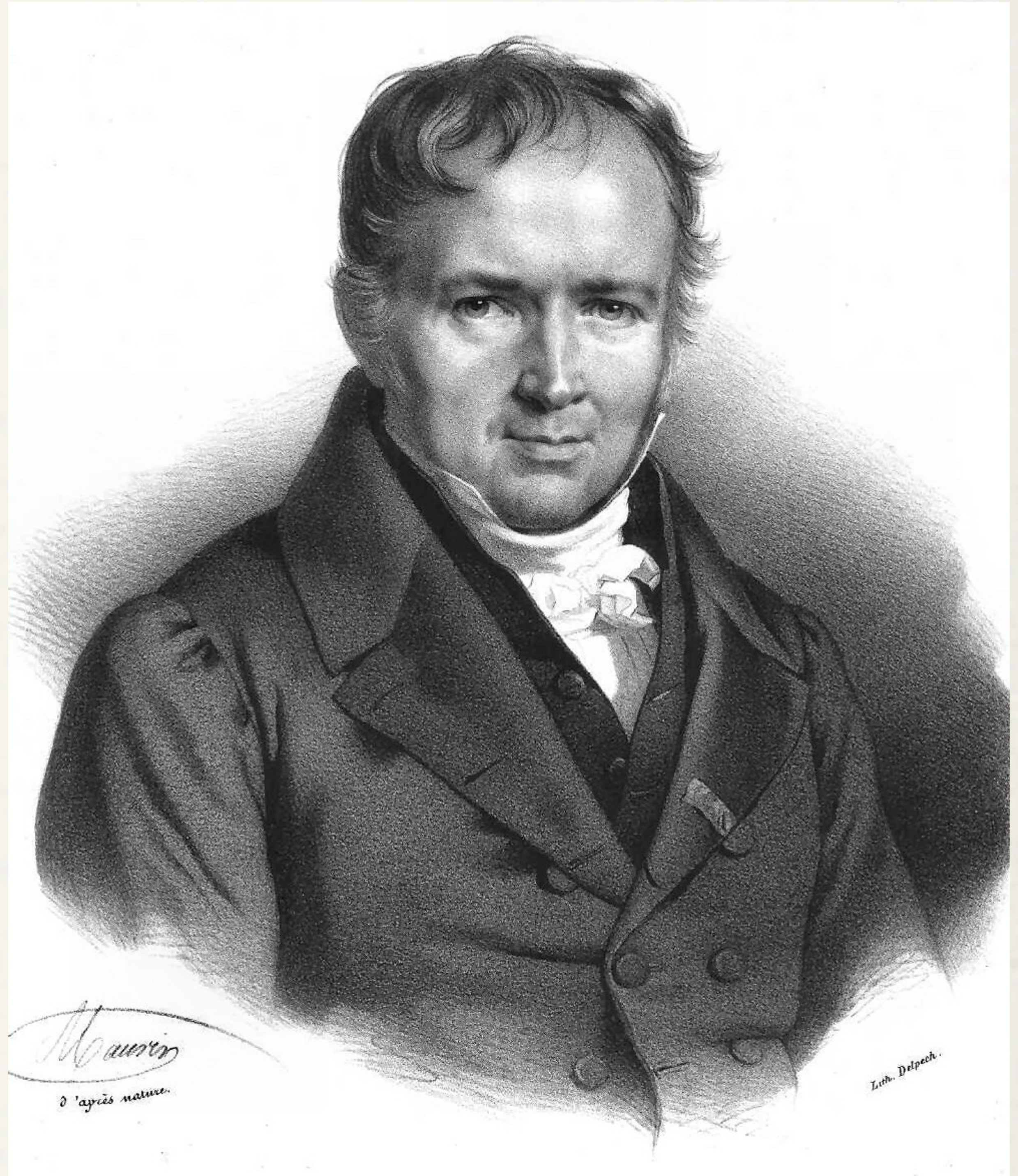
Siméon Denis Poisson



