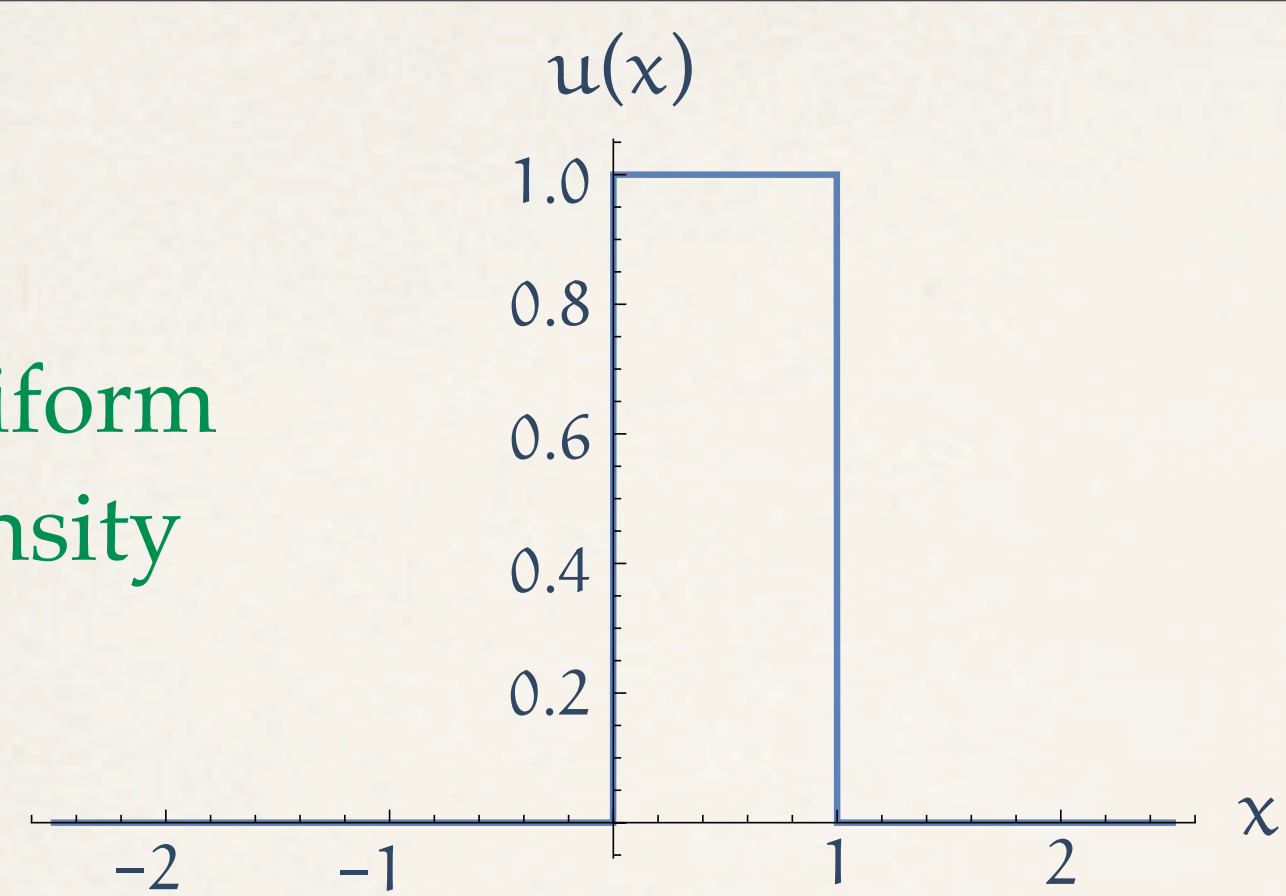


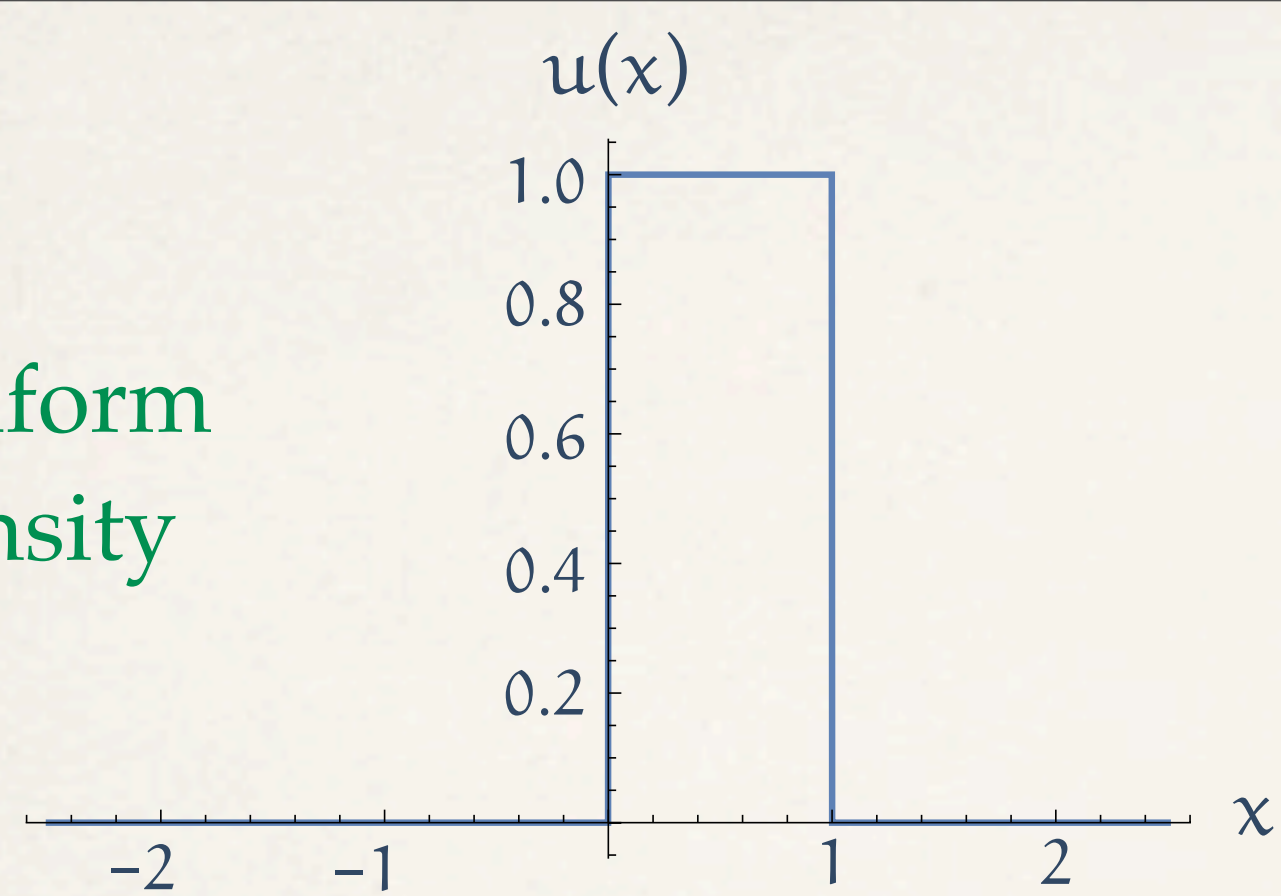
The basic densities

uniform
density



$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

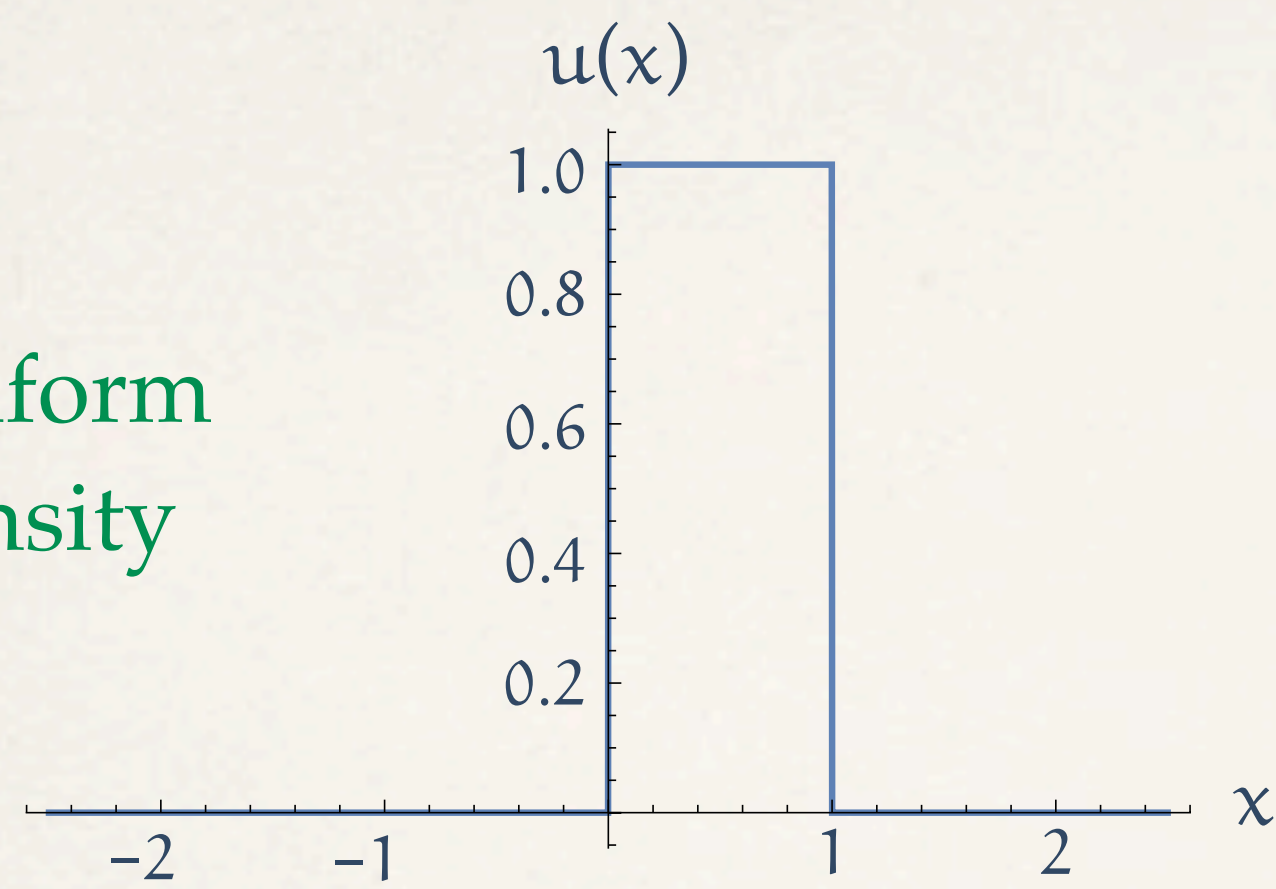
uniform
density



$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) \, dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$

