



LEHMAN BROTHERS  
christies.com

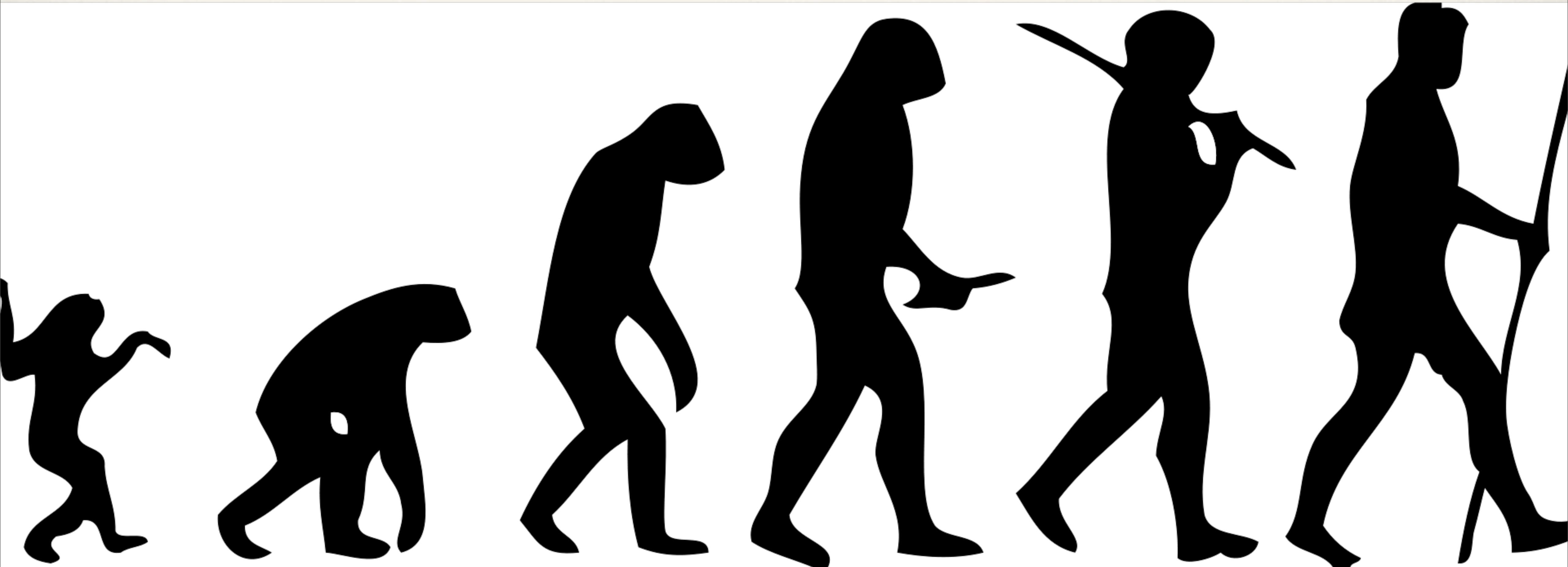
Lehman Brothers:  
Artwork & Ephemera

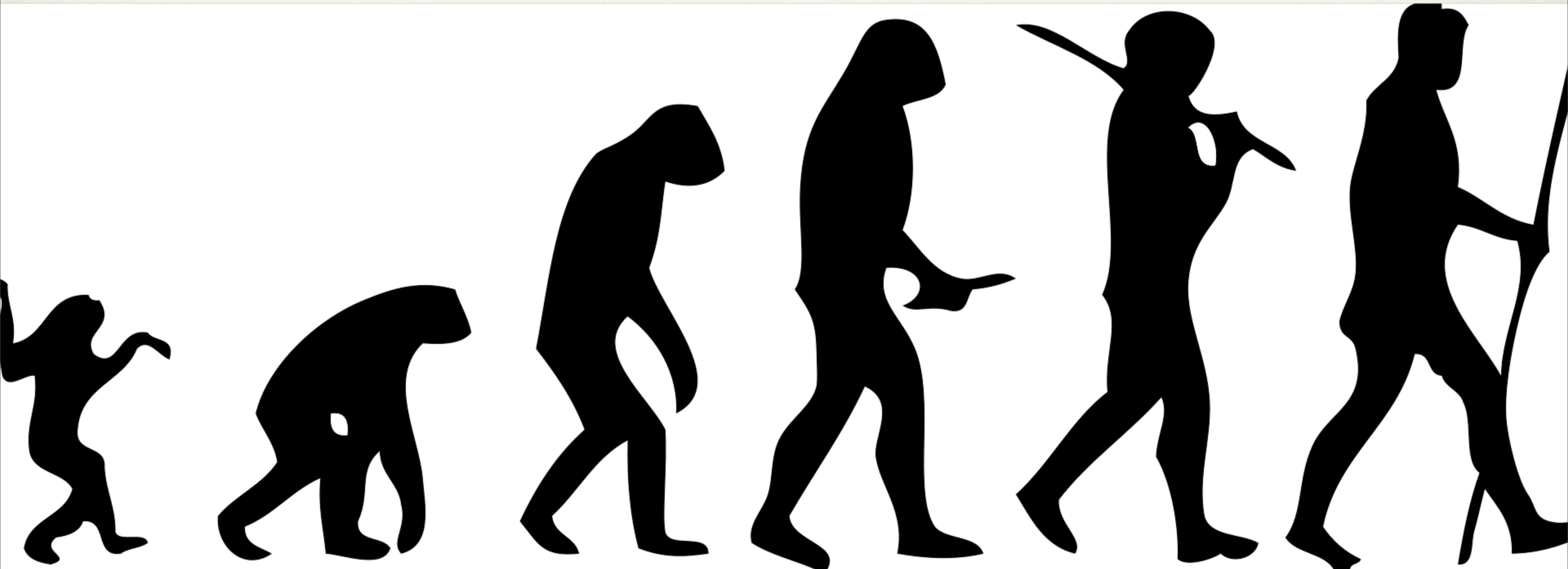
Sale date:  
Wednesday, 29th September, 12pm

