Feedback — Problem Set 7

Help Center

You submitted this homework on Sun 3 Mar 2013 10:45 AM PST. You got a score of 7.00 out of 7.00.

Question 1

War Game

- Two opposed armies are poised to seize an island.
- Each army can either "attack" or "not-attack".
- Also, Army 1 is either "weak" or "strong" with probability p and (1-p), respectively. Army 2 is always "weak".
- Army's 1 type is known only to its general.
- An army can capture the island either by attacking when its opponent does not or by attacking when its rival does if it is strong and its rival is weak. If two armies of equal strength both attack, neither captures the island.
- The payoffs are as follows
 - \circ The island is worth M if captured.
 - An army has a "cost" of fighting, which is equal to s > 0 if it is strong and w > 0 if it is weak (where s < w < M).
 - There is no cost of attacking if its rival does not attack.
- These payoffs are pictured in the payoff matrices below:

Weak		
1\2	Attack	Not-attack
Attack	-w,-w	M,0
Not-attack	0,M	0,0

with probability p

Strong	

1\2	Attack	Not-attack
Attack	M-s,-w	M,0
Not-attack	0,M	0,0

with probability 1-p. When p=1/2, which is a pure strategy Bayesian equilibrium (there could be other equilibria that are not listed as one of the options): (1's type - 1's strategy; 2's strategy)

Your Answer		Score	Explanation
a) (Weak - Not-Attack, Strong - Attack; Attack);	~	1.00	
○ b) (Weak - Not-Attack, Strong - Attack; Not-Attack);			
c) (Weak - Attack, Strong - Attack; Attack);			
d) It does not exist.			
Total		1.00 / 1.00	

Question Explanation

(a) is true.

- Check (a): If 2 chooses Attack, indeed the Weak type prefers Not-Attack and Strong type prefers Attack. Thus, with probability 1/2, player 1 is a Weak type who chooses Not-Attack and with probability 1/2, player 1 is a Strong type who chooses Attack. Thus, 2 prefers Attack with a payoff (M-w)/2, while Not-Attack gives a lower payoff of 0 (since w < M).
- (b) is not a Bayesian equilibrium because when Attack and Not-Attack are chosen by 1 (depending on the type) with 1/2 probability, player 2 prefers to Attack instead Not-Attack.
- (c) is not a Bayesian equilibrium because when 2 chooses Attack, the Weak type prefers Not-Attack instead of Attack.

Question 2

Rock, Paper, Scissors

Consider the following variation to the Rock (R), Paper (P), Scissors (S) game:

- Suppose that with probability p player 1 faces a Normal opponent and with probability 1-p, he faces a Simple opponent that will always play P.
- Player 2 knows whether he is Normal or Simple, but player 1 does not.
- The payoffs are pictured in the payoff matrices below:

Normal			
1\2	R	Р	S
R	0,0	-1,1	1,-1
Р	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

with probability p

Simple	
1\2	Р
R	-1,1
Р	0,0
S	1,-1

with probability 1-p.

Suppose p=1/3, select all pure strategy Bayesian equilibria (there may be more than one): (Form: 1's strategy; 2's type - 2's strategy)

Your Answer		Score	Explanation
a) (S; Normal - P, Simple - P)	~	0.25	
ø b) (S; Normal - R, Simple - P)	~	0.25	
c) (R; Normal - P, Simple - P)	~	0.25	
d) (P; Normal - P, Simple - P)	~	0.25	
Total		1.00 / 1.00	

Question Explanation

(b) is true.

- Check (b): If 1 chooses S, Normal type prefers R and Simple type plays P. If 2 chooses R with 1/3 and and P with 2/3 probability (depending on the type), 1 is indifferent between P (with payoff =1/3*1) and S (with payoff =1/3*(-1)+2/3*1=1/3) and prefers P or S to R (with payoff = 2/3*(-1)).
- It is easy to check by similar calculations that for each of the other answers (a), (c) and (d) some player would like to deviate.

Question 3

Rock, Paper, Scissors

Consider the following variation to the Rock (R), Paper (P), Scissors (S) game:

- Suppose that with probability p player 1 faces a Normal opponent and with probability 1-p, he faces a Simple opponent that will always play P.
- Player 2 knows whether he is Normal or Simple, but player 1 does not.
- The payoffs are pictured in the payoff matrices below:

Normal			
1\2	R	Р	S
R	0,0	-1,1	1,-1
Р	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

with probability p

Simple	
1\2	Р
R	-1,1
Р	0,0
S	1,-1

with probability 1-p.