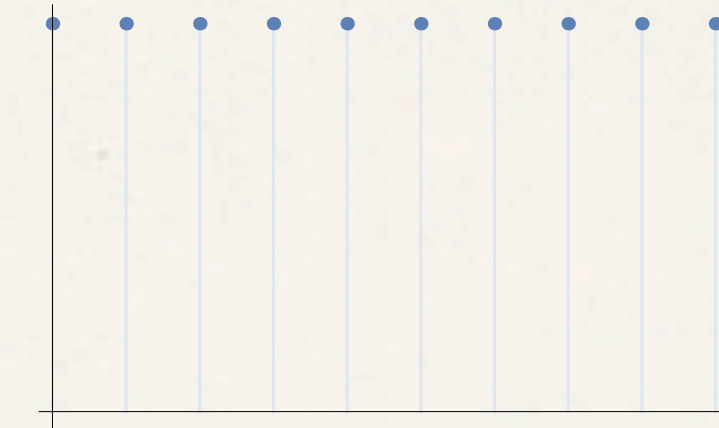
uniform
density



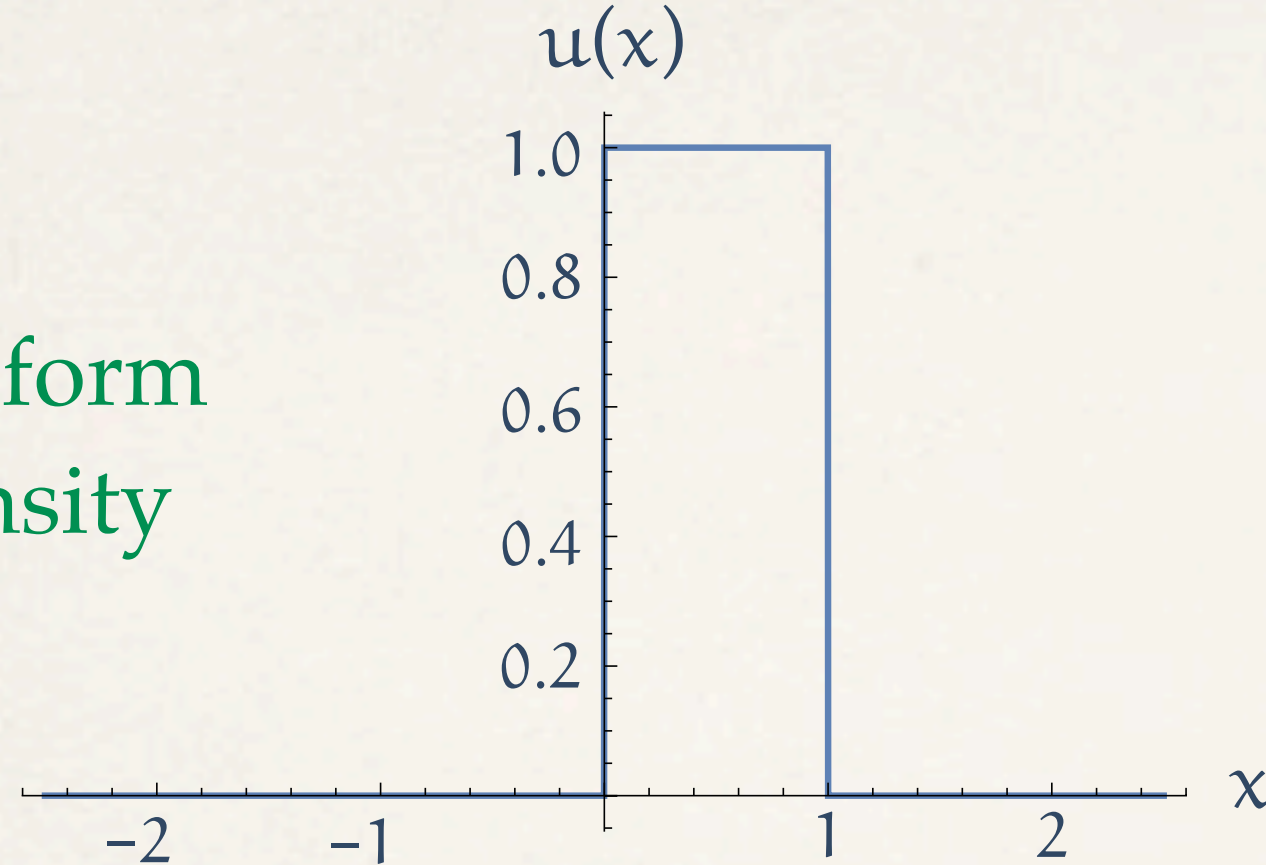
$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) \, dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$

discrete analogue: combinatorial distribution



uniform
density



random choice

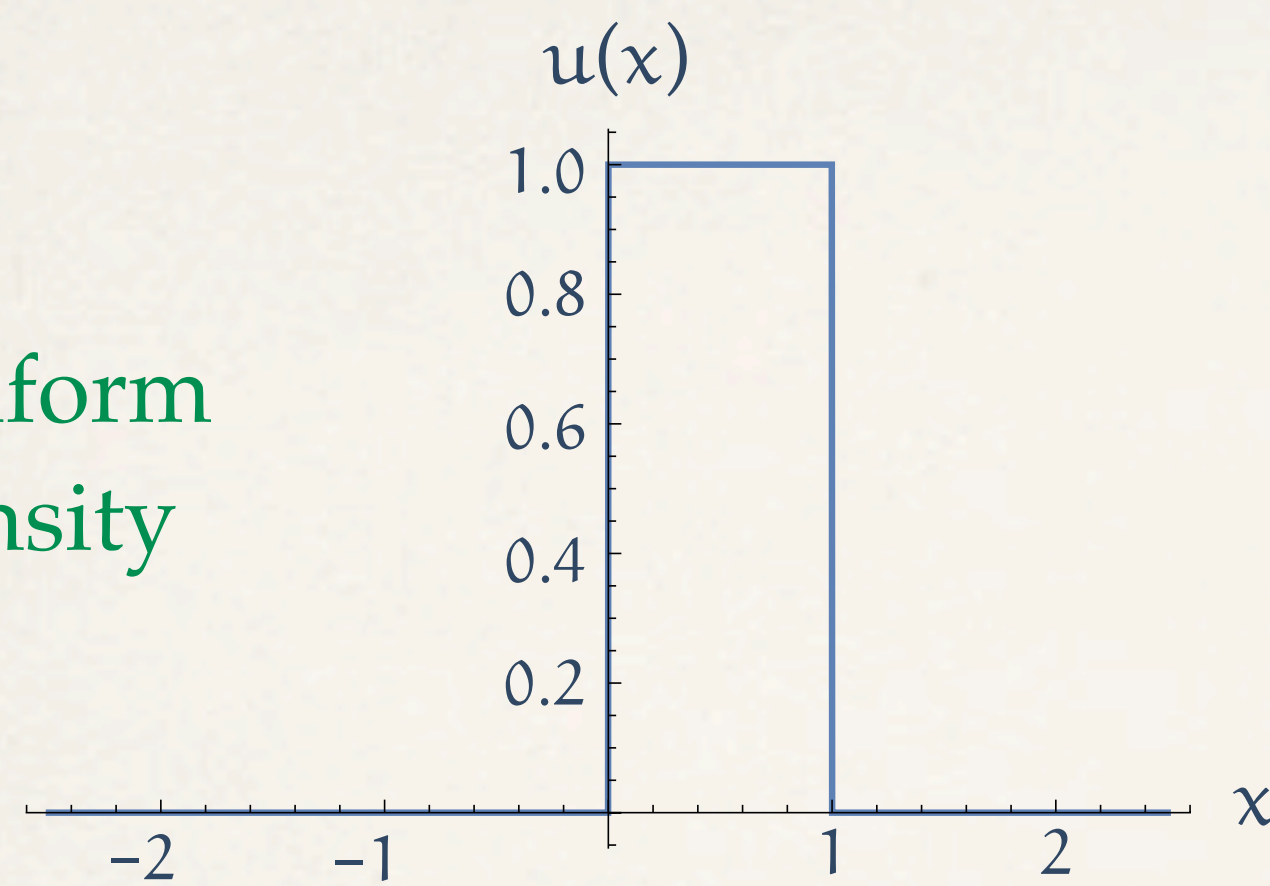
$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) \, dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$

discrete analogue: combinatorial distribution



uniform
density

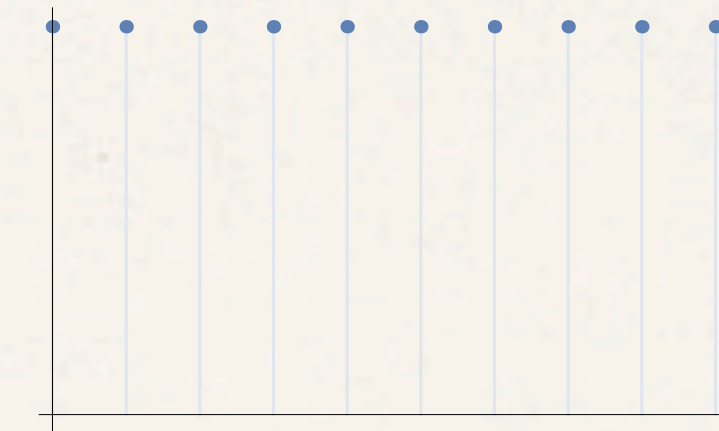


random choice

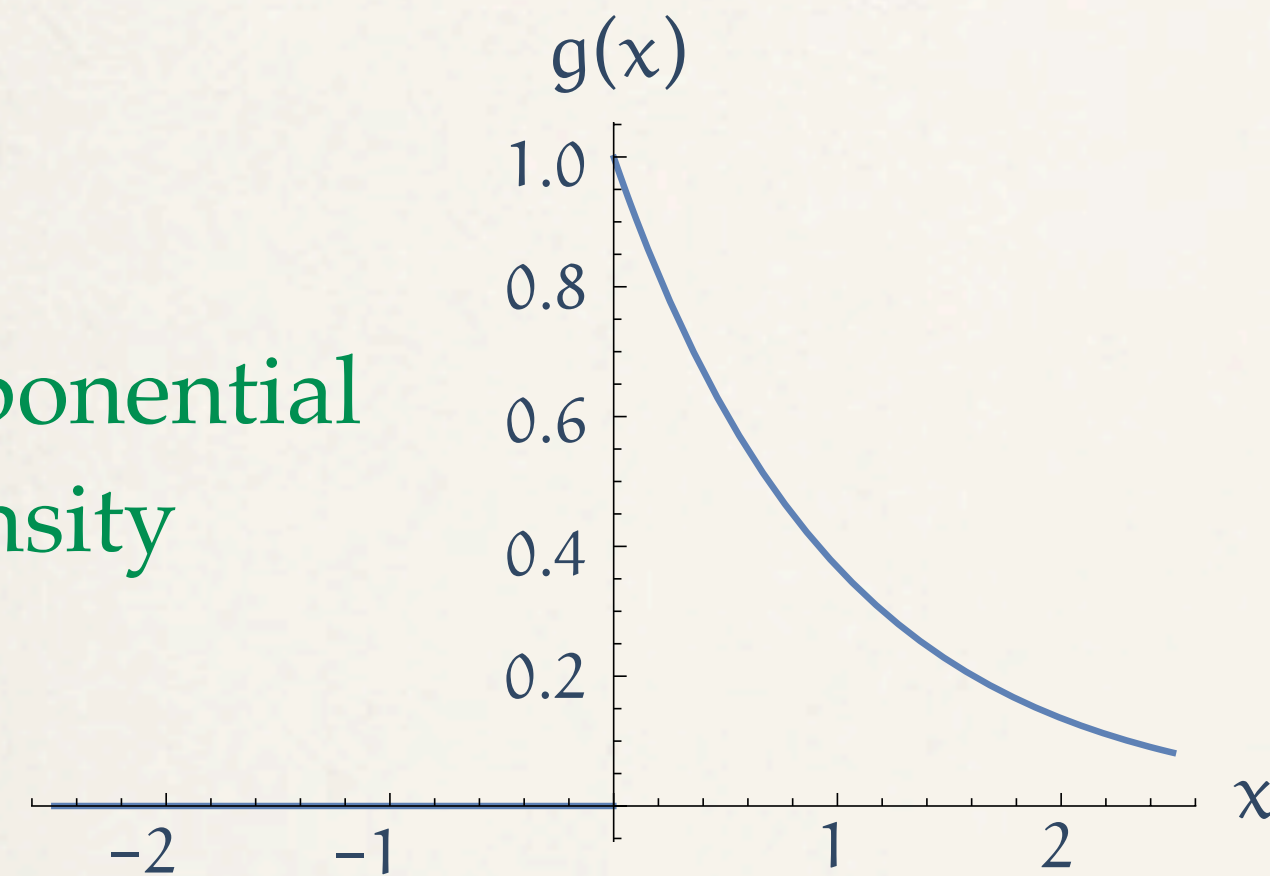
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$

