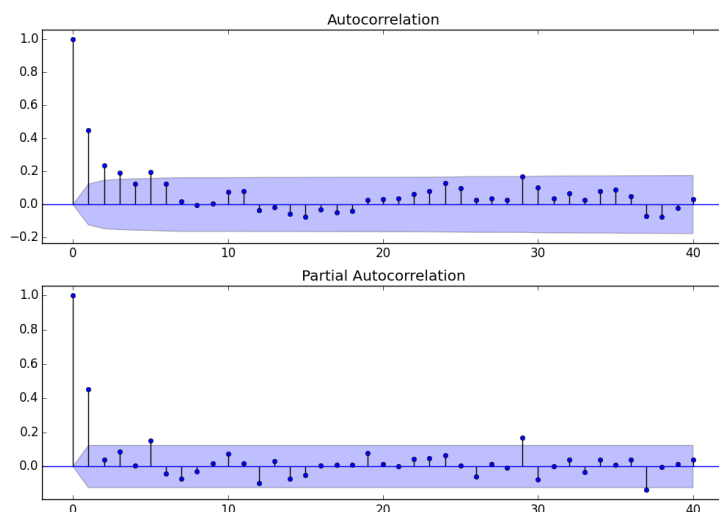


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## Analyse ACF and PACF plots

I want to see if I am on the right track analysing my ACF and PACF plots:



Background: (Reff: Philip Hans Franses, 1998)

1. As both ACF and PACF show significant values, I assume that an ARMA-model will serve my needs
2. The ACF can be used to estimate the MA-part, i.e q-value, the PACF can be used to estimate the AR-part, i.e. p-value
3. To estimate a model-order I look at a.) whether the ACF values die out sufficiently, b.) whether the ACF signals overdifferencing and c.) whether the ACF and PACF show any significant and easily interpretable peaks at certain lags
4. ACF and PACF might suggest not only one model but many from which I need to choose after considering other diagnostic tools

Having that in mind, I would go ahead and say that the most obvious model seems to be ARMA (4,2) as ACF values die out at lag 4 and PACF shows spikes at 1 and 2.

Another way to analyze would be an ARMA(2,1) as I see two significant spikes in my PACF and one significant spike in my ACF (after which the values die out starting from a much lower point (0.4)).

Looking at my in-sample-forecast results (using a simple Mean Absolute Percentage Error) ARMA (2,1) delivers much better results then ARMA(4,2). So I use ARMA(2,1)!

Can you confirm my method and findings of analyzing ACF and PACF plots?

Help appreciated!

EDIT:

Descriptive Statistics:

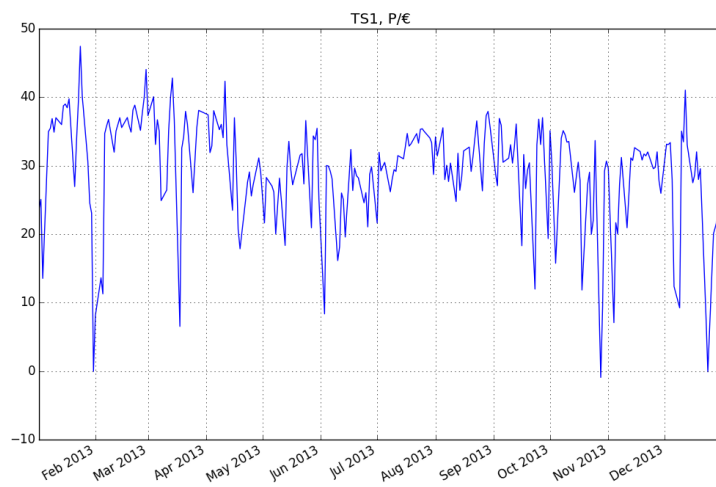
```
count 252.000000
mean 29.576151
std 7.817171
min -0.920000
25% 26.877500
50% 30.910000
75% 34.915000
max 47.430000
```

Skewness of endog\_var: [-1.35798399]

