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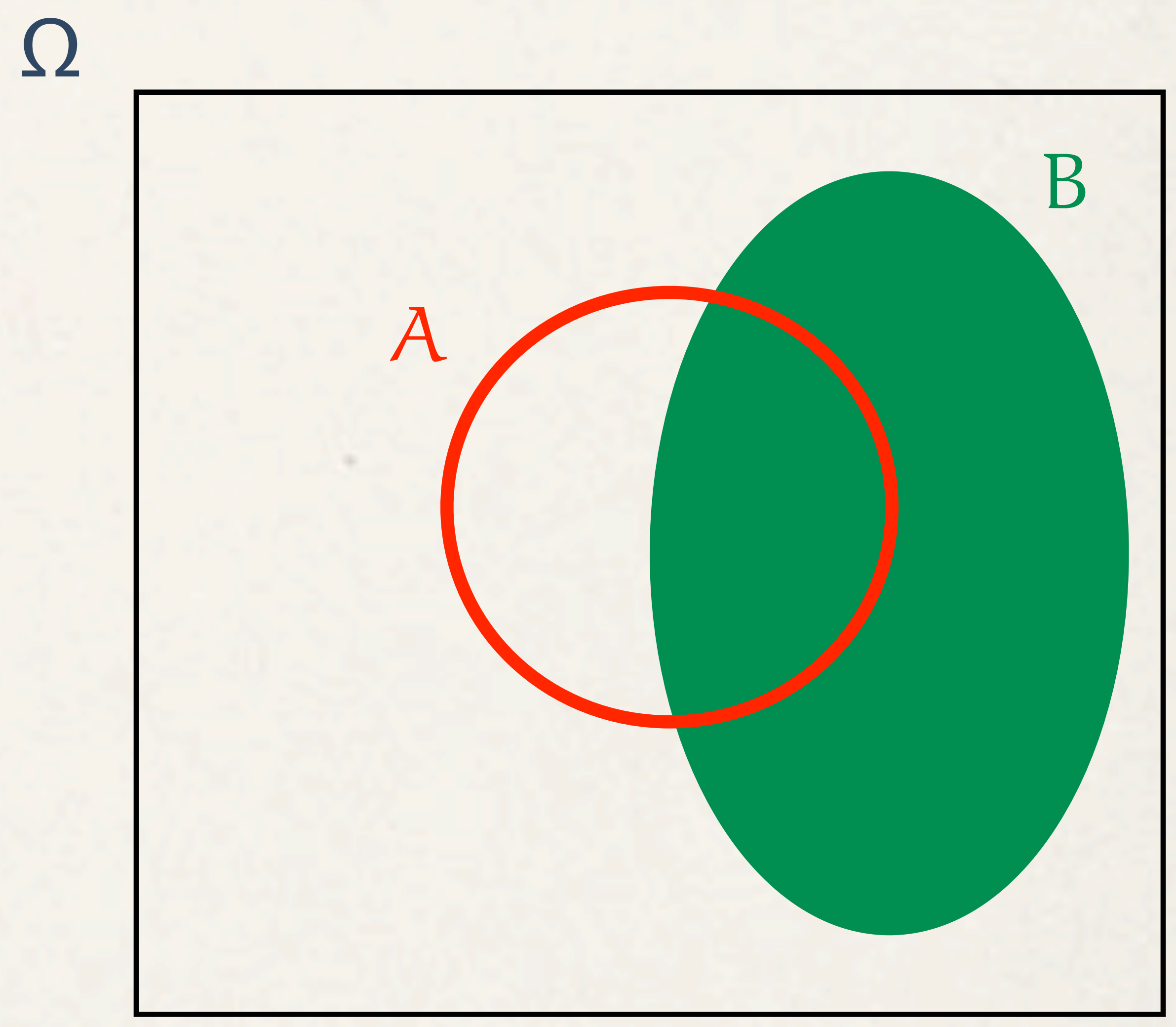

