Exploring Ensemble Methods

In this homework we will explore the use of boosting. For this assignment, we will use the pre-implemented gradient boosted trees in Graphlab-Create. You will:

- Use SFrames to do some feature engineering.
- Train a boosted ensemble of decision-trees (gradient boosted trees) on the lending club dataset.
- Predict whether a loan will default along with prediction probabilities (on a validation set).
- Evaluate the trained model and compare it with a baseline.
- Find the most positive and negative loans using the learned model.
- Explore how the number of trees influences classification performance.

If you are doing the assignment with IPython Notebook

An IPython Notebook has been provided below to you for this assignment. This notebook contains the instructions, quiz questions and partially-completed code for you to use as well as some cells to test your code.

Make sure that you are using GraphLab Create 1.8.3. See this post

(https://eventing.coursera.org/api/redirectStrict/pmf4Le_bw5HPNFOM04g2A3qV4ODldj2mWRS7FEC4-rghpvpUue_IErFwRbxK27JPKhoR_gJYKOHot7VTV7LsBQ.2W49FiHYbIE9U5lbiBwh8g.hB7ysJTJu2SxKTwyTJ1XhsbiOUGrdcbD5zrYmRbhfiZurKkoKzmCVUE4uf_WUie6dSgdtFbaqNLfOKNLcHI8VC7aaOAJGqRzkcKxrrfOww0yOX9703pbYi8obOasFsK1OB8fZbxEMzTvsmoa_h7lXF1YVISTjtnEElp8hVcpFyAy-

 $PKBl8ngBO3uSdLVZsZdtd1yDuoHAtXOg93BbOIr4LebbkFab53pStKkmKtHqcOSXeleLKVmgoRKfKiSNTpmKzU_kdvfnyNEfg5Wn4KzkN9ysnyK0HWH8_5xcXASpY8sBu-kdvfnyNEfg5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNEfg5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn4KzkN9ysnyK0HW8_5xcXASpY8sBu-kdvfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5XyfnyNeffy5Wn5X$

VNIFUuElyFD4TjSejx5VZOeoUa9FxU8YWvDwSHbrFrsf2WaApVGWpq01iJak8EfHFwSNJel0pu0ENSPeZDHp56s2OqKhqSysfTkyveapsplfUqWkwD899nWvdC1HEAYNc-

rkGHv_YMxSkPBl6eS06n5n0VCJI07b4bH9MvCXj_IErlHue5YG5ogTMqZyfUQBQ1eWcbRzCcZWi6q5) for installing the correct version of GraphLab Create.

What you need to download

If you are using GraphLab Create:

- Download the Lending club data In SFrame format: lending-club-data.gl.zip
 (https://eventing.coursera.org/api/redirectStrict/WRCiYUhBGvNgH46_JNyjDQtU0JD_h2He89WyJPjVnz3Q9a909_K
 ePbvRGblOhqZHfA_yByImND97TgyZcEpvxQ.56iyytmnHq5a1o8_MyWS3w.iFfaEImfPDEJ347_DSaj_ Xucq42BuNSUzk9hdefd5Tg_1v_4M-
 - U7qZyh_MJlvYHG2YcBxnY1AFBRux4W9t5f2YDOOC3BVacgl1fbRq4R3xC3k29sa0Ef8QIwpPYjUi2OShbtifnSuv61jcO 5GqLoxj_9aNRI-_1AxvFsiCs1UuFEv4H1DtZQITFBAFa7jti_thGLUb9ukvlMKqmeu9KAK6q7FlvFp_L0zewDQE8-6hSqj_M8-
 - $qQxZHyvHM7JxnRudEAVeiNO0FlTQyU_FattZs7Q41iGZBtyfkdUEzxpamhlNlsUwqmAl464qShywi97XrOtsKZuVD4Fn2a4MhUc1a_qWytgF9cw71SxqACx3lWCuZM2RbmMarLokxSpRrCrXlyJQln9slta8hDpnullg1JnZWkPqADPvU8AF4hhuc3-M6eAqlEObPR9j49pqQN)$
- Download the companion IPython Notebook: module-8-boosting-assignment-1-blank.ipynb
 (https://eventing.coursera.org/api/redirectStrict/FMtpnMlK71jJ8ajcZit_1P36m1z4fogstqT rS7qpRzRTKbqqPeiiBG2Alx6WmRRbKL5xJKNSkthg63GlzrBYA.A17WkPjE1IYAPZaidcvseA.YZxiNoVINijkmUE0Jknrxl xn5fsTYqmaX1sqOTiivCTtQQmS54LTZ3Bw7MeL-MQJkrxmCZXBZZdr12QFd4tpauwH2kbqUQEWBUnjA2J3-

NZboUezFnH6ySqA0B7xkmRkYAni4mQ9F799JE2qzO1H-F9ZT7ywHznHcl08viALYQ8hSDlUv5APamvtdyYDK018zGNdC-l6JjlVMrBJyMxAJcNJjhjxlePvfm34uMQbSL2W-U0vTJ3BlhniU19xpovSu-7U08z830yyWUweLYWpStv7RC8bPRFB30zA_QMTXf6McCdJxiz4cYLWiYv3zqDSHNKdhLu4qbWg7BH-1_JTik34iPOg4_kqjmPtF450zflS7b1rZhTlVj2omn1bL-tdAjOaL8qRRwYw7A7bqUrrPPsA3P_jMVMVooRxeo1tUQS2E4hmiN8ug9X1s8DtAljN77Rkh72TG-D6_DAcWknpjzER6UHVOGarr0BmZSY0w2uyBJqQwPlvt51BcP32O1)

- Save both of these files in the same directory (where you are calling IPython notebook from) and unzip the data file.
- Follow the instructions contained in the IPython notebook.