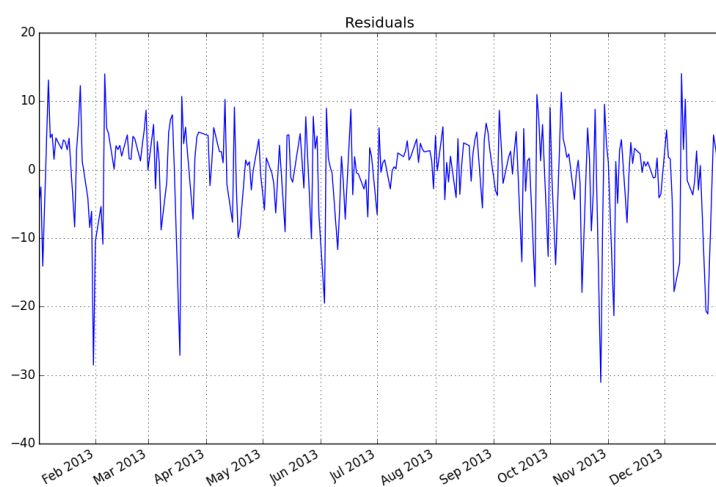
Kurtosis of endog\_var: [ 5.4917757]

Augmented Dickey-Fuller Test for endog\_var: (-3.76140904255411, 0.0033277703768345287, {'5%': -2.8696473721448728, '1%': -3.4487489051519011, '10%': -2.5710891239349585})

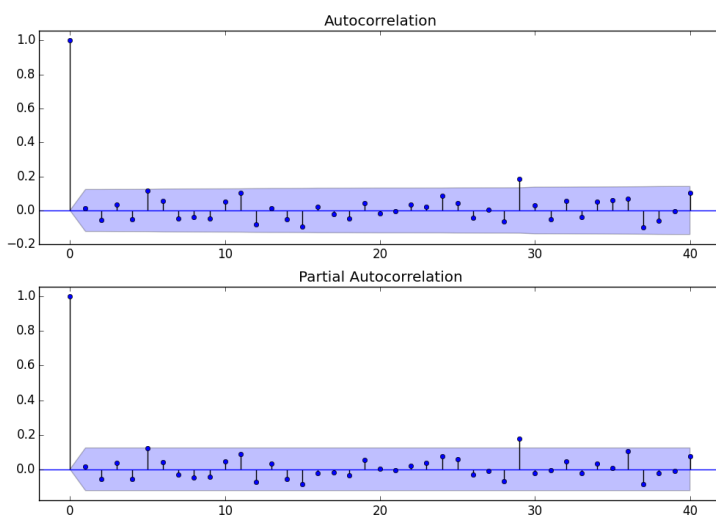
Time-Series:



Residuals (ARMA (2,1):



ACF/PACF of Residuals:



EDIT II:

Data:

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25.41561  
13.88561  
23.31561  
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time-series

model-selection

arma

statsmodels

edited Jan 22 at 22:57

asked Jan 22 at 12:59

 **Peter Knutsen**

6715

- Data look a bit left-skew, perhaps nonstationary. It looks to me like there's some potential issues with the residuals, perhaps even conditional heteroskedasticity. – Glen\_b ♦ Jan 22 at 16:13

In my opinion the skewness suggests anomalous values (pulses) which can only be confirmed by analysis of the original data. – IrishStat Jan 22 at 21:05

3 Answers

Looking at your ACF and PACF is useful in the full context of your analysis as well. Your Ljung-Box Q-statistic; p-value; confidence interval, ACF and PACF should be viewed together. For instance the Q test here:

```
acf, ci, Q, pvalue = tsa.acf(res1.resid, nlags=4, confint=95, qstat=True, unbiased=True)
```

Here - our Q test for autocorrelation is an overall gut check of our graphical interpretation.

Draft notes on Time Series analysis in Statsmodels:  
<http://conference.scipy.org/proceedings/scipy2011/pdfs/statsmodels.pdf>

answered Feb 20 at 23:40



Andrew Owens

226 1 4

It looks to me like you're counting the spikes at lag 0.

Your PACF shows one reasonably large spike at lag 1, suggesting AR(1). This will of course induce a geometric-like decrease in the ACF (which, broadly speaking, you see). You seem to be trying to fit the same dependence twice - both as AR and MA.