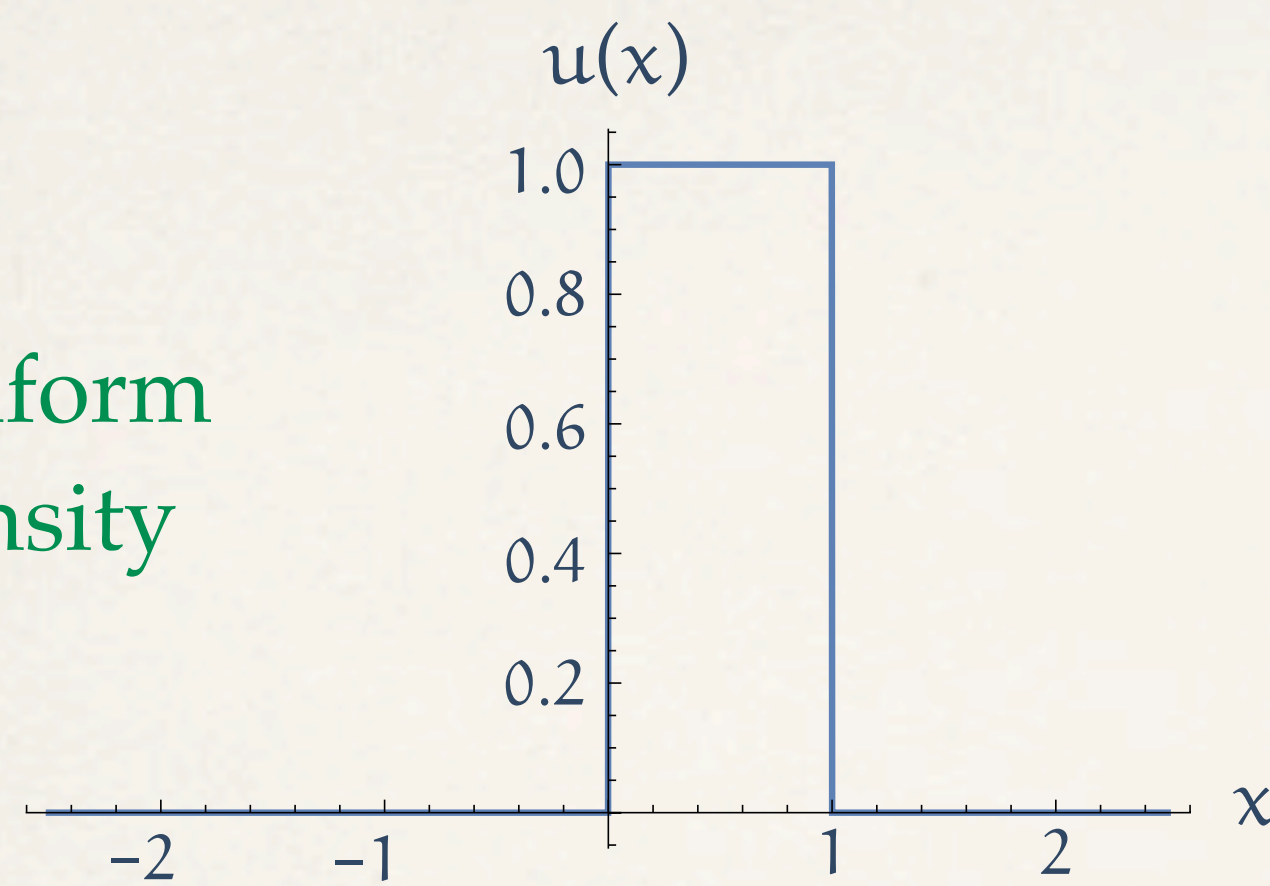


exponential
density



$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

uniform
density

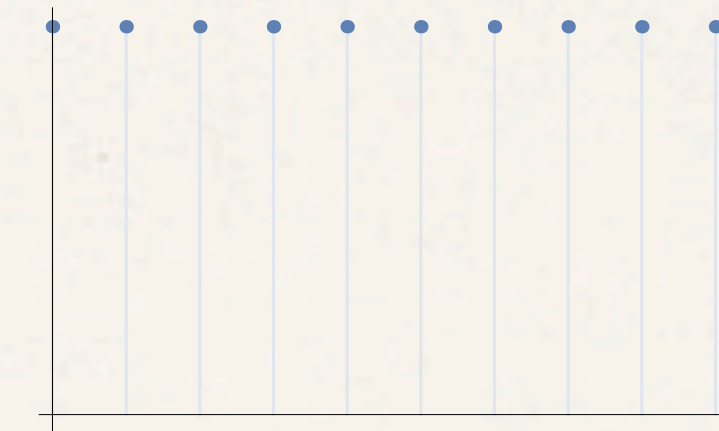


random choice

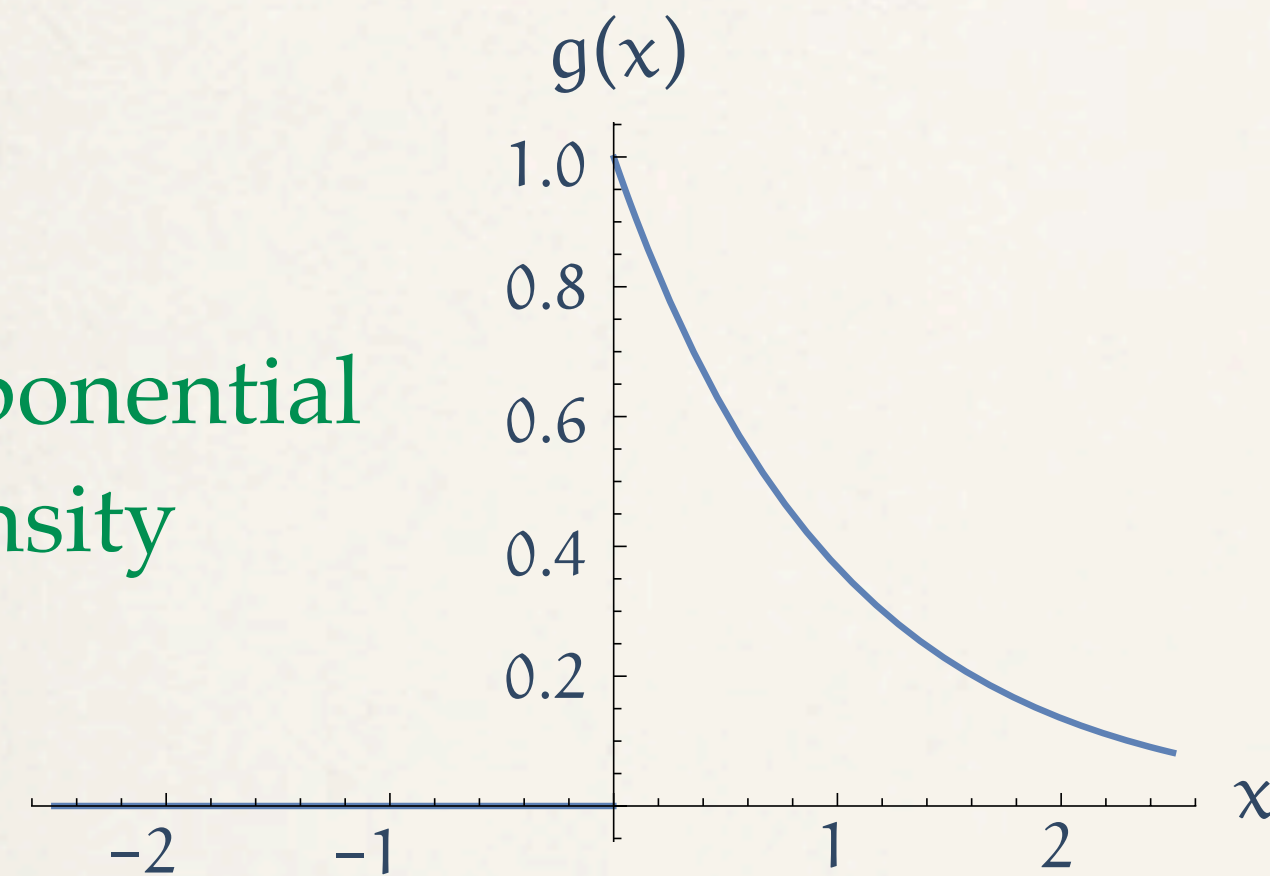
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$



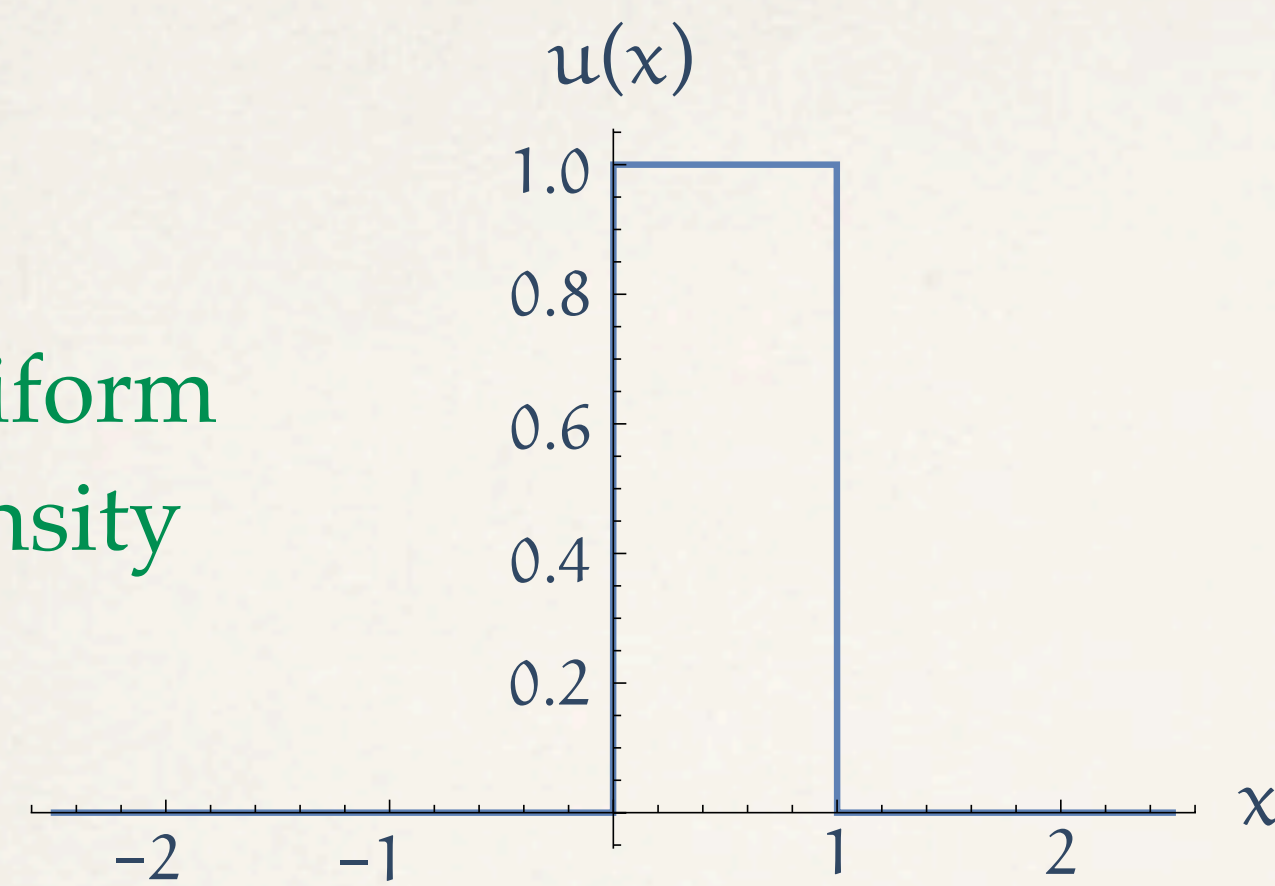
exponential
density



$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

$$\int_{-\infty}^{\infty} g(x) dx = \int_0^{\infty} e^{-x} dx = -e^{-x} \Big|_0^{\infty} = -0 + 1 = 1$$

uniform
density

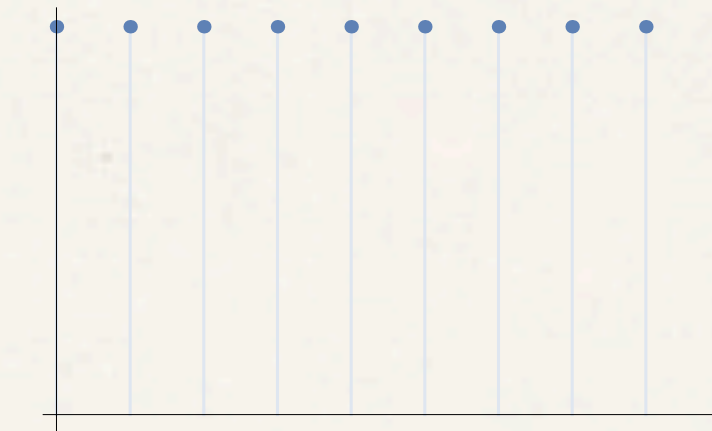


random choice

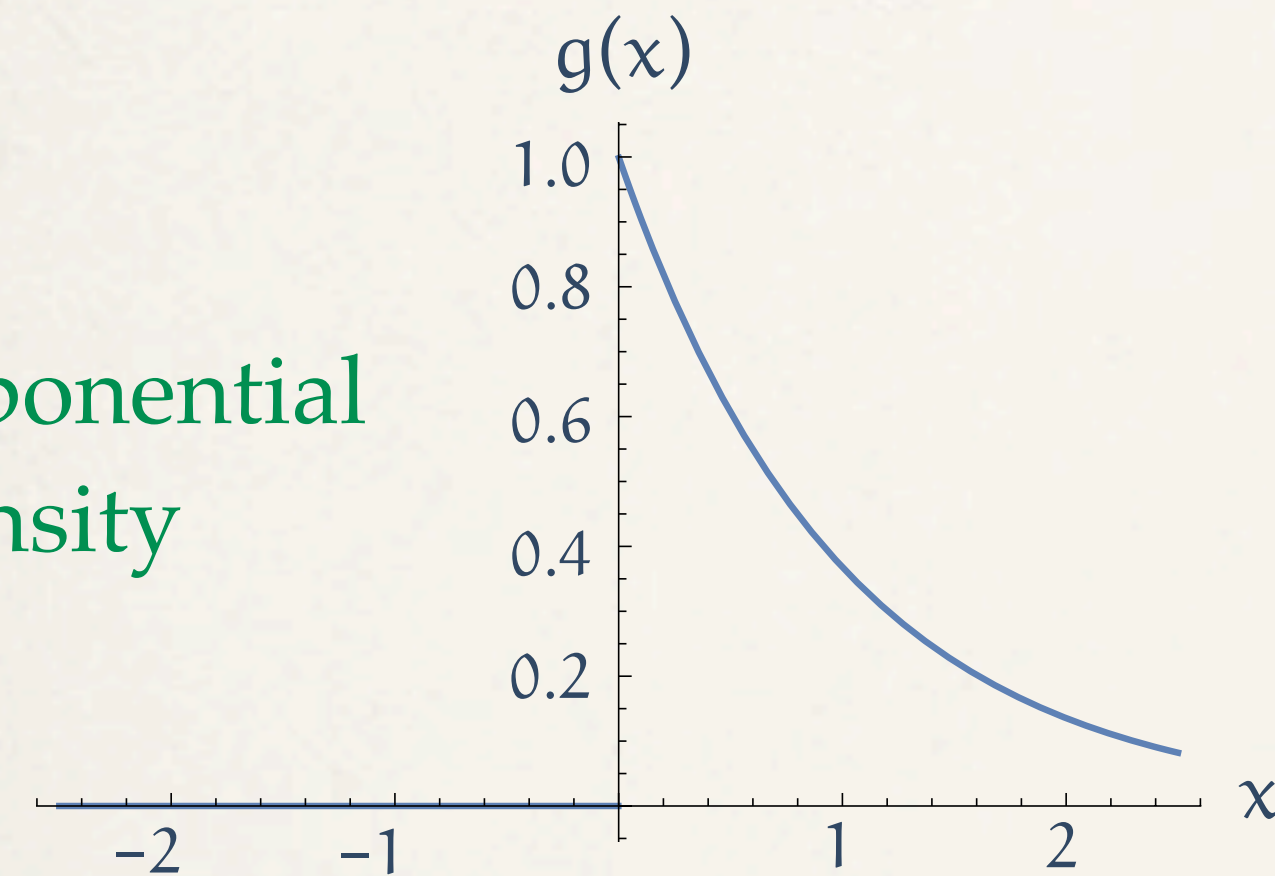
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$



