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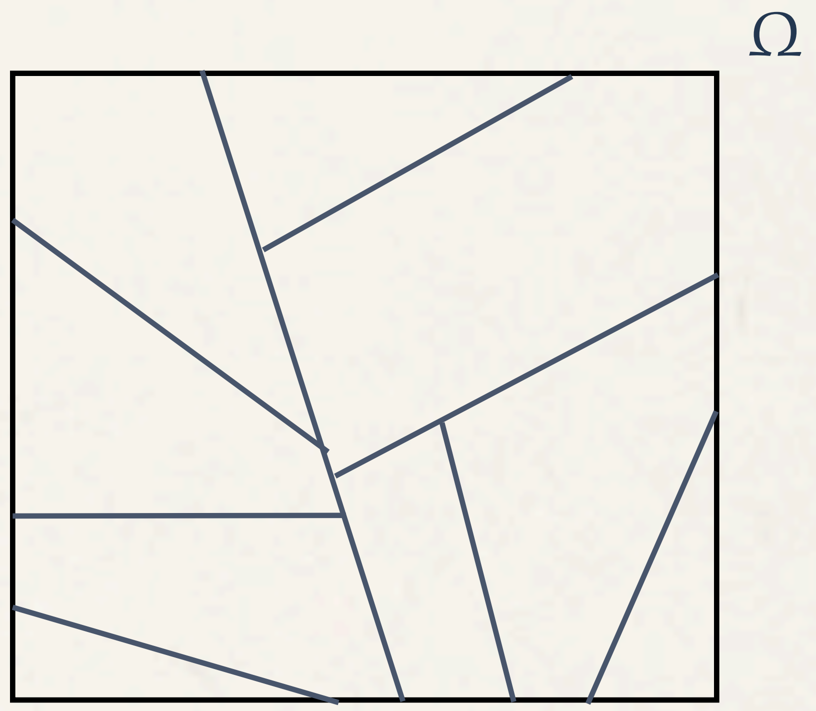

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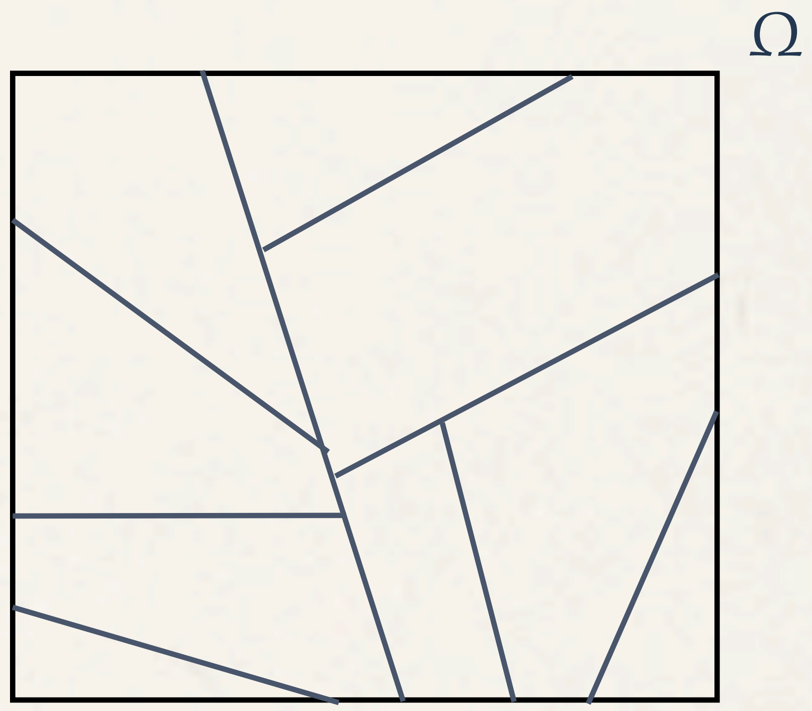

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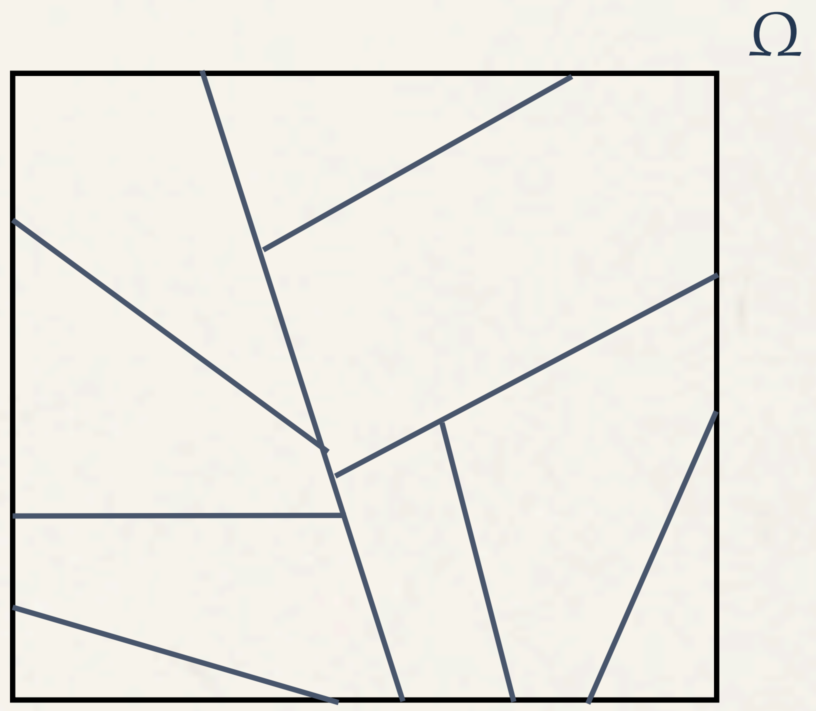