I'd have just tried AR(1) on that to start with and seen if there was anything left worth worrying over.

edited Jan 22 at 13:45

answered Jan 22 at 13:34



Glen\_b ♦

121k 12 195 412

Peter; my answer had a typo in it (I had AR(1) correct in the last para, but typed MA(1) in the second paragraph), which is fixed now. – Glen\_b ♦ Jan 22 at 13:48

Thanks for your answer. Counting from lag 0 is of course a cardinal mistake! I tried AR(1) and the result was not as good as ARMA(2,1)! – Peter Knutsen Jan 22 at 14:26

It may well be the case that it's not as good - nevertheless, the AR(1) would be the place to start. What did the PACF of residuals look like, for example? What does the original series look like? There's much that might be going on that can't be gleaned easily from an ACF and PACF of the data. – Glen\_b ♦ Jan 22 at 14:39

Thanks. I posted some additional information which might lead to new insights. – Peter Knutsen Jan 22 at 15:02

The sole reliance on the ACF and PACF using tools suggested in the mid 60's is sometimes but seldomly correct except for simulated data. Model Identification tools like AIC/BIC almost never correctly identify a useful model but rather show what happens when you don't read the small print regarding the assumptions. I would suggest that you start as simply as possible BUT not too simply and estimate a tentative model ; AR(1) as suggested by Glen\_b . The residuals/analysis from this tentative model can be used to compute yet another ACF and PACF suggesting potential model augmentation or model simplification. Note that interpretation ala your references REQUIRE that the current series/residuals are free of any deterministic structure i.e. Pulses, Level Shifts, Local Time Trends and Seasonal Pulses and furthermore that the series has constant error variance and that the parameters of the tentative model are invariant over time. If you wish you can post your data and I will attempt to help you form a useful model.

EDIT AFTER DATA WAS REPORTED :

365 values were delivered and analyzed, yielding the following AR(1) model with identified Pulses and 2 Level Shifts .

215-675-0652  
VERSION: 01/22/2015 06:40

MODELLING OUTPUT SERIES:NOSEAS

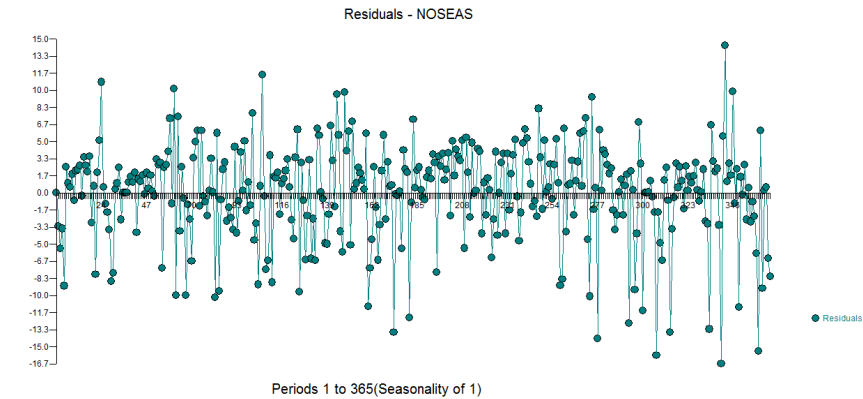
```

Y(T) = 35.148
+ [X1(T)] [ (- 27.6842) ] :PULSE 356
+ [X2(T)] [ (- 30.6971) ] :PULSE 31
+ [X3(T)] [ (- 26.8650) ] :PULSE 301
+ [X4(T)] [ (- 22.7138) ] :PULSE 358
+ [X5(T)] [ (- 26.1459) ] :PULSE 362
+ [X6(T)] [ (+ 2.9238) ] :LEVEL SHIFT 194
+ [X7(T)] [ (- 8.0312) ] :LEVEL SHIFT 105
+ [X8(T)] [ (- 28.2898) ] :PULSE 77
+ [X9(T)] [ (- 26.0516) ] :PULSE 32
+ [X10(T)] [ (- 23.2761) ] :PULSE 36
+ [X11(T)] [ (- 26.1168) ] :PULSE 76
+ [X12(T)] [ (- 14.3966) ] :PULSE 308
+ [X13(T)] [ (- 20.5078) ] :PULSE 35
+ [X14(T)] [ (- 20.4270) ] :PULSE 154
+ [X15(T)] [ (- 14.0550) ] :PULSE 4
+ [X16(T)] [ (- 20.6135) ] :PULSE 153
+ [X17(T)] [ (- 18.6130) ] :PULSE 357
+ [X18(T)] [ (- 15.3091) ] :PULSE 69
+ [X19(T)] [ (- 18.7496) ] :PULSE 302
+ [X20(T)] [ (- 11.5644) ] :PULSE 132
+ [X21(T)] [ (- 26.8954) ] :PULSE 343
+ [X22(T)] [ (- 16.1270) ] :PULSE 167
+ [X23(T)] [ (- 11.0503) ] :PULSE 174
+ [X24(T)] [ (- 18.7255) ] :PULSE 341
+ [X25(T)] [ (- 18.5606) ] :PULSE 266
+ [X26(T)] [ (- 17.8317) ] :PULSE 291
+ [ (1- .383B** 1) ] ** -1 [A(T)]

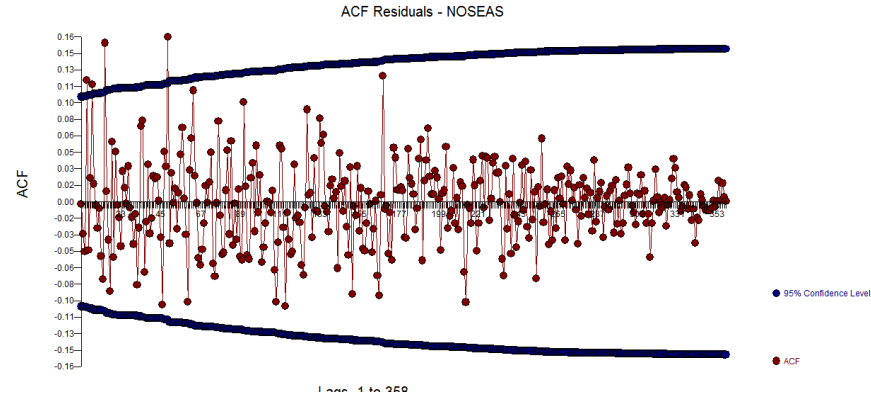
```

