

# ASSIGNMENT 5

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Download all python codes from

[https://github.com/balumurisandhyarani550/  
Assignment5/tree/main/Assignment5](https://github.com/balumurisandhyarani550/Assignment5/tree/main/Assignment5)

and latex-tikz codes from

[https://github.com/balumurisandhyarani550/  
Assignment5/tree/main/Assignment5](https://github.com/balumurisandhyarani550/Assignment5/tree/main/Assignment5)

∴ Vertex **c** is given by

$$\begin{pmatrix} \frac{7}{2} & -1 \\ 1 & 0 \\ 0 & 0 \end{pmatrix} \mathbf{c} = \begin{pmatrix} -10 \\ \frac{-7}{2} \\ 0 \end{pmatrix} \quad (2.0.7)$$

$$\Rightarrow \begin{pmatrix} \frac{7}{2} & -1 \\ 1 & 0 \end{pmatrix} \mathbf{c} = \begin{pmatrix} -10 \\ \frac{-7}{2} \end{pmatrix} \quad (2.0.8)$$

$$\Rightarrow \mathbf{c} = \begin{pmatrix} \frac{-7}{2} \\ \frac{-9}{4} \end{pmatrix} \quad (2.0.9)$$

$$\begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} \frac{-7}{2} \\ \frac{-9}{4} \end{pmatrix} \quad (2.0.10)$$

## 1 QUESTION No 2.18(QUAD FORMS)

Find the zero's of the quadratic polynomial  $x^2 + 7x + 10$  and verify the relationship between the zero's and the coefficients.

## 2 SOLUTION

Given

$$y = x^2 + 7x + 10 \quad (2.0.1)$$

$$x^2 - y + 7x + 10 = 0 \quad (2.0.2)$$

compare with standard form of equation

$$ax^2 + bxy + cy^2 + 2dx + 2ey + f = 0 \quad (2.0.3)$$

$$a = 1, b = 0, c = 0, d = \frac{7}{2}, e = \frac{-1}{2}, f = 10$$

Here,

$$\mathbf{V} = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}, \mathbf{u} = \begin{pmatrix} \frac{7}{2} \\ \frac{-1}{2} \end{pmatrix}, f = 10 \quad (2.0.4) \text{ and,}$$

Using eigenvalue decomposition,

$$\mathbf{D} = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}, \mathbf{P} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \quad (2.0.5)$$

Now,

$$\begin{pmatrix} \mathbf{u}^T + \eta \mathbf{p}_1^T \\ \mathbf{V} \end{pmatrix} \mathbf{c} = \begin{pmatrix} -f \\ \eta \mathbf{p}_1 - \mathbf{u} \end{pmatrix} \quad (2.0.6)$$

Now,

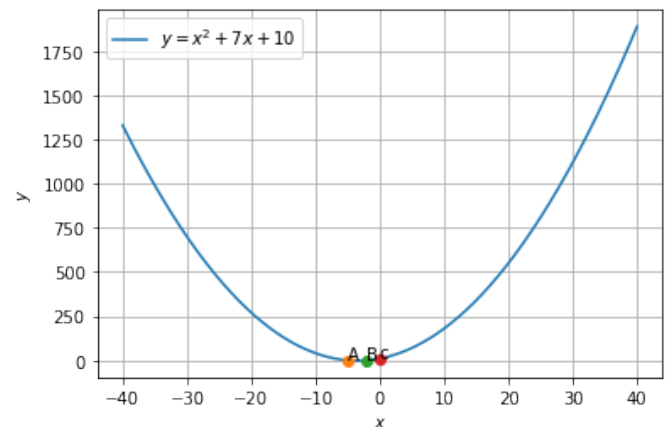


Fig. 2.1:  $y = x^2 + 7x + 10$

$$\mathbf{p}_1^T \mathbf{c} = \begin{pmatrix} 0 & 1 \end{pmatrix} \begin{pmatrix} \frac{-7}{2} \\ \frac{-9}{4} \end{pmatrix} \quad (2.0.11)$$

$$= \frac{-9}{4} \quad (2.0.12)$$

$$\mathbf{p}_2^T \mathbf{V} \mathbf{p}_2 = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad (2.0.13)$$

$$= 1 \quad (2.0.14)$$

∴

$$(\mathbf{p}_1^T \mathbf{c})(\mathbf{p}_2^T \mathbf{V} \mathbf{p}_2) = \frac{-9}{4} < 0 \quad (2.0.15)$$

Hence, the given equation has real roots.