

# Maxcut





**Negative results**

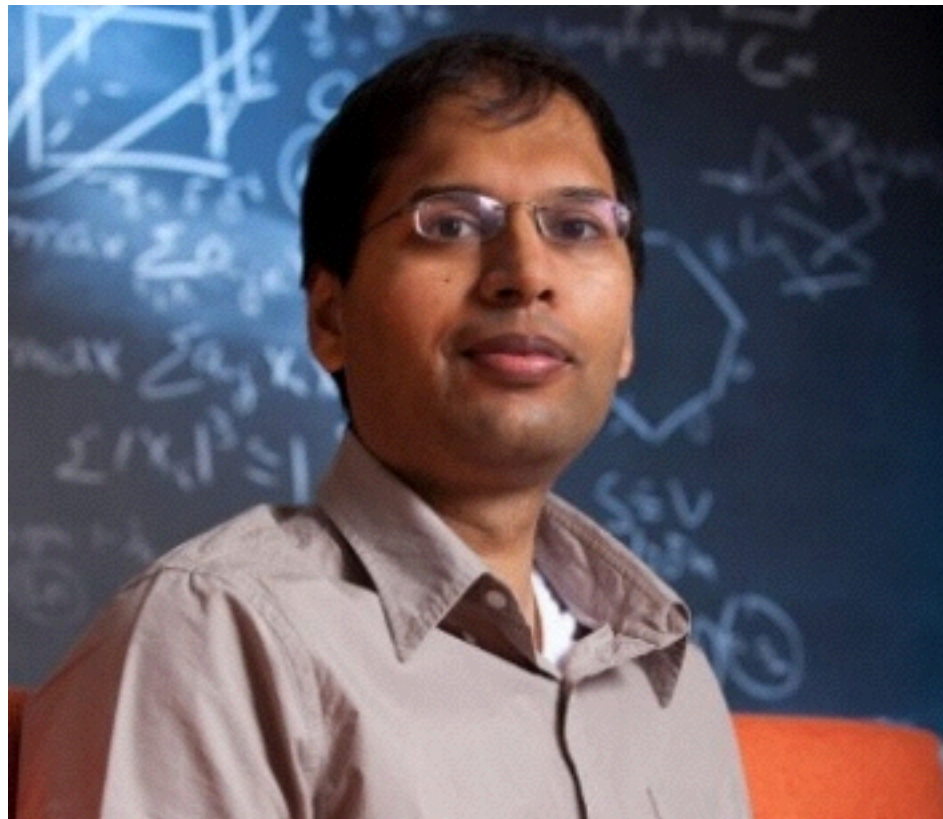


**KARP**fest80





**If the Unique Games Conjecture holds then  
approximating MaxCut  
better than 0.878...  
is NP-hard**



**Subash  
Khot**



**Guy  
Kindler**

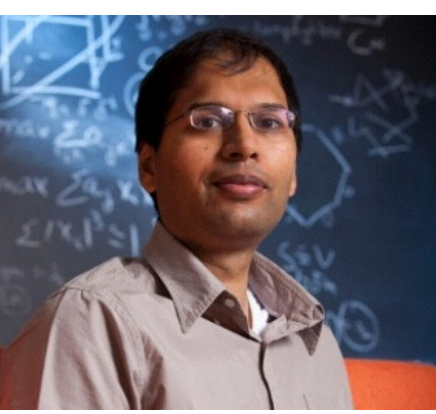


**Elchanan  
Mossel**



**Ryan  
O'Donnell**

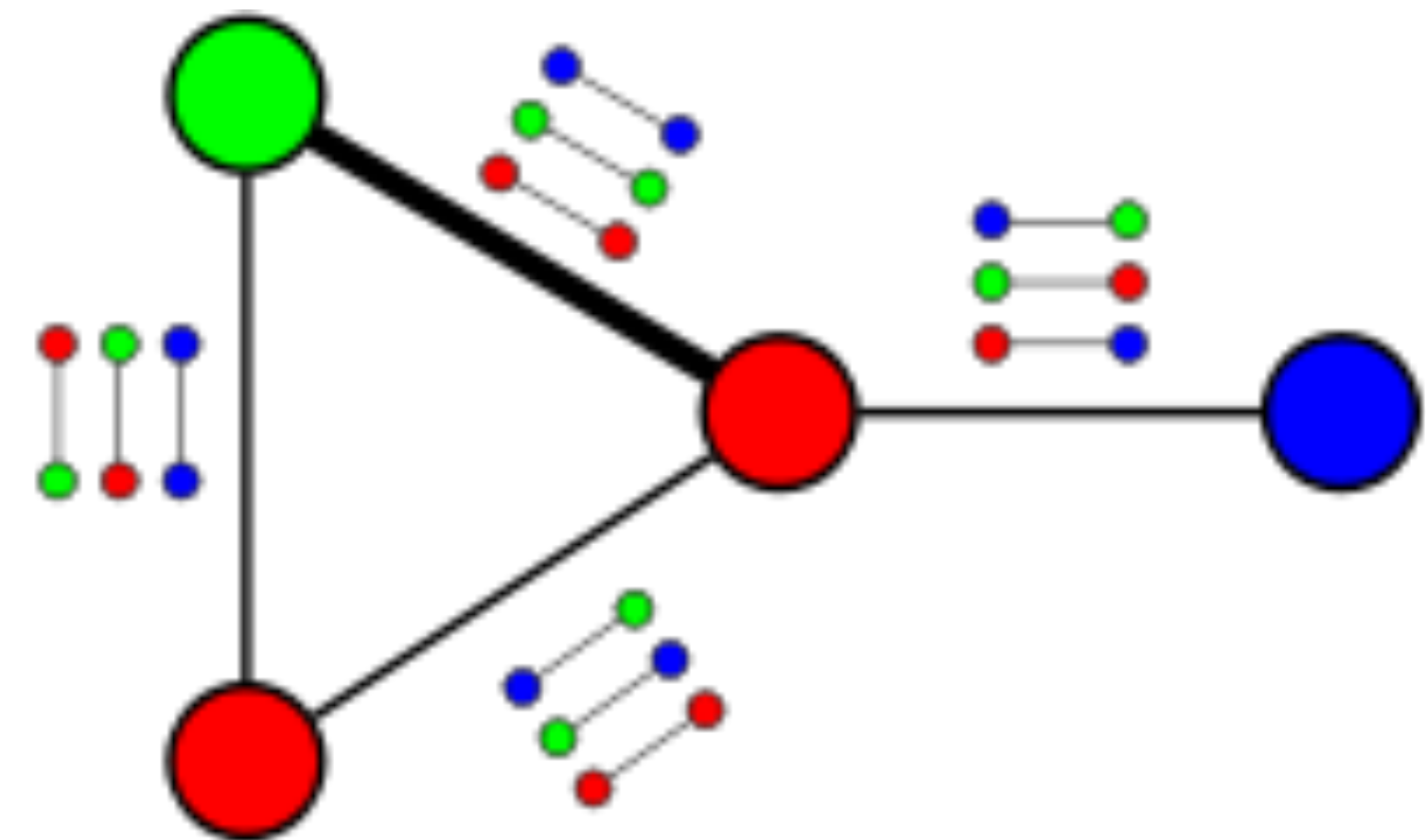
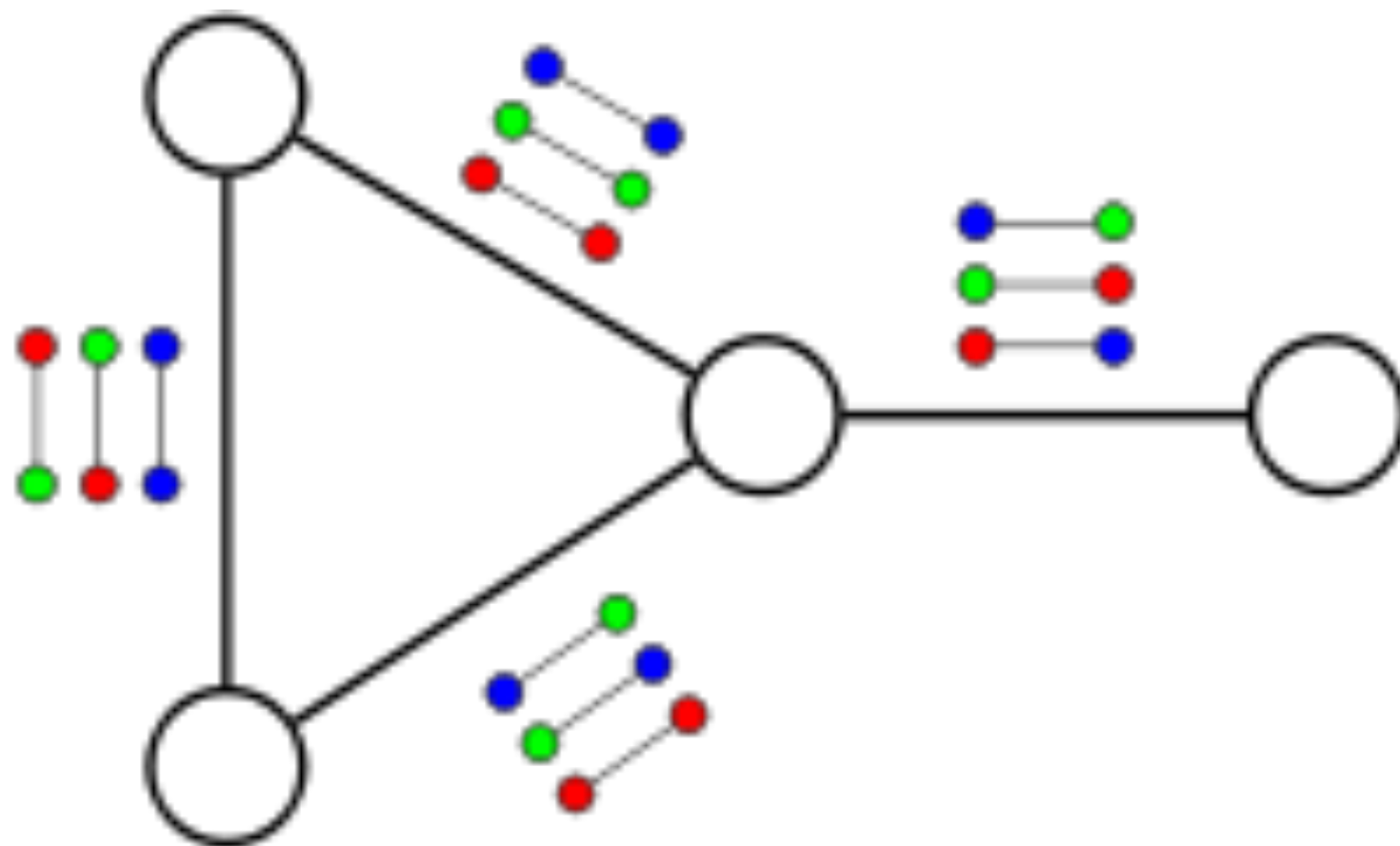
# UGC: the following problem is (?) NP-hard



**Input:**

- graph with for each edge  $\{u,v\}$ , permutation rule “if  $u$  is red then  $v$  must be green; if  $u$  is green then  $v$  must be blue; if  $u$  is blue then  $v$  must be yellow...” such that:
  - either there is a coloring satisfying 90% of the edge rules,
  - or no coloring satisfies more than 10% of the edges rules

**Output:** decide which of the two holds!





**Positive results**



# Ellipsoid method ... for SDPs



**Leonid  
Khachiyan**



**Martin  
Grötschel**



**László  
Lovász**



**Alexander  
Schrijver**



# SDP relaxation of MaxCut



**Charles  
Delorme**



**Svatopluk  
Poljak**



# Randomized rounding and .878... approx



**Michel  
Goemans**



**David  
Williamson**



# Maxcut