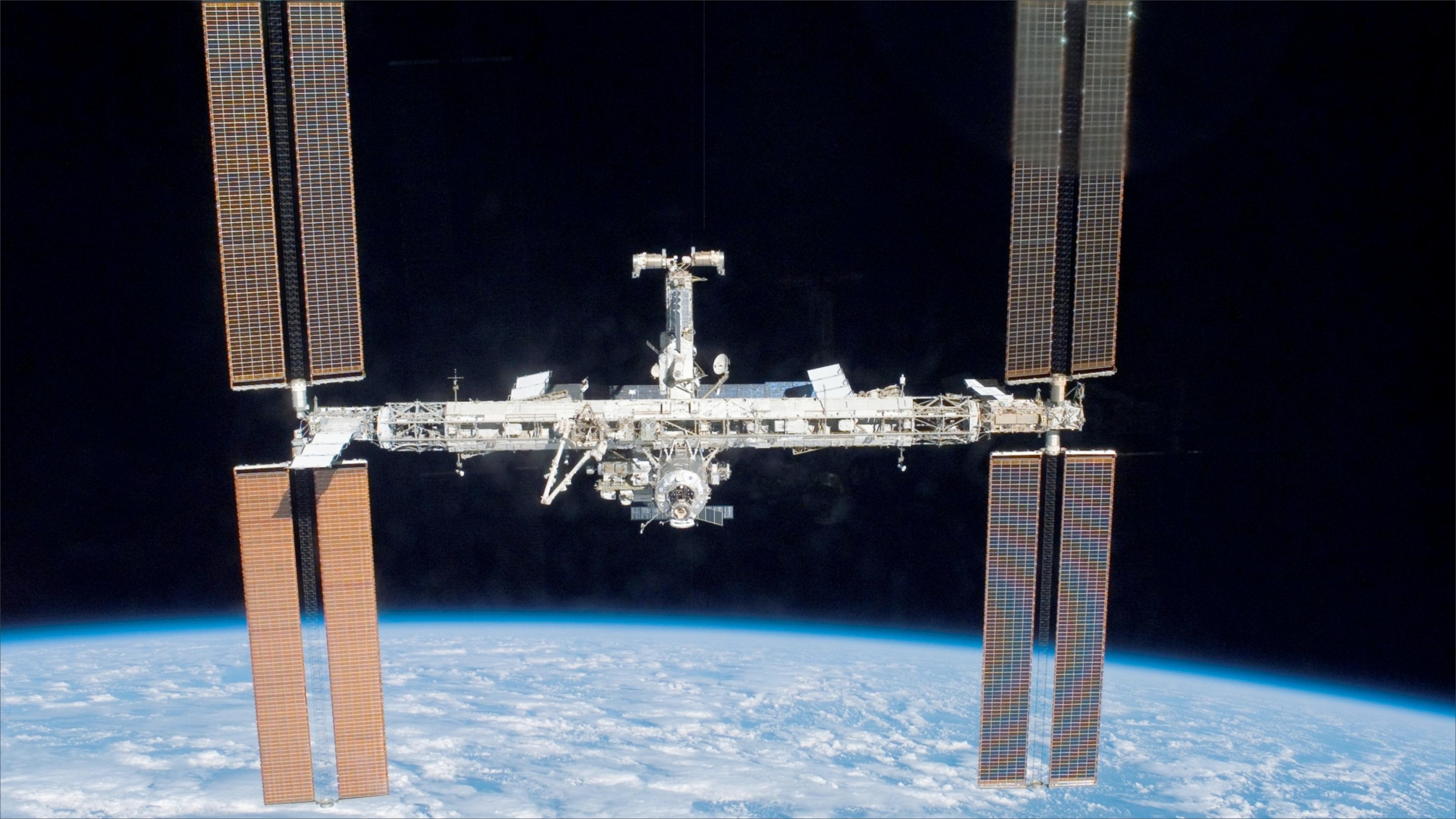
Lot 1002: Lehman Brothers Corporate Sign  
Polished & brushed metal

