≡ Item Navigation

Cartesian Partial Derivatives

Transform the Cartesian partial derivatives into polar form.

(a) Let $f=f(x(r,\theta),y(r,\theta))$. Using the chain rule and the definition of polar coordinates, show that

$$rac{\partial f}{\partial r} = \cos heta rac{\partial f}{\partial x} + \sin heta rac{\partial f}{\partial y}, \qquad rac{\partial f}{\partial heta} = -r \sin heta rac{\partial f}{\partial x} + r \cos heta rac{\partial f}{\partial y}.$$

(b) Invert the result of Part (a) to show that

$$\frac{\partial}{\partial x} = \cos \theta \frac{\partial}{\partial r} - \frac{\sin \theta}{r} \frac{\partial}{\partial \theta}, \qquad \frac{\partial}{\partial y} = \sin \theta \frac{\partial}{\partial r} + \frac{\cos \theta}{r} \frac{\partial}{\partial \theta}.$$

✓ Completed

Go to next item

🖒 Like 🖓 Dislike \square Report an issue