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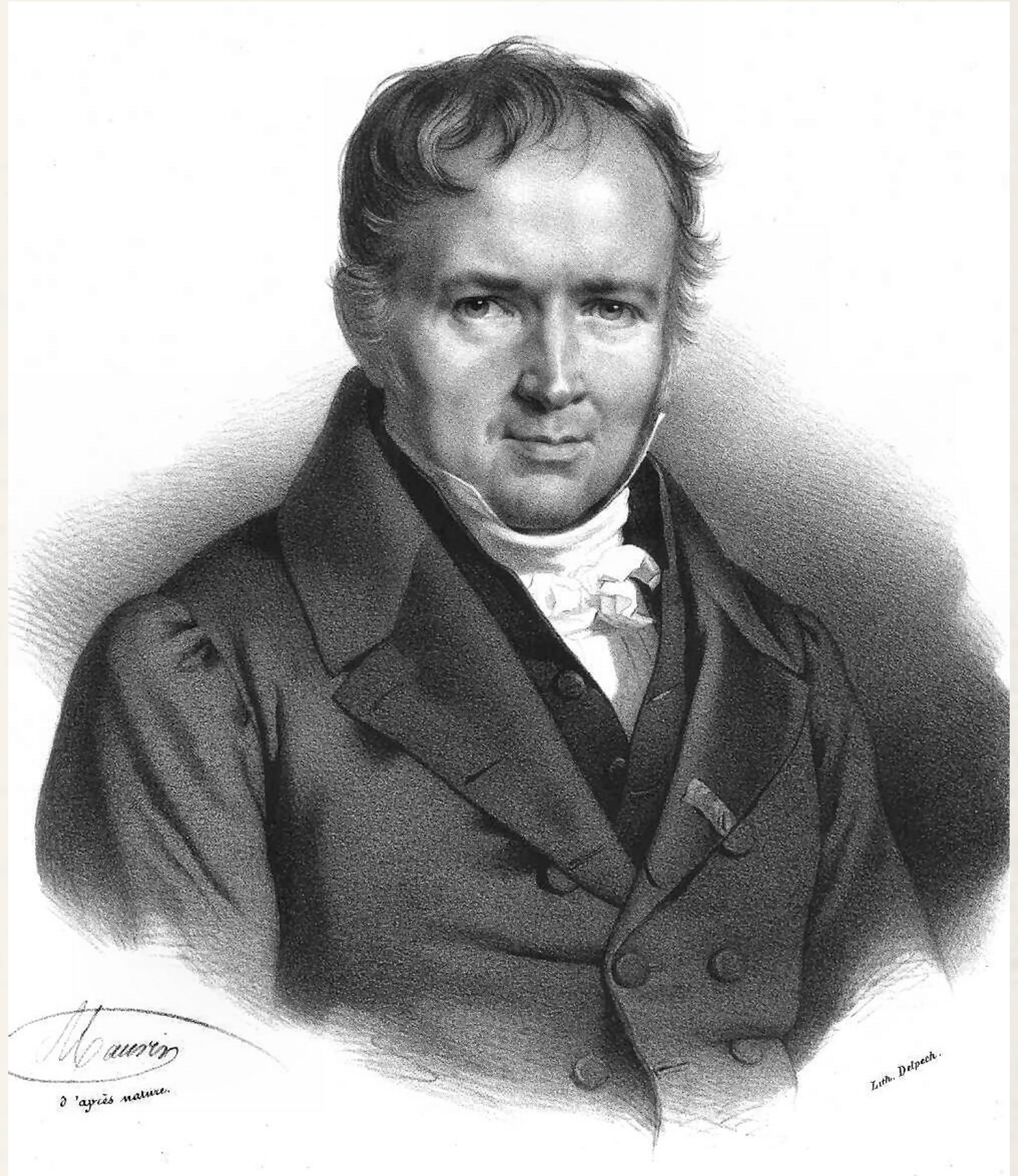