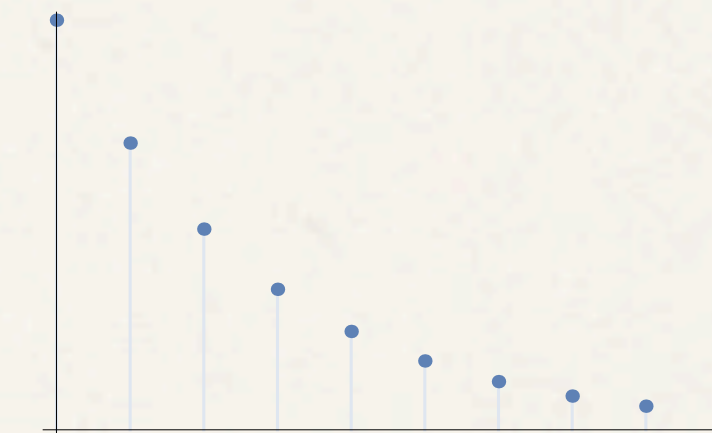
exponential
density



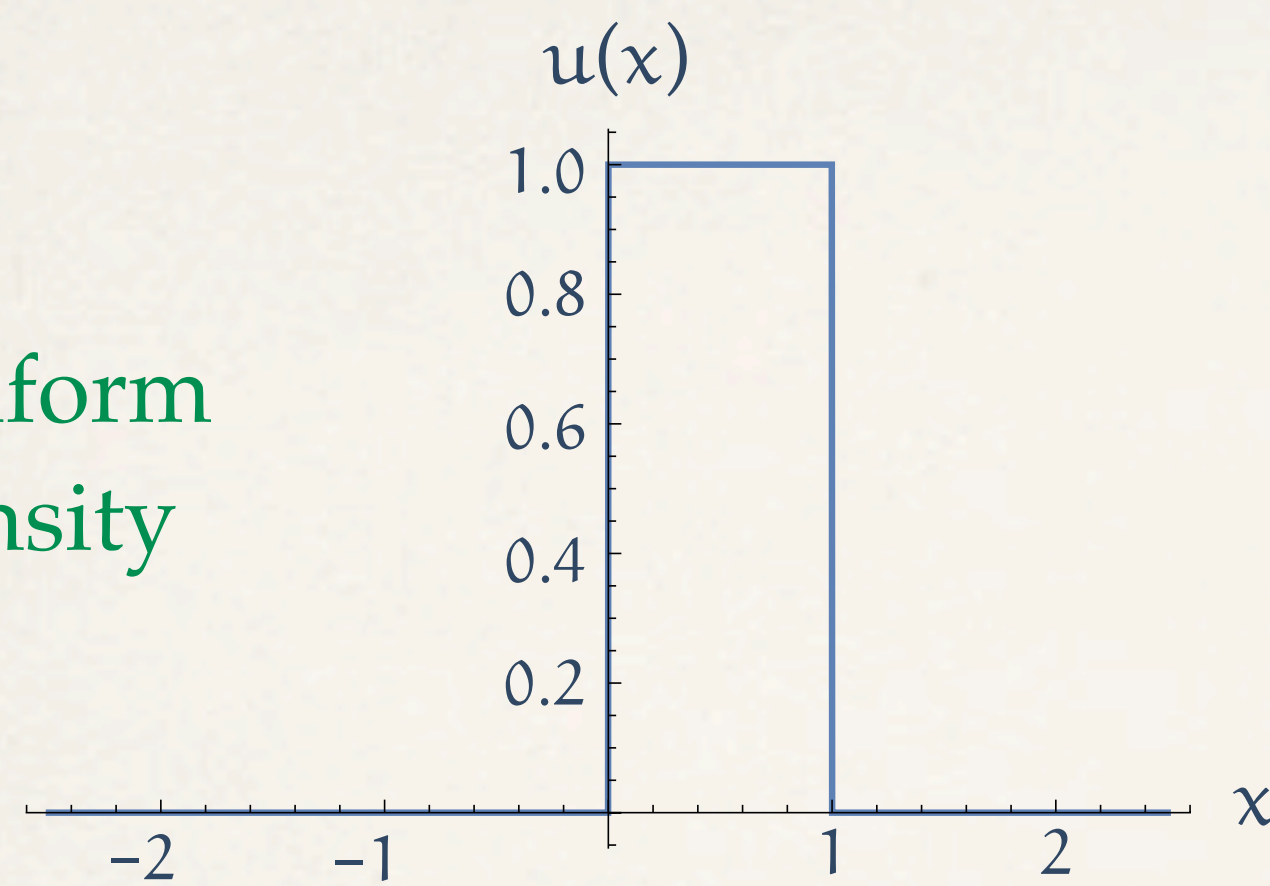
discrete analogue: geometric distribution

$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

$$\int_{-\infty}^{\infty} g(x) dx = \int_0^{\infty} e^{-x} dx = -e^{-x} \Big|_0^{\infty} = -0 + 1 = 1$$



uniform
density

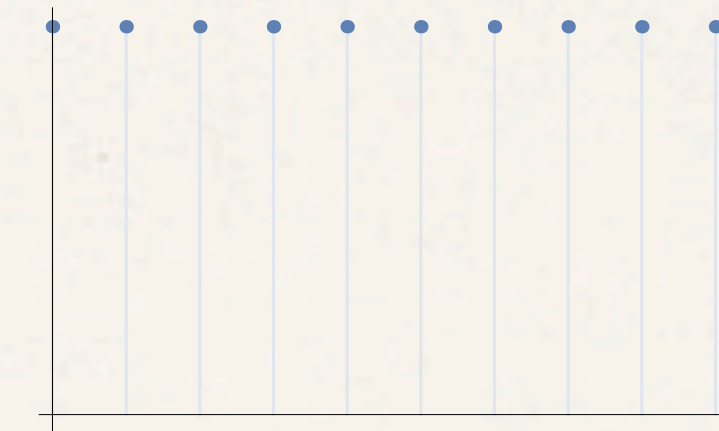


random choice

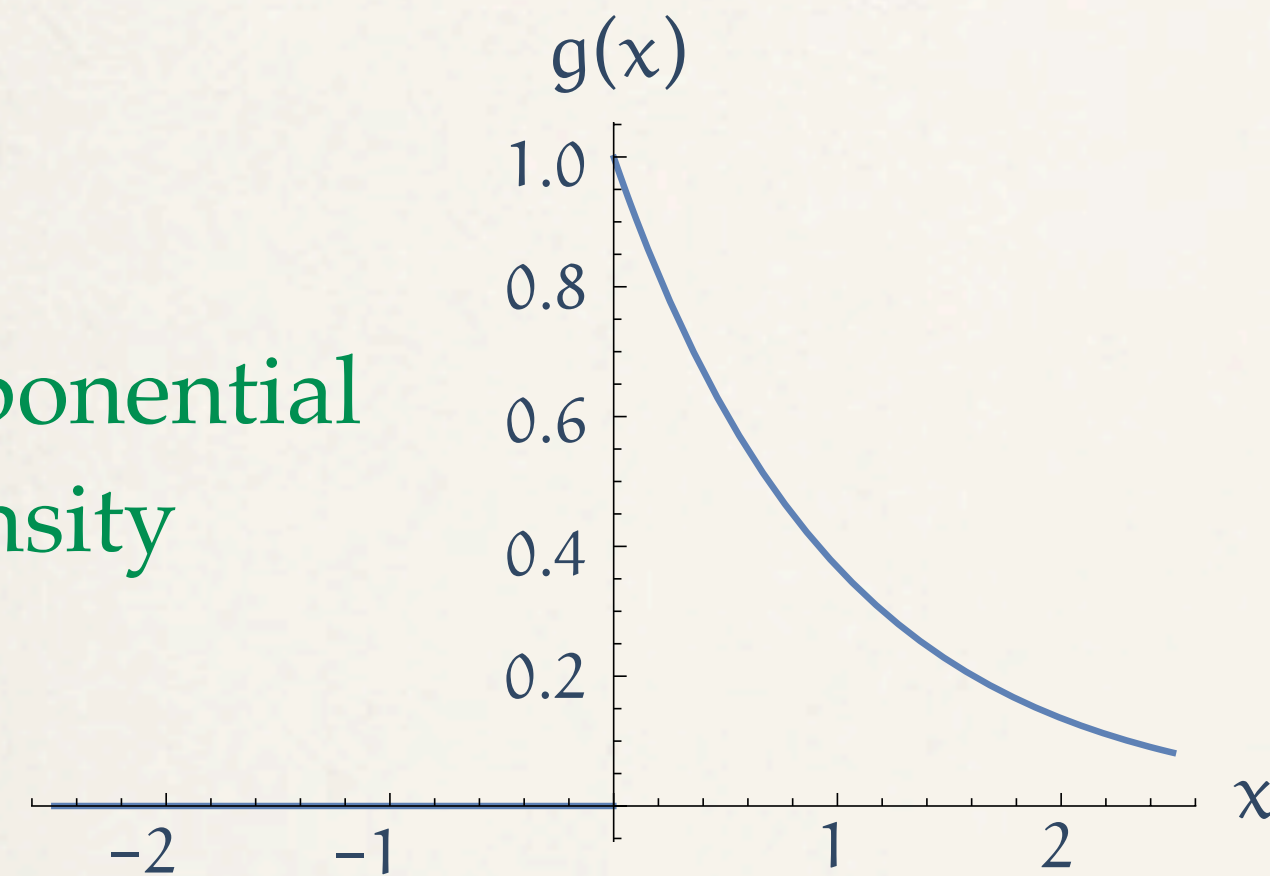
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$



