

# Tableau 7

Is the outcome of a coin toss *really* random?

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# The toss of a coin

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Air resistance

Gravitational force



Initial velocity

Angular velocity

Mass density

Floor elasticity



Air resistance

Gravitational force



Initial velocity

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Floor elasticity

A coin toss as a deterministic physical system



Air resistance

Gravitational force



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A coin toss as a deterministic physical system



Air resistance

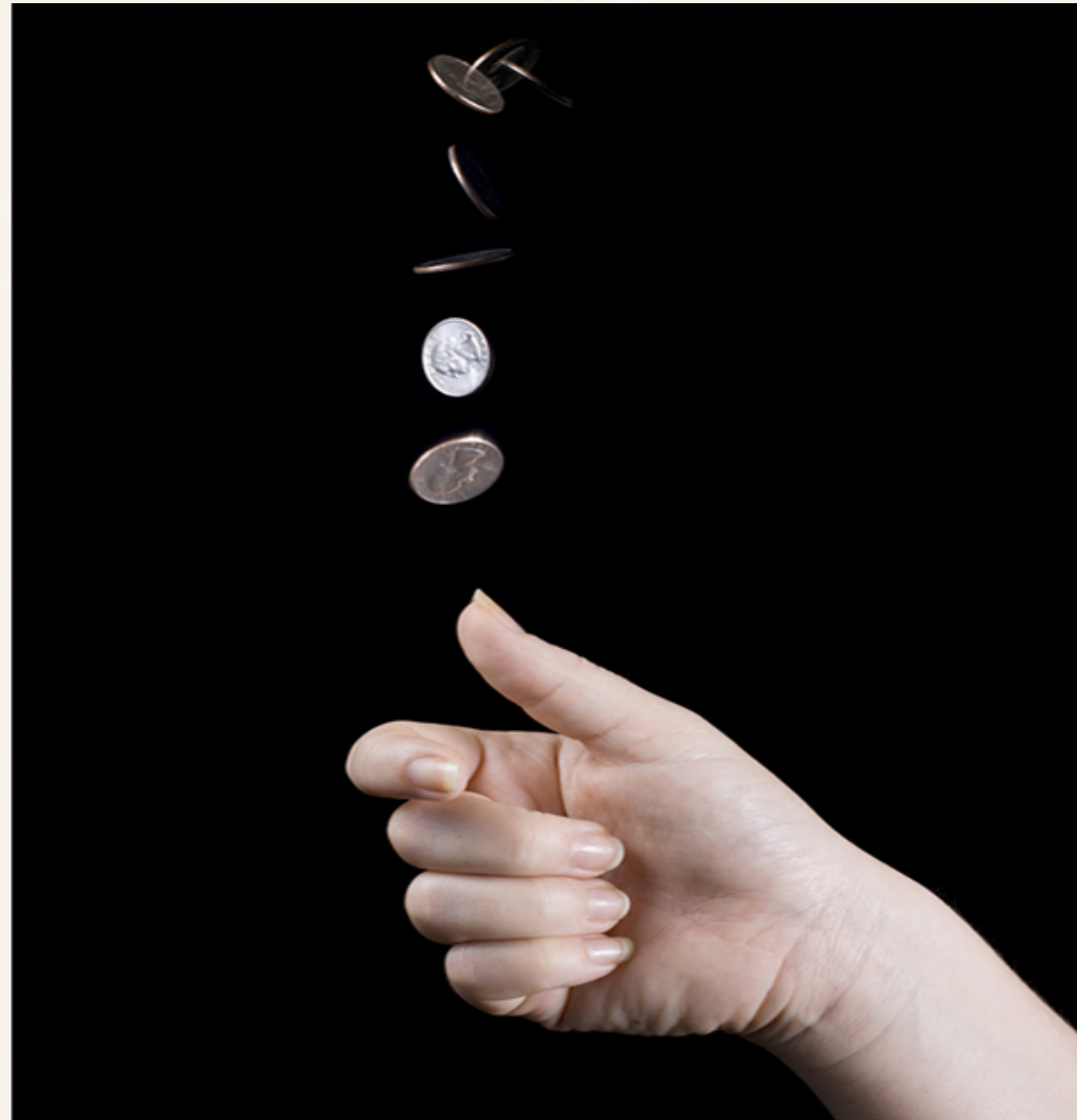
Gravitational force

Initial velocity

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A coin toss as a deterministic physical system



