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If $q_0 = 0.1$ then, after $n = 90$ generations, $q_{90} = 0.01$.

Slogan

We may expect the lethal gene to die out, eventually, but the rate of decay is painfully slow.

$$q_n = \frac{1}{q_0^{-1} + n}$$