exponential
density

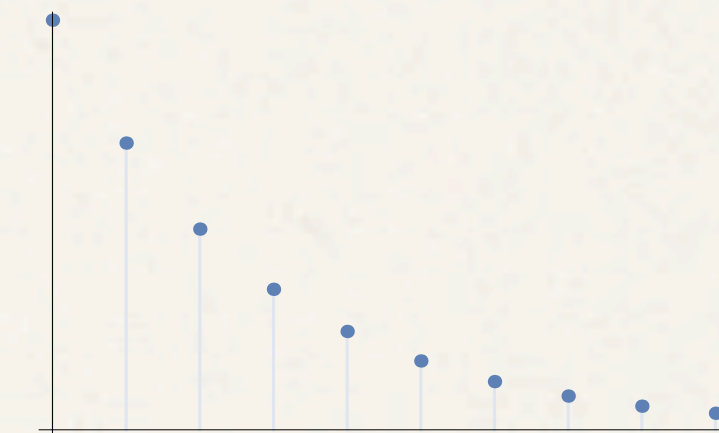


waiting times, queues

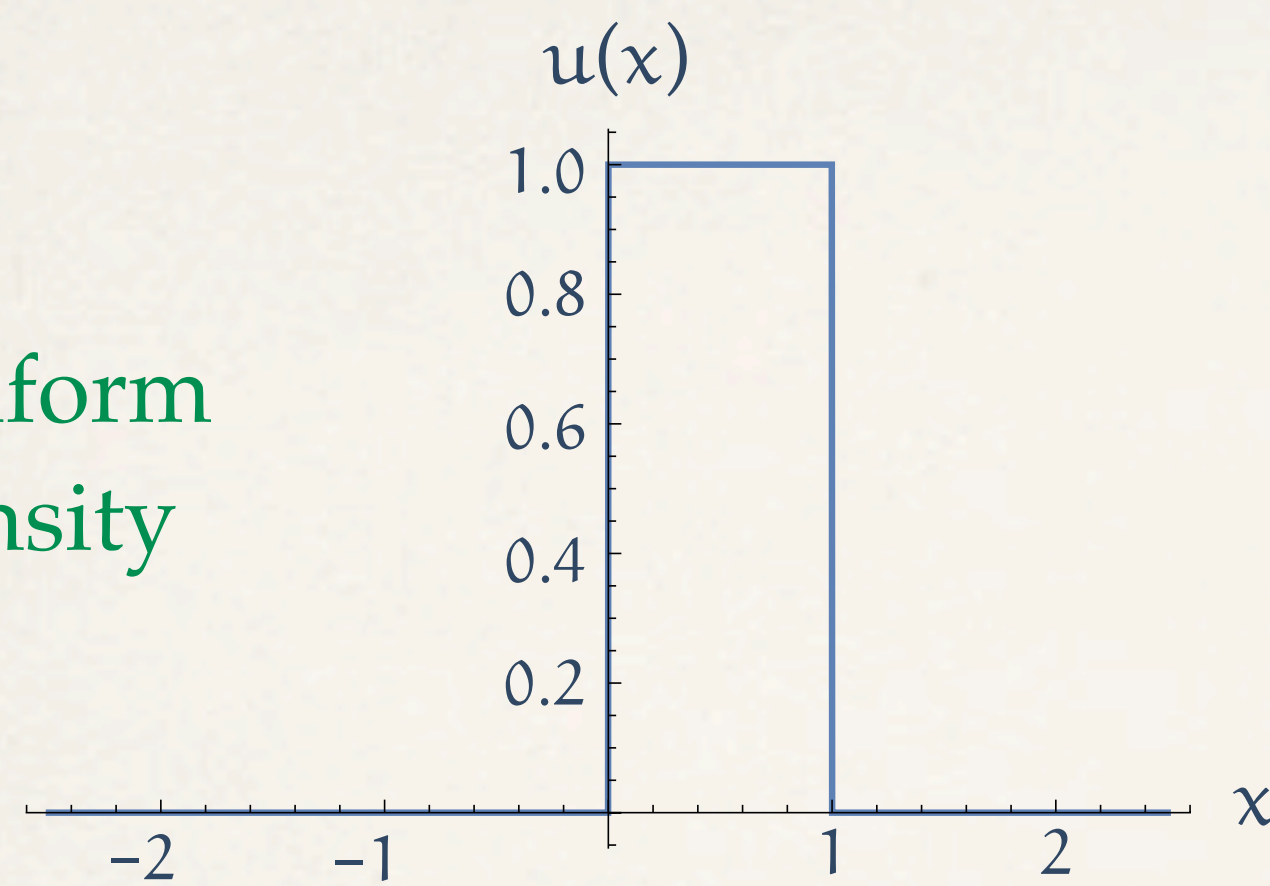
discrete analogue: geometric distribution

$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

$$\int_{-\infty}^{\infty} g(x) dx = \int_0^{\infty} e^{-x} dx = -e^{-x} \Big|_0^{\infty} = -0 + 1 = 1$$



uniform
density

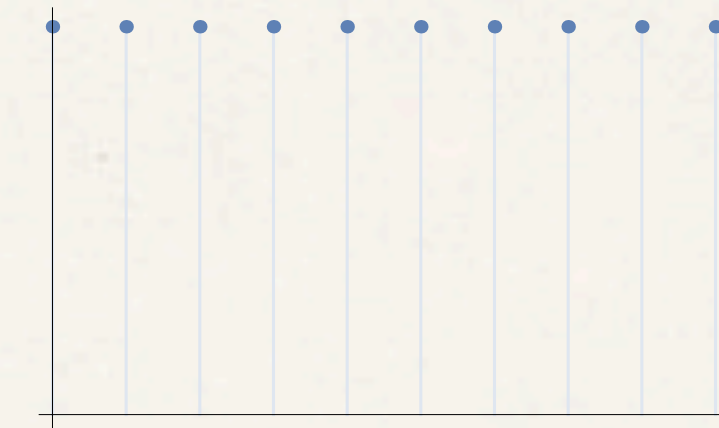


random choice

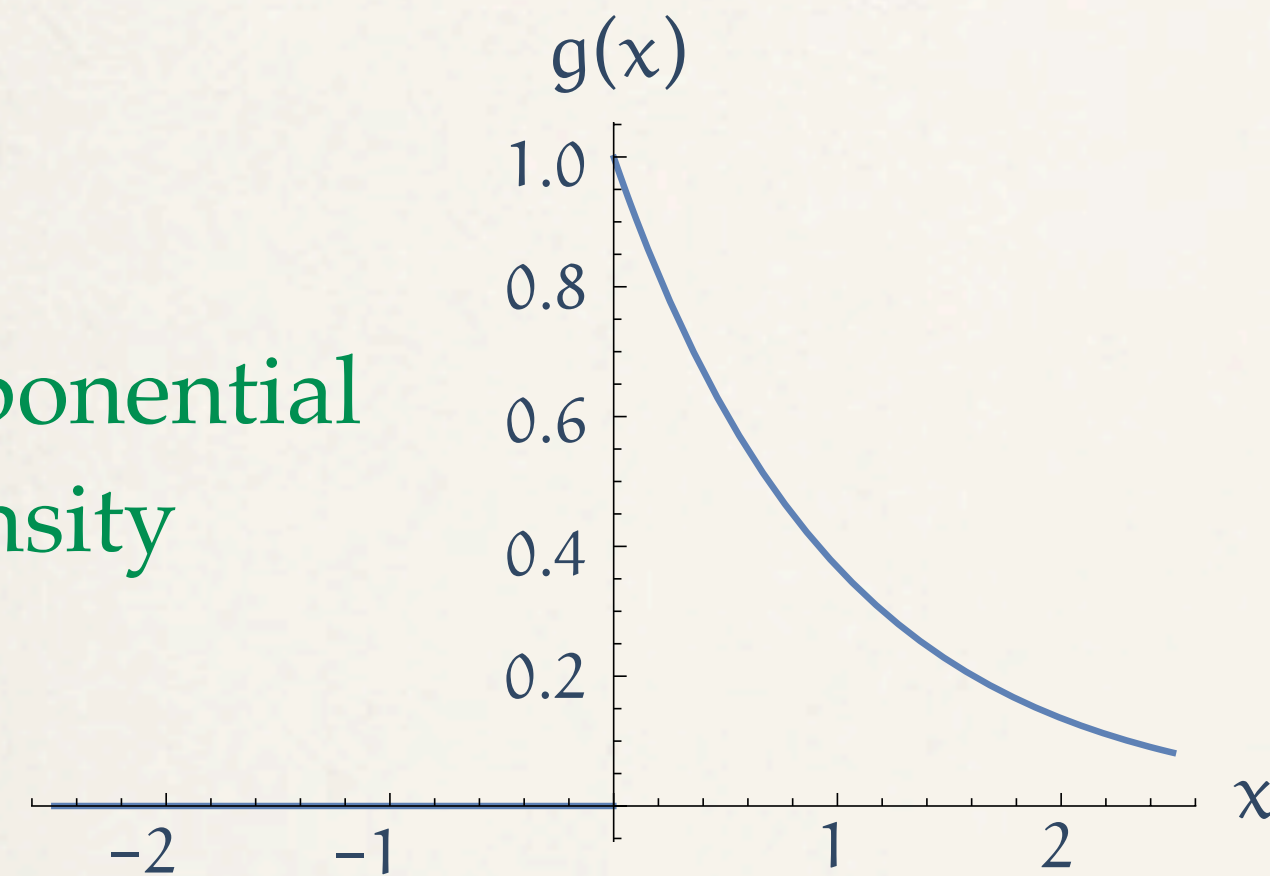
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$



exponential
density

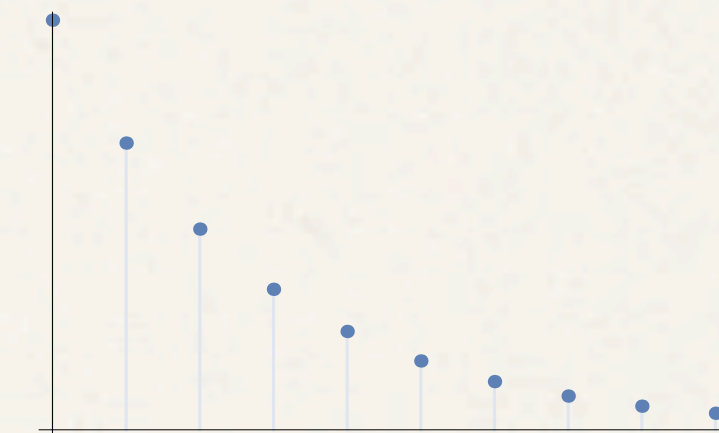


waiting times, queues

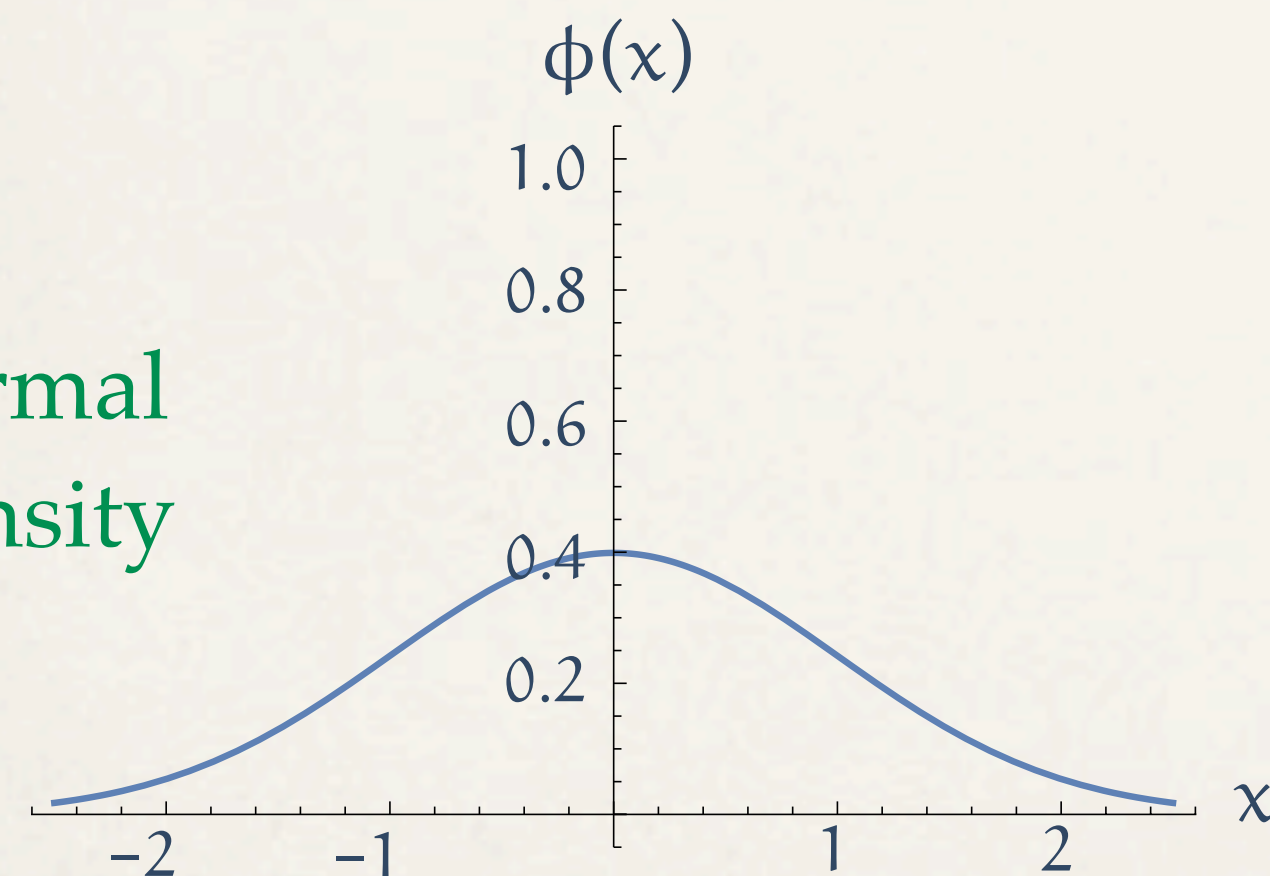
discrete analogue: geometric distribution