If you are not using GraphLab Create

- If you are using SFrame, download the LendingClub dataset in SFrame format: lending-club-data.gl.zip
 (https://eventing.coursera.org/api/redirectStrict/WRCiYUhBGvNgH46_JNyjDQtU0JD_h2He89WyJPjVnz3Q9a909_K
 ePbvRGbIOhqZHfA_yByImND97TgyZcEpvxQ.56iyytmnHq5a108_MyWS3w.iFfaEImfPDEJ347_DSaj_ Xucq42BuNSUzk9hdefd5Tg_1v_4M-
 - U7qZyh_MJlvYHG2YcBxnY1AFBRux4W9t5f2YDOOC3BVacgl1fbRq4R3xC3k29sa0Ef8QlwpPYjUi2OShbtifnSuv61jcO 5GqLoxj_9aNRI-_1AxvFsiCs1UuFEv4H1DtZQlTFBAFa7jti_thGLUb9ukvlMKqmeu9KAK6q7FlvFp_L0zewDQE8-6hSqj_M8-
 - $qQxZHyvHM7JxnRudEAVeiNO0FITQyU_FattZs7Q41iGZBtyfkdUEzxpamhlNIsUwqmAl464qShywi97XrOtsKZuVD4Fn2a4MhUc1a_qWytgF9cw71SxqACx3lWCuZM2RbmMarLokxSpRrCrXlyJQIn9sIta8hDpnullg1JnZWkPqADPvU8AF4hhuc3-M6eAqlEObPR9j49pqQN)$
- If you are using a different package, download the LendingClub dataset in CSV format: lending-club-data.csv.zip (https://eventing.coursera.org/api/redirectStrict/tbLhdjZ-
 - $6hinvcCQyf991Ns2z6bs]ht75VUJqyONSJ0PJpLo2A8thQe_JSjF5Yt3kz3BnwdFOO6pnN3Zfbg_Zw.RR0UcryKlusfAHZihgl7IQ.hBuBUB08mKU6qOP6GIMDN7be5wHBllIJJ3UNrluVNcm2e4rxLj3x9JTli2EgNzbdKBA5ZLdWGSJnmGW3KTB_XNOBCtb1WWOXspnm4zf2BzfZdg3UzeNLvJOAC0rbzDHVBP6dnO0KKL_mNQ03W-$
 - eELL21|n4ddgK3sFX4uX3mwlmyhAs76sutA5aw2uP-
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 - $i TovWtdZUvkdcosVm7TmNRdMPelKARnWBcoh1cZxMBt1SxF7FiK1jNlwFLq1yllRljkDNhxu_ybOf3EZiXeLGE3GRTuobclwLWDjRuyq3)\\$

If you are using GraphLab Create and the companion IPython Notebook

Open the companion IPython notebook and follow the instructions in the notebook.

If you are using other tools

This section is designed for people using tools other than GraphLab Create. Even though some instructions are specific to scikit-learn, most part of the assignment should be applicable to other tools as well. However, we highly suggest you use SFrame (https://eventing.coursera.org/api/redirectStrict/Z0S34a_FJO-XKmgcE1euLCyM2-j8QJDWPWDZOXc2GseL6XR9FPEZIYVPNpdd88oaOH67CN-wgEeJolp9ptw7wQ.SNHM-pzcvaeWyloVeChdlQ.Bcy64aM1qUacvZz-Wmud5e-n83jXXHcPRVbfBbZByRAOlufvWLNMWTt-Jv63d_OxRqjP0YogoJMeUvMxBocrVu3TXYgyBPozV6hsYu1WCkJAgrfbVqfF8xzwwly3xctlYlH9ftPpdHXiDuGPoVV1wL7x r1Zj7vEJB7ZAoGN77NsZGflVDPzfxQHkbXPlnguGjxDjeUtWmwNgyQY2mrnJ5YoY_Pf9k-zxYdcWN_dB_diGUiTXfhrU8cYlwo_rybw5HU6QOJX8Qa4q0AmydkP41Ptkqn1Gq93ld-Jw93Ns1rvfPjlBn7qBBX6tnQlWZmcv) since it is open source. In this part of the assignment, we describe general instructions, however we will tailor the instructions for SFrame and scikit-learn.

• If you choose to use SFrame and scikit-learn, you should be able to follow the instructions here and complete the assessment. All code samples given here will be applicable to SFrame and scikit-learn.

 You are free to experiment with any tool of your choice, but some many not produce correct numbers for the quiz questions.

Load the Lending Club dataset

We will be using a dataset from the LendingClub

(https://eventing.coursera.org/api/redirectStrict/3qCgZHTgoJmaj8lpr6bUXXXMpLrq9jGsUapXbLWOyOq9tJuwlFkUtXtFsidEsGVRBOpAaw59yO2S7H3aqciSRA.HlJbUsBYXIvvgCKyOkaZwg.NgcxJFf2xgw6jDsQHsVy94Gn3zBAW1HipOV4Pf-RvYpn5XpwJ5-1iePCpNYPPzGhuNKcGPO-

 $0n2TXPjuRjIKQ_v0mo3u9DedbrlaWQsZWSyumnZ753dc4Sp_dnHDXhgKKuqWx7E4yBY-Mxw1BteQ4Ydv5JAg4Ok-IIAj0zuR9Ow_s-ahh26gfPvBhYfnrfmfTSF3rfYidrS3ctn-left for the control of the contr$