Air resistance

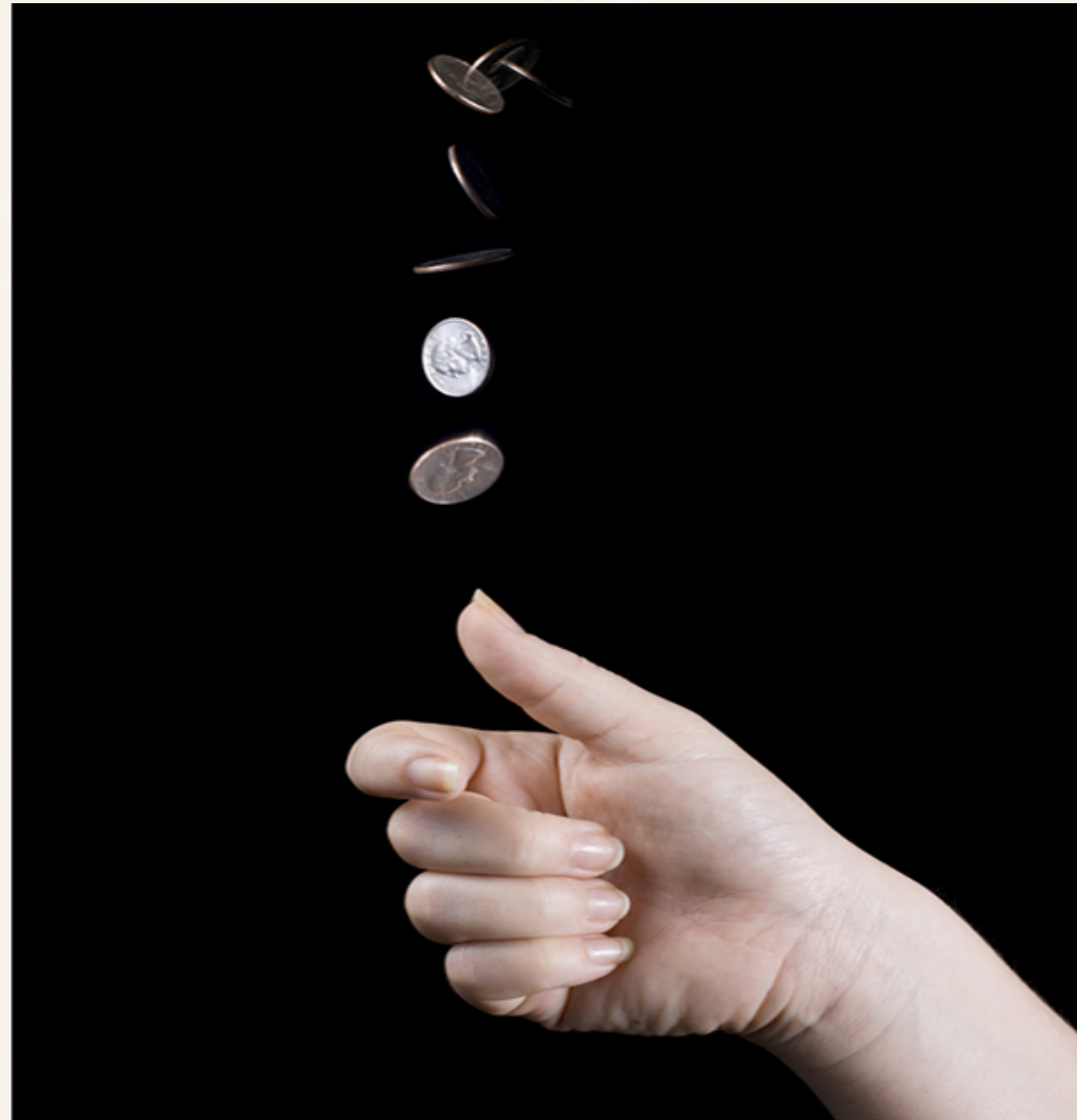
Gravitational force

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A coin toss as a deterministic physical system



# A sanitised model of a coin toss

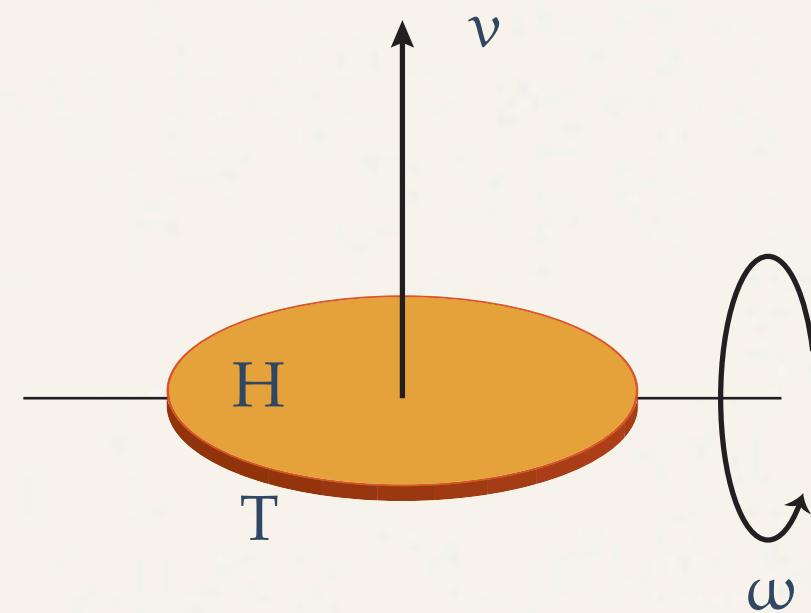
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# A sanitised model of a coin toss