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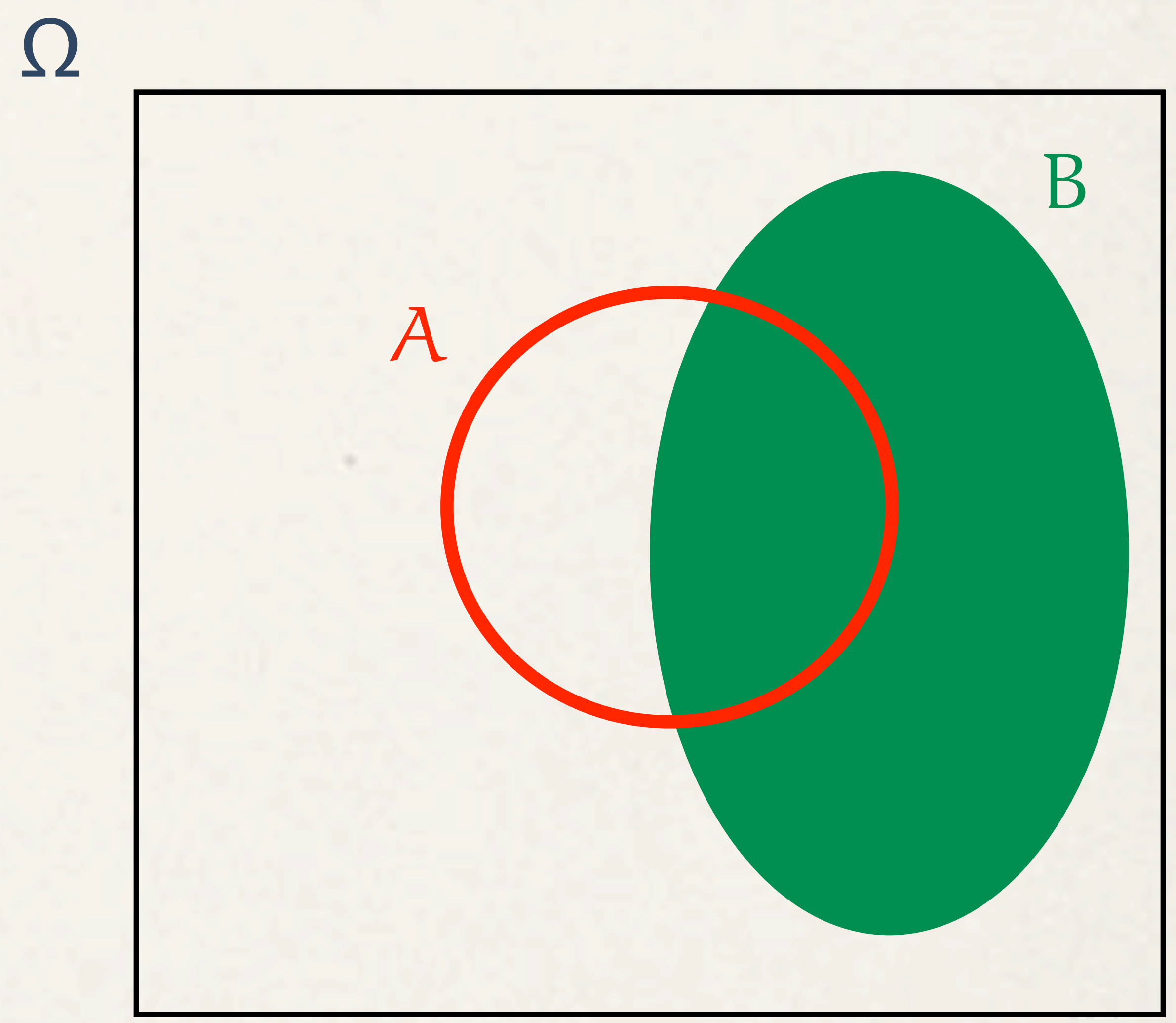

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