 $ieVFV8P8ASxzmBeB1Wlzkdq7OZGIR0LX9rrRoaT_QPZObxRK6Pe5_EZx0qKCpiiQx_iMSlzqrOdXCIGeUURO0l49iKz9yLS\\ eY6h-RRAA8dQB2MoCOH3qi0K8naZjTJdQRxdwUWkcYtl2wzrU5cc6PXZDZHPrGGm1HXpva2uH59qfY_3B-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlEdu4qm6UDZBcX3CxMN6ylCZ-aMbT3EgozCGS4ymWgiGNhX85xw8aR9-p6KlpawrfHrx4XymjT5ntEfv3Twm6bZHMlAgymbQfyAdy$

rKJvzHu_BM_6PMGbIQXoIKgb9AsbyfY9SjMtZY6VLumcZwqQ3Y_QHdvloCmw-6gjL-

urMHQs74yQnSWniXAHrNKyc6lYgvLvDilSvsrH58L9-

zmMgdulTefurn7g413mO_DH2bXV-

UGyLN1K7bRdNbwLxwUc8jCFnTqyb9oZrCyu2JMrMKyXmeKekEvZR1TlL4e1RSWg_qr20jDlwjbzHXDLVP3W4dtJ5OgPe F-

maHGlADbrVwxpanFWavPOBCrCT8H_YL1vpLQwErhQrrNV0Pr0_xhrB9HCal6X8GsfHzkWvVXXaFS7WO_R_Emr0Q2ET cvdlVB067QHNAOH2PQML9Be6T3YSMupYwY6zeHES5xjuCA7ZYhpNhvhTd6G22GefW0CeoKvs4Kz9pRvAMoNJeQX0 1TdvFAkbxSkHD14a6yXWO_Bsock1jzR5iKNdyRL3etp82SgcuTTHfsNK7U1_2k0YDrSV-j-

EJ0apWdmNXIOcwm9TvpzuBFwyXjDbb3AiqcqVIOJFTlko1_0qIIG-

KVTGo6wtfDF7lzTap3WxUbbbla1A7MtgLmdg2zhqV-

zs73IdI1RPgx_GSPIJ3XMxkfShyxW8nOSpFMLGp6ujiARh5iJq8DgfXXpr6g56-

5GYMdn_HHBBJN0ZoVsk7A1C4QkGNdTdTgN3ynvdiwJE_uAWie3jjLp5VD-S9lw_AN-Zwx9BDWLoiDw-

kZDIPoOPN5TwaBLo8uO5E4TaLJ5AT2bi-x-afRSDcuQlmka7klgkh-LPwiqSPzJ7-

 $Vsee Uqd7xrVKJo2uDJlzrnj0cZTquqObdR0F3oFCSQWIVDZvtt-vvzvoXOrC5IPDL23vkoPhglZXgUi3qOxfnFhD32sCi9He-Pob03ws1_fA). \\$

1. Load the dataset into a data frame named loans. Using SFrame, this would look like

```
import sframe
loans = sframe.SFrame('lending-club-data.gl/')
```

Note: To install SFrame (without installing GraphLab Create), run

```
pip install sframe
```

Exploring some features

2. Let's quickly explore what the dataset looks like. First, print out the column names to see what features we have in this dataset. On SFrame, you can run this code:

```
loans.column names()
```

Here, we should see that we have some feature columns that have to do with grade of the loan, annual income, home ownership status, etc.

Modifying the target column

The target column (label column) of the dataset that we are interested in is called bad_loans. In this column 1means a risky (bad) loan 0 means a safe loan.

In order to make this more intuitive and consistent with the lectures, we reassign the target to be:

- +1 as a safe loan
- -1 as a risky (bad) loan
- 3. We put this in a new column called **safe_loans**.

```
# safe_loans = 1 => safe
# safe_loans = -1 => risky
loans['safe_loans'] = loans['bad_loans'].apply(lambda x : +1 if x==0 else -1)
loans = loans.remove_column('bad_loans')
```

Selecting features

In this assignment, we will be using a subset of features (categorical and numeric). The features we will be using are **described in the code comments** below. If you are a finance geek, the LendingClub (https://eventing.coursera.org/api/redirectStrict/J7uVG5-

iylFP5WF_xcRXrMexUbY0uhfzIjN7FUPoCYH7QWVp1OWZkQra4Z4F6sRnKl13OnNy4-

 $\label{thm:continuity} Zpl11hCTpUnA.zMOaD0m7U4hWEwYDBU2lPw.DPohASZT67qTDBqTasrg5WNnMSdbpmR3gSioObnPahskUOGCogmjDM2wQr1ds5U-lyRRjpHMxv0BMhrKe8o2qZJURl7zL8Dkw4KfEjankUxphycerTzTCMPJDWwWAWpduWQZUGEjJW4-iiNJQJAJawYYl4mEy5FelHvipXYRLpmCaXT6K9tLbT-$

oZCqlM9yU6I_VQVN7Zqqhihe0w7J1tYZK9U2DH9FCuzmsJO4Z32KVYKBRX4-

9mpZcEn403CB2qSE3SErPSaOjj117HK329GeuOQS0CKVOalz6m5C-Yj4) website has a lot more details about these features.

4. The features we will be using are described in the code comments below. Extract these feature columns and target column from the dataset. We will only use these features.

Skipping observations with missing values

Recall from the lectures that one common approach to coping with missing values is to **skip** observations that contain missing values.

5. Using SFrame, we run the following code to do so:

```
loans, loans_with_na = loans[[target] + features].dropna_split()

# Count the number of rows with missing data
num_rows_with_na = loans_with_na.num_rows()
num_rows = loans.num_rows()
print 'Dropping %s observations; keeping %s ' % (num_rows_with_na, num_rows)
```

In Pandas, we'd run

```
loans = loans[[target] + features].dropna()
```

Your tool may provide a function to skip observations with missing values. Consult appropriate manuals.

Fortunately, as you should find, there are not too many missing values. We are retaining most of the data.

Notes to people using other tools

If you are using SFrame, proceed to the section "Make sure the classes are balanced".