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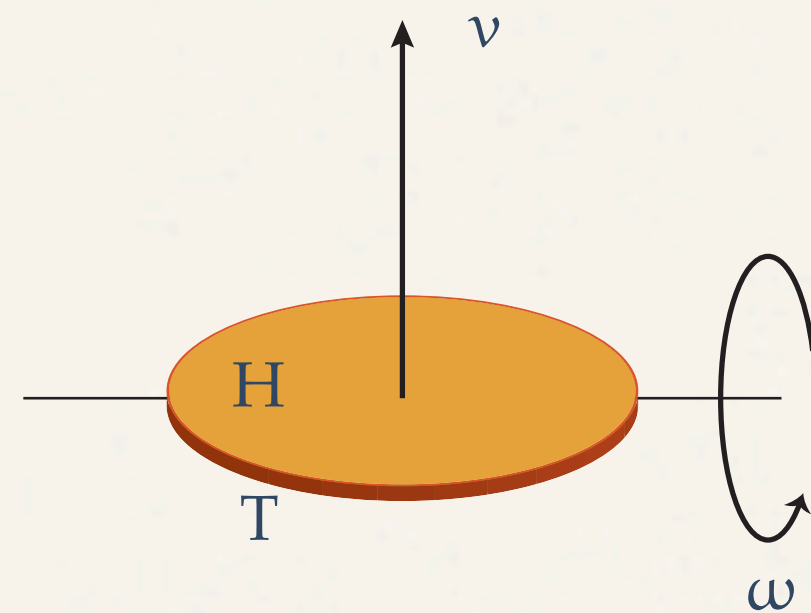


- ❖ **Coin:** thin uniform disk, one side marked “Head”, the other “Tail”.
- ❖ **Initial conditions (time  $t = 0$ ):** Head facing upwards; the coin is tossed straight up with initial velocity  $v$  and angular velocity  $\omega$  about the horizontal axis. Measure coin height vertically from centre of mass at rest, coin rotation with respect to horizontal axis. Initial height  $y(0) = 0$ ; initial angular orientation  $\theta(0) = 0$ .
- ❖ **At time  $t$ :** Coin height  $y(t)$ , angle with horizontal  $\theta(t)$ .
- ❖ **Termination time  $t = \tau$ :** Catch the coin at its initial height when its centre of mass returns to its initial position. Final height  $y(\tau) = 0$ ; final angular orientation  $\theta(\tau)$ .



# A sanitised model of a coin toss

$$y(0) = 0, \quad \theta(0) = 0$$



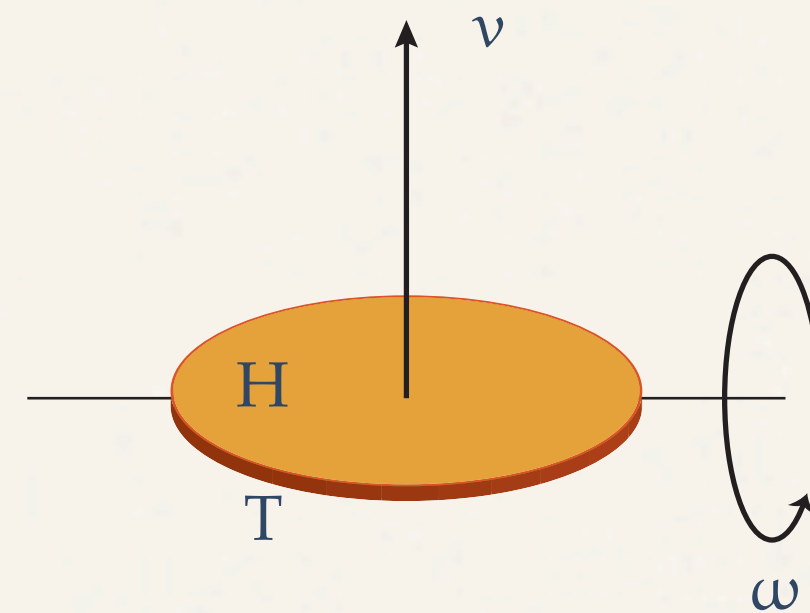
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# A sanitised model of a coin toss

