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- *Distributive properties:* Unions distribute over intersections; intersections distribute over unions.

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De Morgan’s laws

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