

The art of making money: portfolios and the stock market

The price of a stock

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Investment at
previous close

Value at close

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The stock market after a day of trading

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