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## 5. F5.

5(a)

1/1 point (graded)

We want to model motion that is not diffusive. Instead all movement tends in one direction, like traffic in one direction along a highway.

The partial differential equation that models this situation is called the transport equation.

$$\frac{\partial u}{\partial t} + c \frac{\partial u}{\partial x} = 0, \qquad c > 0.$$

Suppose that the initial condition is u(x,0) = f(x). Which of the following are solutions to the partial differential equation? (Choose all that apply.)

 $\bigcap f(x+ct)$ 



 $\bigcap f\left( x
ight) e^{-ct}$ 

~

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✓ Correct (1/1 point)

## 5(b)

2/2 points (graded)

Use separation of variables  $u\left(x,t\right)=v\left(x\right)w\left(t\right)$  to solve the transport equation for c=1

$$\frac{\partial u}{\partial t} + \frac{\partial u}{\partial x} = 0.$$

Note that in this case, you will find that you can find eigenfunctions for  $\lambda$  any real number. Type **lambda** for  $\lambda$  in your answers. Enter eigenfunctions such that v(0) = w(0) = 1.

$$v\left(x
ight) = egin{bmatrix} \mathrm{e}^{\left(-\mathsf{lambda*x}
ight)} \end{array}$$

$$w\left(t
ight)=egin{array}{c} {
m e}^{\left({
m lambda*t}
ight)} \end{array}$$

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