

MOOC Econometrics

Lecture 4.1 on Endogeneity: Motivation

Dennis Fok

Motivating example

We want to explain

- *Number of flights at an airport per month (y) using*
- *Number of travel insurances made in previous month (x)*

Suppose OLS yields

$$y = 10,000 + .25x + e$$

Test

How should we interpret the obtained coefficients?

What does the estimate .25 really mean?

Interpretation of parameters

Given the estimates (y : flights, x : insurances)

$$y = 10,000 + .25x + e$$

Correct: 4,000 *insurances sold* \rightarrow *expected number of flights*
 $= 10,000 + .25 \times 4,000 = 11,000$

- High x tends to go together with high y .
- The identified correlation yields adequate predictions.

Incorrect: *Selling 4,000 additional insurances causes*
 $.25 \times 4,000 = 1,000$ *additional flights*

- The regression does not identify a *causal* impact!
- A third variable (*travel demand*) affects y (*flights*) and x (*insurances*).

Endogeneity

OLS requires some assumptions:

- explanatory variables should be exogenous
- violation of this: *endogeneity*.

In this set of lectures, you will learn to:

- 1 Understand/recognize endogeneity.
- 2 Know the consequences of endogeneity.
- 3 Estimate parameters under endogeneity.
- 4 Know the intuition of the new estimator.
- 5 Argue/test assumptions underlying this new estimator.

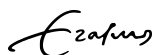
Stochastic vs. non-stochastic regressors

Standard assumptions for linear model ($y = X\beta + \varepsilon$) include

A2 Explanatory variables are *non-stochastic*

Implications:

- Obtain new data: X stays constant (and y changes)
- Need “controlled experiment”
- OLS estimator b converges to true coefficient β for $n \rightarrow \infty$ (OLS is *consistent*)



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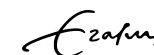
Economic models

In economics:

- Controlled (or natural) experiments are rare
- New data with same X cannot be obtained
- Explanatory variables are *stochastic*!

If X stochastic:

- new data set \rightarrow new X values
- X can be correlated with other variables
- If X correlated with ε
 - ▶ X is endogenous
 - ▶ There is another variable that affects y and X
 - ▶ OLS does not properly estimate β (inconsistent)
- If X uncorrelated with ε
 - ▶ X is exogenous
 - ▶ OLS consistent



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Other examples of endogeneity – Omitted variables

- True model is

$$y = X_1\beta_1 + X_2\beta_2 + \eta$$

but we ignore X_2 and perform OLS on

$$y = X_1\beta_1 + \varepsilon$$

- We have: $\varepsilon = X_2\beta_2 + \eta$
- X_1 correlated with ε (X_1 is endogenous) if
 - ▶ X_1 correlated with X_2 and
 - ▶ $\beta_2 \neq 0$

Derivation:

$$\begin{aligned}\text{Cov}(X_1, \varepsilon) &= \text{Cov}(X_1, X_2\beta_2 + \eta) \\ &= \text{Cov}(X_1, X_2)\beta_2 + \underbrace{\text{Cov}(X_1, \eta)}_{=0}\end{aligned}$$



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Omitted variable – Example

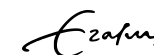
Model *student's grade* using *attendance* at lectures.

Test

Which omitted factor would lead to endogeneity of attendance?

Three possible omitted factors:

- 1 Difficulty of exam
NO: not correlated with attendance.
- 2 Motivation of the students?
YES: correlates with attendance and affects grade.
- 3 Compulsory attendance yes/no?
NO: does not directly impact the grade



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Other examples – Strategic behavior

Consider a model explaining demand using price.

Strategic price setting:

- ① Sets high price when high demand is expected
- ② Price and sales positively correlated
- ③ Price will be endogenous in regression of demand on price.



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Other examples – Measurement errors

- y (eg. salary) depends on x^* (eg. intelligence)
- x^* (intelligence) difficult to observe
- $x = x^* + \text{measurement error}$: noisy measurement (eg. IQ score)
- measurement error: x is endogenous in $y = \alpha + \beta x + \varepsilon$



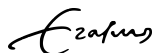
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Summary & what's next?

- Endogeneity is a common problem
- OLS is not useful under endogeneity

Upcoming topics:

- How to solve for endogeneity?
- How to test for endogeneity?