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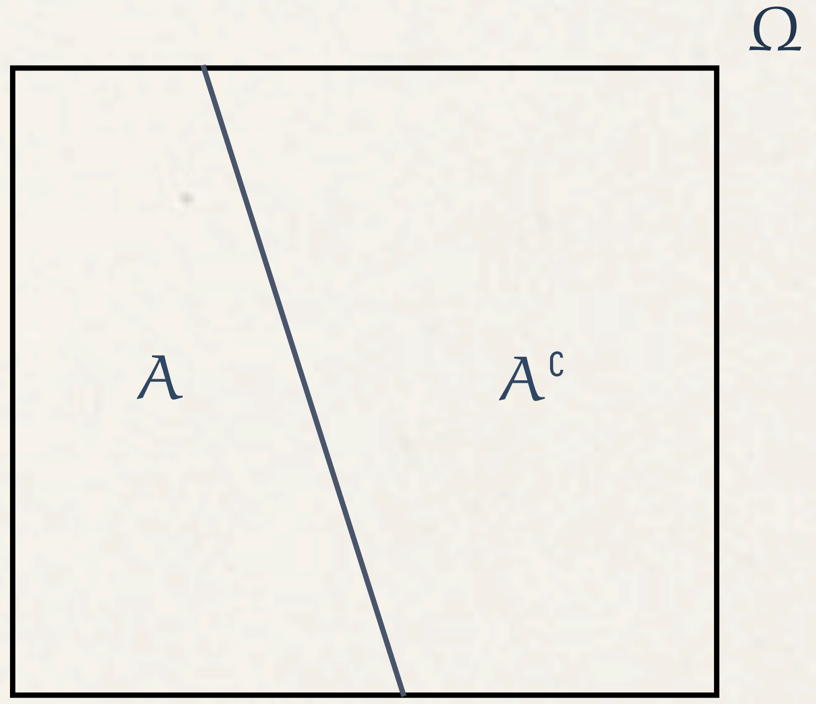

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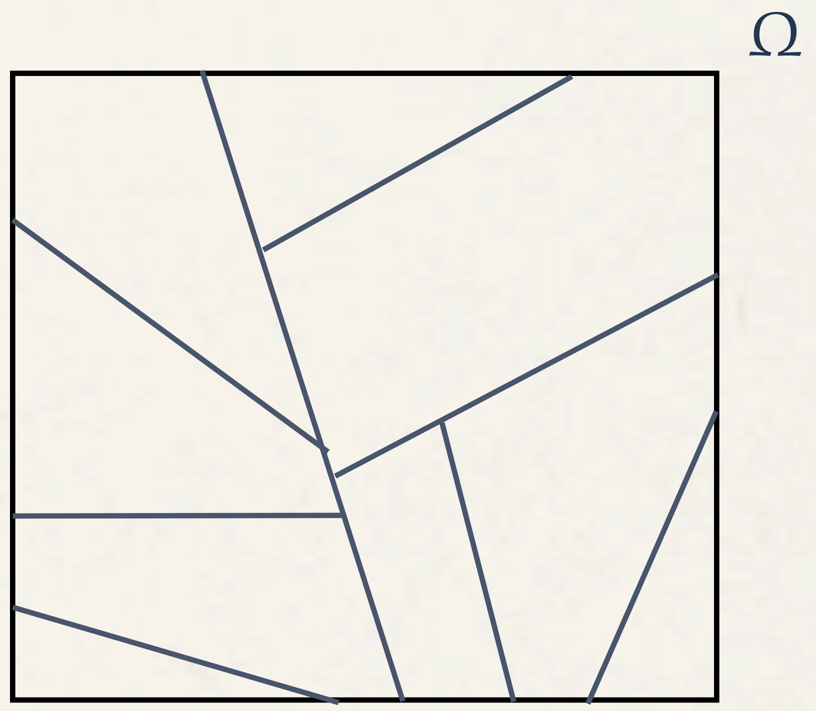

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$$\mathbf{P}(A) + \mathbf{P}(A^c) = 1$$