

Assignment-8

B.SandhyaRani

Download all python codes from

then

<https://github.com/balumurisandhyarani/Assignment8/tree/main/Assignment8>

and latex-tikz codes from

<https://github.com/balumurisandhyarani550/Assignment8/tree/main/Assignment8>

$$(\mathbf{B}^\top \mathbf{A} \mathbf{B})^\top = [\mathbf{B}^\top (\mathbf{A} \mathbf{B})]^\top \quad (2.0.10)$$

$$= (\mathbf{A} \mathbf{B})^\top (\mathbf{B}^\top)^\top \quad (2.0.11)$$

$$= (\mathbf{B}^\top \mathbf{A}^\top) \mathbf{B} \quad (2.0.12)$$

$$= \mathbf{B}^\top (-\mathbf{A}) \mathbf{B} \quad (2.0.13)$$

$$= -(\mathbf{B}^\top \mathbf{A} \mathbf{B}) \quad (2.0.14)$$

therefore

$$\mathbf{B}^\top \mathbf{A} \mathbf{B} \quad (2.0.15)$$

1 QUESTION No-2.42

is skew symmetric.

Show that the matrix

$$\mathbf{B}^\top \mathbf{A} \mathbf{B} \quad (1.0.1)$$

is symmetric or skew symmetric according as \mathbf{A} is symmetric or skew symmetric.

2 SOLUTION

If \mathbf{A} be symmetric i.e.,

$$\mathbf{A}^\top = \mathbf{A} \quad (2.0.1)$$

then

$$(\mathbf{B}^\top \mathbf{A} \mathbf{B})^\top = [\mathbf{B}^\top (\mathbf{A} \mathbf{B})]^\top \quad (2.0.2)$$

$$(\mathbf{A} \mathbf{B})^\top (\mathbf{B}^\top)^\top \quad (2.0.3)$$

$$= (\mathbf{B}^\top \mathbf{A}^\top) \mathbf{B} \quad (2.0.4)$$

$$= \mathbf{B}^\top \mathbf{A}^\top \mathbf{B} \quad (2.0.5)$$

$$= \mathbf{B}^\top \mathbf{A} \mathbf{B} \quad (2.0.6)$$

$$(2.0.7)$$

Hence

$$\mathbf{B}^\top \mathbf{A} \mathbf{B} \quad (2.0.8)$$

is symmetric.

If \mathbf{A} is skew symmetric i. e.,

$$\mathbf{A}^\top = -\mathbf{A} \quad (2.0.9)$$