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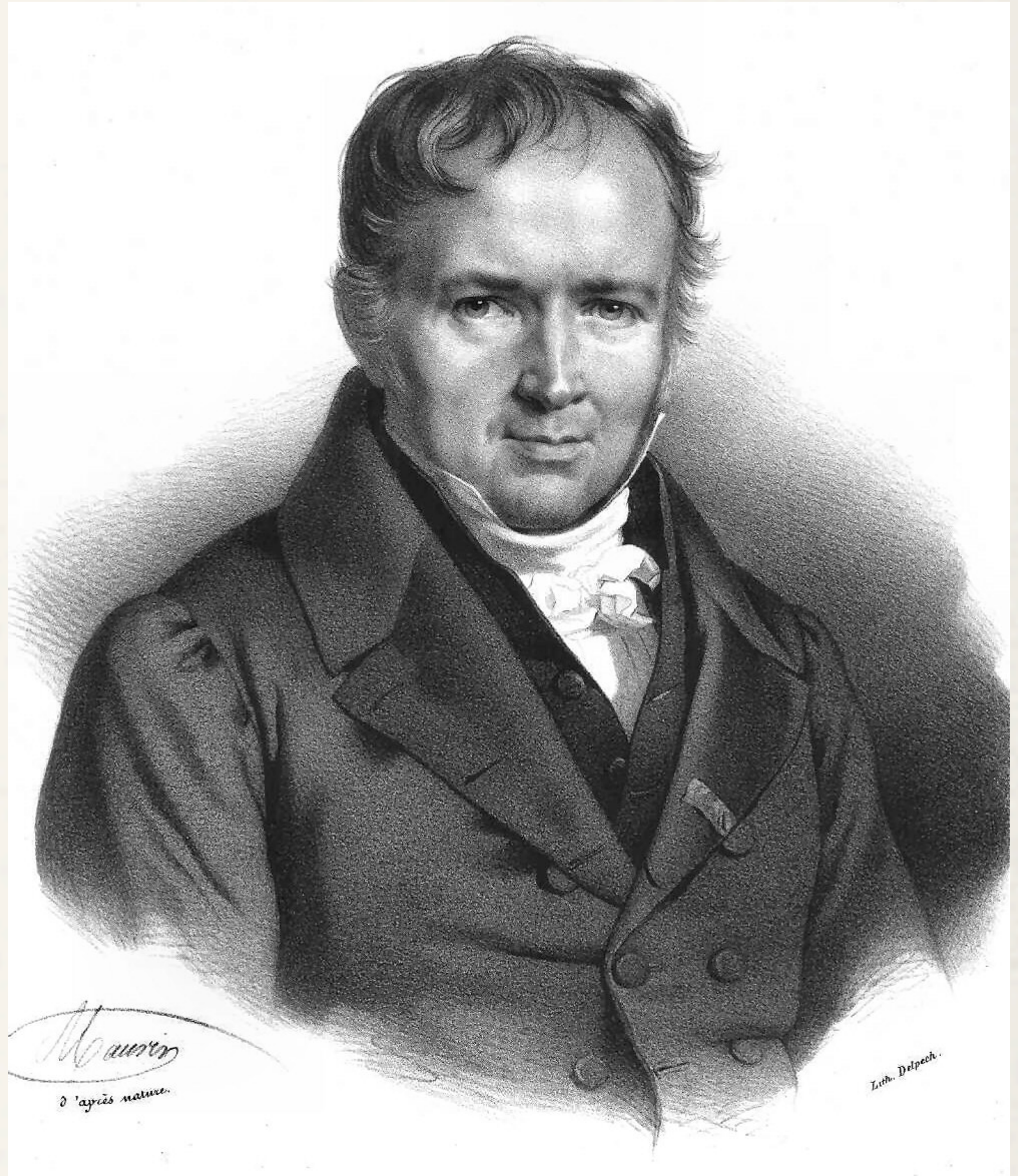