If you are NOT using SFrame, download the list of indices for the training and validation sets: module-8-

assignment-1-train-idx.json (https://eventing.coursera.org/api/redirectStrict/O-

4FS_HAoN7Vu8fB82pYkxSbfzgrJMc8fzgPld1ayi_tW62e1koLUt5YRRagjLzNfYBLCtQM0OpEEPHNS-0tjg.6YxZHz15T-Oc39QLQkgLSA.PW5PoTISGnQkWSMF3NBdORXbsUNn06_rRr-

 $C3b8JoO78w3SYkKSVtKdOEyECoG7th78VUCiLO9SYRppnkyfur9T2Ubd2kL9enMYN4kzXnR_VfNPHB_mSIPJLy5RcttyPm0AKF24u-0LWksJxJTfY_Rw4E8iH7fdTqlc5n9dDkeGK_2J_7mxX2hvDDEgCed4JUWDPo_0-$

 $y8EzaaEyfF7oWGAlo_LG2qOVUl5xSGn9RKmff5IU_q8yRW1P3T9NxGgH6eRnWu4b2iBZqUn2BWgUp7GZBnLjh0xcCttx\\ RmEGN0ZrOzHbzaZG_lu-$

BIMV6lcsEW4iDVmFkTsm3xbdH90QMQ0lrAuqAmguMJXsPDHlyWe_3tyGrStTGYdklBvBwi6XxOKdJBjmKX3AYIDGAQjx MoleAaawYWEwrguRMn6GrcFS0l0KsSeSTtRv-YYtl8LZ-

KnFD9_lsfoYigBVVtQAA_ZZOLPUWAoSn9hih4xUgbguFHQKiRze6pW_E_E7zY6L), module-8-assignment-1-validation-idx.json (https://eventing.coursera.org/api/redirectStrict/EMWR77UTpb56MnjnWSeepwQDPp-

iDWKQUpURomh9vQc0cysCOEMz_DmUflOOl9_Ukmf07hiKDGMfYu3m4PQUFg.KWABAU5-

NPDoG9wzHwt4HA.pfe6joM7jbftJ7RMwMjI2u-

IPo76U9cX0nvSIFJXnP851on7o9FbJ57GqblaNHZ9yrwZYlrmeQ5S4fpPTKy08EZ-

zSzb461OMDajreHL8UdoXvRGWYtuxmSrXgnQ2gj0oC3Xg92yZTOuRYnzSCHrfxU8lqp2l8lLmb-ifisM-

Yzvkx6GJtTKWXBxmk7BnkEBrMcy80rqvE6dwJUKy4_-P_tiJ1tG456EBJsrFN3jVZFgILa3afwrPiqsuruipS-GO-

iNA2nNBjxlOGUGsVKCVCBl37OZLOvDpBpe1wbX-

 $RPyAAzaGFK2gCvpX0tcQ1APN3u4h2bY1EEum9G4mUXIzYD5d3QF9TxuXVhDd0VdvKI051zcRFSoRBoPi9CNZzL61u_L0XLL35MOOEkKHW462xpKhiwTouF9tGh-\\$

XcmD5BAzwN0fNujpqAYTtM3_2byYDCQjJ9NH_p6Ie8OfP4HDoVQwC5Yd6TWolQwqwOO1n1-

cd3CodDYCXF9EiFkrh7Xy6dFAHB7vW2OHTkzYPnQFcQ). Then follow the following steps:

- Apply one-hot encoding to **loans**. Your tool may have a function for one-hot encoding. Alternatively, see #7 for implementation hints.
- Load the JSON files into the lists train_idx and validation_idx.
- Perform train/validation split using train_idx and validation_idx. In Pandas, for instance:

```
train_data = loans.iloc[train_idx]
validation_data = loans.iloc[validation_idx]
```

IMPORTANT: If you are using a programming language with 1-based indexing (e.g. R, Matlab), make sure to increment all indices by 1.

Note. Some elements in loans are included neither in **train_data** nor **validation_data**. This is to perform sampling to achieve class balance.

Now proceed to the section "Gradient boosted tree classifier", skipping three sections below.

Make sure the classes are balanced

6. We saw in an earlier assignment that this dataset is also imbalanced. We will undersample the larger class (safe loans) in order to balance out our dataset. We used seed=1 to make sure everyone gets the same results.

```
safe_loans_raw = loans[loans[target] == 1]
risky_loans_raw = loans[loans[target] == -1]

# Undersample the safe loans.
percentage = len(risky_loans_raw)/float(len(safe_loans_raw))
safe_loans = safe_loans_raw.sample(percentage, seed = 1)
risky_loans = risky_loans_raw
loans_data = risky_loans.append(safe_loans)

print "Percentage of safe loans :", len(safe_loans) / float(len(loans_data))
print "Percentage of risky loans :", len(risky_loans) / float(len(loans_data))
print "Total number of loans in our new dataset :", len(loans_data)
```

Note: There are many approaches for dealing with imbalanced data, including some where we modify the learning algorithm. These approaches are beyond the scope of this course, but some of them are reviewed in this paper (https://eventing.coursera.org/api/redirectStrict/Mdh1pnOSNRunP_W6QXfPwNfpr1ppPHnjMbafV4Klq2a-dPALdcsTA4s8Him3YEfuJjuNg7f533Oey2p1HObThQ.NkrFkwOykVnFeGlr_C8YoQ.8aTUh8RL7nuqmbV6IPDBQfy7WZlO16zQCZ4dQnE_h-rHVSE9RHxoULqy4f1v7u9wmDRUKdTesYteRrUFB1nUy8499q-YlUyg0DDc7c4kaJ9J-nptC85r0mN45b8vES9NCoj8uJcOTKNImjB2TXnDGfgs0mP9tixz9LmrQVA8eh9NBVnz9WxCxmtCwOmofLh_e4So-C7faWCl91stUJGwUuhkDSU6BJjJdFTSHdxzflpLpqkc1gfvr18Z1cAaGRB4HBZxaoBByxGEO17aY_p44KcF-zR9saM9rtkpNRlkKrOzmHvzPhN3rj4x1p_ZxuCFYUWnSTCyV_f7lj0MH2JQlL9J3SpVqHkwJNeenfy-LnXWjFrZbfwcfvjo4cl4DDjNtOGj7gFxUHOEQ5k-

2Nooul9fs8F1aVjprwlYAd1RP1CHCobwnPQiZORaLi7ao5N5qQbKhcSb39thHhLl4t5o-

iaPSGJ3QgHoo7R1To0loHf2GAKCJJy7_8rs_aC47JbHkQNUzShXmaX2pbbdrK9D_ZBwhARkFXzbvQCZTo_g2fA9588K34K qw0_Cn4U1pk1T5kcrzgkNWzhH4DuwA6AMZME08gM1mhJ7U3azRwm68WhcsUMoczDm3XQqlGzD4Wab). For this assignment, we use the simplest possible approach, where we subsample the overly represented class to get a more balanced dataset. In general, and especially when the data is highly imbalanced, we recommend using more advanced methods.

