

Lesson Learning Objectives

LO 1. Define the multiple linear regression model as

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_k x_k$$

where there are k predictors (explanatory variables).

- **LO 2.** Interpret the estimate for the intercept (b_0) as the expected value of y when all predictors are equal to 0, on average.
- **LO 3.** Interpret the estimate for a slope (say b_1) as "All else held constant, for each unit increase in x_1 , we would expect y to be higher/lower on average by b_1 ."
- **LO 4.** Define collinearity as a high correlation between two independent variables such that the two variables contribute redundant information to the model -- which is something we want to avoid in multiple linear regression.
- **LO 5.** Note that R^2 will increase with each explanatory variable added to the model, regardless of whether or not the added variable is a meaningful predictor of the response variable. Therefore we use adjusted R^2 , which applies a penalty for the number of predictors included in the model, to better assess the strength of a multiple linear regression model:

$$R_{adj}^2=1-rac{SSE/(n-k-1)}{SST/(n-1)}$$

where n is the number of cases and k is the number of predictors.

Note that R^2_{adj} will only increase if the added variable has a meaningful contribution to the amount of explained variability in y, i.e. if the gains from adding the variable exceeds the penalty.

- **LO 6.** Define model selection as identifying the best model for predicting a given response variable.
- **LO 7.** Note that we usually prefer simpler (parsimonious) models over more complicated ones.
- **LO 8.** Define the full model as the model with all explanatory variables included as predictors.