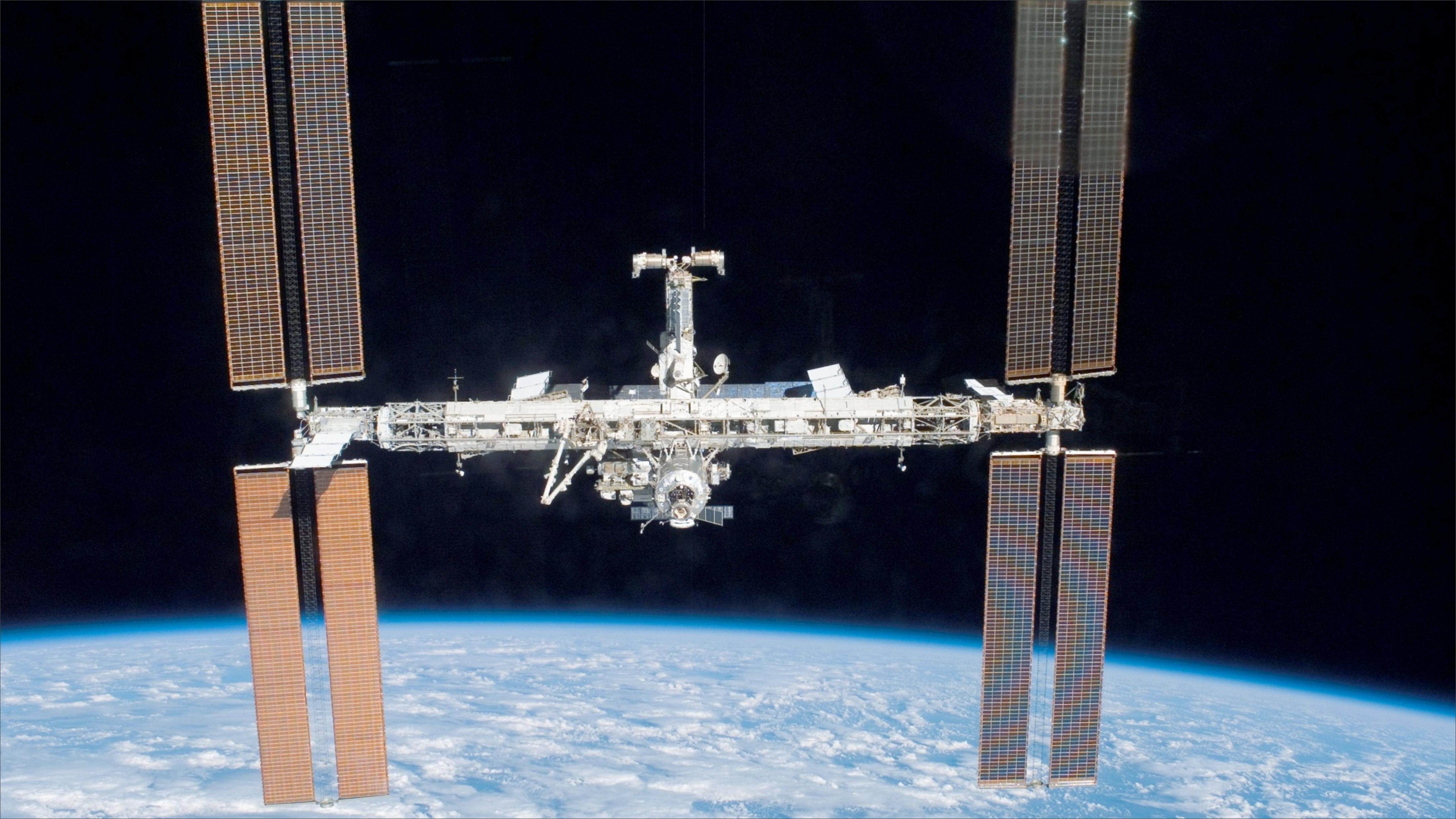
£2,000 - £3,000

$$P(H_{r+s} \mid H_r) \approx \frac{r+1}{s+r+1}$$











une Liste de  
Membres du  
Conseil des  
Cinq-Cents  
Resignation  
des Directoires

Buonaparte  
Seves - Ducos



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# A phenomenon's lifetime

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A phenomenon has continued unabated for  $R = r$  days. What are the chances that it will persist for another  $s$  days?