One-hot encoding¶ (https://eventing.coursera.org/api/redirectStrict/La7UXGqktRNf2pRTG2nvpXSP-KT9GF_krVRyCxUwN_z6gQV5vvx2L_IQ1UU_BU8UGP7xvQIE06j5Ak3DO7tQtQ.WXu4KiZQMCLhtuz95M kx5g.wyRLq8eTqBcoLlW94g_OtUxO8xv5BAwOf01Xd8KqtMU7VMME7ZIziwbD2ojdKdF7_pobC2zrN0j8 SMJHH1oPVoph5sagt4RxXyBSdUvw_K16yH5j4hoRQ6XB2bd0UWwOZN9ol05w87lRRvVktTAFkiCutTd3I EfWhNraZ3-

qUqB7aXGmi8aiTz8KD3xDGtDYK1XPTzgrjyt6W5GwxZucgy3R8BFQap1Y53JSomCKbwH96pmgLBAh29 RAPstiFfPKVZB0LWPcRoLmQxct3xhTjAjm_KfZzAmELFw31_cuUkvBee8RUg1WCXIwFbt0FYGZumydl29 MdOW2rnJSZcODyt4zOvrsAXV_SVePOgUO9nZkggwv6B5YIFol9AzFafoQyARiu1YfXyAExKl2omCzt3ypCl swsSniL85770xVqGt8JN3y2a1DObglUyHQMmI-

UqBkKhG1Cgya3cQqoPk7Fpt1yqD1wXQJMoRFFcAK1vxGwQFo2ggu2F3walKoU7Huj1UPCaEx1QQkMT_l1kcURXH9i2koEXZ3I4NNlCg8GFljyF7e4RR2blQPaK4Q2uGJ)

For scikit-learn's decision tree implementation, it numerical values for it's data matrix. This means you will have to turn categorical variables into binary features via one-hot encoding.

7. We've seen this same piece of code in earlier assignments. Again, feel free to use this piece of code as is. Refer to the API documentation for a deeper understanding.

```
loans_data = risky_loans.append(safe_loans)

categorical_variables = []
for feat_name, feat_type in zip(loans_data.column_names(), loans_data.column_types()):
    if feat_type == str:
        categorical_variables.append(feat_name)

for feature in categorical_variables:
    loans_data_one_hot_encoded = loans_data[feature].apply(lambda x: {x: 1})
    loans_data_unpacked = loans_data_one_hot_encoded.unpack(column_name_prefix=feature)

# Change None's to 0's
for column in loans_data_unpacked.column_names():
    loans_data_unpacked[column] = loans_data_unpacked[column].fillna(0)

loans_data.remove_column(feature)
    loans_data.add_columns(loans_data_unpacked)

loans_data.column_names()
```

Note that the column names are slightly different now, since we used one-hot encoding.

Split data into training and validation

8. We split the data into training data and validation data. We used seed=1 to make sure everyone gets the same results. We will use the validation data to help us select model parameters.

```
train_data, validation_data = loans_data.random_split(.8, seed=1)
```

Call the training and validation sets **train_data** and **validation_data**, respectively.

Gradient boosted tree classifier

Gradient boosted trees are a powerful variant of boosting methods; they have been used to win many Kaggle (https://eventing.coursera.org/api/redirectStrict/KnTrWD3xT74NGLQrJVlpkRAXvl7cvp_hA1ymmyZafS9BNwR1M7Pa ECc729sbtPtHuk92Nrcn7KNgoqvwuk 91w.nyWnwAl hKYPdUH55i-EiA.v9lkhG-fi97S7-

FsLhyq3b81z500WdChlaGzZGRiC69F1QvonnQ34MSlOlShyWBKEN957w9nVP_WY1rApvmsz3LlrFMPZTvLOt1nPhePX 0NFBpkopR9CRIHwiSK62J-

xcd34rOj8TusTCVIQOZ51rLOMQyBx_cJX9EwnHL9X4qAvXlt3oA0KWIWeUuaujvccuAsV8VywkpvNUvbj-VPX_O0xHDpV9ZBcben-sXXI5c2xb8_fuUbrZHwgr01CJZL4kxdRvstfk92enzAJuptSNg) competitions, and have been widely used in industry. We will explore the predictive power of multiple decision trees as opposed to a single decision tree.

Additional reading: If you are interested in gradient boosted trees, here is some additional reading material:

GraphLab Create user guide

(https://eventing.coursera.org/api/redirectStrict/hwMb6v9mB7J6HS03vflWOXJk8pPCfKX3YTAOW91Kp4iVJzFcMcTz3p9jRrclOJOMeeWzaCkL1k3i5Y1XPQgF5A.MUomUlxkedZLHejLYEwvfg.5xVWENYgK7K73vuVdb1mL26hH6if8W-6sLmCLQl9sJO-v8JepaN3cT2LNAiHpWCqNu3LnHQm5lQns5mCJ70a_zLq7HTZO0KbxEitcbW5Rw7iw6NK-y0Agv1aleqmqJL1HEL50FiuF7wutCIRlOWtNWPjBT4T4o8UQ-

ejXjqVnFlUrkuKjm1FVjfyxXFQLufaDNEBLuNWOuHFrTycEpTVBXGlKYR-

 $eUvSNDoyO1dgM9HTN6JvsHvwbi404V4DbZnm5lxm8m4mCWrL4LewxxMofjd1qM4YTb9_3qINcaZ8JeVAzT2BD_ICcAscxJIPgHK-DSJfor_vv7vOZuS3Fn3u3ORifdJgJCBldYFqjywh8Psf8iHruJYDgp4-iHPdJZ3FbHagQIrHOwmVt84391HX-i5SBHu6ws6oDmfh75lRyrc)$

