

## Feedback — Final Exam (One timed attempt only! You only have 4 hours once you open the exam.)

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You submitted this exam on **Fri 8 Mar 2013 12:13 PM PST**. You got a score of **10.00** out of **10.00**.

### Question 1

1\2	x	y	z
a	2,5	2,1	0,1
b	3,2	4,4	1,1
c	1,0	1,1	1,2

Find the strictly dominant strategies (there may be zero, one or more):

Your Answer		Score	Explanation
<input type="checkbox"/> 1) a;	✓	0.17	
<input type="checkbox"/> 2) b;	✓	0.17	
<input type="checkbox"/> 3) c;	✓	0.17	
<input type="checkbox"/> 4) x;	✓	0.17	
<input type="checkbox"/> 5) y;	✓	0.17	
<input type="checkbox"/> 6) z;	✓	0.17	
Total		1.00 / 1.00	

### Question Explanation

No strategy is a dominant strategy.

- **a** is strictly dominated by **b** and so is not dominant;
- if 2 plays  $z$  then 1 is indifferent between **c** and **b**, while if 2 plays  $y$  then **b** is strictly better than **c**, and so neither is strictly dominant.
- Similarly, when 1 plays **a**,  $x$  is the unique best response for 2; when 1 plays **b**,  $y$  is the unique best response for 2; when 1 plays **c**,  $z$  is the unique best response for 2, and so none of them is dominant.

## Question 2

1 \ 2	x	y	z
<b>a</b>	2,5	2,1	0,1
<b>b</b>	3,2	4,4	1,1
<b>c</b>	1,0	1,1	1,2

Find the weakly dominated strategies (there may be zero, one or more):

Your Answer		Score	Explanation
<input type="checkbox"/> 1) a;	✓	0.17	
<input type="checkbox"/> 2) b;	✓	0.17	
<input checked="" type="checkbox"/> 3) c;	✓	0.17	
<input type="checkbox"/> 4) x;	✓	0.17	
<input type="checkbox"/> 5) y;	✓	0.17	
<input type="checkbox"/> 6) z;	✓	0.17	

Total

1.00 / 1.00

**Question Explanation**

(3) is correct.

- For 1, **c** is weakly dominated by **b**. When 2 plays  $x$  or  $y$ , **b** is strictly better than **c**; when 2 plays  $z$ , 1 is indifferent between **b** and **c**.
- From the previous answer, player 2 has no weakly dominated strategies.

**Question 3**

1 \ 2	x	y	z
<b>a</b>	2,5	2,1	0,1
<b>b</b>	3,2	4,4	1,1
<b>c</b>	1,0	1,1	1,2

Which strategies survive the process of iterative removal of strictly dominated strategies (there may be zero, one or more)?

Your Answer		Score	Explanation
<input type="checkbox"/> 1) a;	✓	0.17	
<input checked="" type="checkbox"/> 2) b;	✓	0.17	
<input checked="" type="checkbox"/> 3) c;	✓	0.17	
<input type="checkbox"/> 4) x;	✓	0.17	
<input checked="" type="checkbox"/> 5) y;	✓	0.17	
<input checked="" type="checkbox"/> 6) z;	✓	0.17	
Total		1.00 / 1.00	

**Question Explanation**

(2), (3), (5) and (6) are the survivors.

- **a** is dominated by **b**.
- $x$  is dominated by  $y$ , once **a** is removed.
- No further removals can be made.

**Question 4**

1\2	x	y	z
<b>a</b>	2,5	2,1	0,1
<b>b</b>	3,2	4,4	1,1
<b>c</b>	1,0	1,1	1,2

Find all strategy profiles that form pure strategy Nash equilibria (there may be zero, one or more):

Your Answer		Score	Explanation
<input type="checkbox"/> 1) (a, x);	✓	0.11	
<input type="checkbox"/> 2) (a, y);	✓	0.11	
<input type="checkbox"/> 3) (a, z);	✓	0.11	
<input type="checkbox"/> 4) (b, x);	✓	0.11	
<input checked="" type="checkbox"/> 5) (b, y);	✓	0.11	
<input type="checkbox"/> 6) (b, z);	✓	0.11	
<input type="checkbox"/> 7) (c, x);	✓	0.11	

<input type="checkbox"/> 8) (c, y);	✓	0.11
<input checked="" type="checkbox"/> 9) (c, z).	✓	0.11
Total		1.00 / 1.00

### Question Explanation

(5) (b, y) and (9) (c, z) are pure-strategy Nash equilibria.