$$y(t), \theta(t)$$

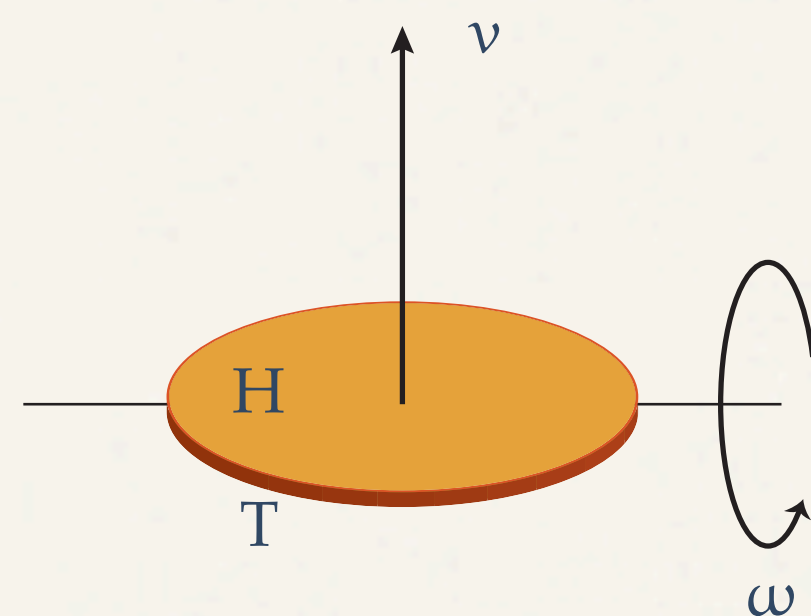
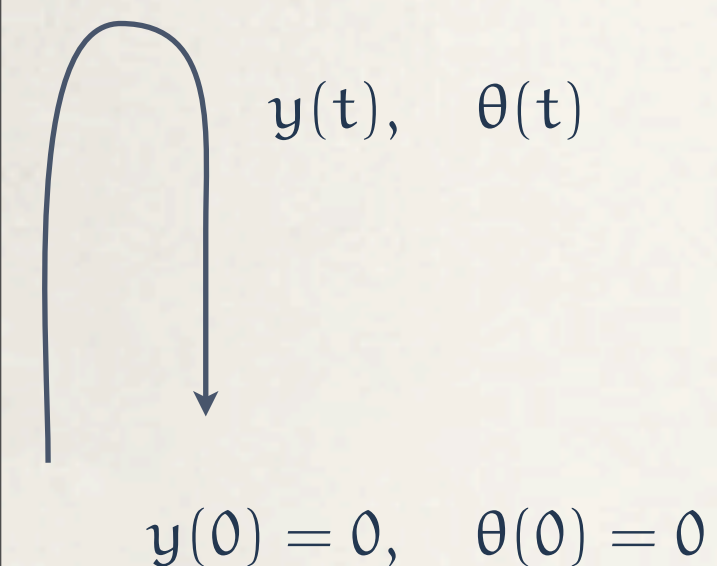
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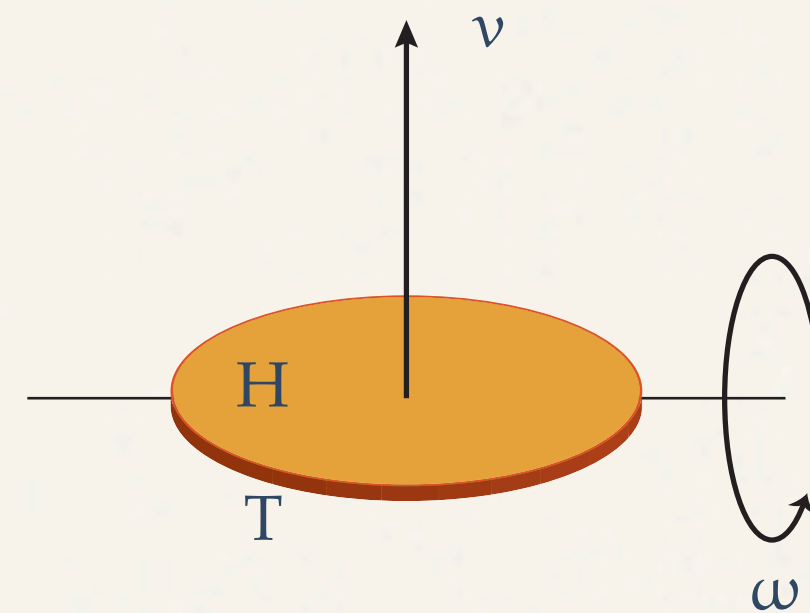
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# A sanitised model of a coin toss

$y(t), \theta(t)$

$y(\tau) = 0, \theta(\tau)$   
 $y(0) = 0, \theta(0) = 0$



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