

Question 10

Looking at reciprocals:

If the family of intervals A_n is defined as $\left[0, \frac{1}{n}\right]$ then the interval defined by $\left[0, \frac{1}{n+1}\right]$ (where $n \in \mathbb{N}$) is always a subset of the interval $\left[0, \frac{1}{n}\right]$ as $\frac{1}{n+1}$ will always be smaller than $\frac{1}{n}$.

Therefore $A_{n+1} \subset A_n$.

$$\bigcap_{n=1}^{\infty} A_n = 0$$

So $A_n = \left[0, \frac{1}{n}\right]$ has the stated properties required.