

#lab 7 Gauss method :

import numpy as np

import sys

Reading number of unknowns

n = int(input('Enter number of unknowns: ')) # its saves the shape of matrix

Making numpy array of n x n+1 size and initializing

to zero for storing augmented matrix

a = np.zeros((n,n+1)) # its forms the a[][]

Making numpy array of n size and initializing

to zero for storing solution vector

x = np.zeros(n) # it assign the argument of x with 0

Reading augmented matrix coefficients

print('Enter Augmented Matrix Coefficients:') #its reads actual matrix value

for i in range(n): # loop for running upto n -1 if the users ip shape 3 goes to goes to 0 to 2

for j in range(n+1):

a[i][j] = float(input('a['+str(i)+'']['+ str(j)+'']='))

Applying Gauss Elimination

for i in range(n):

if a[i][i] == 0.0:

sys.exit('Divide by zero detected!')

for j in range(i+1, n):

ratio = a[j][i]/a[i][i]

for k in range(n+1):

a[j][k] = a[j][k] - ratio * a[i][k]

Back Substitution

x[n-1] = a[n-1][n]/a[n-1][n-1]

for i in range(n-2,-1,-1):

x[i] = a[i][n]

for j in range(i+1,n):

x[i] = x[i] - a[i][j]*x[j]

x[i] = x[i]/a[i][i]

Displaying solution

print('\nRequired solution is: ')

for i in range(n):

print('X%d = %0.2f' %(i,x[i]), end = '\t')

```
Enter number of unknowns: 3
Enter Augmented Matrix Coefficients:
```

```
a[0][0]=1
a[0][1]=2
a[0][2]=3
a[0][3]=6
a[1][0]=2
a[1][1]=-1
a[1][2]=3
a[1][3]=4
a[2][0]=2
a[2][1]=3
a[2][2]=5
a[2][3]=10
```

```
Required solution is:
```

```
X0 = 1.00      X1 = 1.00      X2 = 1.00
```

```
C:\Users\DELL\Desktop\Numerical Methods Lab>
```

Lab 8:

#Power Method

Power Method to Find Largest Eigen Value and Eigen Vector

Importing NumPy Library

import numpy as np

import sys

Reading order of matrix

n = int(input('Enter order of matrix: '))

Making numpy array of n x n size and initializing

to zero for storing matrix

a = np.zeros((n,n))

Reading matrix

print('Enter Matrix Coefficients:')

for i in range(n):

for j in range(n):

a[i][j] = float(input('a['+str(i)+']['+ str(j)+']='))

Making numpy array n x 1 size and initializing to zero

for storing initial guess vector

x = np.zeros((n))

Reading initial guess vector

print('Enter initial guess vector: ')

for i in range(n):

x[i] = float(input('x['+str(i)+']='))

Reading tolerable error

tolerable_error = float(input('Enter tolerable error: '))

Reading maximum number of steps

max_iteration = int(input('Enter maximum number of steps: '))

Power Method Implementation

lambda_old = 1.0

condition = True

step = 1

while condition:

Multiplying a and x

```

x = np.matmul(a,x)
# Finding new Eigen value and Eigen vector
lambda_new = max(abs(x))
x = x/lambda_new
# Displaying Eigen value and Eigen Vector
print('\nSTEP %d' %(step))
print('-----')
print('Eigen Value = %0.4f' %(lambda_new))
print('Eigen Vector: ')
for i in range(n):
    print('%0.3f\t' % (x[i]))
# Checking maximum iteration
step = step + 1
if step > max_iteration:
    print('Not convergent in given maximum
iteration!')
    break
# Calculating error
error = abs(lambda_new - lambda_old)
print('error='+ str(error))
lambda_old = lambda_new
condition = error > tolerable_error

```

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STEP 7
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Eigen Value = 7.6499
Eigen Vector:
0.597
0.485
1.000
error=0.003930879316461855

STEP 8
-----
Eigen Value = 7.6486
Eigen Vector:
0.597
0.485
1.000
error=0.0013088801273761774

STEP 9
-----
Eigen Value = 7.6490
Eigen Vector:
0.597
0.485
1.000
error=0.0004356735382291532

```

Discussion and Conclusion:

The Gauss elimination method systematically reduces a system of linear equations to an upper triangular form, making it efficient for direct solutions, especially for small to medium-sized systems. It ensures accuracy but can become unstable with ill-conditioned matrices unless partial pivoting is used. On the other hand, the Power method is an iterative technique specifically designed to find the dominant eigenvalue and its corresponding eigenvector of a matrix. It is simple to implement and works well when the dominant eigenvalue is significantly larger than the others. However, it may fail or converge slowly if this condition is not met. Both methods highlight the balance between direct and iterative strategies in numerical methods—Gauss focusing on precision and generality, while Power emphasizes simplicity and specific applications in eigenvalue problems.