

Figure 1: Relative Motion e=0.0

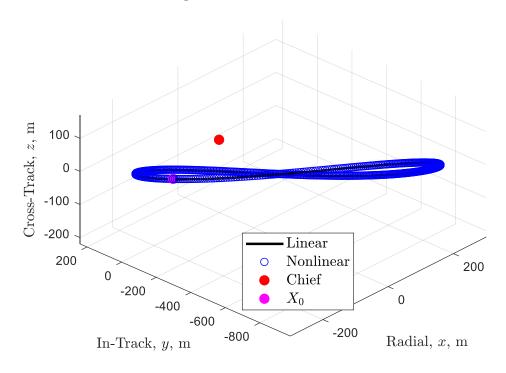


Figure 2: Relative Motion e=0.2

Linear and Nonlinear Relative Motion Simulation

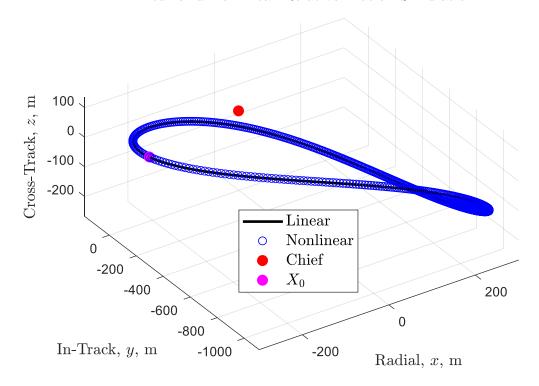


Figure 3: Relative Motion e=0.4

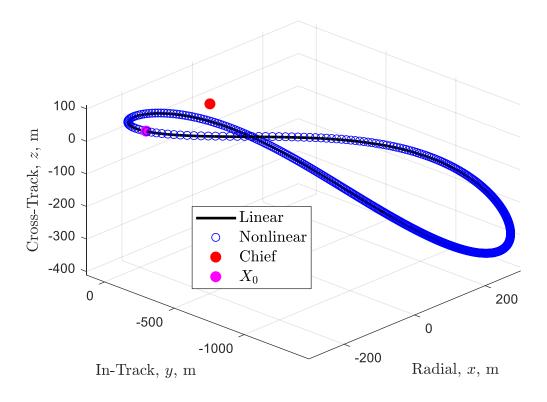


Figure 4: Relative Motion e=0.6

Linear and Nonlinear Relative Motion Simulation

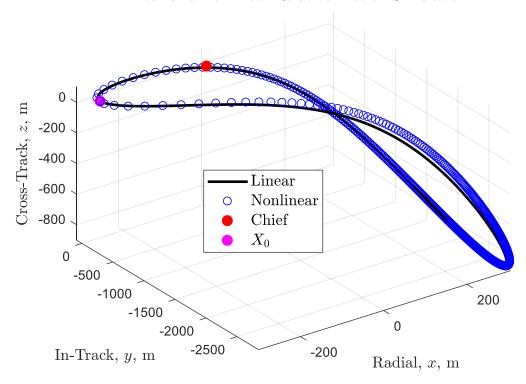


Figure 5: Relative Motion e=0.8

Data

Chief Orbital elements:

```
a = 7000e3;
ecc = [0 0.2 0.4 0.6 0.8]
inc = 45*pi/180;
raan = pi/6;
argper = pi/6;
f0 = 0;
```

Initial Conditions:

```
x0 = -300;
y0 = -300;
z0 = 100;
xd0 = 0;
yd0 = eccFactor*x0;
zd0 = -0.2;
```

Observations:

- As the eccentricity of the chief increases the magnitude of relative motion of the deputy increases. This is because of the increase in the cross-track and in-track increased relative motion.
- The motion becomes more and more out-of-plane with the increasing e of the chief. When the e is zero, the relative motion is planar.
- The speed of the deputy is faster when close to the chief, as seen in the high e value simulations.
- The linear and nonlinear simulations diverge more with increasing eccentricity of the chief.