$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

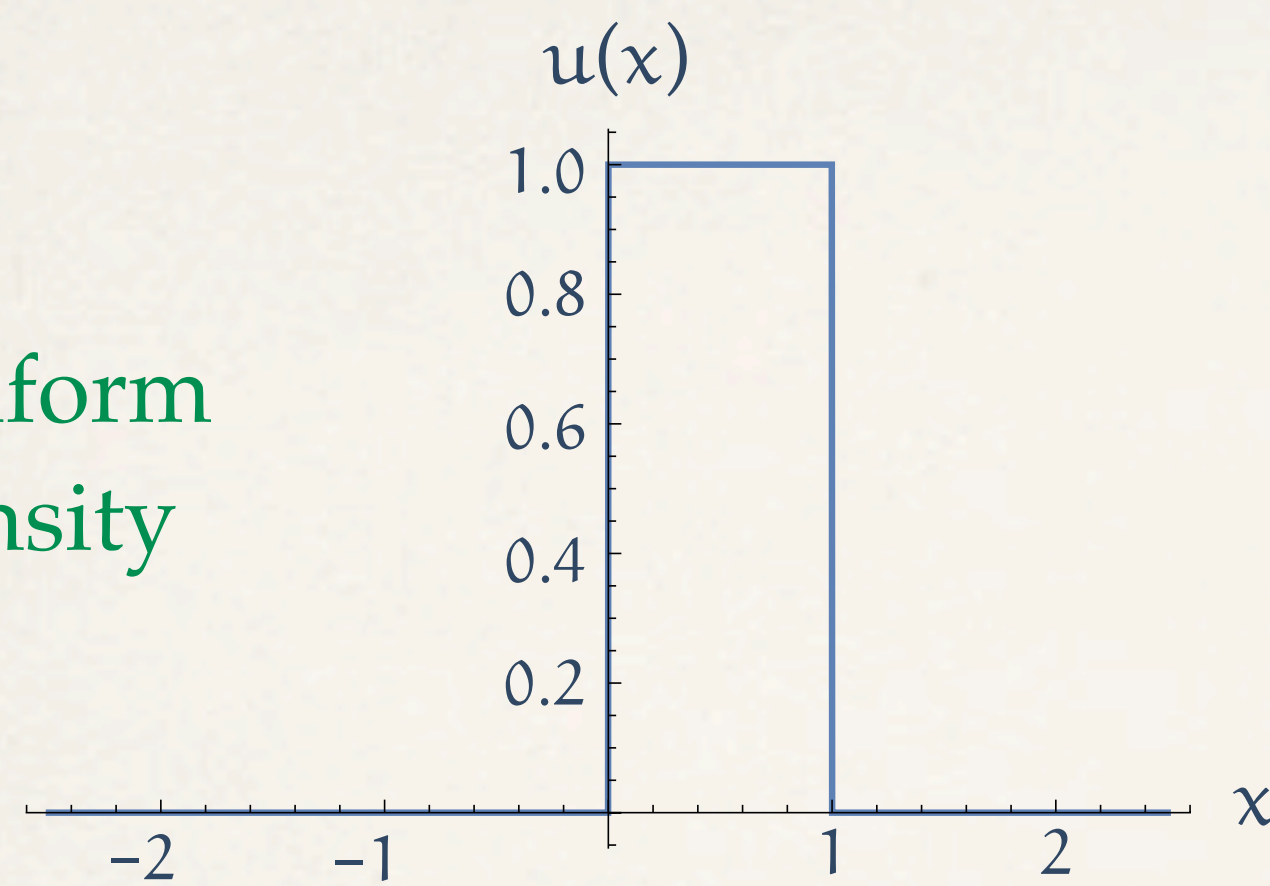
$$\int_{-\infty}^{\infty} g(x) dx = \int_0^{\infty} e^{-x} dx = -e^{-x} \Big|_0^{\infty} = -0 + 1 = 1$$



normal
density



uniform
density

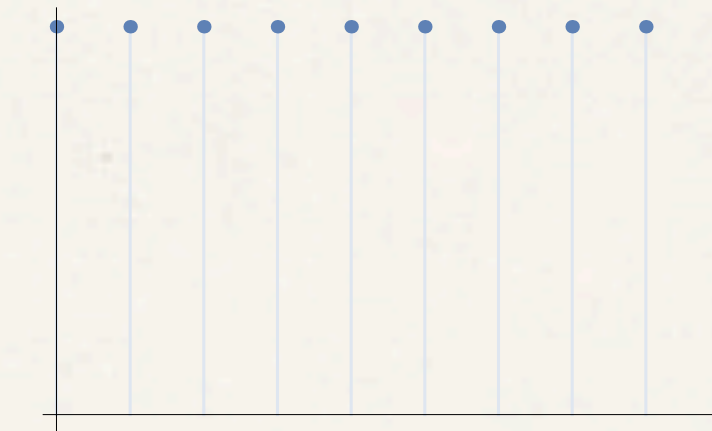


random choice

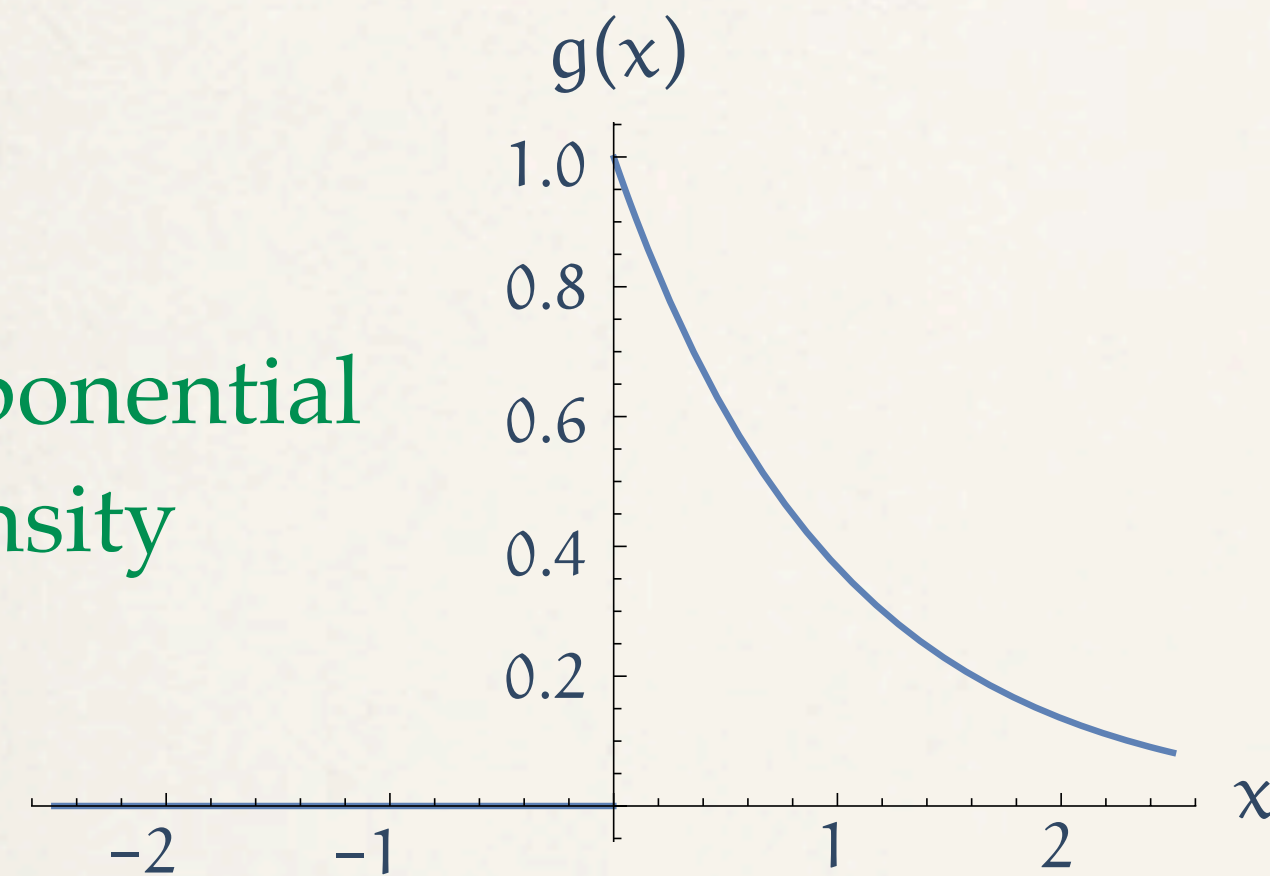
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$



exponential
density

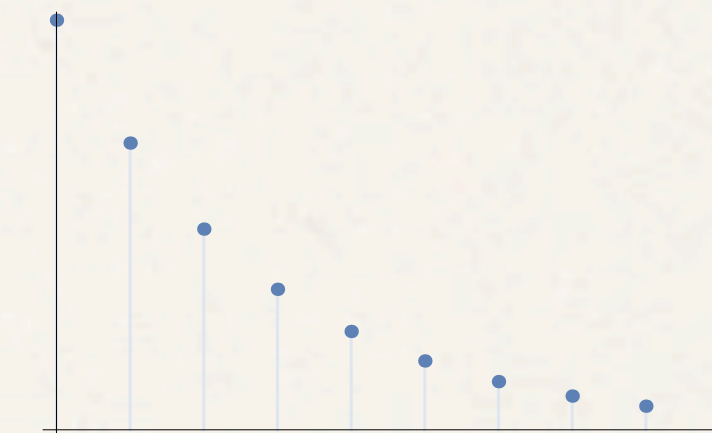


waiting times, queues

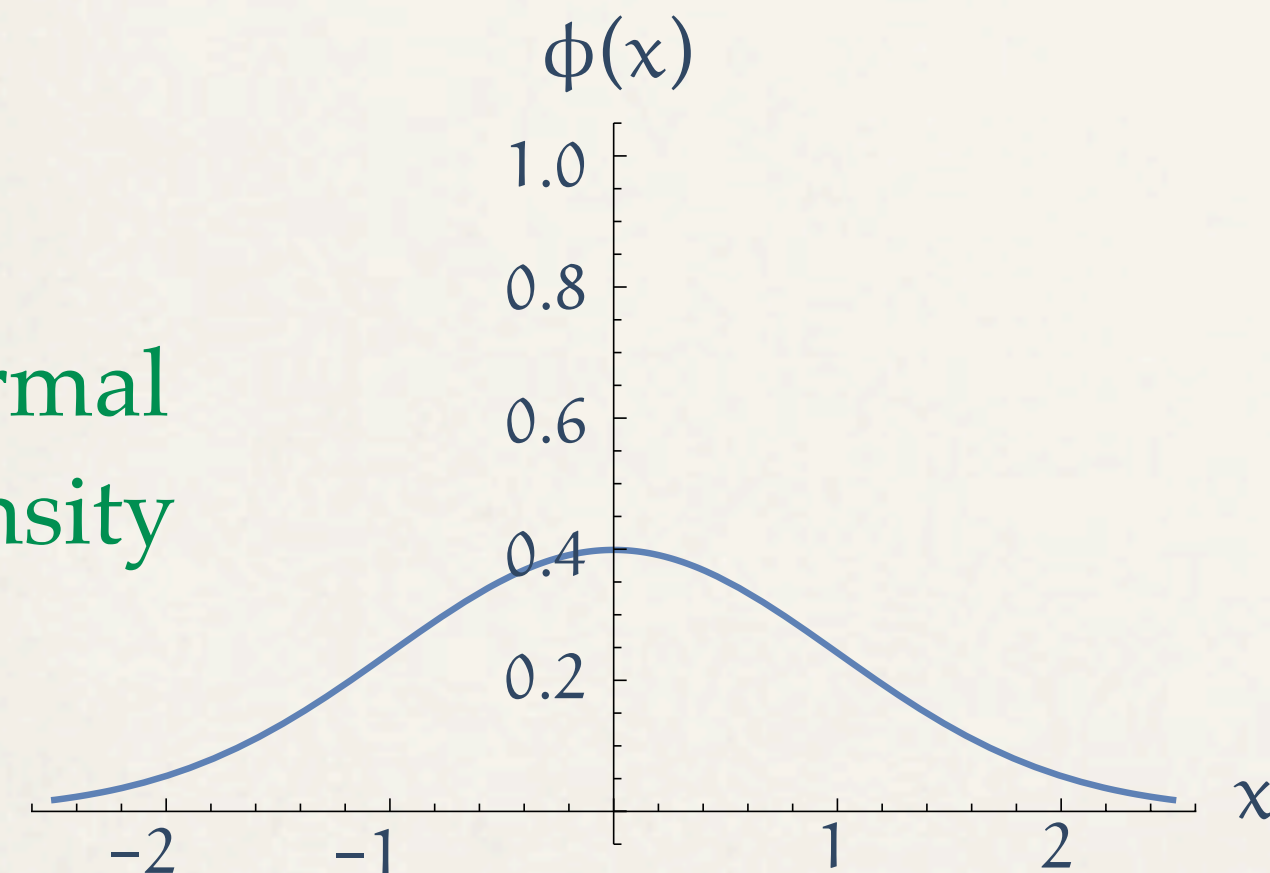
discrete analogue: geometric distribution

$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

$$\int_{-\infty}^{\infty} g(x) dx = \int_0^{\infty} e^{-x} dx = -e^{-x} \Big|_0^{\infty} = -0 + 1 = 1$$