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TRAINING EXERCISE 4.1

- Train yourself by making the training exercise (see the website).
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Lecture 4.2 on Endogeneity: Consequences

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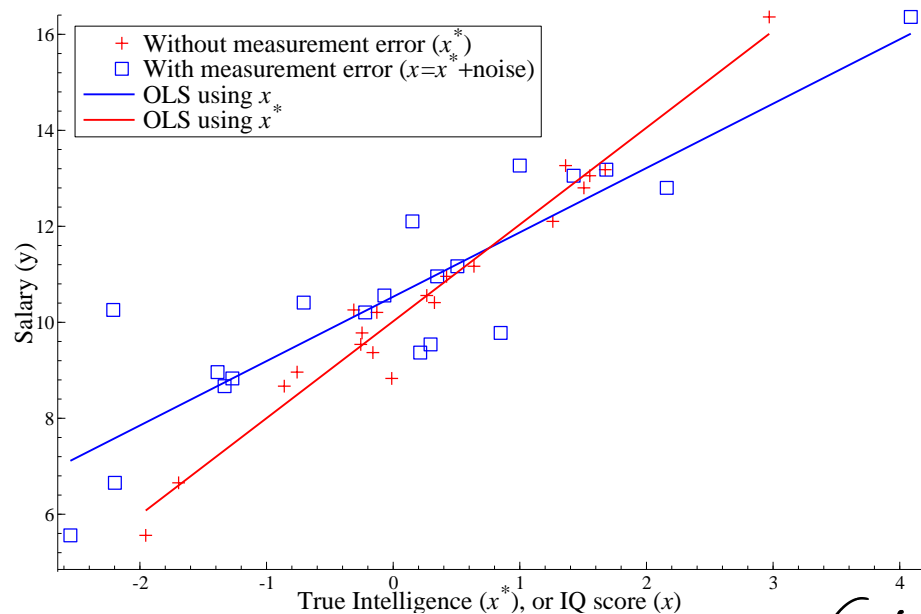
Endogeneity

- Common problem in economics
 - 1 Omitted variables
 - 2 Strategic behavior
 - 3 Measurement errors

→ X is correlated with ε
- Endogeneity violates the basic assumptions

→ How bad is this?

Simulated example, $y = 1 + 2x^* + u$



Measurement error example

Under measurement error (and endogeneity in general):

- we obtain the wrong coefficients!

Test

Can we say anything about the direction of the bias?

Direction of bias in the measurement error case

OLS is “biased towards zero”

→ OLS underestimates true effect

Intuitively:

- x -values on the *left* likely have negative measurement errors
- x -values on the *right* likely have positive measurement errors

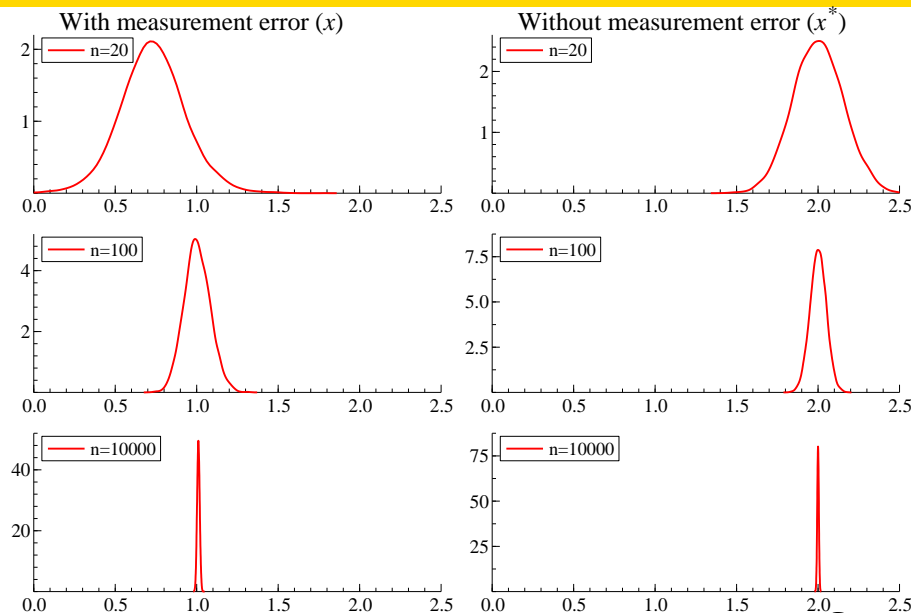
Measurement errors “stretch” the scatter in the horizontal direction

