



# How to calculate a p-value from the t-distribution for a two-tailed t-test?

Asked 1 year, 4 months ago Active 1 year, 4 months ago Viewed 124 times



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The resulting  $t$  statistic from a t-test follows a t-distribution with parameter  $k = \text{freedom-degrees}$ . For us to compute the probability of  $t$  to occur, we use the cumulative distribution function of the t-distribution ( $CDF_t$ ).



For a left-sided test, this is equal to finding the probability on the y-axis of the CDF, which intersects with the given  $t$  value.



For a right-sided test, this is equal to  $1 - \text{the left-sided p-value}$ .

What about the two-sided test? I am not sure how this p-value is computed using the CDF.

So far I have only seen this method: (from

<https://stackoverflow.com/questions/45045802/how-to-do-a-one-tail-pvalue-calculate-in-python>)

$$p = CDF_t(t, df) * 2$$

i.e. the left-sided p-value multiplied by two.. which strikes me as odd, as the p-value ranges from 0 to 1, this equation generates a p-value in the domain  $[0, 2]$ .

hypothesis-testing

t-test

p-value

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asked Apr 30 '20 at 20:49



**hirschme**

**630** 7 19

1 Answer

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For an easy way of understanding, the two sided  $p$  value turns out to be equal to double the smallest one-sided  $p$  value. Since these sum to 1, the smallest is in the domain  $[0, 0.5]$ , so the two sided is in the domain  $[0, 1]$ .



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edited Apr 30 '20 at 21:36

answered Apr 30 '20 at 21:18



**E. Rei**

**151** 9

- 1   This is easy and (crucially) correct, but why do you say it's intuitive? Perhaps you can elaborate on that. – [Dave](#) Apr 30 '20 at 21:29
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-  I guess intuitive wasn't the right word to use. Kind of meant easy to remember. Edited that out of the answer – [E. Rei](#) Apr 30 '20 at 21:36
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- 1   @H.Green that makes sense. But it also means that the equation I wrote in the question is incomplete right? – [hirschme](#) Apr 30 '20 at 22:22
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