

Questions This test exercise is of an applied nature and uses data that are available in the data file TestExer3. We consider the so-called Taylor rule for setting the (nominal) interest rate. This model describes the level of the nominal interest rate that the central bank sets as a function of equilibrium real interest rate and inflation, and considers the current level of inflation and production. Taylor (1993)<sup>1</sup> considers the model:

$$it = r^* + \pi_t + 0.5(\pi_t - \pi^*) + 0.5gt,$$

with  $it$  the Federal funds target interest rate at time  $t$ ,  $r^*$  the equilibrium real federal funds rate,  $\pi_t$  a measure of inflation,  $\pi^*$  the target inflation rate and  $gt$  the output gap (how much actual output deviates from potential output). We simplify the Taylor rule in two manners. First, we avoid determining  $r^*$  and  $\pi^*$  and simply add an intercept to the model to capture these two variables (and any other deviations in the means). Second, we consider production  $yy$  rather than the output gap. In this form the Taylor rule is

$$it = \beta_1 + \beta_2\pi_t + \beta_3y_t + \epsilon_t. \quad (1)$$

Monthly data are available for the USA over the period 1960 through 2014 for the following variables:<sup>2</sup>

- INTRATE: Federal funds interest rate
- INFL: Inflation
- PROD: Production
- UNEMPL: Unemployment
- COMMPRI: Commodity prices
- PCE: Personal consumption expenditure
- PERSINC: Personal income
- HOUST: Housing starts

**(a) Use general-to-specific to come to a model. Start by regressing the federal funds rate on the other 7 variables and eliminate 1 variable at a time.**

#### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup>	Aj	ECMP	AIC	BIC
INTRATE	660	0.56	0.56	5.82	3034.26	3047.74	

*Eliminación backward. Máximo p-valor para retener: 0.05*

*Número original de regresoras: 1, regresoras retenidas en el modelo 1*

### Coefficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	1.64	0.16	1.33	1.96	10.37	<0.0001		
INFL	0.94	0.03	0.88	1.01	28.93	<0.0001	836.70	1.00

Error cuadrático medio: 5.774363

### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.61	0.61	5.14	2951.85	2969.82

Eliminación backward. Máximo p-valor para retener: 0.05  
Número original de regresoras: 2, regresoras retenidas en el modelo 2

### Coefficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	0.45	0.20	0.07	0.83	2.31	0.0211		
INFL	1.01	0.03	0.95	1.07	32.16	<0.0001	1034.45	1.05
PERSINC	0.44	0.05	0.35	0.53	9.47	<0.0001	91.50	1.05

Error cuadrático medio: 5.088859

### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.62	0.62	5.12	2946.77	2969.23

Eliminación backward. Máximo p-valor para retener: 0.05  
Número original de regresoras: 3, regresoras retenidas en el modelo 3

### Coefficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	0.45	0.19	0.07	0.83	2.32	0.0208		
INFL	0.99	0.03	0.93	1.05	30.70	<0.0001	943.82	1.12
PERSINC	0.35	0.05	0.25	0.46	6.46	<0.0001	44.64	1.52
UNEMPL	0.14	0.05	0.04	0.25	2.66	0.0080	10.07	1.45

Error cuadrático medio: 5.042220

### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.62	0.62	5.09	2942.16	2964.62

Eliminación backward. Máximo p-valor para retener: 0.05  
Número original de regresoras: 4, regresoras retenidas en el modelo 3

### Coeficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	0.02	0.23	-0.43	0.48	0.10	0.9190		
INFL	0.87	0.05	0.77	0.97	17.23	<0.0001	299.43	2.79
PERSINC	0.30	0.06	0.19	0.42	5.12	<0.0001	29.16	1.79
PCE	0.18	0.05	0.08	0.29	3.42	0.0007	14.70	2.96

Error cuadrático medio: 5.007160

### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.63	0.63	4.94	2920.38	2947.33

Eliminación backward. Máximo p-valor para retener: 0.05

Número original de regresoras: 5, regresoras retenidas en el modelo 4

### Coeficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	-0.21	0.23	-0.66	0.24	-0.91	0.3633		
INFL	0.74	0.06	0.63	0.86	13.19	<0.0001	177.58	3.57
PERSINC	0.26	0.06	0.14	0.37	4.33	<0.0001	22.71	1.84
PCE	0.31	0.06	0.20	0.43	5.32	<0.0001	32.24	3.72
HOUST	-0.02	4.4E-03	-0.03	-0.01	-4.90	<0.0001	28.00	1.37