# The birth of a principle

$$P(H_{r+s} | H_r) \approx \frac{r+1}{s+r+1}$$



# The birth of a principle

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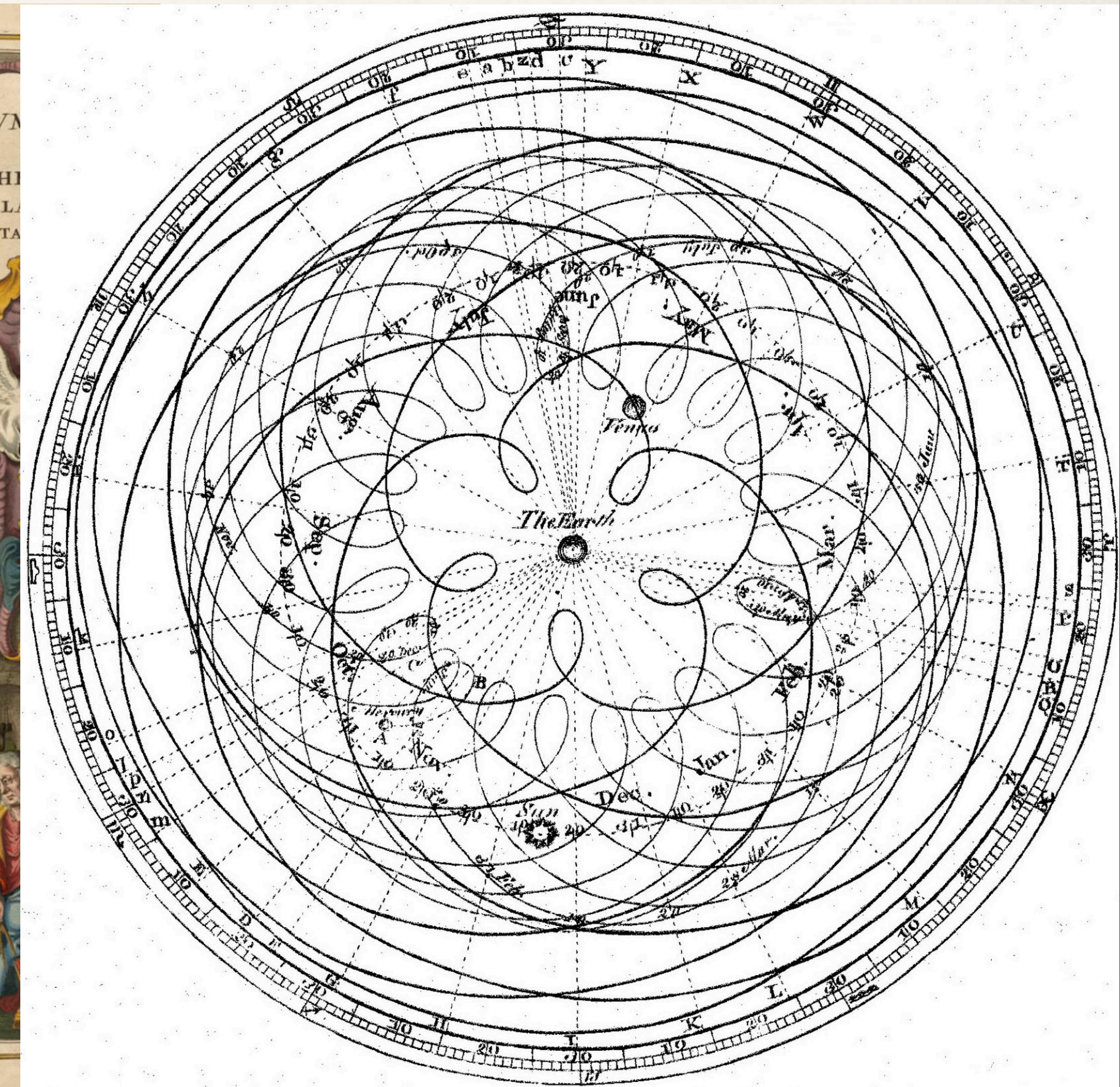
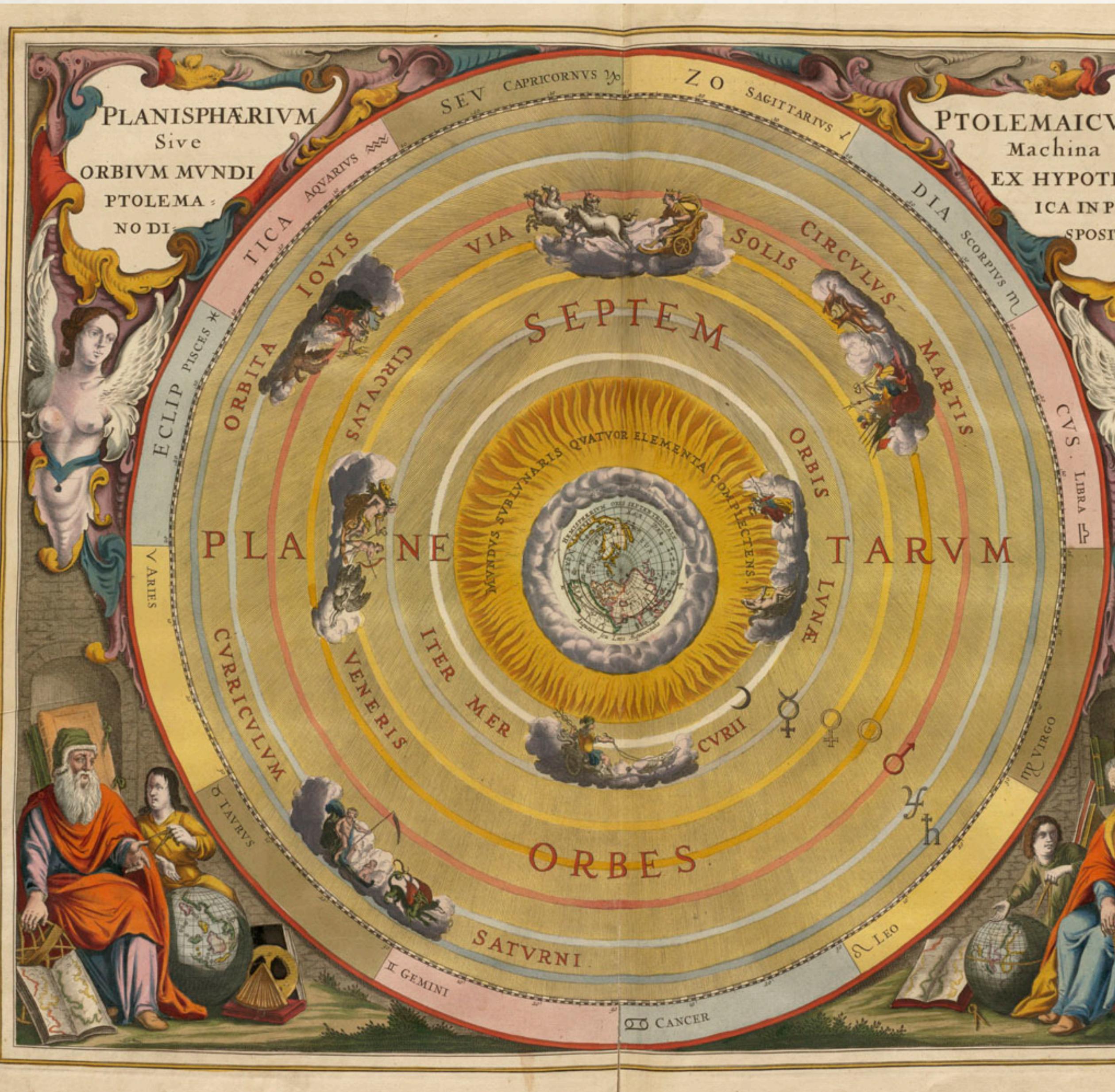