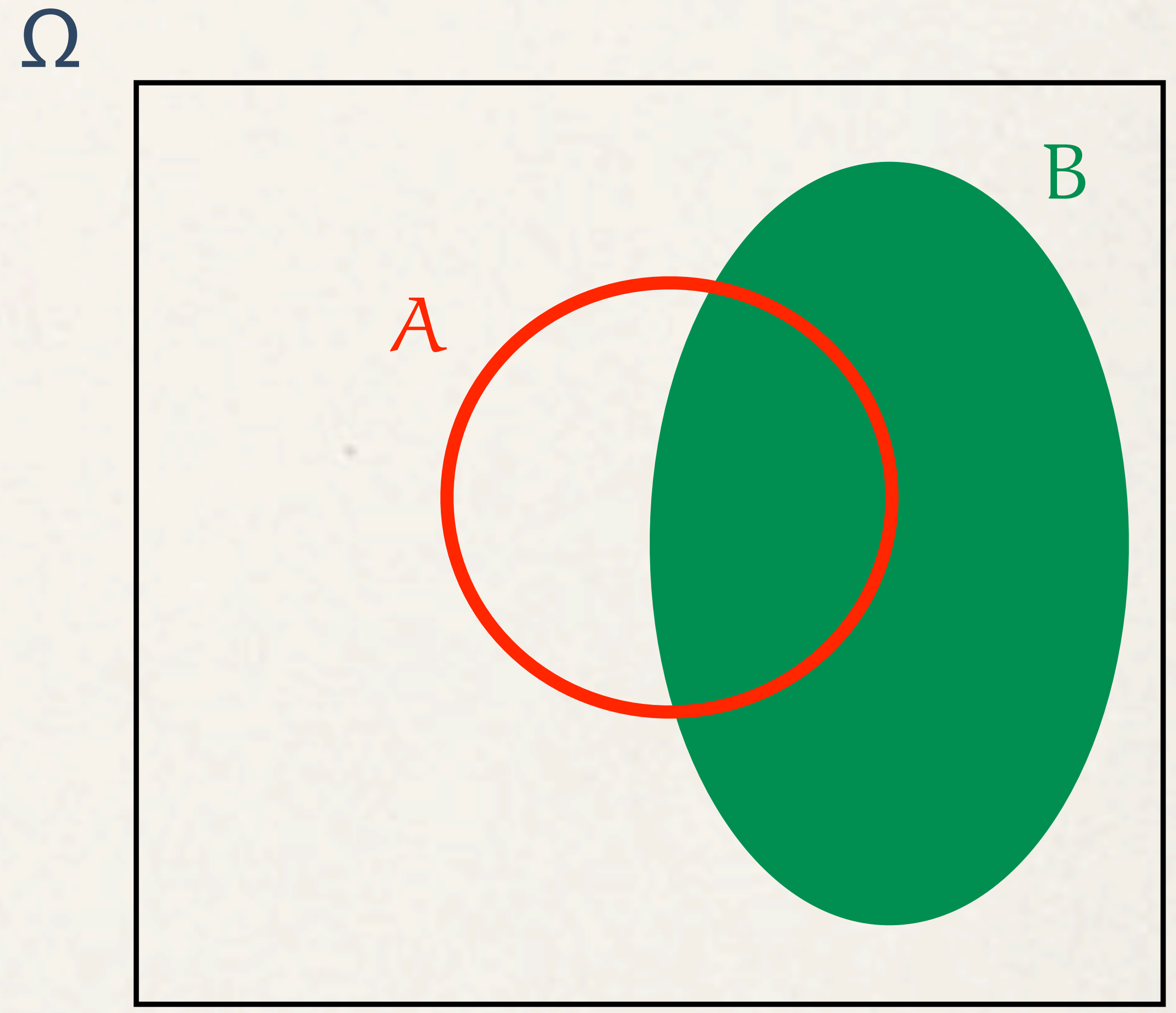

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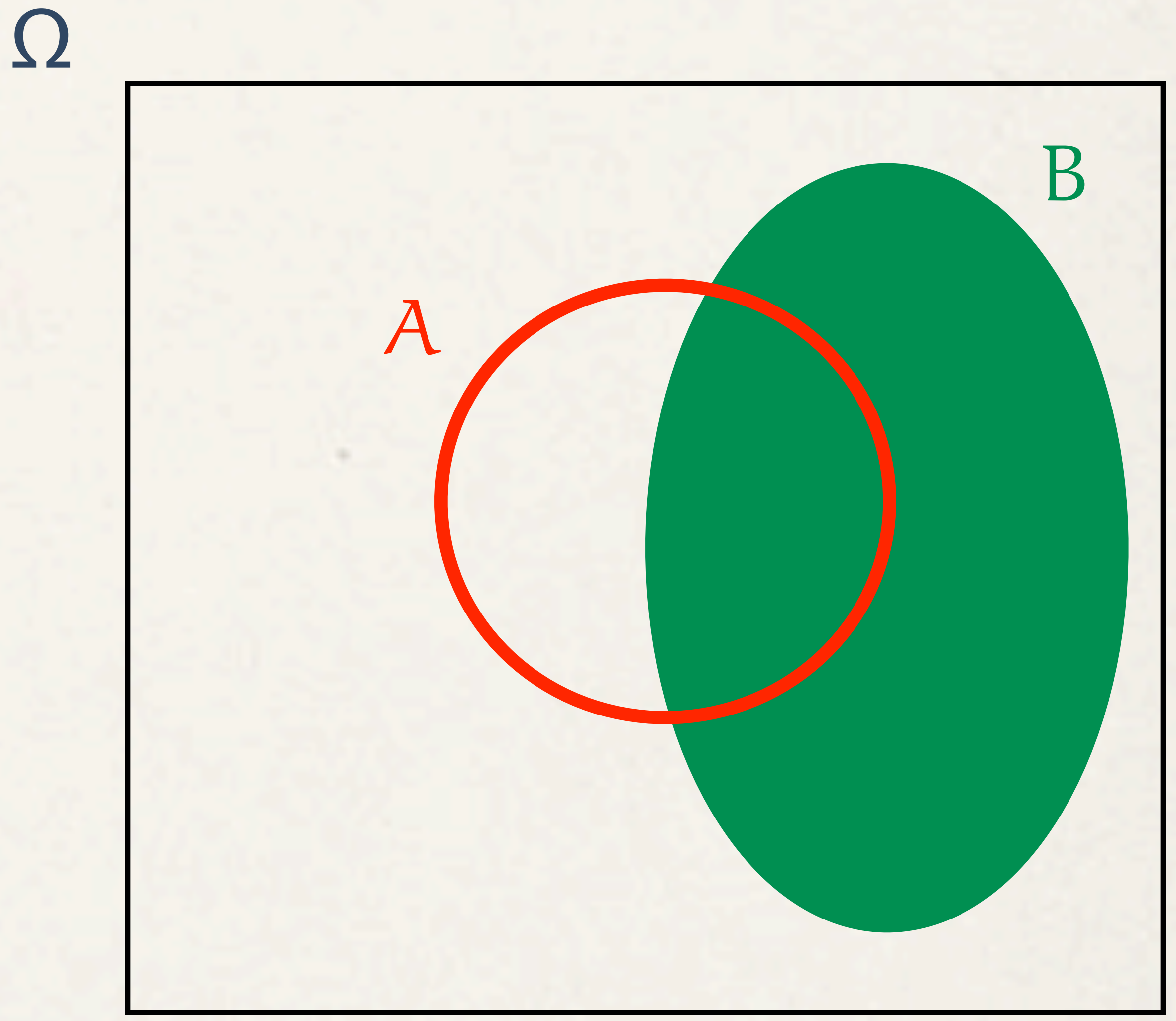