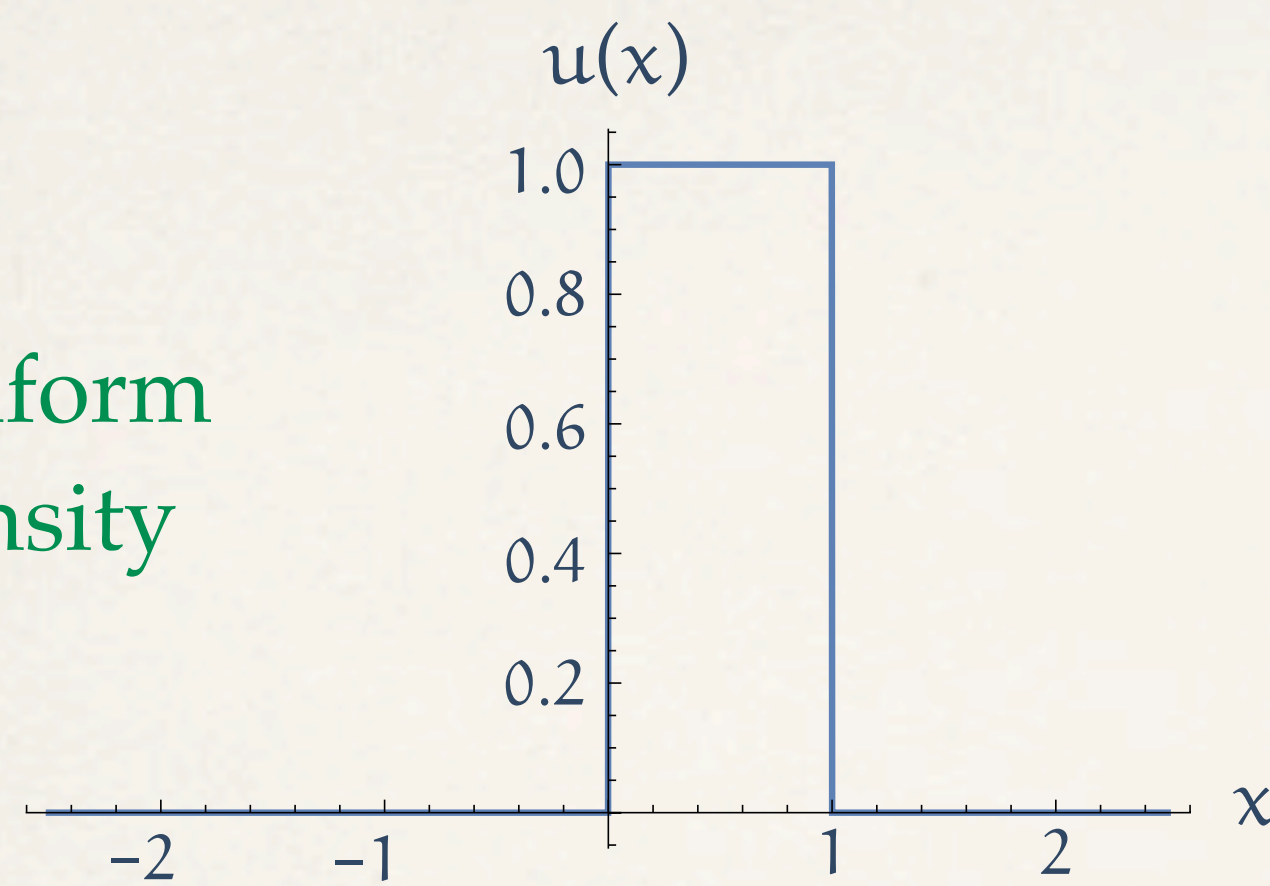


normal
density



$$\phi(x) = \frac{e^{-x^2/2}}{\sqrt{2\pi}}$$

uniform
density



random choice

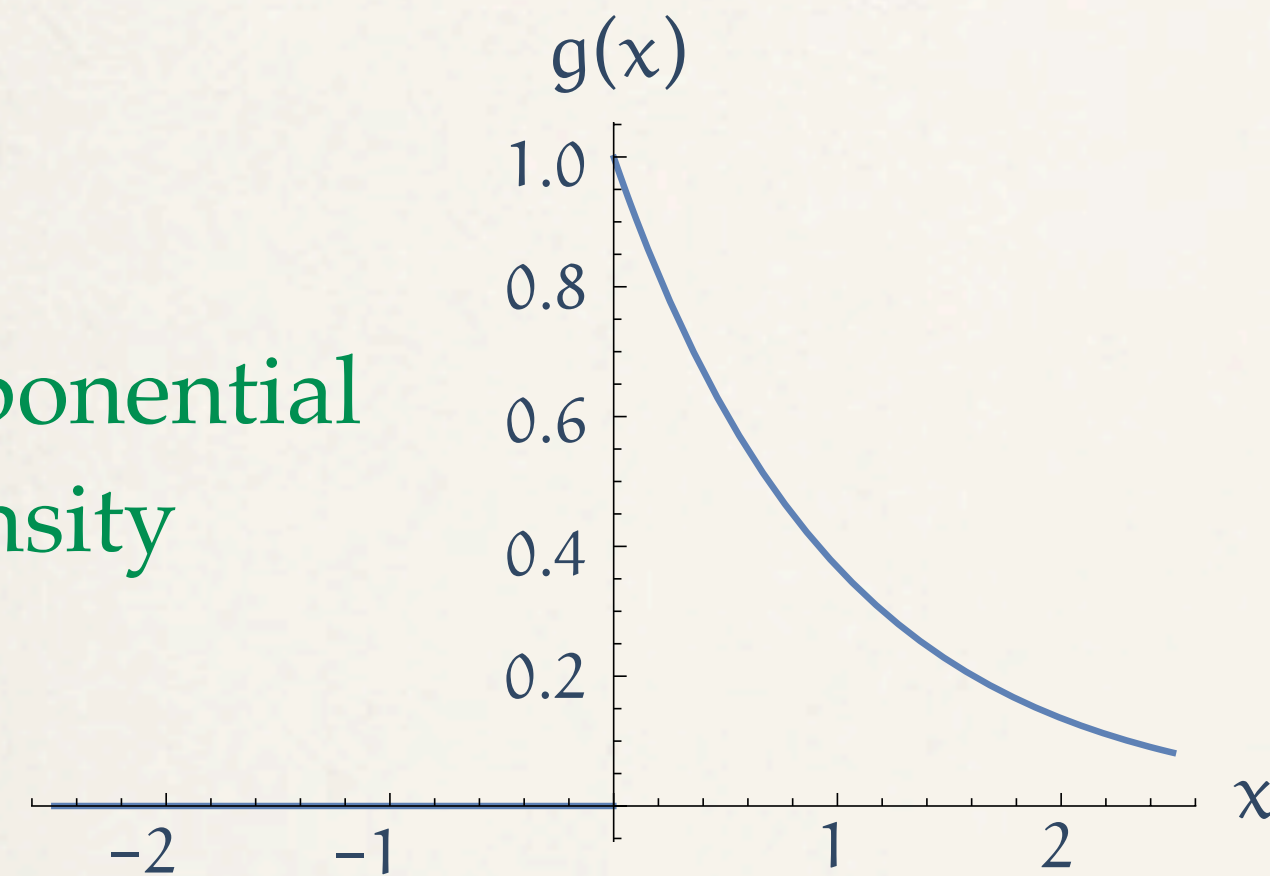
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$



exponential
density

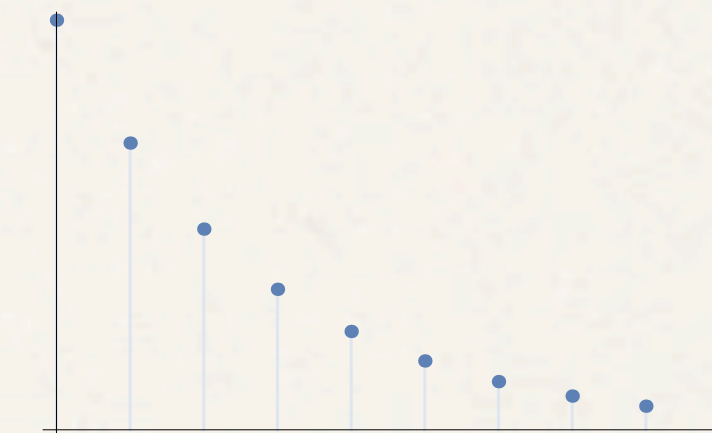


waiting times, queues

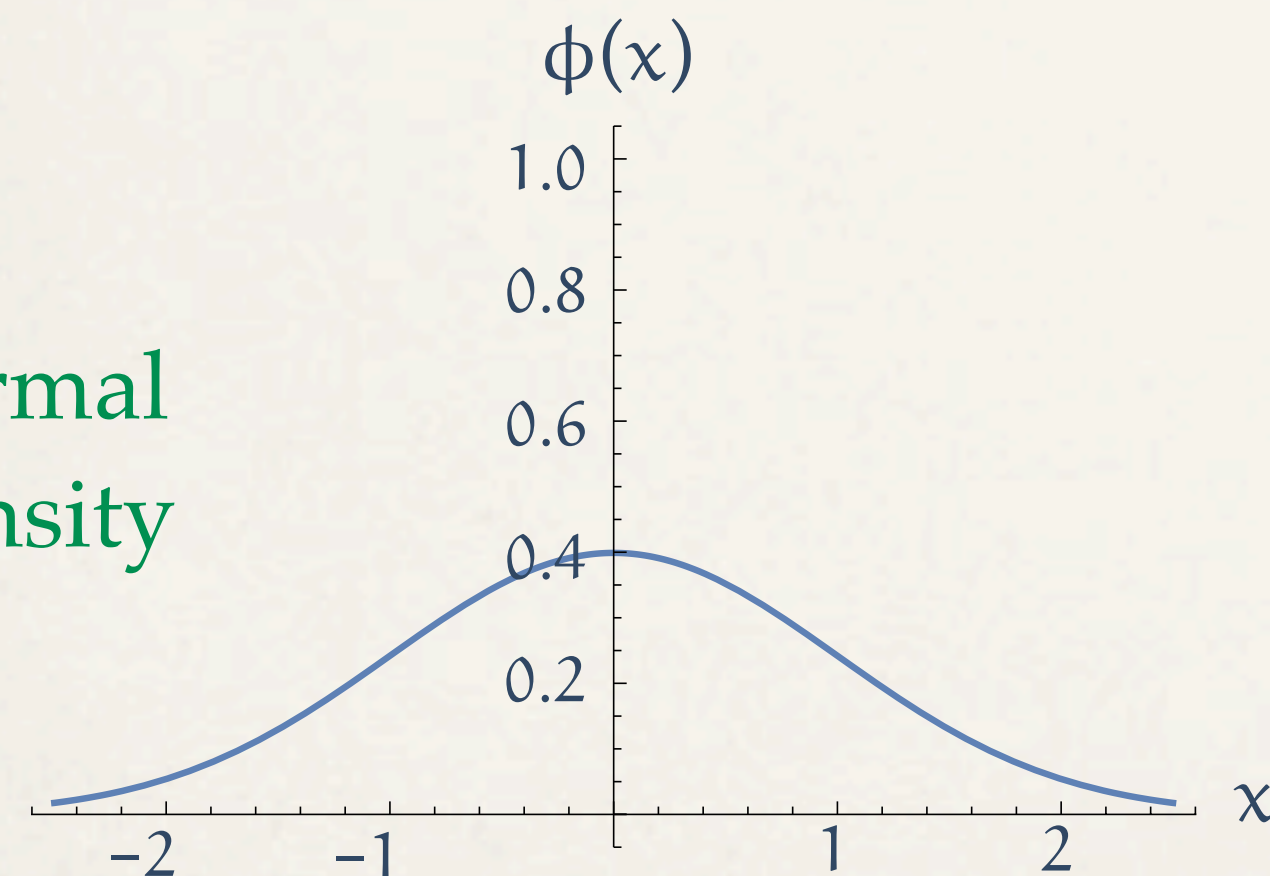
discrete analogue: geometric distribution

$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

$$\int_{-\infty}^{\infty} g(x) dx = \int_0^{\infty} e^{-x} dx = -e^{-x} \Big|_0^{\infty} = -0 + 1 = 1$$