Advanced material on boosted trees
 (https://eventing.coursera.org/api/redirectStrict/feHBWRc48j88z3OTMuKl5v7JH43tMXCZvdOlvQuy9u0Celtlo3A4d
 0UjL5sYuP_1qZKbp4uUbtV6UypqXBQm0g.6RStRGAXvRTBv_l9Kykc2g.HXlzwRvljdsLTfzv4OZlrk0FvgszNajy2vnWQX
 cC73dDFif_979YcOaSrlH2vc1PXKKu4Rb68x56-wqjl13f7K2o5jtFhhZ2qbyldG1_VHGcX5-_7iVtwReEQvY6b BEi8B_we506iGHUHcloF6RicQtz2iNlHehtnbmkpoHeG4bhj9LAm8bAgln3WKNfTBQDBGpy0ZYWE00JuMtsPnUrsS6
 TuHbg0c9ThNPBrEHpG0E623onXUQRLDSsEA4gxM59K2CRwvE11faxd39wFtyES_Z5iljmHpJF9RUSZK1OyKzczMyqZ
 5_xJuvkbDwZJC8q0MytHn8TUmED-CnV_Hya5zyg9DEFwo7BzoC0_k0v9c)

We will now train models to predict safe_loans using the features above. In this section, we will experiment with training an ensemble of 5 trees.

9. Now, let's use the built-in scikit learn gradient boosting classifier (sklearn.ensemble.GradientBoostingClassifier (https://eventing.coursera.org/api/redirectStrict/D5cZU3bCSBo7BpTbED5R6XcWoFFdVFEW_l2mRTxlgMtFq-6iu5o2GcqqhSze6v4rPtHkdd-0J6nKuS4vZaGh9Q.pPlbv1MxmYdLtuKu5DP-

gQ.LYQNNIHOumX0jTX84aqWlUjT5nU2HPlwB2EfDEqEM56lzSHAMbV8fvrH9ocxke7gtvNQjNmOfhkx3cswx2gtaz-mTsamBaobQJmwL6NUL_HKz3y4jymt42inTbpLf2YhFShvvwzVM3lZ6PhvW1gM1EKThknrGVEDIuoXFTTg1OkRqrTqSDM7aXUWrsrz94QEA98U4j6U-Jqf56fl1ZRO-8bWG-qZWRCuuyX1ptmXpqqfujqrHTx5Fe7n4zk29r-1uYtGl7MKRKZn-Jy8efdA9JcFH8j9yLJrW-yjwGxFENVxvcDYG0ElYOPp67sSM66yXllwwus7zckuYq6aLjySMM_fAG-

MdJGV8uN7ScZhBlZdiidkqKo6wKBviuJXFoK8vwft7sLUtpMwWIUJDEm3CBk_bfvwXic9ZYNN501BHznzGTAeA25RpHLY eiJ5loK4Wq-6DDlO5S_yLC-7mopPAQ)) to create a gradient boosted classifier on the training data. You will need to import **sklearn**, **sklearn.ensemble**, and **numpy**.

You will have to first convert the SFrame into a numpy data matrix. See the API

(https://eventing.coursera.org/api/redirectStrict/dicyMRtZPRh3iXS4lGbcp7KaptBlxwmxsvLTTLFTykqMZkv0lF9KZ6O2BcEP07wxu5f1R-

BgBGAgDOXGXIfSmw. ORxTGGIvL0EP5VbxIXTxBQ. s UYDAXNdQJu7bltYfPqDPgLuJ0vOczoWzggVOKwxwNoIEzuLfnUEiNtvHRbONv5YfLy14AaR3vfoQZyHcvFBm3dLZVSXIsdBT37yCZfKvJAswh1RLkUxFO1miu9hXN0YM1rznhEAa8b0kZTlhkh2jTtECELMD3b4nFS2pqp0jjVN-

u_JOTcvZex7PwmyxKrbqZQ5vugyCNtwhaGRC71vf6erwHj0LP0gA5rGenBgQZugQwybM8KQToKfn-5K46tPuWQ00vu5otdKGNSuJsfgez9Dke74WMNnwr61JtUoNsXzAr09BmsrsrZKgy6ozqEFou_WqnkflGGQFES36hSLb-SZOsB_1Nz93vsRwZw7JDbjjd1hwh_iONiClwlLVoSl9JRbpikCUYLqmjGyfxcaHtxTfVFOYTg3siP_uoFfmkoaVJUYLAewd04 pLUwlTMEg) for more information. You will also have to extract the label column. **Make sure to set max_depth=6 and n_estimators=5.**

Making predictions

Just like we did in previous sections, let us consider a few positive and negative examples **from the validation set**. We will do the following:

- Predict whether or not a loan is likely to default.
- Predict the probability with which the loan is likely to default.
- 10. First, let's grab 2 positive examples and 2 negative examples. In SFrame, that would be:

```
validation_safe_loans = validation_data[validation_data[target] == 1]
validation_risky_loans = validation_data[validation_data[target] == -1]

sample_validation_data_risky = validation_risky_loans[0:2]
sample_validation_data_safe = validation_safe_loans[0:2]

sample_validation_data = sample_validation_data_safe.append(sample_validation_data_risky)
sample_validation_data
```

11. For each row in the **sample_validation_data**, write code to make **model_5** predict whether or not the loan is classified as a **safe loan**. (Hint: if you are using scikit-learn, you can use the **.predict()**