→ a flatter regression line

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Distribution of estimator for different n , true value = 2



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Consistency: formal argumentation

If X is endogenous:

- If n grows the OLS estimator converges to the wrong value.
→ OLS is inconsistent

Consider the standard model $y = X\beta + \varepsilon$ and the OLS estimator

$$\begin{aligned} b &= (X'X)^{-1}X'y = (X'X)^{-1}X'(X\beta + \varepsilon) \\ &= (X'X)^{-1}X'X\beta + (X'X)^{-1}X'\varepsilon \\ &= \beta + (X'X)^{-1}X'\varepsilon \end{aligned}$$

So, b can be split into

- 1 True parameter value β
- 2 Random deviation $(X'X)^{-1}X'\varepsilon$

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Asymptotic properties

What happens to b as $n \rightarrow \infty$?

Recall: $b = \beta + (X'X)^{-1}X'\varepsilon$

- β is constant
- Elements of $(X'X)$ and $X'\varepsilon$ are sums over observations:

$$X'X = \begin{pmatrix} \sum_{i=1}^n x_{1i}^2 & \sum_{i=1}^n x_{1i}x_{2i} & \cdots & \sum_{i=1}^n x_{1i}x_{ki} \\ \sum_{i=1}^n x_{1i}x_{2i} & \sum_{i=1}^n x_{2i}^2 & \cdots & \sum_{i=1}^n x_{2i}x_{ki} \\ \vdots & \vdots & \ddots & \vdots \\ \sum_{i=1}^n x_{ki}x_{1i} & \sum_{i=1}^n x_{ki}x_{2i} & \cdots & \sum_{i=1}^n x_{ki}^2 \end{pmatrix}, X'\varepsilon = \begin{pmatrix} \sum_{i=1}^n x_{1i}\varepsilon_i \\ \sum_{i=1}^n x_{2i}\varepsilon_i \\ \vdots \\ \sum_{i=1}^n x_{ki}\varepsilon_i \end{pmatrix}$$

→ these diverge as $n \rightarrow \infty$

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Asymptotic properties

Rewrite $b = \beta + (\frac{1}{n}X'X)^{-1}(\frac{1}{n}X'\varepsilon)$

- $(\frac{1}{n}X'X)$ is an average
→ in general converges to, say, Q
- $(\frac{1}{n}X'\varepsilon)$ also converges in general

Consistency result:

b converges to β as $n \rightarrow \infty$ if

- 1 $\frac{1}{n}X'X$ converges to Q , and
- 2 Q^{-1} exists, and
- 3 $\frac{1}{n}X'\varepsilon$ converges to 0
 - ▶ No correlation between X and ε (for large n)
 - ▶ X is exogenous

X endogenous: b does not converge to β !



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OLS in presence of endogeneity

If X endogenous

- X correlated with ε
- OLS estimator for β is not consistent
- Even with infinite amount of data: OLS does not give useful estimates



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Small sample properties

So far we discussed what happens for $n \rightarrow \infty$

Test

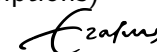
Why can't we derive the bias?

To obtain the bias

- need to evaluate

$$\begin{aligned} E[b] &= E[(X'X)^{-1}X'y] = E[(X'X)^{-1}X'(X\beta + \varepsilon)] \\ &= E[\beta + (X'X)^{-1}X'\varepsilon] = \beta + \underbrace{E[(X'X)^{-1}X'\varepsilon]}_{=?}. \end{aligned}$$

- X is stochastic
- cannot simplify final expectation (without further assumptions)



