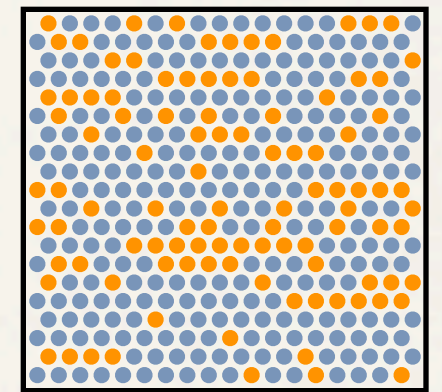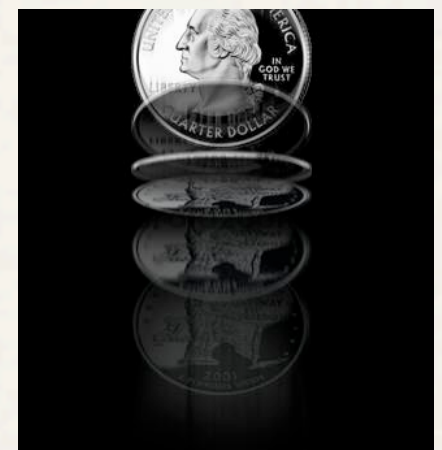# The art of the random sample

$$X_1, X_2, \ldots, X_n \sim \text{Bernoulli}(p)$$

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  ✦ Sampling from epoch to epoch is *with replacement*.

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✤ A question of phrasing.