Solutions to Homework 8

Help Center

Problem sparse_array_out

```
function success = sparse_array_out (A, filename)
    fid = fopen (filename,'w+');
    success = fid>=0;
    if ~success
        error ('Error opening file %s\n',filename)
                                             % locations and values of non-zero element
    [r,c,v] = find(A);
s
                                             % dimensions of A
    [nr,nc] = size(A);
    nze = length(v);
                                             % number of non-zero elements
    fwrite (fid, [nr,nc,nze], 'uint32');
                                           % global data
    for k = 1:nze
                                             % for each non-zero element ...
        fwrite (fid, [r(k),c(k)], 'uint32'); % row-column index
        fwrite (fid, v(k), 'double');
                                            % value
    end
    fclose(fid);
end
```

Problem sparse_array_in

```
function A = sparse array in (filename)
   A = [];
    fid = fopen(filename, 'r');
    if fid<0
        error ('Error opening file %s\n',filename)
    end
    x = fread(fid,3,'uint32');
                                                % global data (nr, nc, nze)
   A = zeros(x(1),x(2));
                                                % initialize new nr x nc matrix
   for k=1:x(3)
                                                % for each non-zero element ...
        z = fread(fid,2,'uint32');
                                                % row, column
        A(z(1),z(2)) = fread(fid,1,'double'); % value
    fclose(fid);
end
```

Probel letter_counter

```
function n = letter_counter(fname)
fid = fopen(fname,'r');
```

Probel letter_counter (alternative solution)

A shorter variant

```
function n = letter_counter(fname)
    n = -1;
    fid = fopen(fname, 'r');
    if fid >= 0
        n = sum(isletter(fread(fid,inf,'char=>char')));
        fclose(fid);
    end
end
```

Problem saddle

```
function s = saddle(M)
   [r c] = size(M);
   s = [];
   if r > 1
      else
      cols = M;
                         % vector is a special case, min would give a single val
ue
   end
   if c > 1
      else
                         % vector is a special case, max would give a single val
      rows = M;
ue
   end
   for ii = 1:c
                         % visit each column
      for jj = 1:r
                         % and each row, that is, each element of M
         if M(jj,ii) == cols(ii) \&\& M(jj,ii) == rows(jj) % if both conditions hold
            s = [s; jj ii];
                                               % saddle point! Let's add i
t!
         end
      end
   end
```

end

Problem prime_pairs

```
function p = prime_pairs(n)
   if isprime(2+n)
                             % many times the answer is 2
       p = 2;
   elseif rem(n,2)
                             % if not, and n is odd, no such prime exists
       p = -1;
   else
       if isprime(p+n)
                            % if p+n is prime
                            % found it! Return immediately
               return;
           end
       end
                             % none found (btw, we never get here)
       p = -1;
   end
end
% It turns out that for n-s smaller than 100,000 that are even, there is
% always a pretty small such prime. In fact, the largest is 227.
% So we could use primes(300) instead of primes(1e5) to make this even
% faster. Also, the for-loop would be slow, if we did not check for even n-s,
% since it would need to go through all primes smaller than 100,000 to
% realize that no solution exists. So, handling the first two cases (p is 2
% and n is odd) separately makes the function very efficient.
```

Problem prime_pairs (alternative solution)

No loop at all. This illustrates yet again that there is always a MATLAB built-in function for almost anything reasonable...

```
function p = prime_pairs(n)
   p = intersect(allp,allp+n); % Get which values are prime when n is added
                            % Check to see if there are any such values
   if isempty(p)
       p = -1;
   else
       p = p(1)-n;
                       % If so, subtract off the n to get the smaller value of
the prime pair
   end
end
% Elegant solution, but because it does not check for odd n and because it
% always handles the entire vector of primes even though the answer, if it
% exists, is small, it is about 4x slower than the for-loop version above
% even though the built-in function intersect is very fast.
```