- It is easy to check the pure-strategy Nash equilibrium: no one wants to deviate from (5) and (9).
- In any of the other combinations at least one player has an incentive to deviate. Thus, they are not equilibria.

## Question 5

1 \ 2	y	z
b	4, 4	1, 1
c	1, 1	2, 2

Which of the following strategies form a mixed strategy Nash equilibrium? ( $p$  corresponds to the probability of 1 playing **b** and  $1 - p$  to the probability of playing **c**;  $q$  corresponds to the probability of 2 playing  $y$  and  $1 - q$  to the probability of playing  $z$ ).

### Your Answer

### Score

### Explanation

- ☐ 1)  $p = 1/3, q = 1/3$ ;
- ☐ 2)  $p = 1/3, q = 1/4$ ;
- ☐ 3)  $p = 2/3, q = 1/4$ ;
- ☒ 4)  $p = 1/4, q = 1/4$ ; ✓ 1.00

Total

1.00 / 1.00

**Question Explanation**

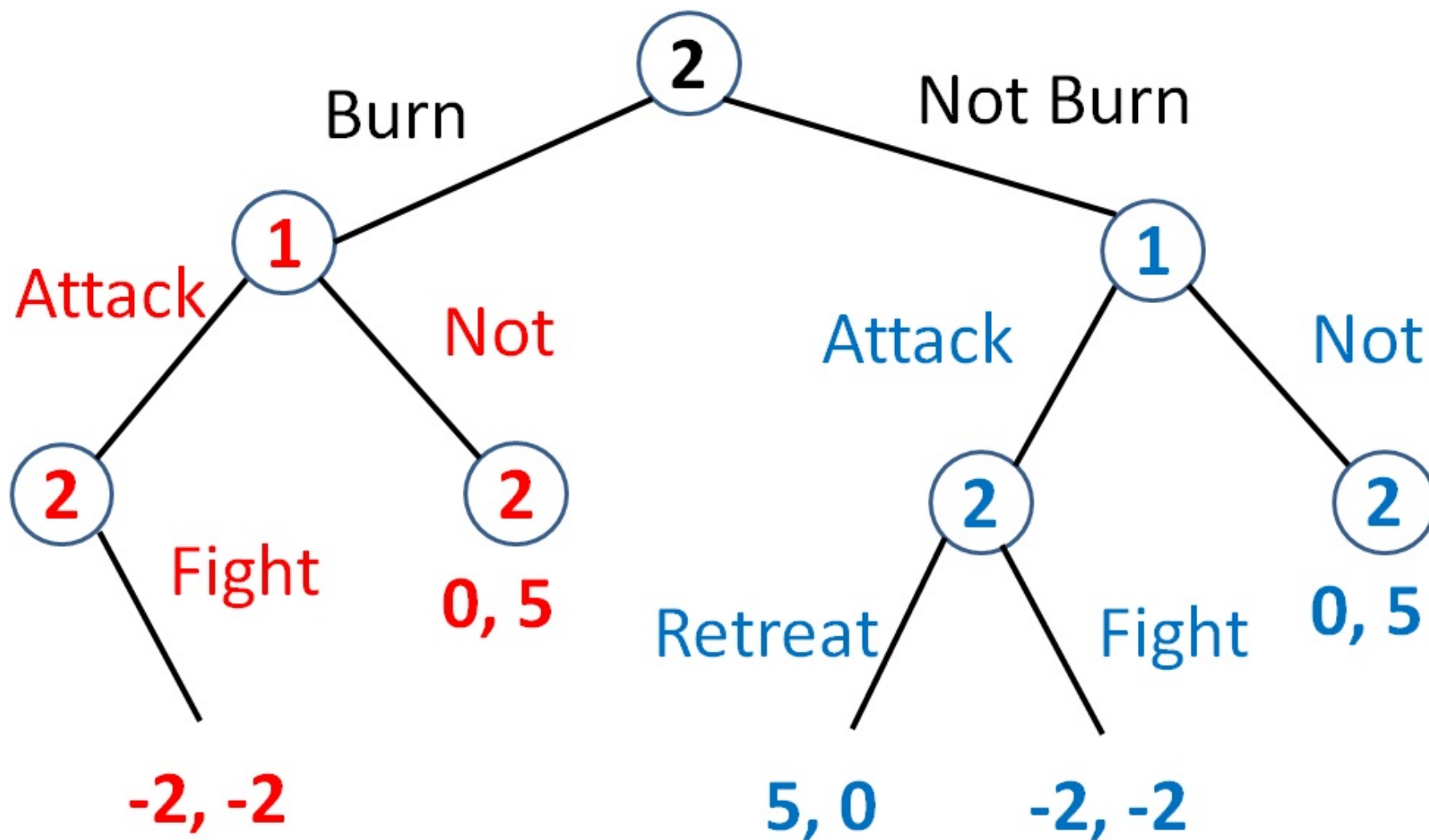
(4) is true.