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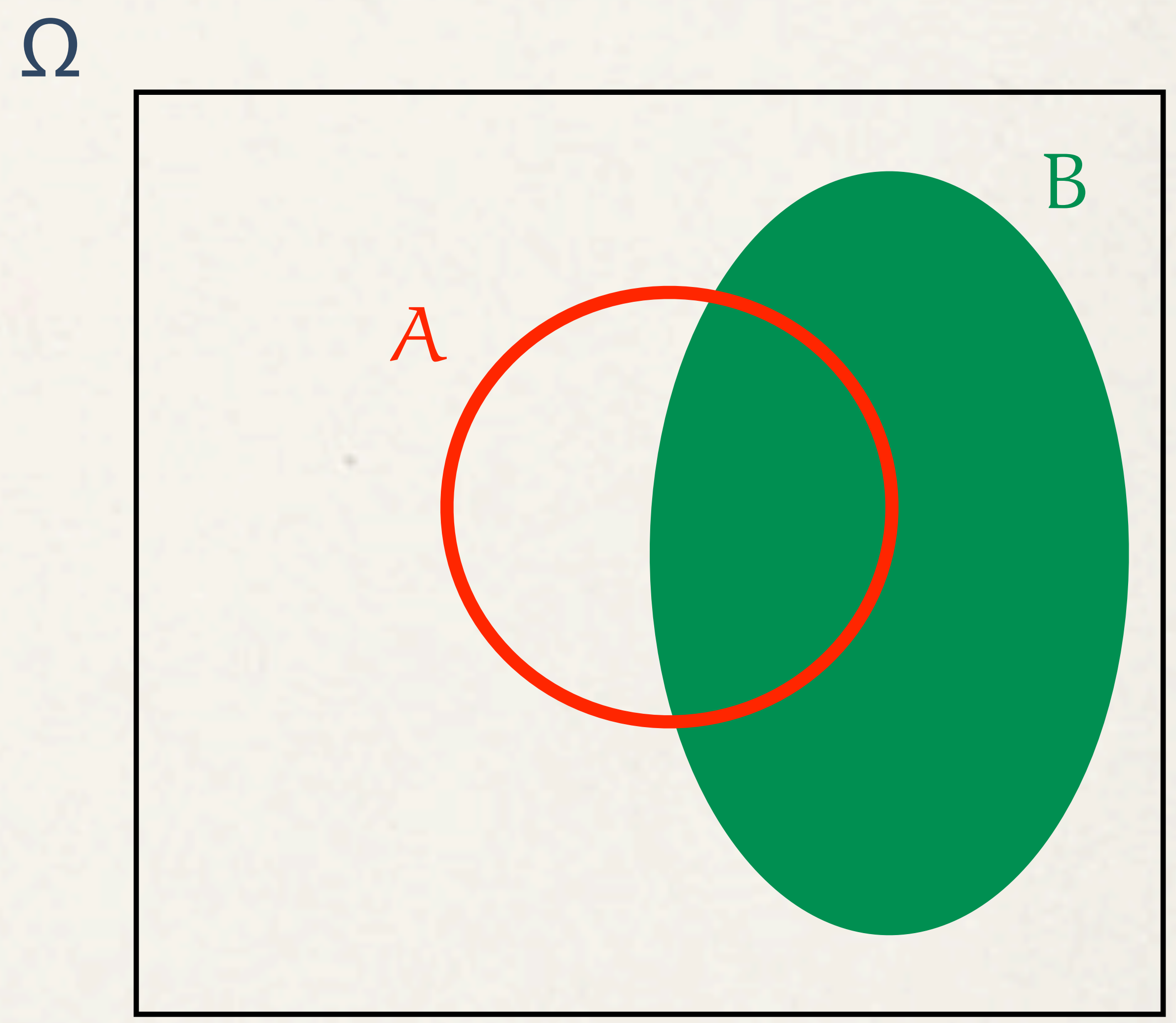

