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Additivity!
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Slogan: If you know $\{f_1, f_2, ..., f_n, ...\}$ then you know $\{s_1, s_2, ..., s_n, ...\}$!