- In a mixed strategy equilibrium in this game both players must mix and so 1 must be indifferent between **b** and **c**, and 2 between  $y$  and  $z$ .
- **b** gives 1 an expected payoff:  $4q + (1 - q)$
- **c** gives 1 an expected payoff:  $1q + 2(1 - q)$
- Setting these two payoffs to be equal leads to  $q = 1/4$ .
- By symmetry we have  $p = 1/4$ .

## Question 6

**Burning the Bridge**

- One island is occupied by Army 2, and there is a bridge connecting the island to the mainland through which Army 2 could retreat.
- Stage 1: Army 2 could choose to burn the bridge or not in the very beginning.
- Stage 2: Army 1 then could choose to attack the island or not.
- Stage 3: Army 2 could then choose to fight or retreat if the bridge was not burned, and has to fight if the bridge was burned.



First, consider the blue subgame. What is a subgame perfect equilibrium of the blue subgame?

Your Answer

Score

Explanation

☐ a) (Attack, Fight).

☒ b) (Attack, Retreat).



1.00

- ☐ c) (Not, Fight).
- ☐ d) (Not, Retreat).

Total

1.00 / 1.00

### Question Explanation

(b) is true.

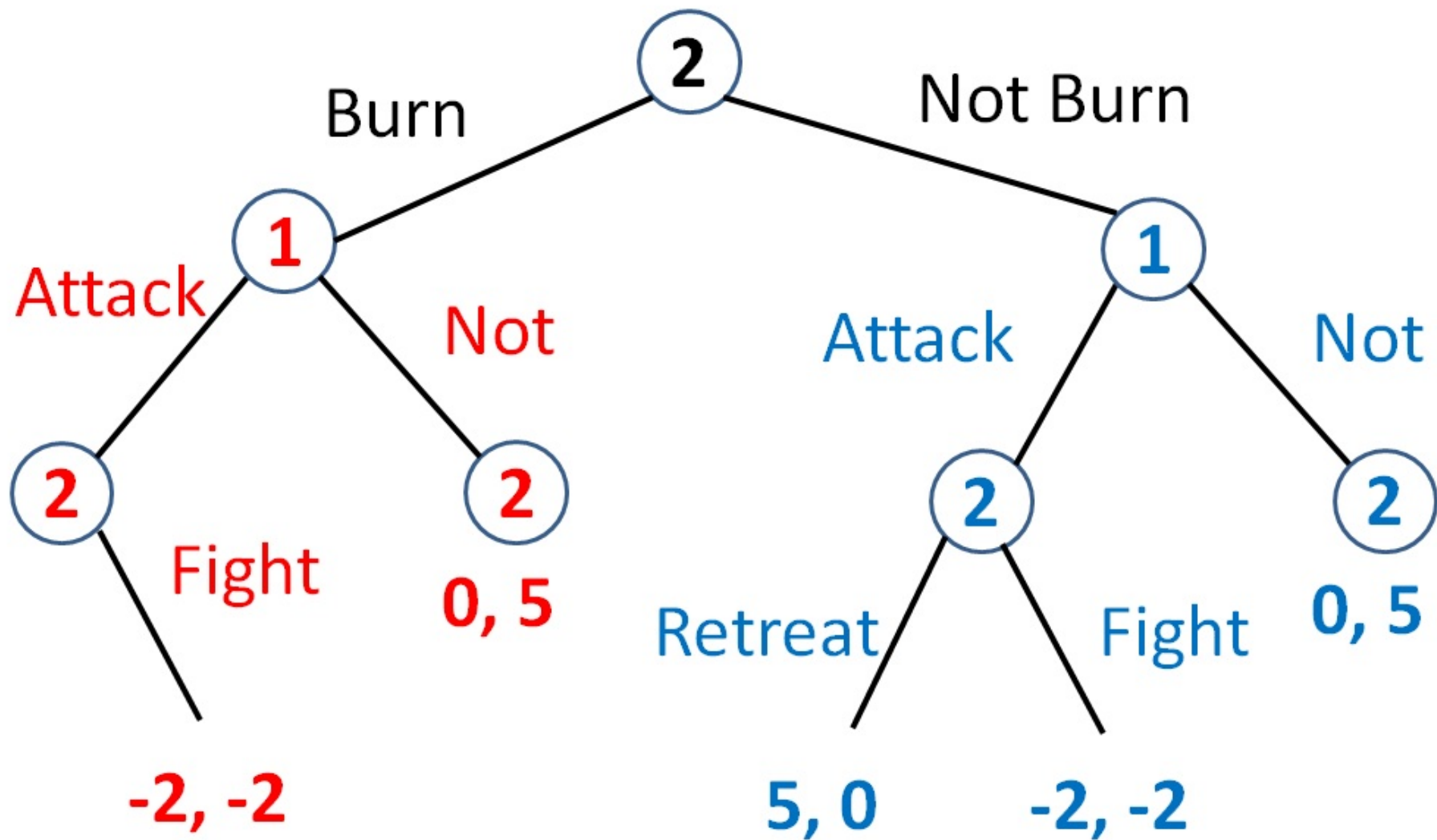
- At the subgame when 1 attacks, it is better for 2 to retreat with a payoff (5, 0).
- If 1 doesn't attack, the payoff is (0, 5).
- It is thus optimal for 1 to attack, and so (Attack, Retreat) is the unique subgame perfect equilibrium in this subgame.

## Question 7

### Burning the Bridge

- One island is occupied by Army 2, and there is a bridge connecting the island to the mainland through which Army 2 could retreat.
- Stage 1: Army 2 could choose to burn the bridge or not in the very beginning.
- Stage 2: Army 1 then could choose to attack the island or not.
- Stage 3: Army 2 could then choose to fight or retreat if the bridge was not burned, and has to fight if the bridge was burned.





What is the outcome of a subgame perfect equilibrium of the whole game?

Your Answer

Score

Explanation

☐ a) Bridge is burned, 1 attacks and 2 fights.

☒ b) Bridge is burned, 1 does not attack.



1.00

☐ c) Bridge is not burned, 1 attacks and 2 retreats.

☐ d) Bridge is not burned, 1 does not attack.