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TRAINING EXERCISE 4.2

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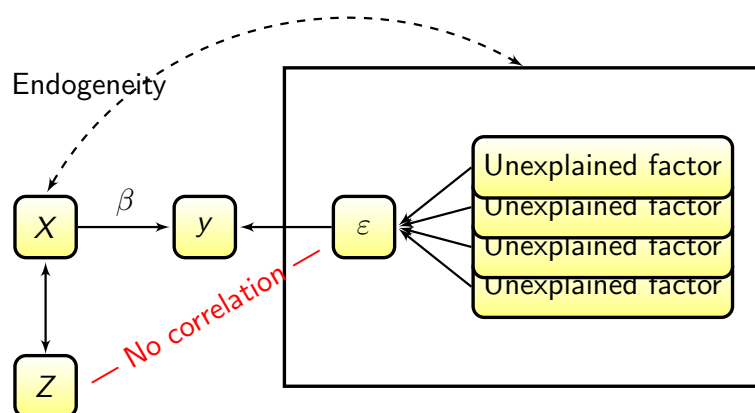
Lecture 4.3 on Endogeneity: Estimation under endogeneity

Dennis Fok

What have we so far?

- Endogeneity is a common problem
- Endogeneity causes OLS to be inconsistent
- Estimation requires another estimation technique

“Solving endogeneity”: Graphical representation



Instrumental variable estimation

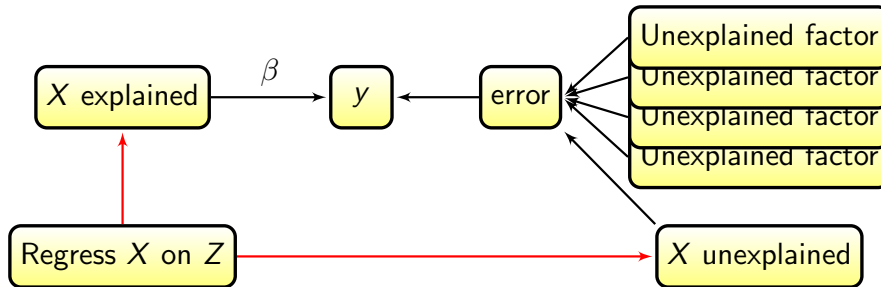
- Z variables are *instruments* if
 - ▶ Z and X are correlated
 - ▶ Z does not correlate with ε
- Correlation between instruments and y is only due to X

$$\begin{aligned} \text{Cov}(Z, y) &= \text{Cov}(Z, X\beta + \varepsilon) = \text{Cov}(Z, X\beta) + \underbrace{\text{Cov}(Z, \varepsilon)}_{=0} \\ &= \text{Cov}(Z, X)\beta \end{aligned}$$

- Use instruments to estimate β

"Solving endogeneity": Graphical representation

- 1 Use Z to decompose X in explained and unexplained part
- 2 Effect size of explained part on y equals β
- 3 Unexplained part is added to error term



Endogeneity is solved as

- X unexplained not correlated with X explained
- X explained is exogenous

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2SLS in matrix notation

Given model

$$y = X\beta + \varepsilon, \quad \text{Var}[\varepsilon] = \sigma^2 I$$

and instruments Z

- 1 Regress X on Z to get explained part:
 - ▶ Model: $X = Z\gamma + \eta$
 - ▶ OLS estimate: $(Z'Z)^{-1}Z'X$
 - ▶ Fitted value: $\hat{X} = \underbrace{Z(Z'Z)^{-1}Z'}_{H_Z} X = H_Z X$

- 2 Regress y on \hat{X} :

$$\begin{aligned} b_{2SLS} &= (\hat{X}'\hat{X})^{-1}\hat{X}'y \\ &= (X'H_Z' H_Z X)^{-1}X'H_Z'y \\ &= (X'H_Z X)^{-1}X'H_Z y \end{aligned}$$

$$\text{Use: } H_Z = H_Z' = H_Z' H_Z$$

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Properties 2SLS

- Variance of b_{2SLS} : $\text{Var}[b_{2SLS}] = \sigma^2(X'H_Z X)^{-1}$
- Estimating σ^2 :
 - ▶ $\hat{\sigma}^2 = \frac{1}{n-k}(y - Xb_{2SLS})'(y - Xb_{2SLS})$
 - ▶ Do **not** use residuals (or reported standard errors) of second stage regression!

