1. 
$$\frac{\partial f}{\partial b}(b) = b + b = ab$$

$$\frac{\partial f}{\partial b}(b) = \sum_{i=1}^{n} b_{i}^{2} \frac{\partial f}{\partial b_{i}}(b) = 2bi$$

$$\frac{\partial^{2} f}{\partial b_{i}}(b) = \sum_{i=1}^{n} b_{i}^{2} \frac{\partial^{2} f}{\partial b_{i}}(b) = I \text{ (pxp) identity matrix}$$

$$\frac{\partial^{2} f}{\partial b_{i}^{2} \partial b_{i}}(b) = \begin{cases} 1 & \text{if } i = 1 \\ 0 & \text{if } i \neq j \end{cases} = \frac{\partial^{2} f}{\partial b_{i}^{2} \partial b_{i}}(b) = I \text{ (pxp) identity matrix}$$

- 2. A (pxp) diagonal matrix x'Ax=\(\int\_{i=1}^{p}a\_{ii}x\_{i}^{2}\) x'Ax = \(\begin{pmatrix} >0 & \text{for all i} \\ <0 & \text{gail} \text{au}\) for all i
- 3. g(b)=(y-Xb)'(y-Xb)=y'y-2y'Xb+b'X'Xb 38(b) = -(2y'X)'+(X'X+(X'X))b=-2X'y+2X'Xb Q (a'b) (b) = (a')'=a X'X symmetric of (b\*) = -2X'y+2X'Xb\* =0 X'Xb'' = 0 exists as  $X'Xb^* = X'y$  X'X has full rank  $b^* = (X'X)^{-1}X'y$ ab'ab (b) = 2X'X => positive definite => b\* is a minimum