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Suppose p=2/3, select all pure strategy Bayesian equilibria (there may be more than one): (Form: 1's strategy; 2's type - 2's strategy)

Your Answer		Score	Explanation
a) (R; Normal - P, Simple - P)	~	0.33	
b) (P; Normal - S, Simple - P)	~	0.33	
c) (S; Normal - R, Simple - P)	~	0.33	
Total		1.00 / 1.00	

Question Explanation

There is no pure strategy Bayesian equilibria.

- Check (a): If 1 chooses R, Normal type prefers P and Simple type plays P. If 2 chooses P with 2/3 and and P with 1/3 probability (depending on the type), 1 prefers S (with payoff =1) instead of R (with payoff = -1) or P (with payoff=0).
- Check (b): If 1 chooses P, Normal type prefers S and Simple type plays P. If 2 chooses S with 2/3 and And P with 1/3 probability (depending on the type), 1 is indifferent between R (with payoff = 2/3*1+1/3*(-1)=1/3) and S (with payoff = 2/3*(0)+1/3*1=1/3) and prefers R or S to P (with payoff = 2/3*(-1)+1/3*(0)=-2/3).
- Check (c): If 1 chooses S, Normal type prefers R and Simple type plays P. If 2 chooses R with 2/3 and A P with 1/3 probability (depending on the type), 1 prefers P (with payoff = 2/3*(1)+1/3*0=2/3) instead of R (with payoff = 2/3*(0)+1/3*(-1)=-1/3) or S (with payoff=2/3*(-1)+1/3*(1)=-1/3).
- Thus it doesn't exist, as (a), (b) and (c) are the only possible pure equilibria given 2's best responses.

Question 4

Work or Startup

- An engineer has a talent t in {1,2} with equal probability (prob= 1/2), and the value of t is private information to the engineer.
- The engineer's pure strategies are applying for a job or being an entrepreneur and doing a startup.
- The company's pure strategies are either hiring or not hiring the engineer.

- If the engineer applies for the job and the company does not hire, then the engineer becomes an entrepreneur and does a startup.
- The utility of the engineer is t (talent) from being an entrepreneur, and w (wage) from being hired.
- The utility of the company is (t-w) from hiring the engineer and 0 otherwise.
- These are pictured in the payoff matrices below, with the engineer being the row player and the company being the column player.

t=2	Hire	No
Startup	2,0	2,0
Work	w,2-w	2,0
t=1	Hire	No
t=1 Startup		No ⁻ 1,0

Suppose w=2, which of the below are pure strategy Bayesian equilibria, there may be more than one and check all that apply. (Form:

Engineer's strategy, company's strategy)

Your Answer		Score	Explanation
lacksquare a) ($t=2$ Startup, $t=1$ Work, Hire);	~	0.25	
ightharpoonup b b) ($t=2$ Startup, $t=1$ Work, Not);	~	0.25	
$\ \square$ c) ($t=2$ Work, $t=1$ Work, Hire);	~	0.25	
$ ightharpoonup ext{d)} \; (t=2 \; ext{Work,} \; t=1 \; ext{Work, Not)};$	~	0.25	
Total		1.00 / 1.00	

Question Explanation

(b) and (d) are true.

- Because w=2, type t=1 prefers to work if the company hires and type t=2 is indifferent between work and startup.
- Given that type t=1 prefers to work, the company prefers not to hire since it loses money from type t=1 and only breaks even from t=2.

• Thus (b) and (d) are true.

Question 5

Work or Startup

- An engineer has a talent t in $\{1,2\}$ with equal probability (prob= 1/2), and the value of t is private information to the engineer.
- The engineer's pure strategies are applying for a job or being an entrepreneur and doing a startup.
- The company's pure strategies are either hiring or not hiring the engineer.
- If the engineer applies for the job and the company does not hire, then the engineer becomes an entrepreneur and does a startup.
- The utility of the engineer is t (talent) from being an entrepreneur, and w (wage) from being hired.
- The utility of the company is (t-w) from hiring the engineer and 0 otherwise.
- These are pictured in the payoff matrices below, with the engineer being the row player and the company being the column player.