Error cuadrático medio: 4.837317

### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.64	0.63	4.90	2914.28	2945.72

Eliminación backward. Máximo p-valor para retener: 0.05

Número original de regresoras: 6, regresoras retenidas en el modelo 5

### Coeficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	-0.24	0.23	-0.69	0.22	-1.03	0.3051		
INFL	0.72	0.06	0.61	0.83	12.60	<0.0001	163.46	3.67
PERSINC	0.24	0.06	0.12	0.36	4.05	0.0001	21.40	1.86
PCE	0.34	0.06	0.22	0.46	5.76	<0.0001	38.14	3.84
HOUST	-0.02	4.4E-03	-0.03	-0.01	-4.68	<0.0001	26.89	1.38
COMPRI	-0.01	2.6E-03	-0.01	-2.3E-03	-2.84	0.0046	13.06	1.07

Error cuadrático medio: 4.785620

### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.64	0.63	4.90	2914.28	2945.72

Eliminación backward. Máximo p-valor para retener: 0.05  
Número original de regresoras: 7, regresoras retenidas en el modelo 5

### Coefficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	Cp	Mallows	VIF
const	-0.24	0.23	-0.69	0.22	-1.03	0.3051			
INFL	0.72	0.06	0.61	0.83	12.60	<0.0001	163.46	3.67	
PERSINC	0.24	0.06	0.12	0.36	4.05	0.0001	21.40	1.86	
PCE	0.34	0.06	0.22	0.46	5.76	<0.0001	38.14	3.84	
HOUST	-0.02	4.4E-03	-0.03	-0.01	-4.68	<0.0001	26.89	1.38	
COMMPRI	-0.01	2.6E-03	-0.01	-2.3E-03	-2.84	0.0046	13.06	1.07	

Error cuadrático medio: 4.785620

Coefficients <sup>a</sup>								
Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.	95.0% Confidence Interval for B	
		B	Std. Error	Beta			Lower Bound	Upper Bound
1	(Constant)	-.215	.245		-.877	.381	-.695	.266
	INFL	.697	.062	.552	11.233	.000	.575	.819
	PROD	-.058	.040	-.076	-1.445	.149	-.136	.021
	UNEMPL	.104	.097	.056	1.078	.282	-.086	.294
	COMMPRI	-.006	.003	-.051	-1.858	.064	-.011	.000
	PCE	.343	.069	.268	4.949	.000	.207	.479
	PERSINC	.246	.061	.134	4.071	.000	.128	.365
	HOUST	-.019	.005	-.122	-4.157	.000	-.029	-.010
2	(Constant)	-.286	.236		-1.211	.226	-.749	.178
	INFL	.694	.062	.550	11.198	.000	.572	.816
	PROD	-.025	.026	-.033	-.963	.336	-.075	.026
	COMMPRI	-.007	.003	-.060	-2.316	.021	-.012	-.001
	PCE	.367	.065	.287	5.611	.000	.239	.496
	PERSINC	.251	.060	.136	4.161	.000	.133	.370
	HOUST	-.021	.004	-.132	-4.760	.000	-.030	-.012
3	(Constant)	-.236	.230		-1.026	.305	-.688	.216
	INFL	.718	.057	.568	12.598	.000	.606	.830
	COMMPRI	-.007	.003	-.069	-2.842	.005	-.013	-.002
	PCE	.340	.059	.266	5.761	.000	.224	.456
	PERSINC	.240	.059	.130	4.052	.000	.124	.357
	HOUST	-.021	.004	-.129	-4.682	.000	-.029	-.012

a. Dependent Variable: INTRATE

$$\text{INTRATE} = -0.236 + 0.718 \cdot \text{INFL} + 0.240 \cdot \text{PERSINC} + 0.340 \cdot \text{PCE} - 0.021 \cdot \text{HOUST} - 0.007 \cdot \text{COMMPRI}$$

(b) Use specific-to-general to come to a model. Start by regressing the federal funds rate on only a constant and add 1 variable at a time. Is the model the same as in (a)?

## Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.64	0.63	4.93	2915.34	2951.28

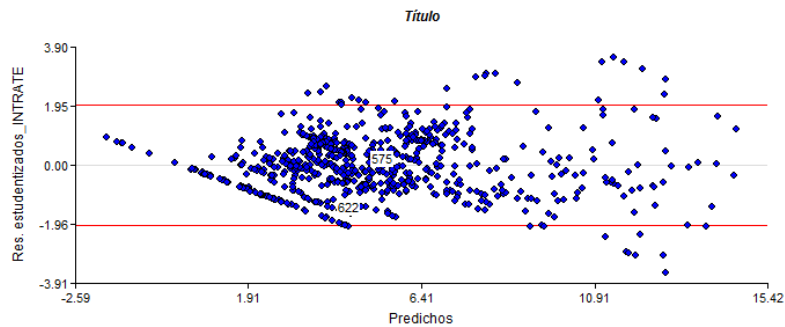
Selección Forward. Máximo p-valor para entrar: 0.05

Número original de regresoras: 7, regresoras retenidas en el modelo 6

## Coeficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	-0.29	0.24	-0.75	0.18	-1.21	0.2263		
PCE	0.37	0.07	0.24	0.50	5.61	<0.0001	37.43	4.72
PROD	-0.02	0.03	-0.08	0.03	-0.96	0.3357	6.93	2.06
INFL	0.69	0.06	0.57	0.82	11.20	<0.0001	131.20	4.35
HOUST	-0.02	4.4E-03	-0.03	-0.01	-4.76	<0.0001	28.63	1.40
PERSINC	0.25	0.06	0.13	0.37	4.16	<0.0001	23.29	1.93
COMMPRI	-0.01	2.8E-03	-0.01	-9.9E-04	-2.32	0.0209	11.36	1.23

Error cuadrático medio: 4.786145



## Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.64	0.63	4.90	2914.28	2945.72

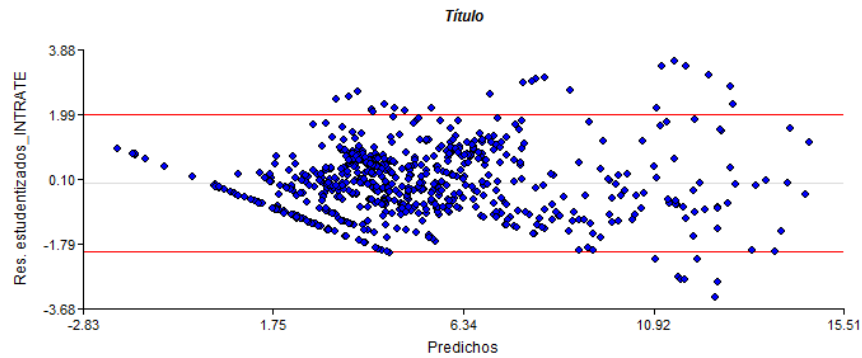
Selección Forward. Máximo p-valor para entrar: 0.05

Número original de regresoras: 6, regresoras retenidas en el modelo 5

## Coeficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	-0.24	0.23	-0.69	0.22	-1.03	0.3051		
INFL	0.72	0.06	0.61	0.83	12.60	<0.0001	163.46	3.67
PCE	0.34	0.06	0.22	0.46	5.76	<0.0001	38.14	3.84
HOUST	-0.02	4.4E-03	-0.03	-0.01	-4.68	<0.0001	26.89	1.38
PERSINC	0.24	0.06	0.12	0.36	4.05	0.0001	21.40	1.86
COMMPRI	-0.01	2.6E-03	-0.01	-2.3E-03	-2.84	0.0046	13.06	1.07

Error cuadrático medio: 4.785620



### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.63	0.63	4.94	2920.38	2947.33

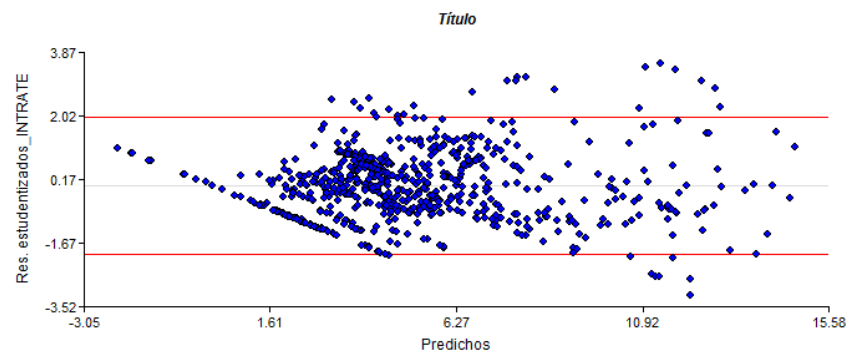
Selección Forward. Máximo p-valor para entrar: 0.05

Número original de regresoras: 5, regresoras retenidas en el modelo 4

### Coefficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	-0.21	0.23	-0.66	0.24	-0.91	0.3633		
PCE	0.31	0.06	0.20	0.43	5.32	<0.0001	32.24	3.72
INFL	0.74	0.06	0.63	0.86	13.19	<0.0001	177.58	3.57
HOUST	-0.02	4.4E-03	-0.03	-0.01	-4.90	<0.0001	28.00	1.37
PERSINC	0.26	0.06	0.14	0.37	4.33	<0.0001	22.71	1.84