(https://eventing.coursera.org/api/redirectStrict/JM0iMBL7lUDtbxgvuFtkUkWqiFuprji4eHSDaPVPUd746lOhAsjCAKM L19lt5Jrc0NQR9Ya85bUKTQFwmkHiqg.PVyNmvZpa5WyCq2aO_yLpA.TjxW_htmeeVaQBFYdBTAXhvlelgqb9EBjWenvE

5P5An6nlSOUZvkgGAWnAu1_bRtUwtvLo_ViXPWxRzoUV4GAC5zz7l2pewcDfUcX84Ni_k3gjDG59whuUWKfzL8qTAcmziu6cmB-kzZSD4UtuB3y9HU0el7_Wih-

PDTDwh9rAEPDTCXsWghV7luYaTJXUDjLeq066O36RMhSAxcyF1H0PSgTcocuflWW_5pT48ep1-

6ktv3fF47hi2ysP5wo0ZiQbdPvkSyie-DPY36LxBbS8UcdrJpxT2ich4tjxIDZ-

nuU_QvnW5y3AiBidkA42ucWaucBhC_LOOP6yN2iTN2sG988P0MPOVJKYEbHTfAHXGuSZyEI1SZ89hHUa-KzdYz-UH8E0hIT_dPlvigkW4u1vth97jnYQpvPeSxAtuhVhmFTBsvMlJIoHqHsNWGINOtz6gS8GSnj5HXu5qb344LT2j4-zNrYTyhMty7xRmStECQw9KQrEpXSqOaRfZChCh0To9Qk_C12vn5VMxiBUFS7H9rnpeMLlk23o1a5dPrTs9GlhvfUCGn4oiUyvJLrgYu3-MwJSYWgnBl8UI1cy1KrwtEOZCRo0vUXecp-HPalAA) method)

Quiz question: What percentage of the predictions on sample_validation_data did model_5 get correct?

Prediction Probabilities

12. For each row in the **sample_validation_data**, what is the probability (according **model_5**) of a loan being classified as **safe**? (Hint: if you are using scikit-learn, you can use the **.predict_proba()**

(https://eventing.coursera.org/api/redirectStrict/ynmFF7Ey5HdvxiaMUfkX4m8tXp6u9m4KnwXQD8XHiA9WpmXpJFw UL3sVO2R9A9b-8f_Zhwlj_jLsnodjuciEGw.m8p6E--sVvzEoIVosH_6Pg.xmB8t2fh7HtRUeQMfifuLLfcKixYXRlrkSI-z-RxULFYooasF84GQ4IAyvfkRmQOxtzbraCHy_r7qTxChLlwVvPUJ82ZFBDFovW9D-

 $kXrA4yWgaQGJ1CMllg1n6MWY3FXt4HY4rss0DARH641tKi83XakvaGczZuTOnYuUjWokliHGfRx8_RkWMm65itupnQxHKD87DnZVK2feUtss73sdBuT2wpEylZqQviRcL6Ey_mhRz9JnfrTuBXlDdG2M0l5610dS0dCUsiSsNABCv9hta3y2utiUnCTOTdzdKiFUhZs5Bn0TRQx1DllpUnJ_F0xieprUV8BQhOZR0wP4dkrUBCo0w55PA_0J_d2r1BA8NKqT-$

GbWlwqZKn8RpvBwkCuQP7aSO4mufa2-FaxvDxv0yt1pqOeQgMyYJ3AzblqFkBKR6LB1NO9GRbiAiiVEOKji-

NyVUTcEFhXAFQ9scHZuFtAD8NJ7eau1rfQFX7ZR_DJPiwM3vzAfQhKrZ2XdrkXF4Qog0lbErkUun6AkJnl15n1La8ek2eoHuwkeEEqlKYvTYL2kERjc-cWmTlUOmXvabpb4u7_m0QS_goX9wzLRz3Az-

2zeXmQwOmlTnO2p1TFVtKHd9zzC8lbQUs4Va) method)

Quiz Question: Which loan has the highest probability of being classified as a safe loan?

Checkpoint: Can you verify that for all the predictions with probability >= 0.5, the model predicted the label +1?

Evaluating the model on the validation data

Recall that the accuracy is defined as follows:

$$\label{eq:accuracy} \text{accuracy} = \frac{\text{\# correctly classified examples}}{\text{\# total examples}}$$

13. Evaluate the accuracy of the **model_5** on the **validation_data**. (Hint: if you are using scikit-learn, you can use the **.score()**

(https://eventing.coursera.org/api/redirectStrict/Els4D1QSQchqUnWhkAsWou5Lw3N7WnstD2xEdB3zlyHK69s079m gdoOJnPwDGVoCjHlCAwAk1OGCp4jz7FBkPQ.ObzY6pcdBqsIZ1g594yPyA.QnsD-

eIrY1MzV1c7orURYT6OzoMgQGcxxXthetbKGKF724_ywdqfr3yYqEWmAAQAH348jy7cM0RHbhX6hco6i7hyRfCxvV9R-eANZrPaDIFPzB5hckU3zukGYG5l0dVAQn3yi8r3387WZwdCOddw_LVIUGxwgeMR3xOZEyZU4O_SqlUM1ES_5rSha2LT XPrGAjf1oHNGnJL3HnSY6ZAUHCj1nj1MDZyR1dWpROxMG1kin2ZfRH-

vBKB_1TbhAl9dG5zd3tOk9W3ADF-pNJKzv_htVYBTcxuA8uRni5l3OSV54QOlOiSTG6AW4sZuielmYyYp6yL-guYeDlW9Q1I-FQwus8_vuUcBeHrsG4bYBo5zAX_lphzyEFlN41-

MkZq5_IRTq23Ce8WGa0n9Z6IfW0yesY5XpqI2FC16zCr5d_NSaY0CB-sNT0-dTF-

RUKQu4Xy2cpsBTAWUg_T3m82VZLBfnm5rLZu8V1QUbKXc649qiaMbo_KPftl43NHTU866Lw-ql98k8KgOezF4yjTLQG_w) method)

14. Calculate the number of false positives made by the model on the validation data.

Quiz question: What is the number of **false positives** on the **validation_data**?