Problem bowl

```
function score = bowl(balls)
                                             % index into balls
   index = 0;
                                             % multiply next ball
   first = 1;
   second = 1;
                                             % multiply ball after next
   score = 0;
                                             % cummulative sum
   if sum(balls > 10 \mid balls < 0) > 0
                                             % single hit must be between 0 and 10 i
nclusive
       score = -1;
                                             % error!
       return;
   end
   for ii = 1:10
                                             % first ten frames
       index = index + 1;
                                            % take next ball
       if index > length(balls)
                                             % not enough balls
                                             % error!
           score = -1;
           return;
       end
       score = score + first * balls(index);  % count score including extra from prev
ious strike or spare
       first = second;
                                             % move multiplier value from second to
first
       second = 1;
                                             % reset multiplier for the ball after n
ext to 1
       if balls(index) == 10
                                             % strike
                                             % so next counts extra
           first = first + 1;
                                             % and so is the one after next
           second = 2;
           continue;
                                             % go to next frame, there is no second
ball in this one
       end
       index = index + 1;
                                            % take next ball
       if index > length(balls)
                                            % not enough balls
           score = -1;
                                             % error
           return;
       end
       score = score + first * balls(index);
                                            % count score including extra f
rom previous strike
       first = second;
                                                     % move multiplier value from se
cond to first
                                                     % reset multpilier for the ball
       second = 1;
after next to 1
       first = first + 1;
                                                     % so next counts extra
       elseif balls(index) + balls(index -1) > 10 % cannot score higher than 10 i
n a frame
                                                     % error!
           score = -1;
           return;
       end
   end
```

```
for ii = [first second]
                                                % max 2 extra balls if needed
        if ii < 2
                                                % no extra ball here
            break;
                                                % we are done
        end
                                               % take next ball
        index = index + 1;
        if index > length(balls)
                                               % not enough balls
                                                % error!
            score = -1;
            return;
        end
        score = score + (ii-1) * balls(index); % extra balls: count them one less than
a normal ball
    end
    if index < length(balls)</pre>
                                                % additional ball in the input
                                                % error!
        score = -1;
    end
end
```

Problem maxsubsum

traditional brute-force solution with four nested loops

```
function [x y rr cc s] = maxsubsum(A)
    [row col] = size(A);
   % initialize result to the 1-by-1 subarray at the top left corner of A
   x = 1;
                                                 % top left corner of subarray
   y = 1;
                                                 % top left corner of subarray
                                                 % height of subarray
   rr = 1;
                                                 % width of subarray
    cc = 1;
                                                 % sum
    s = A(1,1);
    for r = 1:row
                                                 % height of subarray
        for c = 1:col
                                                 % width of subarray
            for ii = 1:row-r+1
                                                 % start position row
                for jj = 1:col-c+1
                                                 % start position col
                    tmp = sum(sum(A(ii:ii+r-1,jj:jj+c-1))); % sum up candidate
                                                 % if larger than current max
                    if tmp > s
                        s = tmp;
                                                 % set the new values
                        x = ii;
                        y = jj;
                        cc = c;
                        rr = r;
                    end
                end
            end
        end
    end
end
```

Problem maxsubsum (alternative solution)

Using Kadane's algorithm. Kadane's algorithm finds the contiguous subvector with the max sum within a vector using a single loop. For a detailed explanation, google "Kadane's algorithm maximum subarray problem." It is much faster than the previous solution because it needs only three nested loops. Try both with a 100x100 matrix and you'll see the difference:)

```
function [fx1 fy1 rr cc mx] = maxsubsum(A)
    [row col] = size(A);
    mx = A(1,1)-1;
    for ii = 1:row
        tmp = zeros(1,col);
        for jj = ii:row
            tmp = tmp + A(jj,:);
            [y1 y2 cur] = kadane(tmp);
            if cur > mx
                mx = cur;
                fx1 = ii;
                rr = jj-ii+1;
                fy1 = y1;
                cc = y2-y1+1;
            end
        end
    end
end
function [x1, x2, mx] = kadane(v)
    mx = v(1);
    x1 = 1; x2 = 1;
    cx1 = 1;
    cur = 0;
    for ii = 1:length(v)
        cur = cur+v(ii);
        if(cur > mx)
            mx = cur;
            x2 = ii;
            x1 = cx1;
        end
        if cur < 0
            cur = 0;
            cx1 = ii + 1;
        end
    end
end
```

Problem queen check

It uses the fact that a diagonal either starts in the first column or ends in the last column (or both). Only sum and max built-in functions are used.

```
function ok = queen_check(board)
  n = 8;
  ok = true;
  v = board(:);
                             % create a vector in col major order
  w = v(end:-1:1);
                             % reverse order, so last col becomes first
col
  for ii = 1:n
     tests = [
                             % row #ii
          sum(board(:,ii))
           sum(board(ii,:))
                             % col #ii
           sum(v(ii:n+1:(n-ii+1)*n)) % diagonal starting in the first column goi
ng down
          ng up
          ng up
          ng down
          1;
     if max(tests) > 1
                             % these should be all 0 or 1
        ok = false;
                             % otherwise return false
        return;
     end
  end
end
```

Problem queen check (alternative solution)