. note that

this had been a popular guess . The residuals from this model are plotted here



. There is a suggestion of variance hetero-scedasticity but this is a symptom and one needs to find the correct cure which we will ultimately find. Proceeding the acf of the residuals shown here



exhibits a suggestion of model inadequacy. A closer look at the table of the acf of the residuals is

LAG	ACF VALUE	STND. ERROR	T- RATIO	CHI-SQUARE & PROBABILITY	PACF VALUE	STND. ERROR	T- RATIO
1	-.003	.052	-.05	.0 NA	-.003	.052	-.05
2	-.032	.052	-.61	.4 NA	-.032	.052	-.61
3	-.049	.052	-.93	1.3 NA	-.049	.052	-.94
4	.119	.053	2.27	6.5 NA	.118	.052	2.26
5	-.047	.053	-.89	7.3 NA	-.051	.052	-.98
6	.023	.053	.44	7.5 NA	.029	.052	.56
7	.115	.053	2.15	12.5 NA	.126	.052	2.40
8	.017	.054	.32	12.6 NA	-.002	.052	-.03
9	-.003	.054	-.06	12.6 NA	.019	.052	.36
10	-.026	.054	-.48	12.8 NA	-.021	.052	-.41
11	-.006	.054	-.12	12.9 NA	-.033	.052	-.63
12	-.053	.054	-.99	13.9 NA	-.047	.052	-.89
13	-.076	.054	-1.40	16.1 NA	-.091	.052	-1.73
14	.156	.055	2.85	25.4 NA	.149	.052	2.86
here	---	---	---	---	---	---	---

suggesting structure at lags 7 and 14. Putting the the two clues together ( sample size of 365 and significant weekly i.e. lag 7 structure ) I decided to investigate whether or not this was indeed daily data. New users often omit very important information when they define their data on the mistaken premise that the computer should be smart enough to figure everything out. Note that the lag 7 and lag 14 clues were swamped in the OP'S ACF and PACF plots. The presence of deterministic structure in the residuals increase the error variance thus suppressing the acf. Once the outliers/pulses/level shifts were identified the acf revealed the presence of an autoregressive structure /daily indicators which then needed to be accounted for.

I then analyzed the data allowing the software to proceed with the clue that it was daily data. With only 365 values it is not possible to properly construct models containing seasonal/holiday predictors BUT that is possible with more than 1 year of data.