t=2	Hire	Not
Startup	2,0	2,0
Work	w,2-w	2,0
t=1	Hire	Not
t=1 Startup		Not 1,0

Suppose w=1, which of the below are pure strategy Bayesian equilibria, there may be more than one and check all that apply. (Form:

Engineer's strategy, company's strategy)

Your Answer		Score	Explanation
lacksquare a) ($t=2$ Work, $t=1$ Startup, Hire);	~	0.25	
lacksquare b) ($t=2$ Work, $t=1$ Startup, Not);	~	0.25	
ightharpoonup c) ($t=2$ Startup, $t=1$ Work, Hire);	~	0.25	

 \checkmark d) (t=2 Startup, t=1 Work, Not);

0.25

Total 1.00 / 1.00

Question Explanation

(c) and (d) are true.

- Because w=1, t=1 is indifferent between work and startup and t=2 prefers to startup.
- Given t=1 is indifferent and t=2 prefers not to work, the company is indifferent between hire or not since w-t=1-1=0.
- Thus (c) and (d) are true.

Question 6

Battle of Sexes

Modify the Battle of Sexes to have incomplete information:

- There are two possible types of player 2 (column):
 - \circ "Meet" player 2 wishes to be at the same movie as player 1, just as in the usual game. (This type has probability p)
 - \circ "Avoid" 2 wishes to avoid player 1 and go to the other movie. (This type has probability 1-p)
- 2 knows her type, and 1 does not.
- They simultaneously choose P or L.
- These payoffs are shown in the matrices below.

Meet	L	Р
L	2,1	0,0
Р	0,0	1,2

with probability p

Avoid	L	Р
L	2,0	0,2
Р	0,1	1,0

with probability 1 - p.

When p = 1/2, which is a pure strategy Bayesian equilibrium: (1's strategy; 2's type - 2's strategy)

Your Answer		Score	Explanation
a) (L; Meet - L, Avoid - P);	✓	1.00	
b) (P; Meet - P, Avoid - L);			
o) (L; Meet - P, Avoid - P);			
d) It does not exist.			
Total		1.00 / 1.00	

Question Explanation

(a) is true.

- Check (a): If 1 chooses L, indeed the Meet type prefers L and Avoid type prefers P. Thus with probability=1/2, 2 is a Meet type who chooses L and with probability=1/2, 2 is a Avoid types who chooses P. Thus, 1 prefers L with a payoff of 1/2*2, while P gives a lower payoff of 1/2*1.
- (b) is not a Bayesian equilibrium because when L and P are chosen by 2 (depending on the type) with 1/2 probability, 1 prefers L instead of P.
- (c) is not a Bayesian equilibrium because when 1 chooses L, the Meet type prefers L instead of P.

Question 7

Battle of Sexes

Modify the Battle of Sexes to have incomplete information:

- There are two possible types of player 2 (column):
 - "Meet" player 2 wishes to be at the same movie as player 1, just as in the usual game. (This type has probability p)

 \circ "Avoid" 2 wishes to avoid player 1 and go to the other movie. (This type has probability 1-p)

- 2 knows her type, and 1 does not.
- They simultaneously choose P or L.
- These payoffs are shown in the matrices below.

Meet	L	Р
L	2,1	0,0
Р	0,0	1,2

with probability p

Avoid	L	Р
L	2,0	0,2
Р	0,1	1,0

with probability 1 - p.

When p=1/4, which is a pure strategy Bayesian equilibrium : (1's strategy; 2's type - 2's strategy)

Your Answer		Score	Explanation
○ a) (L; Meet - L, Avoid - P);			
○ b) (P; Meet - P, Avoid - L);			
o (L; Meet - P, Avoid - P);			
d) It does not exist.	~	1.00	
Total		1.00 / 1.00	

Question Explanation

(d) is true.

- Check (a): if 1 chooses L, Meet type prefers L and Avoid type prefers P. If 2 chooses L with 1/4 and P with 3/4 probability (depending on the type), 1 prefers P (with payoff = 3/4*1) instead of L (with payoff = 1/4*2).
- Check (b): if 1 chooses P, Meet type prefers P and Avoid type prefers L. If 2 chooses L with 3/4 and P with 1/4 probability (depending on the type), 1 prefers L (with payoff 3/4*2) instead of P (with payoff = 1/4*1).

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- (c) is not a Bayesian equilibrium because when 1 chooses L, Meet type prefers L instead of P.
- Thus it doesn't exist, as (a) and (b) are the only possible pure equilibria given 2's best responses.