Error cuadrático medio: 4.837317



### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.62	0.62	5.09	2942.16	2964.62

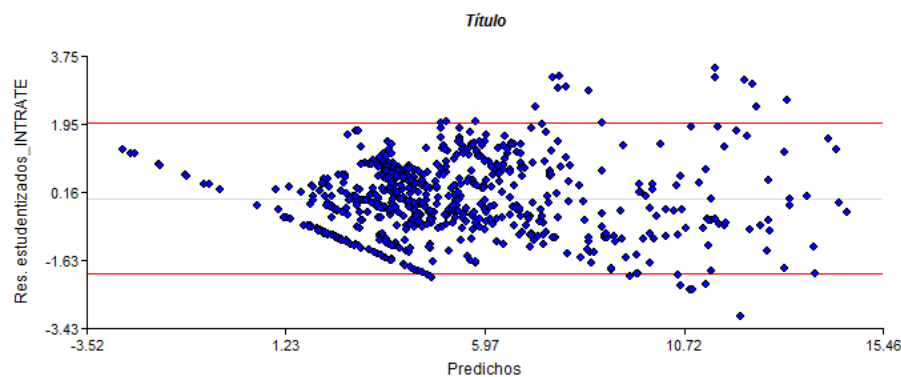
Selección Forward. Máximo p-valor para entrar: 0.05

Número original de regresoras: 4, regresoras retenidas en el modelo 3

### Coeficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	0.02	0.23	-0.43	0.48	0.10	0.9190		
INFL	0.87	0.05	0.77	0.97	17.23	<0.0001	299.43	2.79
PCE	0.18	0.05	0.08	0.29	3.42	0.0007	14.70	2.96
PERSINC	0.30	0.06	0.19	0.42	5.12	<0.0001	29.16	1.79

Error cuadrático medio: 5.007160



### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.61	0.61	5.14	2951.85	2969.82

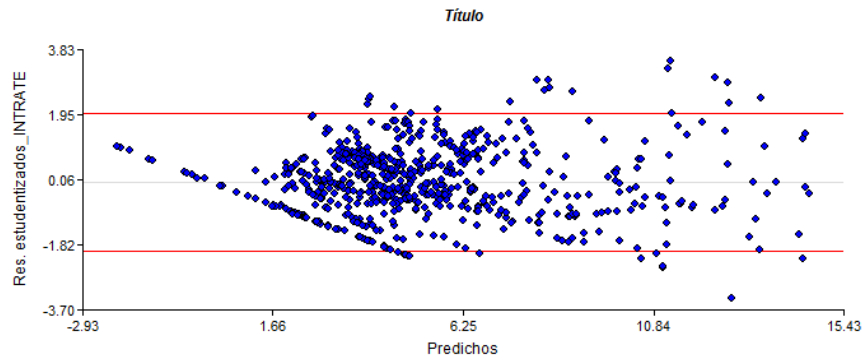
Selección Forward. Máximo p-valor para entrar: 0.05

Número original de regresoras: 3, regresoras retenidas en el modelo 2

### Coeficientes de regresión y estadísticos asociados

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	0.45	0.20	0.07	0.83	2.31	0.0211		
INFL	1.01	0.03	0.95	1.07	32.16	<0.0001	1034.45	1.05
PERSINC	0.44	0.05	0.35	0.53	9.47	<0.0001	91.50	1.05

Error cuadrático medio: 5.088859



## **Análisis de regresión lineal**

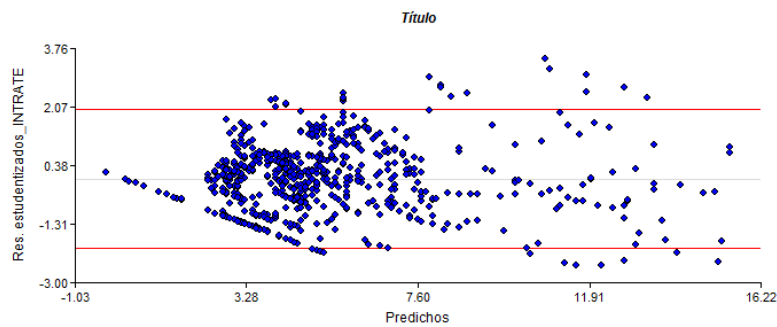
Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.56	0.56	5.82	3034.26	3047.74