Derivation of variance (use $\text{Var}[\varepsilon] = \sigma^2 I$):

$$\begin{aligned} b_{2SLS} &= (X'H_Z X)^{-1}X'H_Z y = (X'H_Z X)^{-1}X'H_Z(X\beta + \varepsilon) \\ &= \beta + (X'H_Z X)^{-1}X'H_Z \varepsilon \\ \text{Var}[b_{2SLS}] &= \text{Var}[(X'H_Z X)^{-1}X'H_Z \varepsilon] \\ &= (X'H_Z X)^{-1}X'H_Z \text{Var}[\varepsilon] ((X'H_Z X)^{-1}X'H_Z)' \\ &= (X'H_Z X)^{-1}X'H_Z (\sigma^2 I) H_Z' X (X'H_Z X)^{-1} \\ &= \sigma^2 (X'H_Z X)^{-1} X' \underbrace{H_Z H_Z'}_{H_Z} X (X'H_Z X)^{-1} = \sigma^2 (X'H_Z X)^{-1} \end{aligned}$$

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Properties of 2SLS

- 2SLS is consistent if (when $n \rightarrow \infty$)
 - ▶ Z and ε not correlated: $\frac{1}{n}Z'\varepsilon \rightarrow 0$
 - ▶ Z not multicollinear: $\frac{1}{n}Z'Z \rightarrow Q_{ZZ}$, and Q_{ZZ} invertible
 - ▶ X and Z sufficiently correlated: $\frac{1}{n}X'Z \rightarrow Q_{XZ}$, and Q_{ZZ} rank k

Sketch of proof:

$$\begin{aligned} b_{2SLS} &= \beta + (X'H_Z X)^{-1}X'H_Z \varepsilon = \beta + (X'Z(Z'Z)^{-1}Z'X)^{-1}X'Z(Z'Z)^{-1}Z'\varepsilon \\ &= \beta + \underbrace{\left(\frac{1}{n}X'Z \left(\frac{1}{n}Z'Z \right)^{-1} \frac{1}{n}Z'X \right)^{-1}}_{(Q_{XZ}Q_{ZZ}^{-1}Q_{XZ}')^{-1}} \underbrace{\frac{1}{n}X'Z \left(\frac{1}{n}Z'Z \right)^{-1}}_{Q_{XZ}Q_{ZZ}^{-1}} \underbrace{\frac{1}{n}Z'\varepsilon}_0 \\ &= \beta + 0 \end{aligned}$$

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Finding instruments

What are good instruments?

- All exogenous variables in X (incl. constant)
- Other instruments are always needed:
 - ▶ At least one for every endogenous variable
 - ▶ Want: strong correlation between Z and X
 - ▶ Need: no correlation between Z and ε



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Summary

If X is in fact **exogenous**

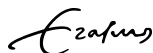
- OLS and 2SLS both consistent
- Variance OLS smaller than variance 2SLS!

→ Use OLS

If X is **endogenous**

- 2SLS is consistent
- OLS inconsistent

→ Use 2SLS



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Examples of instruments

Explain obtained grade using attendance:

Potential instruments:

- Travel time home to university
- Policy change to obligatory attendance

Test

What variable would be an instrument for price when modeling consumer sales of ice cream using $\text{sales} = \alpha + \beta \text{price} + \varepsilon$?

Potential instruments?

- ① Prices of raw materials (valid)
- ② Competitor prices (direct influence on sales, so part of ε)
- ③ Outside temperature (direct influence on sales, so part of ε)



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TRAINING EXERCISE 4.3

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MOOC Econometrics

Lecture 4.4 on Endogeneity: Testing for endogeneity

Dennis Fok

Outline

Given

- Model $y = X\beta + \varepsilon$
- Instruments Z

Two important things to test

- 1 Z satisfies assumptions for instruments?
- 2 X exogenous or endogenous?

Testing the validity of instruments

Valid instruments satisfy three conditions

- 1 There are enough instruments
→ Easy! Just count.
- 2 Instruments are correlated (enough) with X
→ Check significance of instruments in first stage regression
- 3 Instruments are not correlated with ε
→ Perform *Sargan test*

Test correlation Z vs. X

- X_1 potentially endogenous variables
- X_2 exogenous variables
- $Z = (Z^*, X_2)$ instruments

First-stage regression: apply OLS to $X_1 = Z^*\gamma_1 + X_2\gamma_2 + \eta$

Test

Why does 2SLS require $\gamma_1 \neq 0$?

