1

ASSIGNMENT 5

B.SandhyaRani

Download all python codes from

https://github.com/balumurisandhyarani550/ Assignment5/tree/main/codes

and latex-tikz codes from

https://github.com/balumurisandhyarani550/ Assignment5/tree/main/Assignment5

1 Question No 2.18(Quad forms)

Find the zeroes of the quadratic polynomial $x^2 + 7x + 10$ and verify the relationship between the zeros and coefficients.

2 SOLUTION

1) The vector form of equation is

$$y = x^2 + 7x + 10 \tag{2.0.1}$$

$$\mathbf{x}^T \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \mathbf{x} + \begin{pmatrix} 7 & 0 \end{pmatrix} \mathbf{x} + 10 = 0 \qquad (2.0.2)$$

Thus

$$y = 0 \implies x^2 + 7x + 10 = 0$$
 (2.0.3)

$$x^2 + 5x + 2x + 10 = 0 (2.0.4)$$

$$(x+2)(x+5) = 0 (2.0.5)$$

$$x = -2, -5$$
 (2.0.6)

(2.0.7)

The roots are $\alpha = -2$ and $\beta = -5$. Compare given quadratic equation $x^2+7x+10 = 0$ with $ax^2 + bx + c = 0$, we get a=1, b=7, c=10. Sum of the roots

 $\alpha + \beta = \frac{-b}{a} = -7 \tag{2.0.8}$

product of the roots

$$\alpha\beta = \frac{c}{a} = 10 \tag{2.0.9}$$

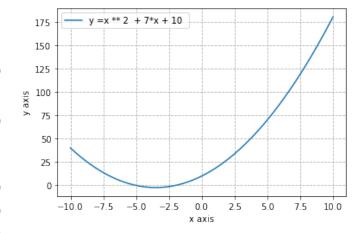


Fig. 2.1: $x^2 + 7x + 10$.