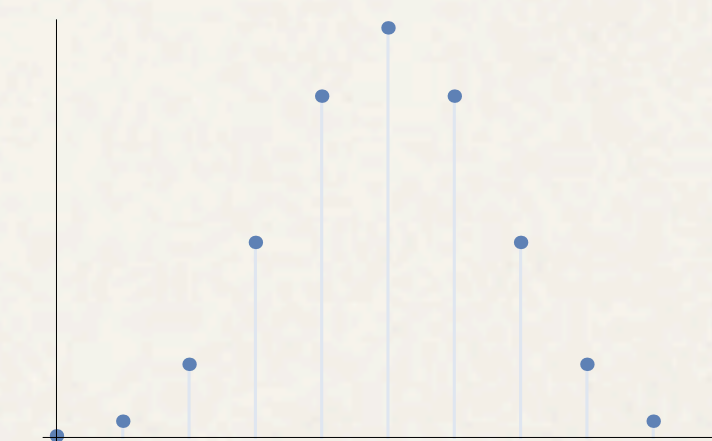


normal
density

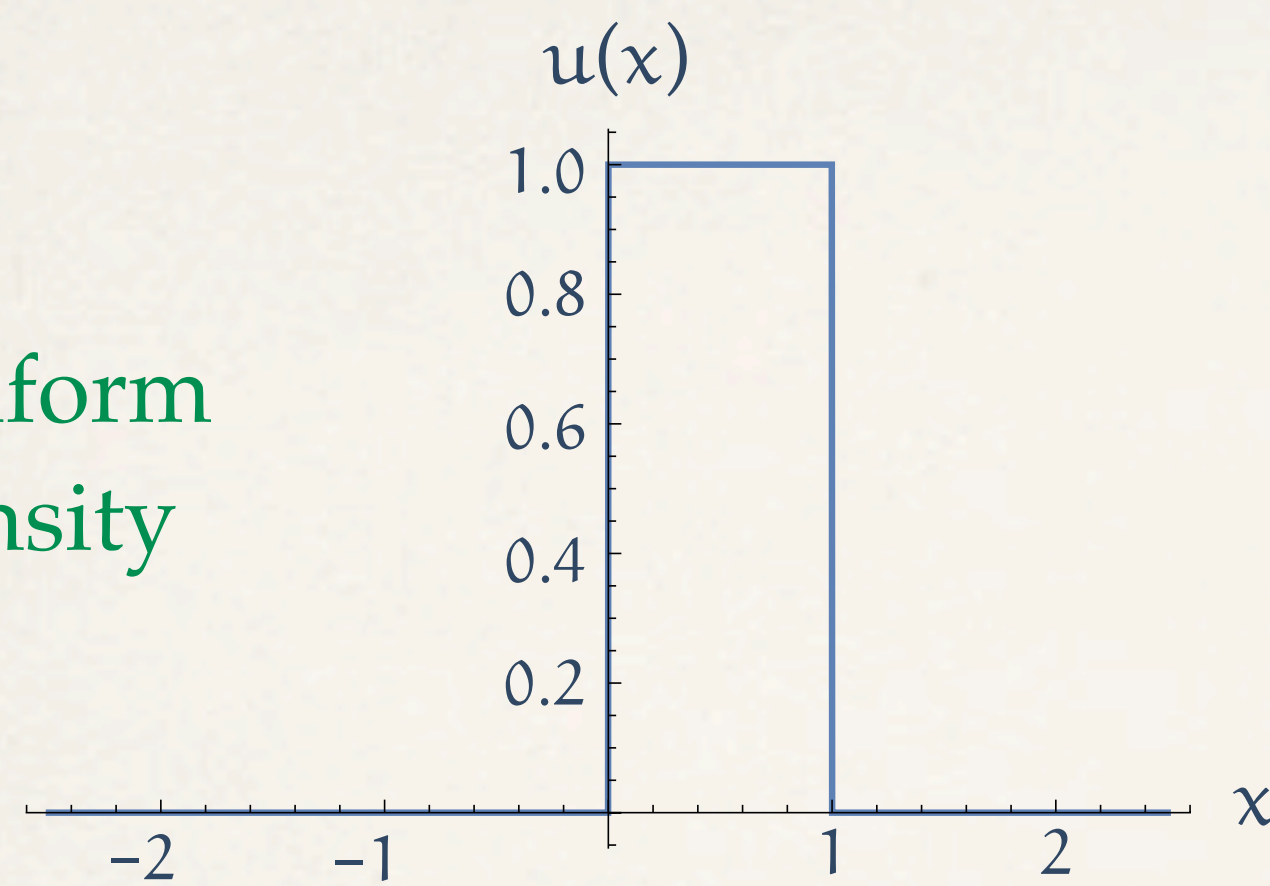


discrete analogue: binomial distribution

$$\phi(x) = \frac{e^{-x^2/2}}{\sqrt{2\pi}}$$



uniform
density



random choice

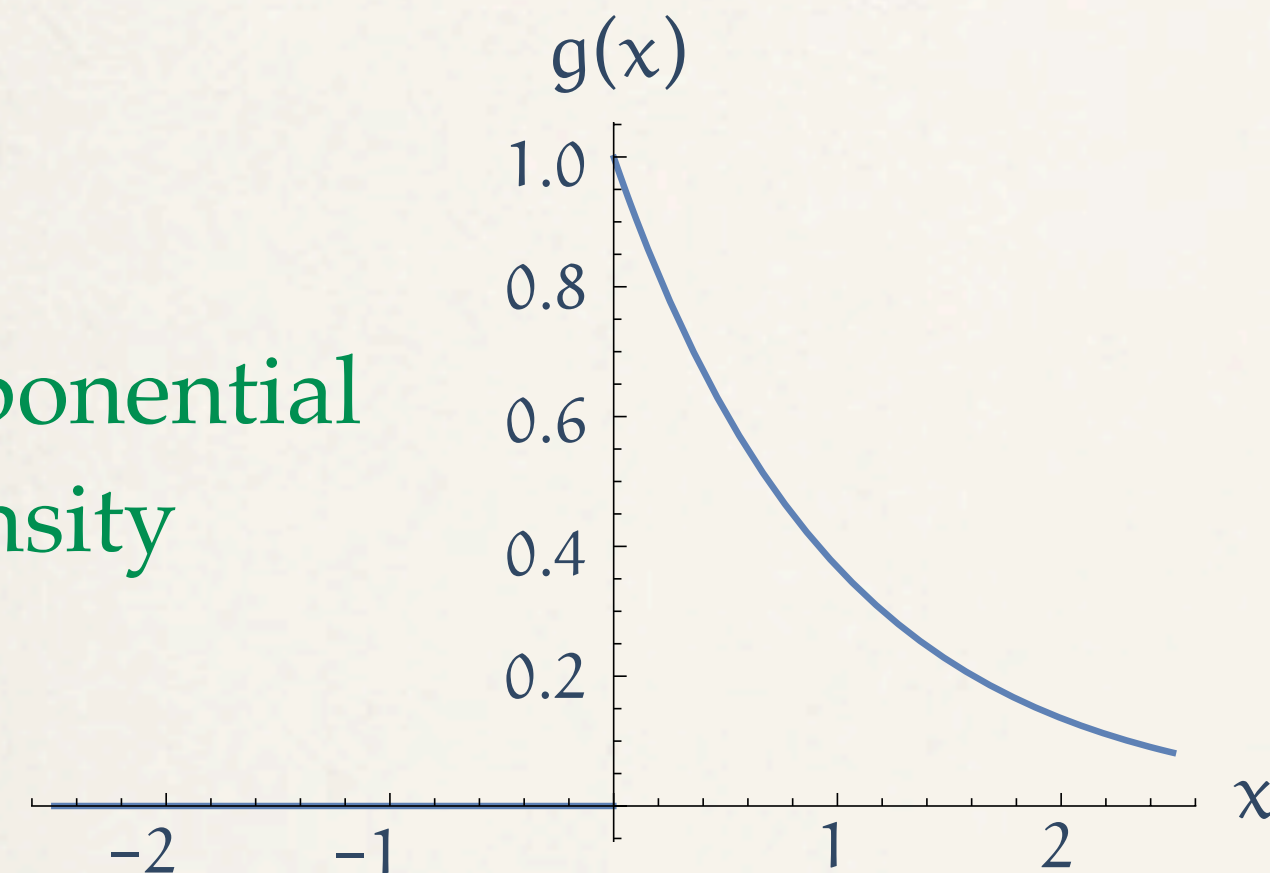
discrete analogue: combinatorial distribution

$$u(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\int_{-\infty}^{\infty} u(x) dx = \int_0^1 1 \cdot dx = x \Big|_0^1 = 1 - 0 = 1$$



exponential
density

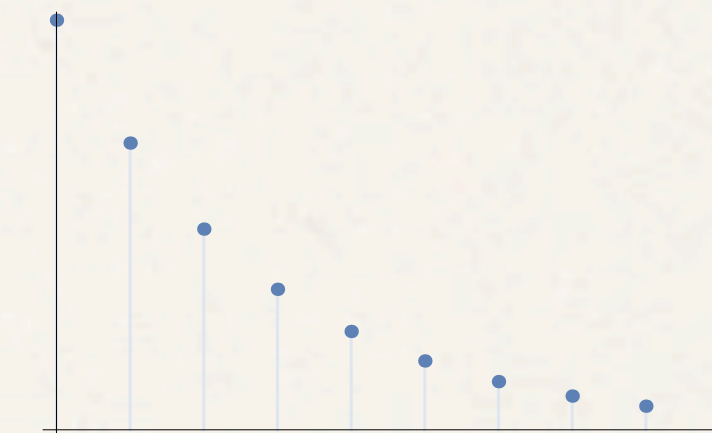


waiting times, queues

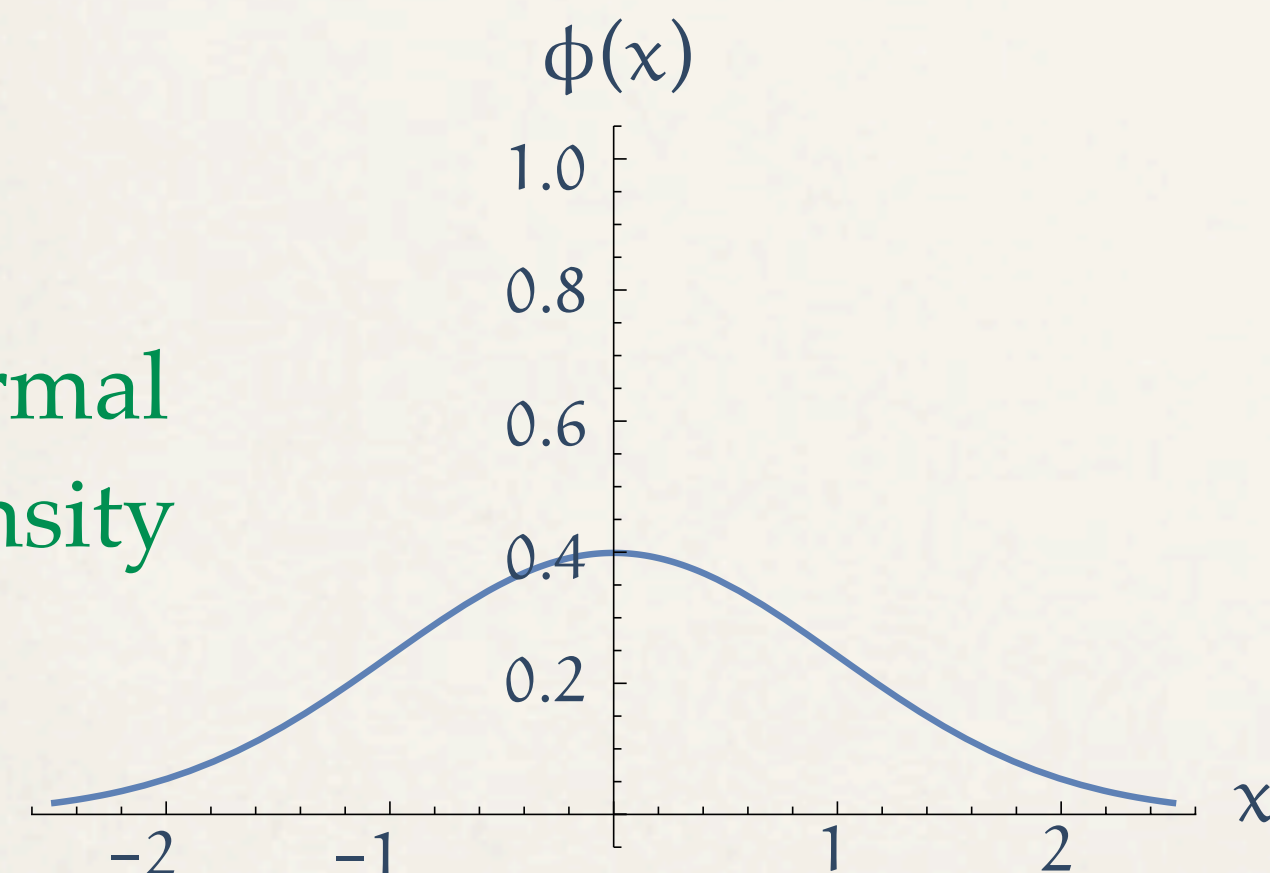
discrete analogue: geometric distribution

$$g(x) = \begin{cases} e^{-x} & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

$$\int_{-\infty}^{\infty} g(x) dx = \int_0^{\infty} e^{-x} dx = -e^{-x} \Big|_0^{\infty} = -0 + 1 = 1$$



normal
density



central tendency, bell curve

discrete analogue: binomial distribution

$$\phi(x) = \frac{e^{-x^2/2}}{\sqrt{2\pi}}$$

