

Problem 10.2

Assume we have a language consisting of object constants *abby*, *bess*, *cody*, *dana* and no function constants.

Prove the goal from the given premises.

Proof Editor		
1.	likes(abby,bess)	Premise
2.	likes(cody,dana)	Premise
3.	$\text{AX:AY:}(\text{likes(X,Y)} \Rightarrow \text{likes(Y,X)})$	Premise
4.	$\text{AY:}(\text{likes(abby,Y)} \Rightarrow \text{likes(Y,abby)})$	Universal Elimination: 3
5.	$\text{likes(abby,bess)} \Rightarrow \text{likes(bess,abby)}$	Universal Elimination: 4
6.	likes(bess,abby)	Implication Elimination: 5, 1
7.	$\text{AY:}(\text{likes(cody,Y)} \Rightarrow \text{likes(Y,cody)})$	Universal Elimination: 3
8.	$\text{likes(cody,dana)} \Rightarrow \text{likes(dana,cody)}$	Universal Elimination: 7
9.	likes(dana,cody)	Implication Elimination: 8, 2
10.	EY:likes(Y,bess)	Existential Introduction: 1
11.	EY:likes(Y,dana)	Existential Introduction: 2
12.	EY:likes(Y,abby)	Existential Introduction: 6
13.	EY:likes(Y,cody)	Existential Introduction: 9
14.	AX:EY:likes(Y,X)	Domain Closure: 12, 10, 13, 11

Assumption

Reiteration

Delete

Negation Introduction

Negation Elimination

And Introduction

And Elimination

Or Introduction

Or Elimination

Implication Introduction

Implication Elimination

Biconditional Introduction

Biconditional Elimination

Universal Introduction

Universal Elimination

Existential Introduction

Existential Elimination

Domain Closure