Surprise, surprise: MATLAB has a built-in function called diag and flip

Problem roman2

Nice and short solution

```
function A = roman2 (R)
% This function initially assumes the supplied input is valid. If it is not valid,
% the result, when converted back to Roman, will differ from the original input.
```

```
Roman = 'IVXLC';
    Arabic = \{1 \ 5 \ 10 \ 50 \ 100\};
    LastValue = 0;
                                   % V is value, LastValue is last V
    A = uint16(0);
                             % scan backward from last character
    for k = length(R):-1:1
        P = strfind(Roman,R(k)); % search list of valid Roman characters
                                    % if invalid
        if isempty(P)
            V = 0;
                                   % value is zero
                                    % else
        else
                                   % value is Arabic equivalent
            V = Arabic{P};
        end
        if V<LastValue
                                   % if subtractive situation
            A = A-V;
                                   % subtract this value
                                   % else
        else
                                   % add this value
           A = A+V;
        end
                                   % (in either case, V=0 did nothing)
        LastValue = V;
                                    % update last value used
    end
    if A>=400 |  ~strcmp(R,A2R(A)) % if out of range or result does
        A = uint16(0);
                                   % not generate original string
    end
                                    % send back zero
end
% convert Arabic to Roman
function R = A2R (A)
% Remove subtraction by including secondary moduli.
    Roman = {'I' 'IV' 'V' 'IX' 'X' 'XL' 'L' 'XC' 'C'};
    Arabic = \{1 \ 4 \ 5 \ 9 \ 10 \ 40 \ 50 \ 90 \ 100\};
    R = ''; k = 9;
    while k>0
                                    % remove larger moduli first
                                  % if value is at least current modulus
       if A>=Arabic{k}
            A = A-Arabic\{k\};
                                  % remove modulus from value
            R = [R Roman\{k\}];
                                  % append Roman character
        else
                                   % else
            k = k-1;
                                    % consider next smaller modulus
        end
    end
end
```

Problem roman2 (alternative implementation)

Uses a Finite State Machine (FSM). For a detailed description, download this PDF document.

6/16/2015

```
% 1st col: current state; 2nd col: input char; 3rd col: next state
    trans = [
       1 'I' 2; 1 'X' 11; 1 'C' 20; 1 'L' 16; 1 'V' 7;
       2 'I' 3; 2 'V' 5; 2 'X' 6;
       3 'I' 4;
       7 'I' 8;
       8 'I' 9;
       9 'I' 10;
       11 'X' 12; 11 'V' 7; 11 'I' 2; 11 'L' 14; 11 'C' 15;
       12 'X' 13; 12 'V' 7; 12 'I' 2;
       13 'V' 7; 13 'I' 2;
       14 'V' 7; 14 'I' 2;
       15 'V' 7; 15 'I' 2;
       16 'V' 7; 16 'I' 2; 16 'X' 17;
       17 'V' 7; 17 'I' 2; 17 'X' 18;
       18 'V' 7; 18 'I' 2; 18 'X' 19;
       19 'V' 7; 19 'I' 2;
       20 'V' 7; 20 'I' 2; 20 'C' 21; 20 'X' 11; 20 'L' 16;
       21 'V' 7; 21 'I' 2; 21 'C' 22; 21 'X' 11; 21 'L' 16;
       22 'V' 7; 22 'I' 2; 22 'X' 11; 22 'L' 16;
    ];
    state = 1;
                                                      % initial state: 1
                                                      % initial value: 0
    num = 0;
   for ii = 1:length(rom)
                                                      % take input from left
       state = next_state(state, rom(ii), trans);
                                                      % find next state
       if state == -1
                                                      % no such transition
           num = 0;
                                                      % illegal roman number
                                                      % get out
           break;
       end
                                                      % otherwise, increase value
       num = num + states(state);
    end
    num = uint16(num);
end
function state = next_state(state,ch,trans)
    for ii = 1:size(trans,1)
                                                     % check each legal transition
       if trans(ii,1) == state && trans(ii,2) == ch % for current state and input c
har
           state = trans(ii,3);
                                                      % return next state
           return;
       end
    end
    state = -1;
                                                      % no transition found
end
```

Problem bell

```
function x = bell(n)
```

```
% Check input (integer >= 1)
    if (n \sim = floor(n)) \mid | (n < 1)
        x = [];
    elseif (n == 1)
        % Special case of n = 1
        x = 1;
    else
        % Make matrix of zeros
        x = zeros(n);
        % Fill in top-left corner for 2-by-2
        x(1:2,1:2) = [1 2;1 0];
        % Loop over remaining "lines"
        for k = 3:n
            \% 1st element of the line k is the last element of line k-1
            x(k,1) = x(1,k-1);
            % Loop over the remaining elements
            for j = 2:k
                % jth element is sum of j-1 element of current line plus
                % j-1 element of previous line
                x(k-j+1,j) = x(k-j+1,j-1) + x(k-j+2,j-1);
            end
        end
    end
end
```

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