Problem 10.4

Assume we have a language consisting of the object constant a and the unary function constant s.

Prove the goal from the given premises.

| Proof Editor | | |
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| | | |
| 1. | falls(a) | Premise |
| 2. | AX:(falls(X) => falls(s(s(X)))) | Premise |
| 3. | AX:(falls(s(X)) => falls(X)) | Premise |
| 4. | falls(X) => falls(s(s(X))) | Universal Elimination: 2 |
| 5. | falls(X) | Assumption |
| 6. | falls(s(s(X))) | Implication Elimination: 4, 5 |
| 7. | falls(s(s(X))) => falls(s(X)) | Universal Elimination: 3 |
| 8. | falls(s(X)) | Implication Elimination: 7, 6 |
| 9. | falls(X) => falls(s(X)) | Implication Introduction: 8 |
| 10. | AX:(falls(X) => falls(s(X))) | Universal Introduction: 9 |
| 11. | AX:falls(X) | Induction: 1, 10 |
| | | |
| Goal | AX:falls(X) | Complete Submit |
| | Assumption Negation Introduction Implication Introduction Reiteration Negation Elimination Implication Elimination Delete And Introduction Biconditional Introduction | Universal Introduction Universal Elimination Existential Introduction |

| And Elimination | Biconditional Elimination | Existential Elimination |
|-----------------|---------------------------|-------------------------|
| Or Introduction | | Induction |
| Or Elimination | | |
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