15. Calculate the number of **false negatives** made by the model on the **validation_data**.

Comparison with decision trees

In the earlier assignment, we saw that the prediction accuracy of the decision trees was around **0.64**. In this assignment, we saw that **model_5** has an accuracy of approximately **0.67**.

Here, we quantify the benefit of the extra 3% increase in accuracy of **model_5** in comparison with a single decision tree from the original decision tree assignment.

As we explored in the earlier assignment, we calculated the cost of the mistakes made by the model. We again consider the same costs as follows:

- False negatives: Assume a cost of \$10,000 per false negative.
- False positives: Assume a cost of \$20,000 per false positive.

Assume that the number of false positives and false negatives for the learned decision tree was

• False negatives: 1936

• False positives: 1503

Using the costs defined above and the number of false positives and false negatives for the decision tree, we can calculate the total cost of the mistakes made by the decision tree model as follows:

```
cost = $10,000 * 1936 + $20,000 * 1503 = $49,420,000
```

The total cost of the mistakes of the model is \$49.42M. That is a lot of money!.

16. Calculate the cost of mistakes made by **model_5** on the **validation_data**.

Quiz Question: Using the same costs of the false positives and false negatives, what is the cost of the mistakes made by the boosted tree model (**model_5**) as evaluated on the **validation_set**?

Reminder: Compare the cost of the mistakes made by the boosted trees model with the decision tree model. The extra 3% improvement in prediction accuracy can translate to several million dollars! And, it was so easy to get by simply boosting our decision trees.

Most positive & negative loans.

In this section, we will find the loans that are most likely to be predicted **safe**. We can do this in a few steps:

- **Step 1**: Use the **model_5** (the model with 5 trees) and make **probability predictions** for all the loans in **validation_data**.
- **Step 2**: Similar to what we did in the very first assignment, add the probability predictions as a column called **predictions** into **validation_data**.
- **Step 3**: Sort the data (in descreasing order) by the probability predictions.
- 17. Start here with Step 1 & Step 2. Make predictions using model_5 for all examples in the validation_data.

Checkpoint: For each row, the probabilities should be a number in the range [0, 1].

18. Now, we are ready to go to **Step 3**. You can now use the prediction column to sort the loans in **validation_data** (in descending order) by prediction probability. Find the top 5 loans with the highest probability of being predicted as a **safe loan**.

Quiz question: What grades are the top 5 loans?

19. Repeat this exercise to find the 5 loans (in the **validation_data**) with the **lowest probability** of being predicted as a **safe loan**.

Effects of adding more trees

In this assignment, we will train 5 different ensemble classifiers in the form of gradient boosted trees.

20. Train models with 10, 50, 100, 200, and 500 trees. Use the **n_estimators** parameter to control the number of trees. Remember to keep **max_depth = 6**.

Call these models model_10, model_50, model_100, model_200, and model_500, respectively. This may take a few minutes to run.

Compare accuracy on entire validation set

Now we will compare the predicitve accuracy of our models on the validation set.

21. Evaluate the accuracy of the 10, 50, 100, 200, and 500 tree models on the validation_data.

Quiz Question: Which model has the best accuracy on the validation_data?

Quiz Question: Is it always true that the model with the most trees will perform best on test data?

Plot the training and validation error vs. number of trees

Recall from the lecture that the classification error is defined as

classification error = 1 - accuracy

In this section, we will plot the training and validation errors versus the number of trees to get a sense of how these models are performing. We will compare the 10, 50, 100, 200, and 500 tree models. **You will need matplotlib** in order to visualize the plots.

22. First, make sure this block of code runs on your computer.

```
import matplotlib.pyplot as plt
%matplotlib inline
def make_figure(dim, title, xlabel, ylabel, legend):
    plt.rcParams['figure.figsize'] = dim
    plt.title(title)
    plt.xlabel(xlabel)
    plt.ylabel(ylabel)
    if legend is not None:
        plt.legend(loc=legend, prop={'size':15})
    plt.rcParams.update({'font.size': 16})
    plt.tight_layout()
```

In order to plot the classification errors (on the **train_data** and **validation_data**) versus the number of trees, we will need lists of all the errors.

Steps to follow:

- Step 1: Calculate the classification error for each model on the training data (train_data).
- **Step 2:** Store the training errors into a list (called **training_errors**) that looks like this: [train_err_10, train_err_50, ..., train_err_500]
- Step 3: Calculate the classification error of each model on the validation data (validation_data).

• **Step 4:** Store the validation classification error into a list (called **validation_errors**) that looks like this: [validation_err_10, validation_err_50, ..., validation_err_500]

Once that has been completed, we will give code that should be able to evaluate correctly and generate the plot.

- 23. Let us start with **Step 1**. Write code to compute the classification error on the **train_data** for models **model_10**, **model_200**, and **model_500**.
- 24. Now, let us run **Step 2**. Save the training errors into a list called **training_errors**.

```
training_errors = [train_err_10, train_err_50, train_err_100, train_err_200, train_err_500]
```

- 25. Now, onto **Step 3**. Write code to compute the classification error on the **validation_data** for models **model_10**, **model_20**, **model_200**, and **model_500**.
- 26. Now, let us run Step 4. Save the training errors into a list called validation_errors.

```
validation_errors = [validation_err_10, validation_err_50, validation_err_100, validation_err_200, validation_err_500]
```

- 27. Now, we will plot the **training_errors** and **validation_errors** versus the number of trees. We will compare the 10, 50, 100, 200, and 500 tree models. We provide some plotting code to visualize the plots within this notebook.
- 28. Run the following code to visualize the plots.

Quiz question: Does the training error reduce as the number of trees increases?

Quiz question: Is it always true that the validation error will reduce as the number of trees increases?