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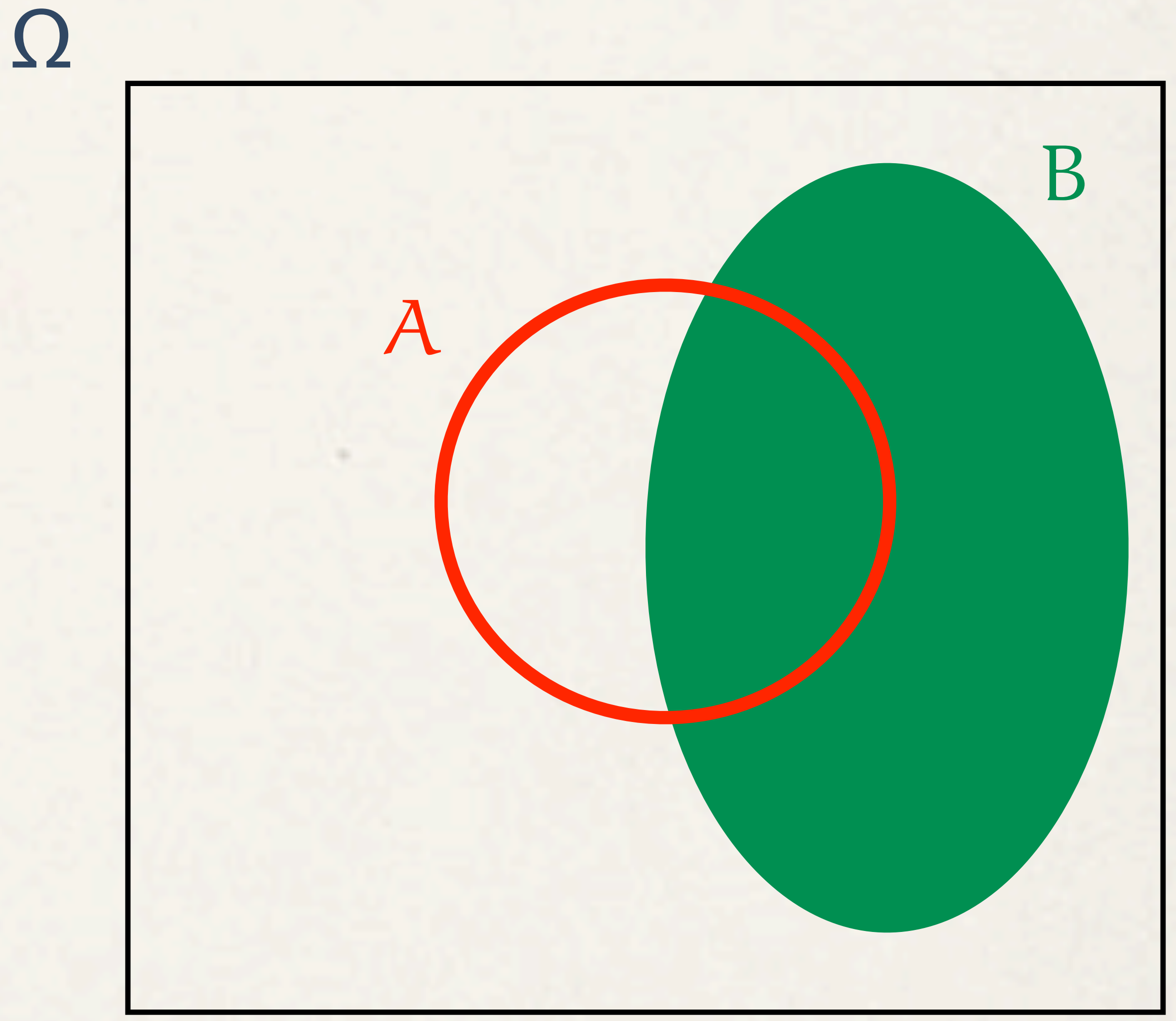

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$\mathbf{P}(B \mid A) = \mathbf{P}(A \mid B)$ if, and only if, $\mathbf{P}(A) = \mathbf{P}(B)$.