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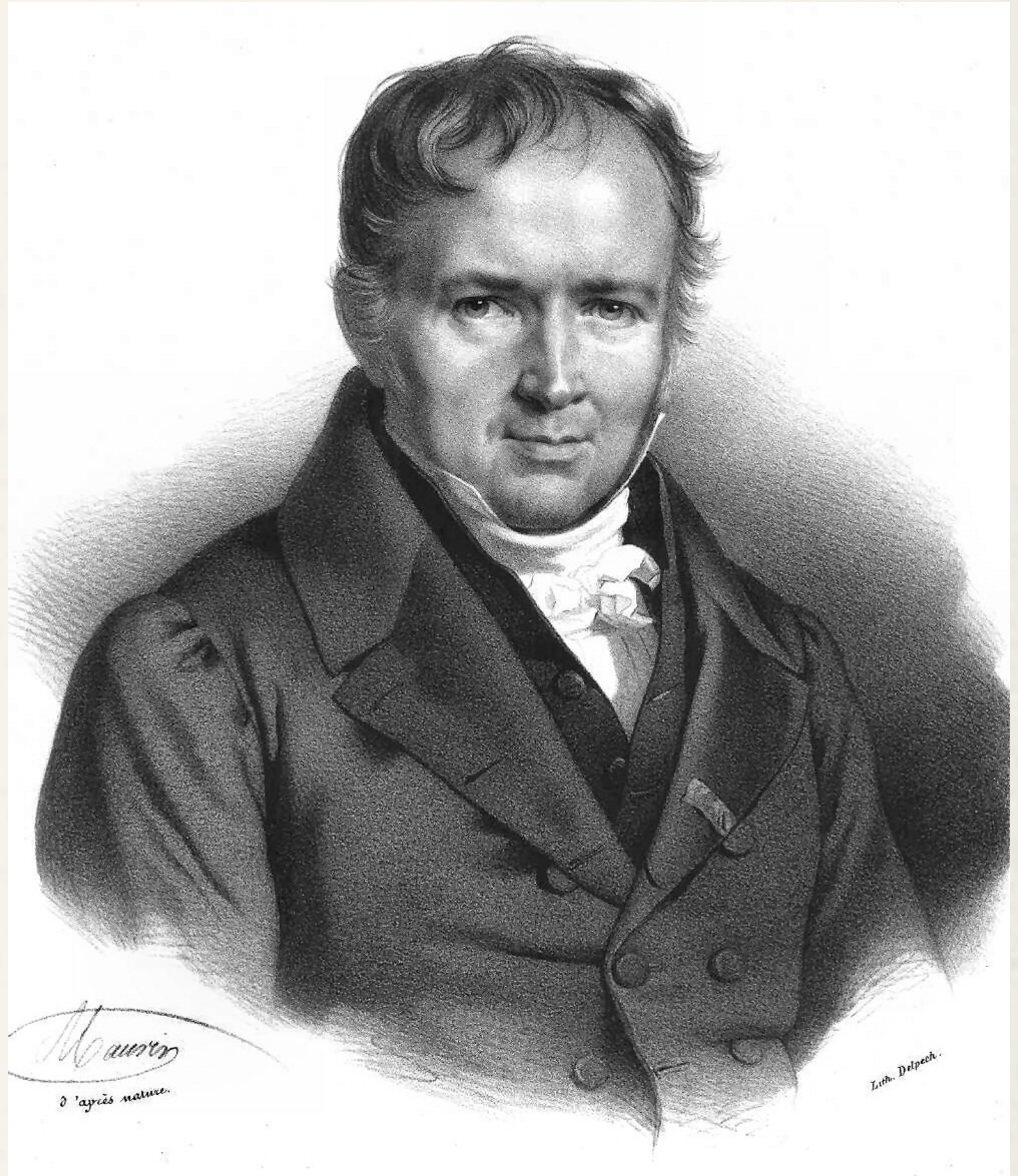

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In the years 1825–1830 in France, juries were comprised of twelve individuals with conviction requiring a vote of seven or more jurists voting to convict.

A probability space for jury verdicts

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The probability of conviction

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