If $\gamma_1 \approx 0$:

- $\hat{X}_1 \approx X_2\hat{\gamma}_2$
→ \hat{X}_1 almost perfectly correlated with X_2
- (Extremely) large estimation uncertainty

Test for sufficient correlation:

- Test $H_0 : \gamma_1 = 0$ in first-stage regression.

Sargan test

Ingredients:

- Model: $y = X\beta + \varepsilon$
- Explanatory variables: $X = (X_1, X_2)$
 X_1 (endogenous), X_2 (exogenous)
- Instruments: $Z = (Z^*, X_2)$

Null hypothesis (H_0): Correlation Z and ε equals 0

Test procedure:

- Rewrite to $H_0 : \delta = 0$ in

$$\varepsilon = Z\delta + \xi$$

- ε cannot be observed
→ Estimate ε using 2SLS



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Notes on the Sargan test

- Test only works when there are “too many” instruments ($m > k$)
- At least k of the instruments should be valid
- Test cannot indicate which instruments are invalid!



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Sargan test

Procedure:

- 1 Use Z to obtain 2SLS estimator b_{2SLS} for β
- 2 Calculate $e_{2SLS} = y - Xb_{2SLS}$
- 3 Regress e_{2SLS} on Z
- 4 $nR^2 \approx \chi^2(m - k)$ under H_0 (valid instruments)
 - ▶ m instruments in Z
 - ▶ k explanatory variables in X

Test

The Sargan test requires $m > k$. What happens when $m = k$?



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Testing for exogeneity of variables – Hausman test

Intuition:

- Use the instruments to split potentially endogenous variables into
 - 1 a guaranteed exogenous part
 - 2 a potentially endogenous part
- Check whether the endogenous and exogenous part affect y differently.



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Ingredients:

- Explanatory variables: $X = (X_1, X_2)$
- Potentially endogenous: X_1 (k_1 variables)
- Exogenous variables: X_2 (k_2 variables)
- Instruments: Z

Null hypothesis (H_0): X_1 is exogenous

Formal procedure:

- 1 Regress y on $X \rightarrow$ calculate $e = y - Xb$
- 2 Regress X_1 on $Z \rightarrow$ calculate residuals V
- 3 Regress e on X and V
- 4 $nR^2 \approx \chi^2(k_1)$ under H_0 of exogeneity



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Lecture 4.5 on Endogeneity: Application

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Application

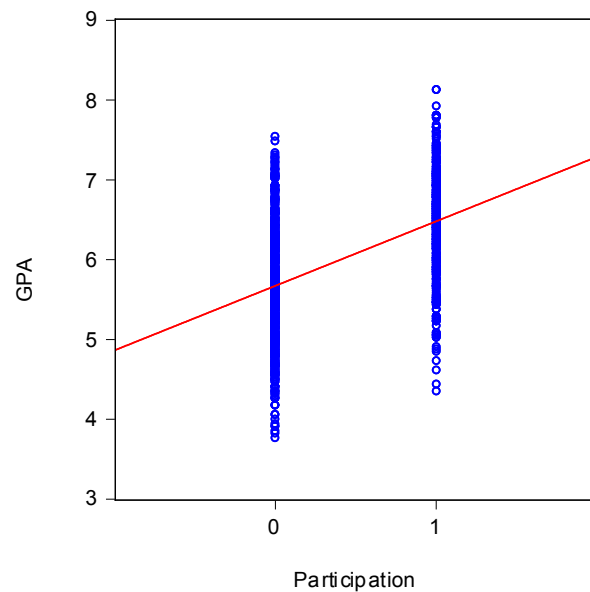
Setting:

- Online learning platform
- Grade Point Average (GPA) in MOOC on engineering
- Impact of preparatory mathematics course
→ participation is voluntary!

Data statistics:

- 1000 learners
- 48.8% male
- 33.7% participated in prep course
- Average GPA 5.94 (on 10 point scale)

Correlation of GPA with participation



Correlation vs. regression

Seems positive impact

- How large?
- Significant?
- Correction for male vs. female?

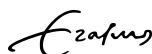
→ Need econometric model!