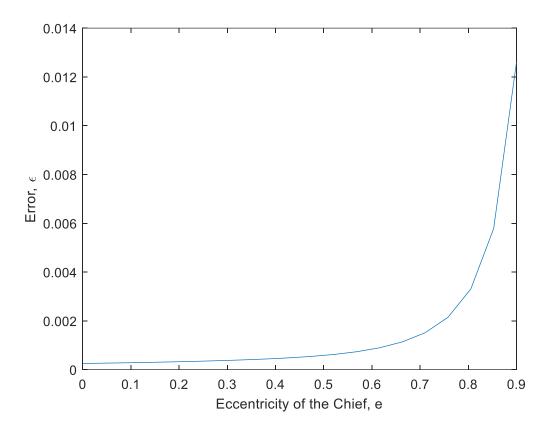


Figure 6: Error Metric as a function of Eccentricity, for Case 2 Chief Orbit

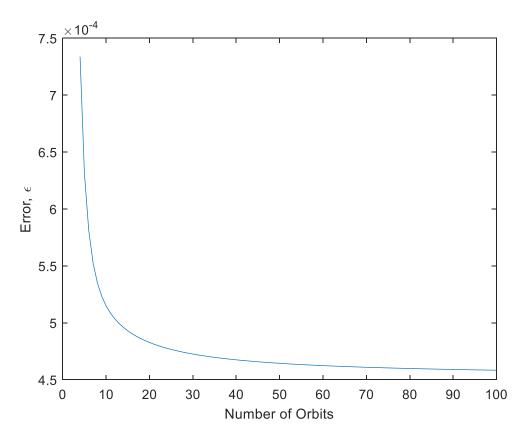


Figure 7: Error Metric as a function of Number of orbits, for Case 2 Chief Orbit

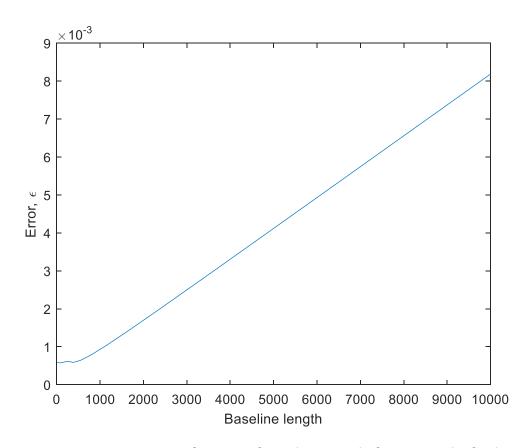


Figure 8: Error Metric as a function of Baseline Length, for Case 2 Chief Orbit

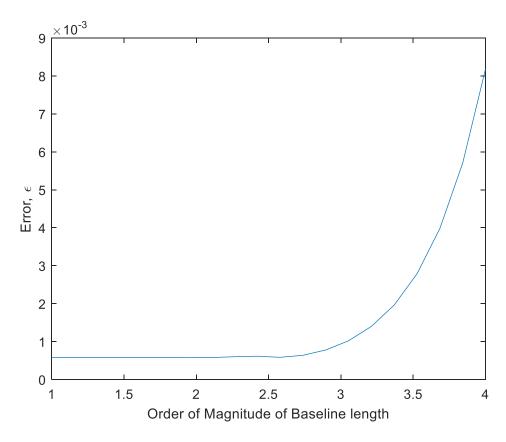


Figure 9: Error Metric as a function of Baseline Length Order of Magnitude, for Case 2 Chief Orbit

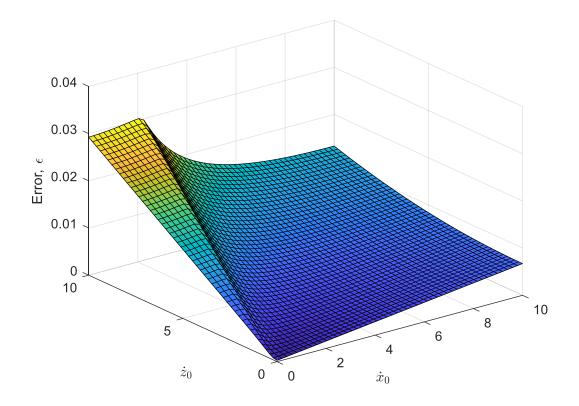


Figure 10: Error Metric as a function of Initial x and z velocities, for Case 2 Chief Orbit

Question e: Which parameter impact the error metric the most?

- Eccentricity of the Chief: The error metric changes 2 orders of magnitude as the eccentricity of the chief goes from 0.1 to 0.9.
- Initial velocities \dot{x}_0 and \dot{z}_0 : The initial relative velocities have huge impact on the error metric as well. The error metric changes 2 orders of magnitude here as well.

Frob-3

$$HCW$$
 Eq
 $\ddot{x} = 3n^2x + 2n \dot{y}$
 $\ddot{y} = -2n \dot{x}$
 $\ddot{z} = -n^2z$
First Solving for $z(x)$ of $y(x)$ because
they are coupled:
 $\ddot{y} = -2n \dot{x}$ \Rightarrow this is Substituted
 $\ddot{x} = 3n^2 \dot{x} + 2n(-2n \dot{x})$
 $\ddot{x} = 3n^2 \dot{x} - 4n^2 \dot{x} = -n^2 \dot{x}$
 $\ddot{x} = -n^2 \dot{x}$
 $(\ddot{x} + n^2 \dot{x}) = 0 \implies dE$ to be Solved
out $t = 0$
 $\dot{z}_0 = 3n^2 x_0 + 2n \dot{y}_0$
this \ddot{x}_0 will be used and with be
Substituted outer in terms of x_0 & y_0

Taking laplace transform.

$$L(\ddot{x}(t) + n^2 \dot{x}(t)) = 0$$
 $L(\ddot{x}(t) + n^2 \dot{x}(t)) = 0$
 L

