

Problem 2

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function [gammaeq, Teq, alphaeq, phieq, XdotSM, YdotSM, iflagterm, niter] = ...
    solvesteadystateaircraft01(Zeq, Veq, psieq, m, S, CLalpha, ...
        CD0, oneoverpiARE, ...
        nitermax)

%
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%
% This function determines for the flight-path angle,
% thrust, angle-of-attack, and roll angle that produce
% steady, level, straight-line motion of a point-mass
% 3-dimensional aircraft that is operating over
% a flat non-rotating Earth (i.e., without Coriolis effects
% due to the Earth's rotation, without centrifugal
% effects due to the Earth's rotation other than the
% mean centrifugal effect at the origin of the coordinate
% system, and with a constant gravitational acceleration).
% While it uses a flat-Earth (i.e., constant) gravity field,
% its constant gravity takes into account the Earth's J2
% oblateness effect at the coordinate system center and
% it subtracts off the centrifugal acceleration of the
% coordinate system center as caused by the Earth's rotation.
%
% This function works by reducing the problem to a
% single equation in the single unknown value of
% angle of attack, alphaeq. This single nonlinear
% equation is solved iteratively using Newton's
% method. Once the angle of attack has been
% determined, the thrust Teq can be computed directly.
% The flight-angle gammaeq and the roll angle
% phieq are obvious.
%
% This function also computes the steady-motion rates
% of change of the northward displacement X and the
% and eastward displacement Y, which are XdotSM
% and YdotSM.
%
%
%
% Inputs:
%
%   Zeq           The steady-motion vertical
%                  displacement, in meters,
%                  relative to the origin of the
%                  local level coordinate system.
%                  A positive value is down. This
%                  coordinate system is centered
%                  at the runway of the Blacksburg,
%                  VA, airport, which is at an
%                  altitude of 649.7 m above sea
%                  level. Therefore, (-Zeq + 649.7)
%                  is the steady-motion aircraft
%                  altitude above sea level.
%
%   Veq           The steady-motion aircraft
%                  velocity in meters/second.
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%
%   psieq           The steady-motion aircraft
%                   heading angle in meters.
%                   psieq = 0 radians is due
%                   north (i.e., along the +X
%                   local-level axis) and
%                   psieq = +pi/2 radians is
%                   due east (i.e., along the
%                   +Y axis).
%
%   m               The aircraft mass in kg.
%
%   S               The wing area, in meters^2, which is
%                   the aerodynamic model's reference area.
%
%   CLalpha         The lift curve slope, dCL/dalpha, which
%                   is non-dimensional.
%
%   CDO             The drag at zero lift, which is non-
%                   dimensional.
%
%   oneoverpiARE    = 1/(pi*AR*e), where AR is the non-
%                   dimensional aspect ratio of the wing
%                   and e is the Oswald efficiency factor.
%                   This composite input quantity is non-
%                   dimensional. It is the coefficient
%                   of CL^2 in the drag coefficient model.
%
%   nitermax        The maximum number of Newton's
%                   method iterations that will be
%                   allowed before the algorithm
%                   quits with an error condition if
%                   it has not reached convergence
%                   prior to executing this many
%                   iterations. A conservative value
%                   for this limit is 50.
%
%   Outputs:
%
%   gammaeq         The steady-motion flight-path
%                   angle in radians. This will
%                   equal 0.
%
%   Teq             The steady-motion thrust, in Newtons.
%
%   alphaeq         The steady-motion angle of attack,
%                   in radians.
%
%   phieq           The steady-motion roll angle,
%                   in radians. This will equal 0.
%
%   XdotsM          The steady-motion northward component
%                   of velocity, in meters/second.
%
%   YdotsM          The steady-motion eastward component
%                   of velocity, in meters/second.
%
%   iflagterm       A termination status flag that
%                   indicates whether the Newton's

