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Variance: $$\sigma^2 := \operatorname{Var}(X) = \sum_{k=-\infty}^{\infty} (k-\mu)^2 \cdot p(k)$$

Slogan

The law of large numbers comes into effect any time we have a sum of independent random variables sharing a common distribution with a given expectation and variance.