Scanned with CamScanner

$$X(s) = \frac{20}{s} + \frac{20}{s^{2}+n^{2}} + \frac{20}{n^{2}} \cdot \frac{1}{s^{2}} - \frac{20}{n^{2}} \cdot \frac{s}{s^{2}+n^{2}}$$

$$Z(x(s)) = \chi(t) = \chi_{0} + \frac{1}{2} \cdot \frac{s}{n} \cdot \frac{s}{n} \cdot \ln(nt) + \frac{1}{2} \cdot \frac{s}{n^{2}} \cdot \frac{s}{n^{2}} \cdot \ln(nt)$$

$$\chi(t) = \chi_{0} + \frac{1}{2} \cdot \frac{1}{n} \cdot \frac{s}{n} \cdot \ln(nt) - \frac{1}{2} \cdot \frac{s}{n} \cdot \ln(nt)$$

$$\chi(t) = \chi_{0} + \frac{3n^{2} \chi_{0} + 2n \dot{y}_{0}}{n^{2}} \cdot \frac{s}{n} \cdot \ln(nt)$$

$$-\frac{3n^{2} \chi_{0} + 2n \dot{y}_{0}}{n^{2}} \cdot \frac{s}{n} \cdot \ln(nt)$$

$$-\frac{3}{2} \cdot \frac{2}{n} \cdot \frac{3}{n} \cdot \frac{s}{n} \cdot \ln(nt)$$

$$-\frac{3}{2} \cdot \frac{2}{n} \cdot \frac{3}{n} \cdot \frac{s}{n} \cdot \ln(nt)$$

$$-\frac{2}{n} \cdot \frac{3}{n} \cdot \frac{s}{n} \cdot \frac{$$

The Second Eq. $\ddot{y}(t) = -2n\dot{z}(t) \implies \text{the Second Eq.}$ $\int \ddot{y}(t) dt = -2n \int \dot{z}(t) dt + C_1$

$$y(t) = -2n x(t) + C_1$$
at $t = 0$

$$x(t = 0) = 4x_0 + \frac{2}{n}y_0 - 3x_0 - \frac{2}{n}y_0$$

$$= x_0$$

$$y'_0 = -2n x_0 + C_1$$

$$C_1 = y'_0 + 2n x_0$$

$$y(t) dt = -2n fx(t) + C_1 + C_2$$

$$\int x(t) = 4x_0 + \frac{2}{n}y_0 + \frac{3}{n}(cos(nt) - 3x_0 sin(nt)$$

$$-\frac{2}{n}y_0 sin(nt)$$

$$y(t) = (4x_0 + \frac{2}{n}y_0 + \frac{3}{n}(cos(nt) - 3x_0 sin(nt))$$

$$-\frac{2}{n}y_0 sin(nt)$$

$$+ C_2$$

$$y(t) = -8n x_0 + \frac{2}{n}(cos(nt) - 3x_0 sin(nt))$$

$$+ C_1 + C_2$$

$$y(t) = -8n x_0 + \frac{2}{n}(cos(nt) + 6x_0 sin(nt))$$

$$+ C_1 + C_2$$

$$y(t) = -8n x_0 + C_1$$

$$+ C_2$$

$$y(t) = -8n x_0 + C_1$$

$$+ C_2$$

$$y(t) = -8n x_0 + C_1$$

$$+ C_3$$

$$+ C_4$$

$$+ C_4$$

$$+ C_5$$

$$y(t) = -6n \times ot - 3y_0 t + \frac{2}{n} x_0 lost lnt) + 6 \times sin (nt) + C_2$$

$$at \quad t = 0$$

$$y_0 = \frac{2}{n} x_0 + C_2$$

$$C_2 = y_0 - \frac{2}{n} x_0$$
The $x(t)$ of $y(t)$ and:

The a(t) & y(t) are:

$$\frac{2(t)}{n} = 4 20 + \frac{2}{n} i j_0 + \frac{2}{n} Sin(nt) - 3 20 Cos(nt)$$

$$-\frac{2}{n} i j_0 Cos(nt)$$

$$\frac{2(t)}{n} = 4 20 + \frac{2}{n} i j_0 Cos(nt)$$

$$\frac{2}{n} i j_0 Cos(nt)$$

$$\frac{2}{n} i j_0 Cos(nt)$$

$$\frac{2}{n} i j_0 Sin(nt) + \frac{2}{n} i j_0 Sin(nt)$$

for 2tt) $\frac{1}{2} + \eta^2 Z = 0$ Taking laplace transform $S^{2}Z(S) - SZ_{0} - \dot{Z}_{0} + \gamma^{2}Z = 0$ $(S^2 + n^2) Z(S) = SZ_0 + Z_0$ $Z(S) = Z_0 \frac{S}{S^2 + n^2} + \frac{Z_0}{n} \frac{n}{S^2 + n^2}$ $\mathcal{L}^{-1}(Z(S)) = Z_0 \, \mathcal{E}_{00}(nt) + \frac{\dot{z}_0}{n} \, \mathcal{S}_{10}(nt)$

$$Z(t) = Z_0 Cos(nt) + \frac{\dot{z}_0}{n} Sin(nt)$$