Total

1.00 / 1.00

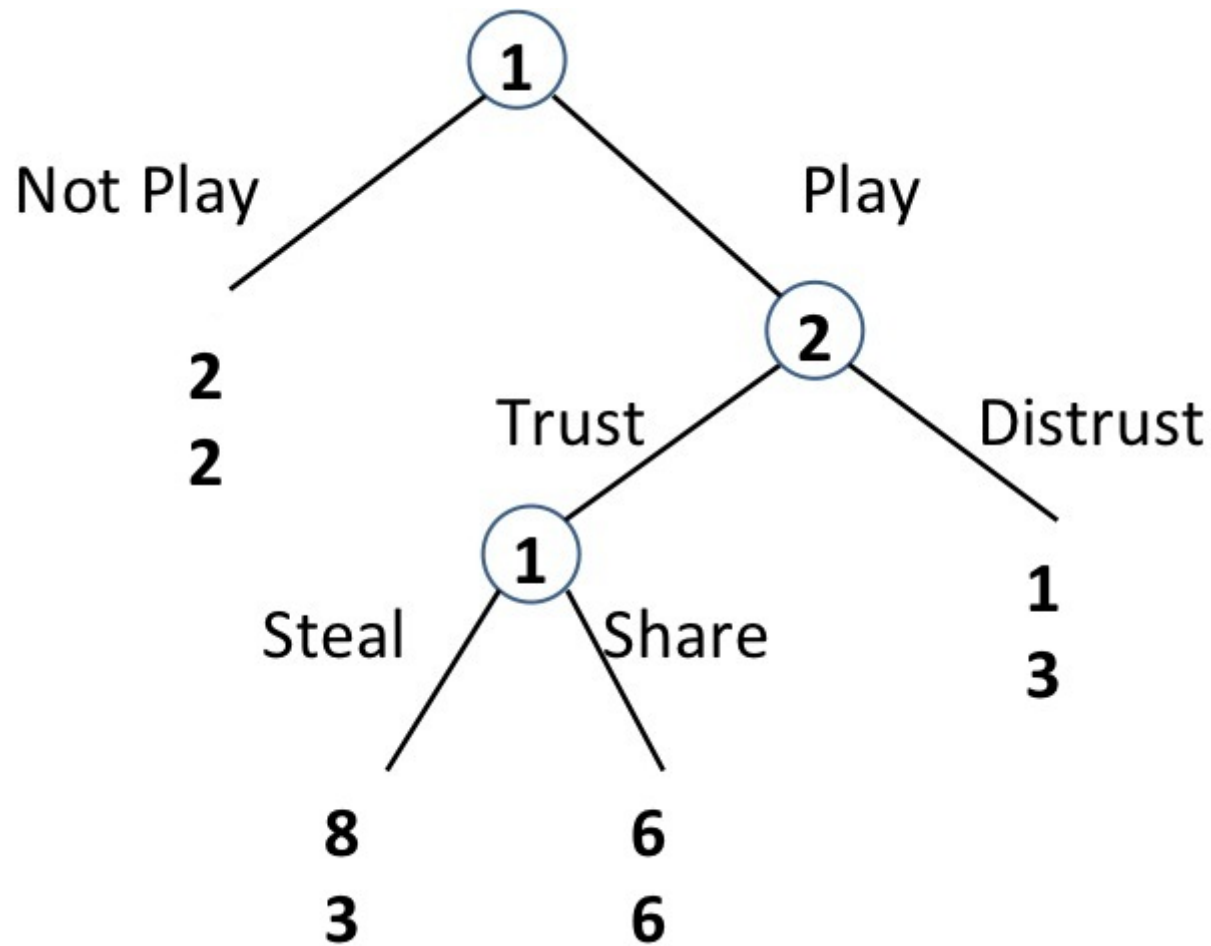
### Question Explanation

(b) is true.

- At the subgame when the bridge is not burned, the equilibrium outcome is (5, 0) from the previous question.
- If the bridge is burned:
  - If 1 attacks, 2 has to fight and gets (-2, -2);
  - If 1 doesn't attack, the payoff is (0, 5).
  - 1 is better off not attacking, with a payoff (0, 5).
- Thus, it is better for 2 to burn the bridge, which leads to (0, 5) instead of (5, 0).

## Question 8

### Repeated Trust Game



There is a probability  $p$  that the game continues next period and a probability  $(1 - p)$  that it ends. What is the threshold  $p^*$  such that when  $p \geq p^*$  ((Play,Share), (Trust)) is sustainable as a subgame perfect equilibrium by a grim trigger strategy, but when  $p < p^*$  ((Play,Share), (Trust)) can't be sustained as a subgame perfect equilibrium? [Here a trigger strategy is: player 1 playing Not play and player 2 playing Distrust forever after a deviation from ((Play,Share), (Trust)).]

Your Answer

Score

Explanation

☐ a) 1/2;

☒ b) 1/3;


1.00

☐ c)  $2/3$ ;

☐ d)  $1/4$ .

Total

1.00 / 1.00

### Question Explanation

(b) is true.