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% method solution for alphaeq has
% converged. Its possible values and
% their meanings are:
%
% 0 Normal successful termination.
%
% 1 Failure to converge in nitermax
% Newton iterations. A warning
% message will be sent to the
% display in this case.
%
% niter The number of Newton iterations that
% have been executed in the attempt
% to solve for alphaeq.
%
%
% Set up the steady-motion flight-path angle and roll angle.
%
gammaeq = 0;
phieq = 0;
%
% Compute the steady-motion northward and eastward velocities
%
Veq_cosgammaeq = Veq*cos(gammaeq);
XdotSM = Veq_cosgammaeq * cos(psieq);
YdotSM = Veq_cosgammaeq * sin(psieq);
%
% Compute the air density using a decaying exponential
% model. This model is good to about 1500 m altitude
% (about 5000 ft). This model recognizes that -Zeq + 649.7
% is the aircraft altitude above sea level in meters.
%
rho_sealevel = 1.225; % kg/m^3
hscale = 10230.; % meters
rho = rho_sealevel*exp((Zeq - 649.7)/hscale); % kg/m^3
%
% Set the flat-Earth gravitational acceleration at the
% Blacksburg airport minus the effects of centrifugal
% acceleration at the Blacksburg airport due to the
% Earth's rotation vector.
%
g = 9.79721; % meters/second^2
%
% Determine the dynamic pressure.
%
qbar = 0.5*rho*Veq*Veq;
%
% Compute the product of qbar and S.
%
qbar_S = qbar*S;
%
% Compute the constant term in the equation that
% will be solved using Newton's method in order to
% determine alphaeq. It takes the form:
%
0 = f(alphaeq) = tan(alphaeq)*CD(alphaeq) + CL(alphaeq) - C0
%
% where C0 = 2*m*g/(rho*(Veq^2)*S) = m*g/(qbar*S);

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%
C0 = m*g/qbar_S;
%
% Initialize the guess of the steady-motion angle of attack
% at zero.
%
alphaeq = 0;
%
% Initialize iflagterm at its nominal successful-case
% value and initialize niter.
%
iflagterm = 0;
niter = 0;
%
% This is the loop that performs one Newton's method
% (also known as the Netwon-Raphson method for
% a scalar equation in a single unknown) iteration
% towards a better guess of alphaeq. It also tests
% whether the guess is close enough to stop
% the iterations.
%
testdone0 = 0;
while testdone0 == 0
    niterp1 = niter + 1;
    if niterp1 > nitermax
        iflagterm = 1;
        disp('warning in solvesteadystateaircraft01.m.: Newton's')
        disp([' method did not converge in ',int2str(nitermax),...
            'iterations.'])
        break
    end
    niter = niterp1;
%
    CL = CLalpha*alphaeq;
    CD = CD0 + CL^2*(oneoverpiAR);
    tan_alphaeq = tan(alphaeq);
    f = tan_alphaeq*CD+CL-C0;
    dCL_dalpha = CLalpha;
    dCD_dalpha = 2*CLalpha*CLalpha*alphaeq*oneoverpiAR;
    dtan_alphaeq_dalpha = 1 + tan_alphaeq^2;
    df_dalpha = tan_alphaeq*dCD_dalpha+dtan_alphaeq_dalpha*CD+dCL_dalpha;
    deltaalphaeq = -f/df_dalpha;
    alphaeq = alphaeq + deltaalphaeq;
%
% Test for convergence.
%
    if abs(deltaalphaeq) <= 1.e-10
        testdone0 = 1;
    end
end
%
% Compute the steady-motion thrust.
%
CL = CLalpha*alphaeq;
CD = CD0 + CL^2*(oneoverpiAR);
D = qbar_S*CD;
Teq = D/cos(alphaeq);

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Output:

γ_{eq}	0
T_{eq}	4.829888745867086e+03
α_{eq}	0.052510385639473
ϕ_{eq}	0
\dot{X}_{SM}	84.264888743087582
\dot{Y}_{SM}	-70.706637065519317