    6.436764329727224   -3.950000393183263

Total momentum
    0.176454273684443    0.192731693478986   -1.278640574034888

Velocity of center of mass
    1.299896094508161    1.419807921962311   -9.419436853311913

Angular velocity about center of mass
    0.254661038188203   -0.435851676485561   -0.666628074221855

```

Forces and Moments

```
dt = t1 - t0;
```

```
Fexttotavg = (ptot1 - ptot0)./dt;

Texttotavg = (h1 - h0)./dt;

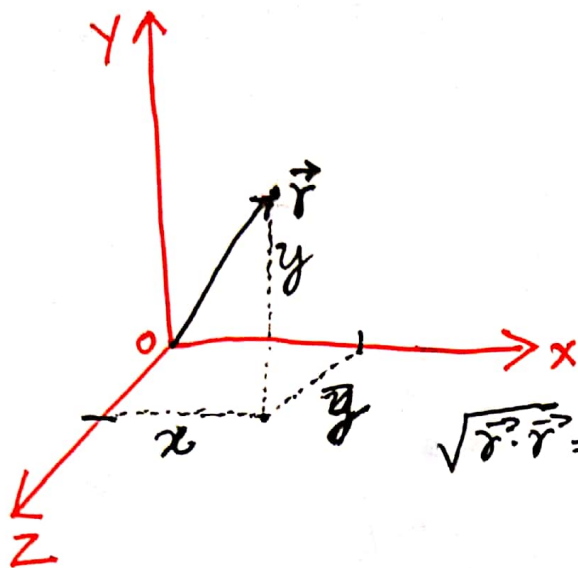
disp('Solution for Forces and Moments:')
disp('Total average external forces')
disp(Fexttotavg)
disp('Total average external moments')
disp(Texttotavg)

Solution for Forces and Moments:
Total average external forces
    8.672036708277311   -2.252115511339435    5.572646985395630

Total average external moments
    0.181021582179245   -0.599260873517558   -0.457072990269928
```

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3)



$$\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$$

Then

$$|\vec{r}| = \sqrt{(x-0)^2 + (y-0)^2 + (z-0)^2}$$

$$\sqrt{\vec{r} \cdot \vec{r}} = \sqrt{|\vec{r}|^2 \cos(0)} = \sqrt{x^2 + y^2 + z^2} \quad \blacksquare$$

4) let,

$$\vec{r}^b = \begin{bmatrix} x^b \\ y^b \\ z^b \end{bmatrix}$$

$$\& \vec{r}^a = \begin{bmatrix} x^a \\ y^a \\ z^a \end{bmatrix}$$

are the components written in a column vector form.

Then

$$\sqrt{(x^a)^2 + (y^a)^2 + (z^a)^2} = \sqrt{\vec{r}^a \cdot \vec{r}^a}$$

from the previous Result

Similarly

$$\sqrt{(x^b)^2 + (y^b)^2 + (z^b)^2} = \sqrt{\vec{r}^b \cdot \vec{r}^b}$$

Given the Relation we can write following from what is given in the question 4.

$$\begin{aligned} \sqrt{\vec{r}^b \cdot \vec{r}^b} &= \sqrt{[x^b \ y^b \ z^b] \begin{bmatrix} x^b \\ y^b \\ z^b \end{bmatrix}} = \sqrt{(R^{ba} \vec{r}^a)^T (R^{ba} \vec{r}^a)} \\ &= \sqrt{\vec{r}^{aT} R^{baT} R^{ba} \vec{r}^a} \end{aligned}$$

from the property of the Orthogonality of R^{ba}

$$R^{baT} = R^{ba^{-1}}$$

$$\therefore R^{baT} R^{ba} = I_{3 \times 3}$$

$$\begin{aligned} \therefore \sqrt{\vec{r}^b \cdot \vec{r}^b} &= \sqrt{\vec{r}^{aT} \vec{r}^a} = \sqrt{[x^a \ y^a \ z^a] \begin{bmatrix} x^a \\ y^a \\ z^a \end{bmatrix}} \\ &= \sqrt{(x^a)^2 + (y^a)^2 + (z^a)^2} \end{aligned}$$

\therefore

$$\sqrt{(x^b)^2 + (y^b)^2 + (z^b)^2} = \sqrt{(x^a)^2 + (y^a)^2 + (z^a)^2} \quad \blacksquare$$