The model that was found is presented here



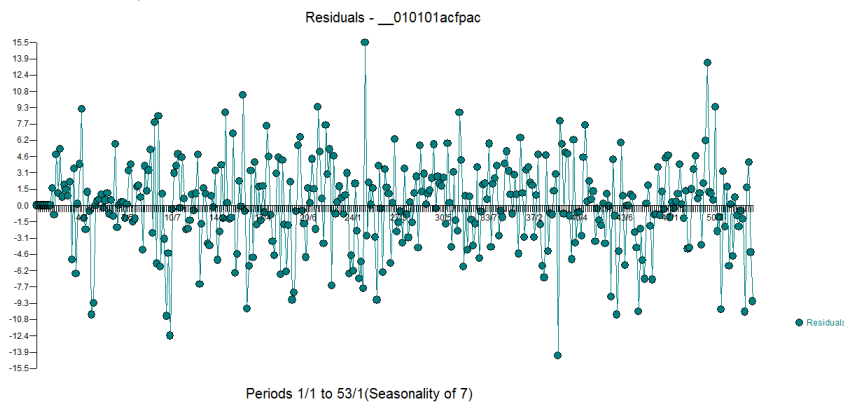
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Y(T) = 32.169
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+ [X2(T)] [(+ 4.0895)]
+ [X3(T)] [(+ 4.8971)]
+ [X4(T)] [(+ 4.7409)]
+ [X5(T)] [(+ 5.7827)]
+ [X6(T)] [(- 33.2875)]
+ [X7(T)] [(- 8.8435)]
+ [X8(T)] [(+ 3.5890)]
+ [X9(T)] [(- 28.3727)]
+ [X10(T)] [(- 27.2964)]
+ [X11(T)] [(- 25.5713)]
+ [X12(T)] [(- 23.6382)]
+ [X13(T)] [(- 22.4020)]
+ [X14(T)] [(- 23.1492)]
+ [X15(T)] [(- 27.1761)]
+ [X16(T)] [(- 19.4441)]
+ [X17(T)] [(- 28.9743)]
+ [X18(T)] [(- 19.3526)]
+ [X19(T)] [(- 11.8816)]
+ [X20(T)] [(- 20.4205)]
+ [X21(T)] [(- 11.3145)]
+ [X22(T)] [(- 14.6556)]
+ [X23(T)] [(- 18.1125)]
+ [X24(T)] [(- 18.8571)]
+ [X25(T)] [(- 15.1483)]
+ [X26(T)] [(- 17.0799)]
+ [X27(T)] [(- 15.4893)]
+ [X28(T)] [(- 16.8814)]
+ [X29(T)] [(- 26.5779)]
+ [X30(T)] [(- 17.7628)]
+ [X31(T)] [(- 14.2254)]
+ [(1- .411B** 1) (1- .200B** 7)]** -1 [A(T)]