- In the infinitely repeated game supporting ((Play,Share), (Trust)):
  - Suppose player 2 uses the grim trigger strategy: start playing Trust and play Distrust forever after a deviation from ((Play,Share), (Trust)).
  - If player 1 deviates and plays (Play, Steal), player 1 earns  $8 - 6 = 2$  more in the current period, but loses 4 from all following periods, which is  $4p/(1 - p)$  in total.
  - Thus in order to support ((Play,Share), (Trust)), the threshold is  $2 = 4p/(1 - p)$ , which is  $p = 1/3$ .
  - Note that given player 1's strategy, player 2 has no incentive to deviate for any value of  $p$ .

## Question 9

### Friend or Foe

- There are two players.
- The payoffs to player 2 depend on whether 2 is a friendly player (with probability  $p$ ) or a foe (with probability  $1 - p$ ).
- Player 2 knows if he/she is a friend or a foe, but player 1 doesn't know.

See the following payoff matrices for details.

<b>Friend</b>	Left	Right
Left	3,1	0,0
Right	2,1	1,0

with probability  $p$

<b>Foe</b>	Left	Right
Left	3,0	0,1
Right	2,0	1,1

with probability  $1 - p$

When  $p = 1/4$ , which is a pure strategy Bayesian equilibrium: (1's strategy; 2's type - 2's strategy)

Your Answer	Score	Explanation
<input type="radio"/> a) (Left ; Friend - Left, Foe - Right);		
<input checked="" type="radio"/> b) (Right ; Friend - Left, Foe - Right);	✓ 1.00	
<input type="radio"/> c) (Left ; Friend - Left, Foe - Left);		
<input type="radio"/> d) (Right ; Friend - Right, Foe - Right);		
Total	1.00 / 1.00	

### Question Explanation

(b) is true.

- For player 2, Left is strictly dominant when a friend and Right when a foe. Thus, that must be 2's strategy in any equilibrium.
- Conditional on 2's strategy, 1 gets an expected payoff of  $3p = 3/4$  when choosing Left and  $2p + (1 - p) = 5/4$  when choosing Right. Thus, 1's best response is to play Right.
- It is easy to check that in any of the remaining options, at least one player has an incentive to deviate.

## Question 10

## Entry Game

Player 1 is a company choosing whether to enter a market or stay out;

- If 1 stays out, the payoff to both players is (0, 3).

Player 2 is already in the market and chooses (simultaneously) whether to fight player 1 if there is entry

- The payoffs to player 2 depend on whether 2 is a normal player (with prob  $1 - p$ ) or an aggressive player (with prob  $p$ ).

See the following payoff matrices for details.

Aggressive	Fight	Not
Enter	-1,2	1,-2
Out	0,3	0,3

with probability  $p$

Normal	Fight	Not
Enter	-1,0	1,2
Out	0,3	0,3

with probability  $1 - p$

Player 2 knows if he/she is normal or aggressive, and player 1 doesn't know. Which is true (there may be zero, one or more):

Your Answer	Score	Explanation
<input checked="" type="checkbox"/> a) When $p > 1/2$ , it is a Bayesian equilibrium for 1 to stay out, 2 to fight when aggressive and not when normal;	✓ 0.25	
<input checked="" type="checkbox"/> b) When $p = 1/2$ , it is a Bayesian equilibrium for 1 to stay out, 2 to fight when aggressive and not when normal;	✓ 0.25	
<input checked="" type="checkbox"/> c) When $p = 1/2$ , it is a Bayesian equilibrium for 1 to enter, 2 to fight when aggressive and not when normal;	✓ 0.25	
<input checked="" type="checkbox"/> d) When $p < 1/2$ , it is a Bayesian equilibrium for 1 to enter, 2 to fight when aggressive and not when normal.	✓ 0.25	

Total

1.00 / 1.00

**Question Explanation**

All are true.

- When 1 enters, it is optimal for the aggressive type to fight and for the normal type not to fight; and those actions don't matter when 1 stays out.
- Conditional on 2's strategy, it is optimal for 1 to enter when  $p < 1/2$ , it is optimal for 1 to stay out when  $p > 1/2$  and it is indifferent for 1 to enter or to stay out when  $p = 1/2$ .