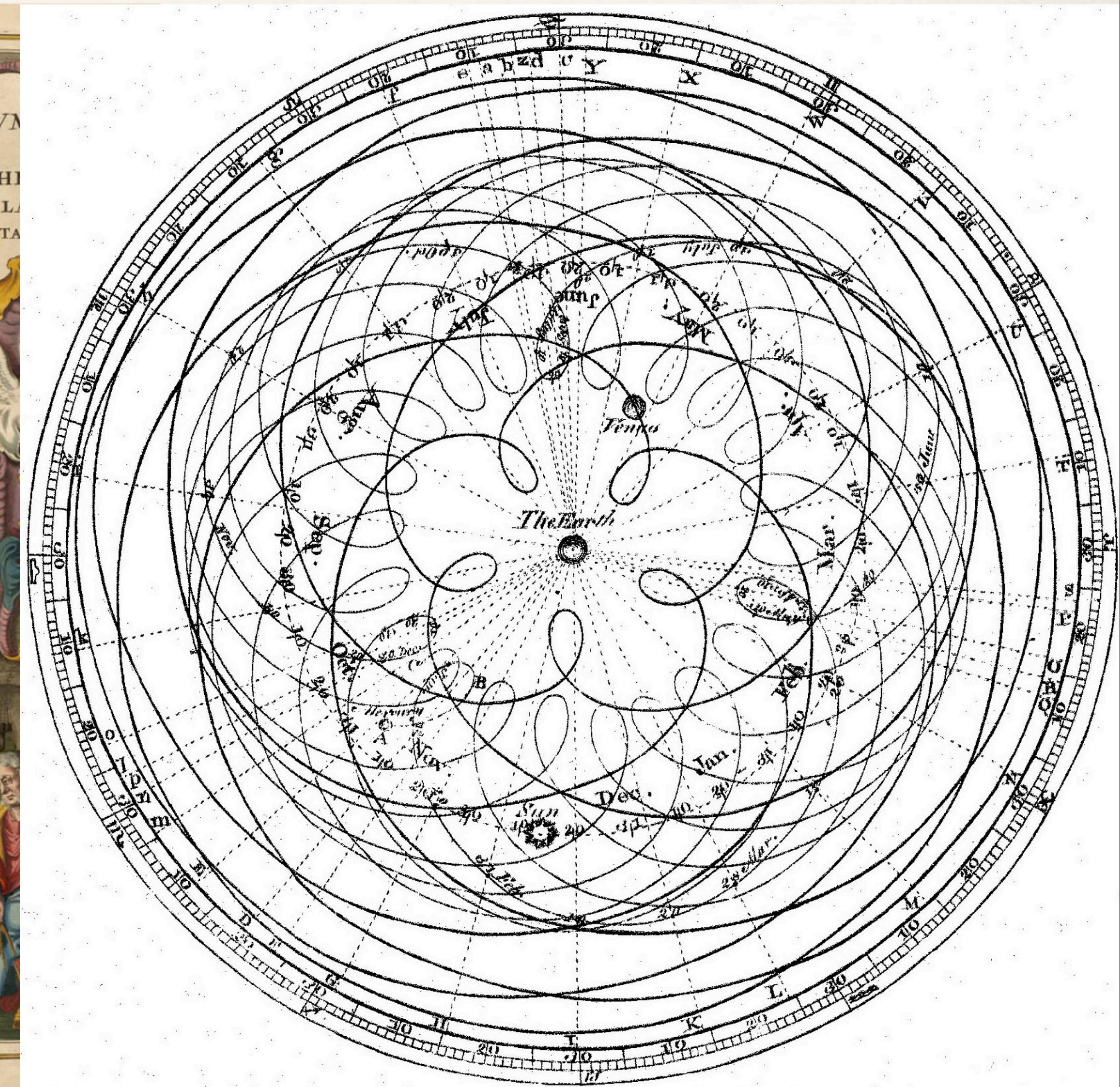
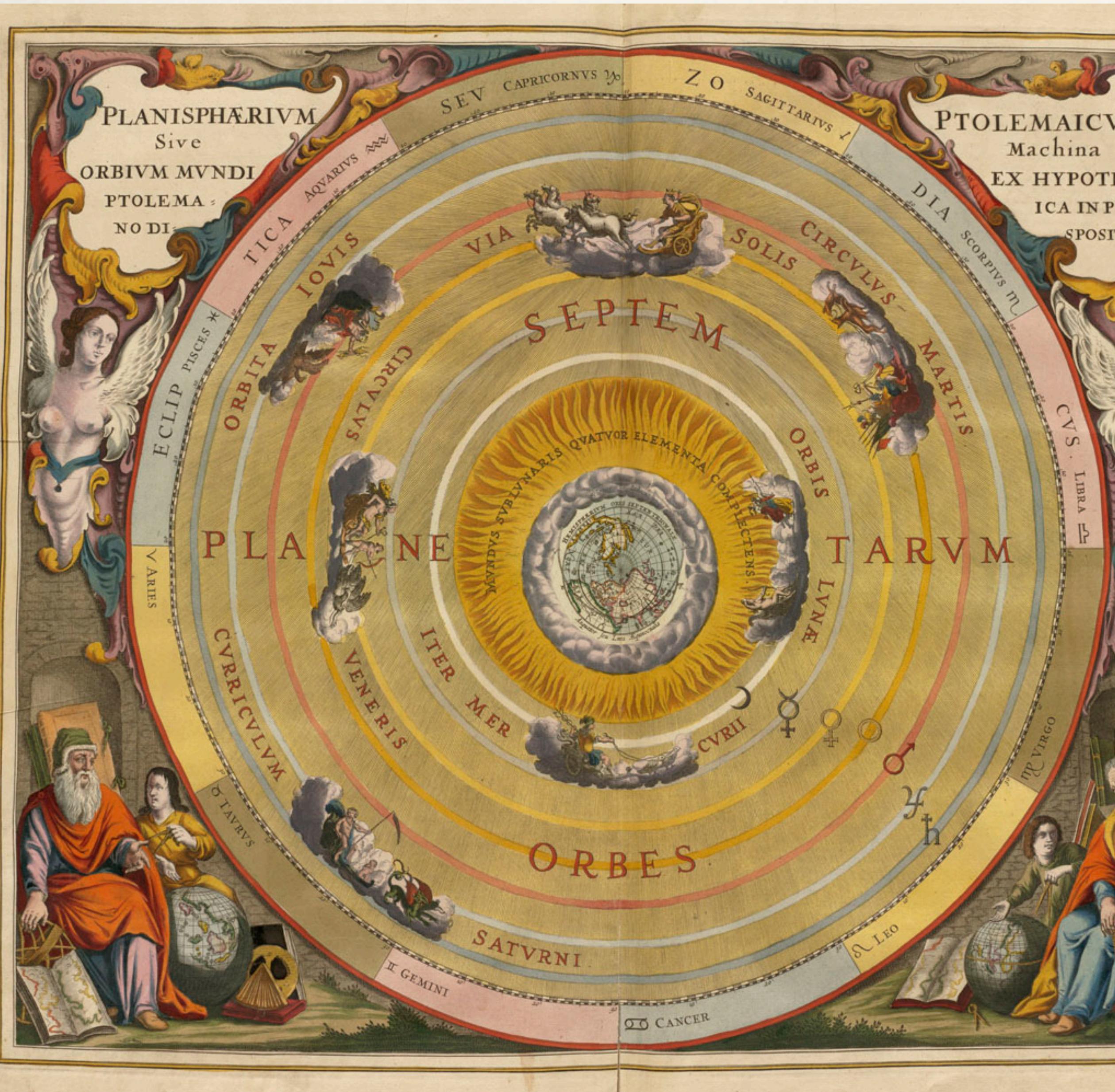
# The birth of a principle