OLS estimation

Regress GPA on

- ① Constant
- ② Gender: dummy variable (male=1, female=0)
- ③ Participation: dummy variable (yes=1, no=0)

| Dependent variable: GPA | | | |
|-------------------------|-------------|----------------|--------------|
| Sample size: 1000 | | | |
| | Coefficient | Standard error | t-statistic |
| Constant | 5.77 | 0.034 | 169.87 |
| Gender | -0.21 | 0.044 | -4.82 |
| Participation | <u>0.82</u> | 0.047 | <u>17.59</u> |
| R^2 | 0.24 | | |



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Discussion of OLS

Should we trust the OLS estimates?

→ No, participation likely endogenous!

- Learners self-select for prep course
- Omitted factors (characteristics of learners) relate to this selection
- Same characteristics may relate to GPA



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Over- or underestimation by OLS?

If prep course participation is endogenous

- OLS is inconsistent
- OLS does not estimate causal effect of prep course

Test

What omitted factor would lead OLS to overestimate the impact of the preparatory course?



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Over- or underestimation by OLS?

Overestimation

- Omitted factor: Motivation
High motivation → Get high GPA & Take course

Underestimation

- Omitted factor: Mathematics level
High level → Get high GPA & Do not take course

Net effect:

- Difficult to judge
- Depends on importance of effects
- Also depends on other variables (age?)



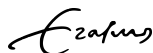
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Consistent estimation

- Use two-stage least squares (2SLS)
- Need instruments!

Test

What variable can you think of that qualifies as instrument for participation?



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Instruments

Instruments should...

- relate to prep course participation
- not affect GPA

Many learner specific variables, such as

- Intelligence (IQ-score)
- Number of MOOCs followed before
- Age of learner

are likely not valid!

→ All will impact performance directly!



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Instruments

Finding instruments

- be creative! ... and lucky

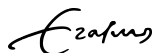
Here

- Learners get email invitation for prep course
- Platform email problem: some did not get email
- Variable

$$\text{Email} = \begin{cases} 0 & \text{if email not received} \\ 1 & \text{if email received} \end{cases}$$

is perfect instrument if

- ▶ Email problem is random
- ▶ Invitation affects participation



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First-stage regression

Explain participation using all instruments (constant, gender, email)

| | | | |
|-----------------------------------|-------------|----------------|--------------|
| Dependent variable: Participation | | | |
| Sample size: 1000 | | | |
| | Coefficient | Standard error | t-statistic |
| Constant | 0.10 | 0.023 | 4.41 |
| Gender | 0.05 | 0.027 | 1.80 |
| Email | <u>0.41</u> | 0.027 | <u>15.35</u> |
| R^2 | 0.20 | | |

→ Email affects participation significantly



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2SLS estimation

| Dependent variable: GPA | | | |
|---|-------------|----------------|-------------|
| Sample size: 1000 | | | |
| Instruments used: Constant, Gender, Email | | | |
| | Coefficient | Standard error | t-statistic |
| Constant | 5.95 | 0.048 | 123.54 |
| Gender | -0.17 | 0.048 | -3.59 |
| Participation | <u>0.24</u> | 0.115 | <u>2.09</u> |
| R^2 | 0.13 | | |

- Prep course still has significant positive impact
- Effect size decreased (from 0.82 (OLS) to 0.24 (2SLS))
- 2SLS increases variance
 - ▶ Only acceptable when Participation is endogenous
 - ▶ Perform Hausman test

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Hausman test (H_0 : Participation is exogenous)

| Dependent variable: Residuals from OLS | | | |
|--|-------------|----------------|-------------|
| Sample size: 1000 | | | |
| | Coefficient | Standard error | t-statistic |
| Constant | 0.18 | 0.044 | 4.02 |
| Gender | 0.04 | 0.044 | 0.93 |
| Participation | -0.58 | 0.105 | -5.55 |
| First-stage residuals (v) | 0.72 | 0.117 | 6.17 |
| R^2 | 0.0368 | | |

- Test-statistic: $nR^2 = 1000 \times 0.0368 = 36.8$
- Reject H_0 (critical value from $\chi^2(1)$: 3.8)
- Participation is endogenous
- 2SLS is needed

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TRAINING EXERCISE 4.5

- Train yourself by making the training exercise (see the website).
- After making this exercise, check your answers by studying the webcast solution (also available on the website).

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