## Introduction to Week Five

**Initial Value Problems** 

Systems of Differential Equations

## Initial Value Problems in MATLAB

Quiz

## Programming Assignment: The Two-Body Problem

**Boundary Value Problems** 

Video: The Two-Body Problem (Part A) | Lecture 58

Reading: Circular orbits

9 min

10 min

10 min

Video: The Two-Body Problem (Part B) | Lecture 59

Ungraded External Tool: Two-Body Problem (audit)

Reading: Reference Solution to "Two-Body Problem (audit)"
1 min

Graded External Tool: Two-Body
Problem
Submitted

Reading: Reference Solution to "Two-Body Problem"

1 min

## Reference Solution to "Two-Body Problem"

e=0.7; m1=1; m2=4;

T=2\*pi./(1-e).^1.5; tspan=linspace(0,T,1000);

options=odeset('RelTol',1.e-6);

%%%%% Solve differential equations for x and y and find x1,y1 and x2,y2

[t,xyuv]=ode45(@(t,xyuv) newton(xyuv),tspan,[-1,0,0,sqrt(1+e)],options);

x=xyuv(:,1); y=xyuv(:,2);

x1=m2/(m1+m2)\*x; y1=m2/(m1+m2)\*y;

 $x2=-m1/(m1+m2)^*x; y2=-m1/(m1+m2)^*y;$ 

% k=0.1;

 $\% R1=k^{*}(m1)^{(1/3)}; R2=k^{*}(m2)^{(1/3)}; \% radius of masses$ 

% theta = linspace(0,2\*pi);

% figure; axis equal; hold on; set(gcf,'color','w');

% axis off;

% xlim([-2,5]); ylim([-2.5,2.5]);

% planet=fill(R1\*cos(theta)+x1(1), R1\*sin(theta)+y1(1),'b'); % sun=fill(R2\*cos(theta)+x2(1), R2\*sin(theta)+y2(1),'r');

% pause(1);

% nperiods=5; %number of periods to plot

% for j=1:nperiods

% for i=1:length(t)

% planet.XData=R1\*cos(theta)+x1(i); planet.YData=R1\*sin(theta)+y1(i);

% sun.XData=R2\*cos(theta)+x2(i); sun.YData=R2\*sin(theta)+y2(i);

% drawnow;

% end

% end

function d\_xyuv\_dt=newton(xyuv)

x=xyuv(1); y=xyuv(2); u=xyuv(3); v=xyuv(4);

 $r=sqrt(x^2 + y^2);$ 

d\_xyuv\_dt=[u; v; -x/r^3; -y/r^3];

end

✓ Completed Go to next item

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