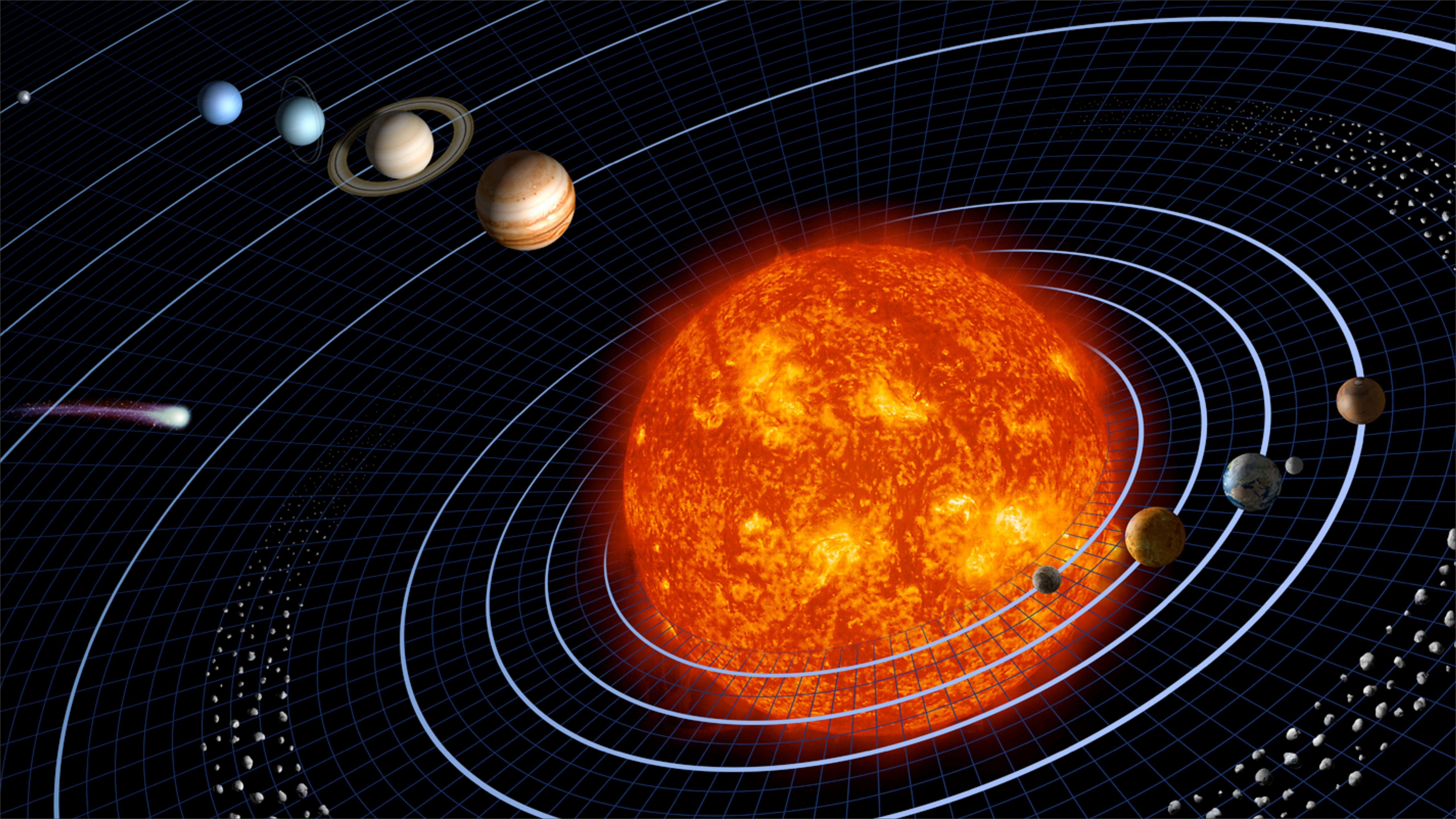
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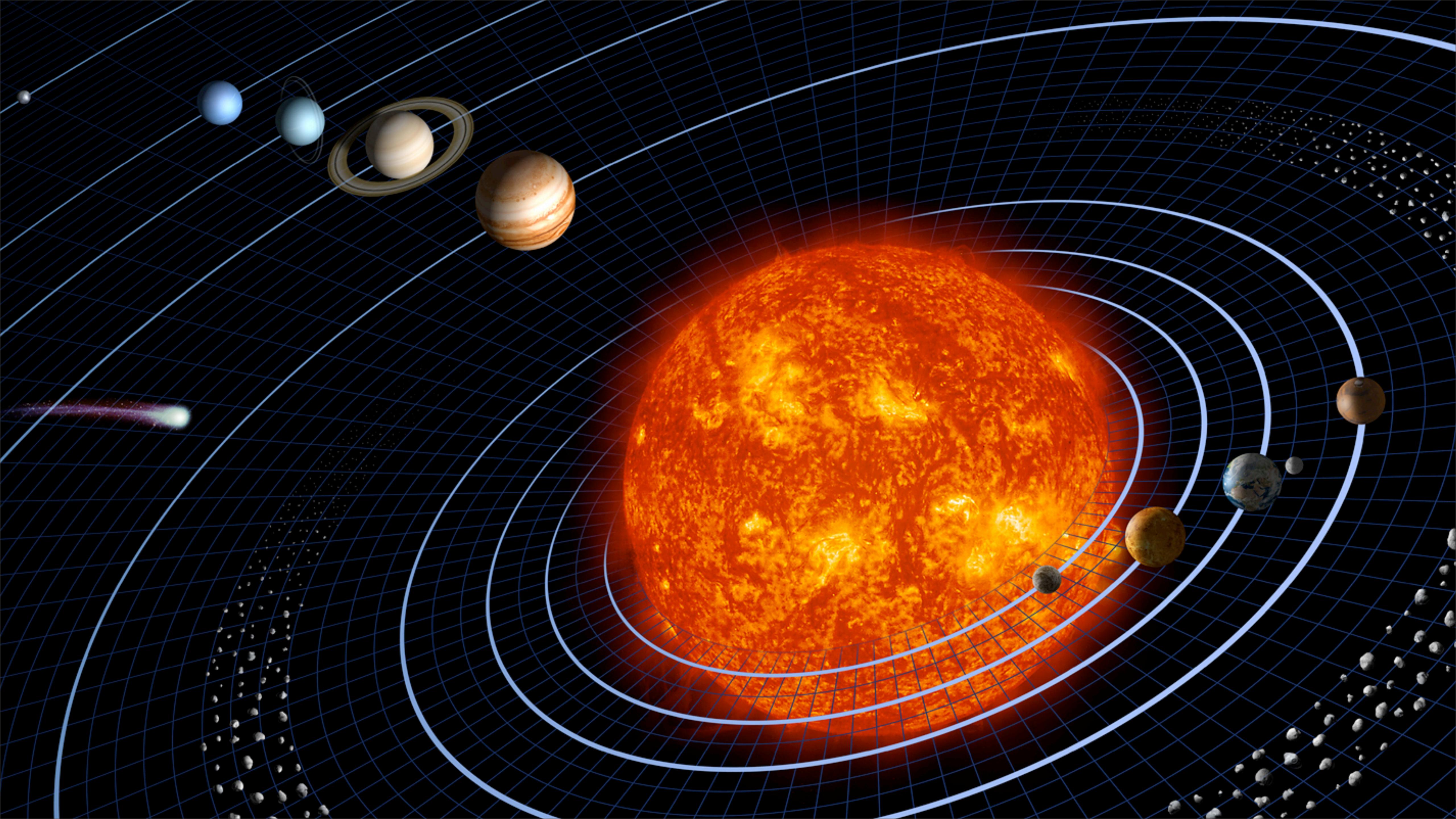