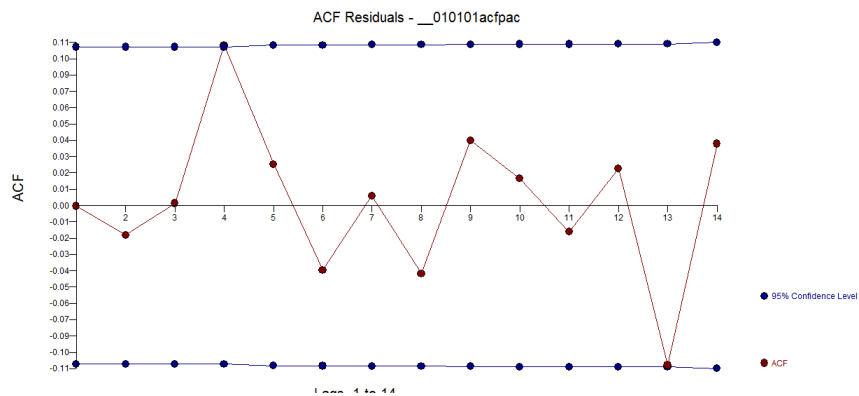
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FIXED_EFF_N10207
FIXED_EFF_N10307
FIXED_EFF_N10407
FIXED_EFF_N10507
:PULSE 01/31/01 5/ 3 31
:LEVEL SHIFT 04/14/01 15/ 6 104
:LEVEL SHIFT 07/03/01 27/ 2 184
:PULSE 12/28/01 52/ 5 362
:PULSE 02/01/01 5/ 4 32
:PULSE 10/28/01 43/ 7 301
:PULSE 12/22/01 51/ 6 356
:PULSE 02/05/01 6/ 1 36
:PULSE 03/18/01 11/ 7 77
:PULSE 12/24/01 52/ 1 358
:PULSE 10/29/01 44/ 1 302
:PULSE 12/07/01 49/ 5 341
:PULSE 10/18/01 42/ 4 291
:PULSE 11/04/01 44/ 7 308
:PULSE 03/17/01 11/ 6 76
:PULSE 06/22/01 25/ 5 173
:PULSE 06/03/01 22/ 7 154
:PULSE 02/04/01 5/ 7 35
:PULSE 12/06/01 49/ 4 340
:PULSE 06/02/01 22/ 6 153
:PULSE 12/23/01 51/ 7 357
:PULSE 10/04/01 40/ 4 277
:PULSE 11/30/01 48/ 5 334
:PULSE 12/09/01 49/ 7 343
:PULSE 12/25/01 52/ 2 359
:PULSE 03/23/01 12/ 5 82

```

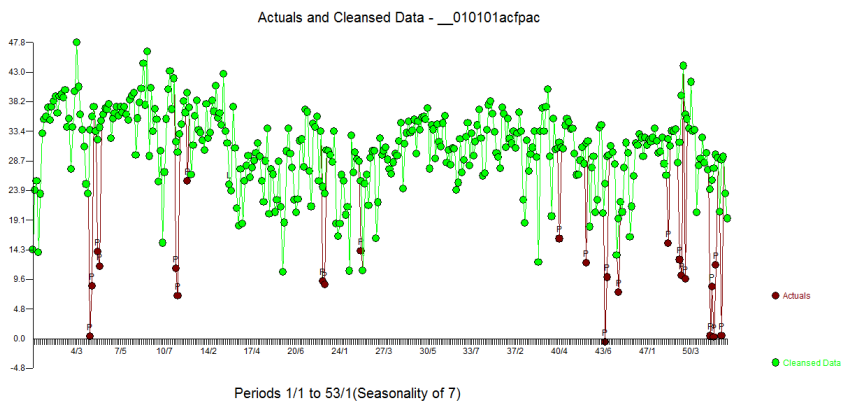
containing 5 daily dummies , two Level Shifts , a number of pulses and an arima model of the form (1,0,0)(1,0,0) . The plot of the residuals no longer evidences the non-constancy structure as a better model is in place.



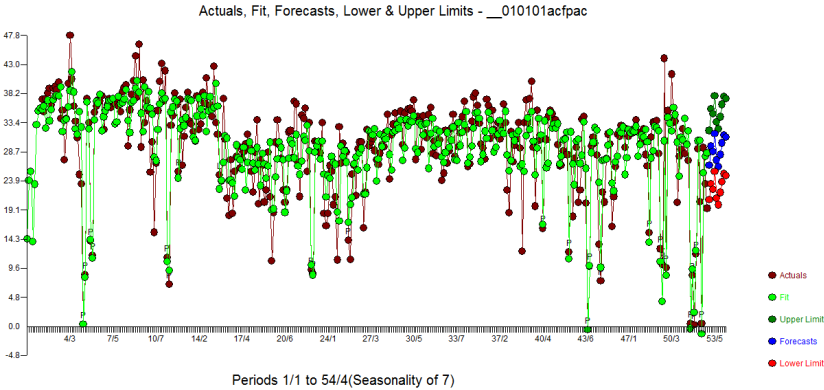
. Th



e acf of the residuals is much cleaner . The Actual /Cleansed graph highlights the unusual pulse points.




. The lesson here is that when one analyzed the data without the critical piece of information that it was a daily time series there were a ton of pulses reflecting an inadequate representation (or perhaps the advanced knowledge of the daily clue) . The Actual/Fit and Forecast is presented here



It would be interesting to see what others would do with the same data set. Note that all analyses were conducted in a hands-free mode using software that is commercially available.

edited Jan 24 at 16:53

answered Jan 22 at 13:43



IrishStat

11.8k 1 11 23

1 early morning mis read ... Don't normally see the lag(0) in my graphs – IrishStat Jan 22 at 13:45

1 It tricked me at first as well. – Glen\_b ♦ Jan 22 at 13:48

Thanks for your answer. As someone without experience in the field of time-series forecasting it is hard to fully understand the procedure of choosing the right model as there is no officially right way to go. Unfortunately i am not allowed to post my raw data. I hope that the additional information is useful (see 'EDIT:') – Peter Knutsen Jan 22 at 14:57

You can scale/mask your data before you present it. Looking at the plot it appears there might be some unusual values which if untreated downwards biases the acf and the pacf incorrectly suggesting sufficiency. There is a visual suggestion of a downwards trend followed by no trend but that is just a guess at this moment. – IrishStat Jan 22 at 17:52

i just added some data which you might use.. – Peter Knutsen Jan 22 at 22:58

http://stats.stackexchange.com/questions/134487/analyse-acf-and-pacf-plots

10/10