Selección Forward. Máximo p-valor para entrar: 0.05  
 Número original de regresoras: 2, regresoras retenidas en el modelo 1

## **Coefficientes de regresión y estadísticos asociados**

Coef	Est.	E.E.	LI (95%)	LS (95%)	T	p-valor	CpMallows	VIF
const	1.64	0.16	1.33	1.96	10.37	<0.0001		
INFL	0.94	0.03	0.88	1.01	28.93	<0.0001	836.70	1.00

Error cuadrático medio: 5.774363





Coefficients <sup>a</sup>							
Model	Unstandardized Coefficients		Standardized Coefficients	t	Sig.	95.0% Confidence Interval for B	
	B	Std. Error	Beta			Lower Bound	Upper Bound
1	(Constant)	1.644		10.370	.000	1.333	1.955
	INFL	.945	.748	28.930	.000	.881	1.009
2	(Constant)	.451		2.311	.021	.068	.834
	INFL	1.012	.801	32.156	.000	.950	1.073
	PERSINC	.435	.236	9.468	.000	.345	.526
3	(Constant)	.023		.102	.919	-.429	.476
	INFL	.875	.693	17.230	.000	.775	.974
	PERSINC	.305	.165	5.118	.000	.188	.421
	PCE	.182	.142	3.423	.001	.077	.286
4	(Constant)	-.210		-.910	.363	-.665	.244
	INFL	.745	.590	13.185	.000	.634	.856
	PERSINC	.257	.139	4.329	.000	.140	.373
	PCE	.311	.243	5.318	.000	.196	.425
	HOUST	-.022	-.136	-4.902	.000	-.030	-.013
5	(Constant)	-.236		-1.026	.305	-.688	.216
	INFL	.718	.568	12.598	.000	.606	.830
	PERSINC	.240	.130	4.052	.000	.124	.357
	PCE	.340	.266	5.761	.000	.224	.456
	HOUST	-.021	-.129	-4.682	.000	-.029	-.012
	COMMPRI	-.007	-.069	-2.842	.005	-.013	-.002

a. Dependent Variable: INTRATE

Model

$$\text{INTRATE} = -0.236 + 0.718 \cdot \text{INFL} + 0.240 \cdot \text{PERSINC} + 0.340 \cdot \text{PCE} - 0.021 \cdot \text{HOUST} - 0.007 \cdot \text{COMMPRI}$$

It is exactly the same in model a.

**(c) Compare your model from (a) and the Taylor rule of equation (1). Consider R<sup>2</sup>, AIC and BIC. Which of the models do you prefer?**

Model Summary									
Model	R	R Square	Adjusted R Square	Std. Error of the Estimate	Change Statistics				
					R Square Change	F Change	df1	df2	Sig. F Change
1	.758 <sup>a</sup>	.575	.574	2.3635700	.575	444.128	2	657	.000

a. Predictors: (Constant), PROD, INFL

ANOVA <sup>a</sup>					
Model		Sum of Squares	df	Mean Square	F
1	Regression	4962.205	2	2481.103	444.128
	Residual	3670.306	657	5.586	
	Total	8632.512	659		

a. Dependent Variable: INTRATE

b. Predictors: (Constant), PROD, INFL

Coefficients <sup>a</sup>								
Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.	95.0% Confidence Interval for B	
		B	Std. Error	Beta			Lower Bound	Upper Bound
1	(Constant)	1.251	.176		7.103	.000	.905	1.597
	INFL	.974	.033	.772	29.792	.000	.910	1.039
	PROD	.095	.020	.125	4.810	.000	.056	.133

a. Dependent Variable: INTRATE

$$It = 1.251 + 0.974 * INFL + 0.095 * PROD$$

### Análisis de regresión lineal

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.57	0.56	5.82	3034.26	3047.74

**Rsquare = 57.5% in (c) is lower than Rsquare in (a) 64% even in AIC, BIC is lower than Taylor Rule**

Variable	N	R <sup>2</sup>	R <sup>2</sup> Aj	ECMP	AIC	BIC
INTRATE	660	0.64	0.63	4.90	2914.28	2945.72

*Selección Forward. Máximo p-valor para entrar: 0.05*

*Número original de regresoras: 6, regresoras retenidas en el modelo 5*

**I prefer model (a) is much stronger.**

**(d) Test the Taylor rule of equation (1) using the RESET test, Chow break and forecast test (with in both tests as break date January 1985) and a Jarque-Bera test. What do you conclude?**

In 1085 is a breakpoint p-0.000 therefore there is a structural change.