*The Copernican principle:* the observation point is not special.









$$P(H_{r+s} | H_r) \approx \frac{r+1}{s+r+1}$$



The *Copernican principle*: the observation point is not special.

A Laplacian prior:  $P\{S \geq s | R = r\} = \frac{r}{s+r}$

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The *Copernican principle*: the observation point is not special.

This is an assumption.

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Consequences: we're as likely to be in the first quartile of the phenomenon's existence as the last.

# Some diverting calculations

$$\mathbf{P}\{S \geq s \mid R = r\} = \frac{r}{s+r}$$

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$$\mathbf{P}\left\{\frac{1}{39}r \leq S < 39r \mid R = r\right\} = \mathbf{P}\left\{S \geq \frac{1}{39}r \mid R = r\right\} - \mathbf{P}\{S \geq 39r \mid R = r\}$$

# Some diverting calculations

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Additivity!

$$\mathbf{P}\left\{\frac{1}{39}r \leq S < 39r \mid R = r\right\} = \mathbf{P}\left\{S \geq \frac{1}{39}r \mid R = r\right\} - \mathbf{P}\{S \geq 39r \mid R = r\}$$

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# Some diverting calculations

$$\mathbf{P}\{S \geq s \mid R = r\} = \frac{r}{s+r}$$

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$$\mathbf{P}\left\{\frac{1}{3}r \leq S < 3r \mid R = r\right\} = \mathbf{P}\{S \geq \frac{1}{3}r \mid R = r\} - \mathbf{P}\{S \geq 3r \mid R = r\}$$

# Some diverting calculations

$$\mathbf{P}\{S \geq s \mid R = r\} = \frac{r}{s+r}$$

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Additivity!

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# Some diverting calculations

$$\mathbf{P}\{S \geq s \mid R = r\} = \frac{r}{s+r}$$

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Additivity!

$$\begin{aligned}\mathbf{P}\left\{\frac{1}{39}r \leq S < 39r \mid R = r\right\} &= \mathbf{P}\{S \geq \frac{1}{39}r \mid R = r\} - \mathbf{P}\{S \geq 39r \mid R = r\} \\ &= \frac{r}{\frac{r}{39} + r} - \frac{r}{39r + r} = \frac{39}{40} - \frac{1}{40} = 0.95\end{aligned}$$

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There is a 95% chance the phenomenon will not persist for more than 39 times the elapsed duration.  
There is a 50% chance the phenomenon will not persist for more than 3 times the elapsed duration.

# And some amusing consequences

J. R. Gott, *Nature* (363), 1993

- Assuming a 4,600 year existence, the Great Pyramid of Cheops will continue to fascinate and intrigue for no more than 180,000 years (at a 95% confidence).
- *Homo sapiens* is thought to have evolved around 200,000 years ago. With 95% confidence the Copernican principle predicts the species will become extinct within 7.8 million years (sic).
- *A doomsday principle*: the manned exploration of outer space has a history going back about 50 years. The Copernican principle suggests a future commitment to exploring space to last (at a 50% confidence) for no more than 150 years!
- **A word of caution**: the Copernican principle says that a long-running phenomenon is likely to persist for a long time; new phenomena are likely to be rapidly extinguished. Its applicability depends on the context.  
Proceed with care.

$$P\left\{ \frac{1}{39}r \leq S < 39r \mid R = r \right\} = 0.95$$

$$P\left\{ \frac{1}{3}r \leq S < 3r \mid R = r \right\} = 0.5$$