

4. Compute

$$(a) \ 2 \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix} = \begin{pmatrix} 2 \\ 0 \\ 4 \end{pmatrix}$$

$$(b) \ 3 \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix} = \begin{pmatrix} 3 \\ 0 \\ 6 \end{pmatrix}$$

$$(c) \ (-1) \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix} = \begin{pmatrix} -1 \\ 0 \\ -2 \end{pmatrix}$$

$$(d) \ \overset{A}{\begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix}} \left( \overset{B}{2 \mid 3 \mid -1} \right) = \begin{pmatrix} 2 & 3 & -1 \\ 0 & 0 & 0 \\ 4 & 6 & -2 \end{pmatrix}$$

$$(e) \ \begin{pmatrix} -3 \\ 0 \\ 1 \end{pmatrix} \left( 1 \mid -2 \mid -1 \right) = \begin{pmatrix} -3 & 6 & 3 \\ 0 & 0 & 0 \\ 1 & -2 & -1 \end{pmatrix}$$

$$(f) \ \overset{A}{\begin{pmatrix} 1 & -3 \\ 0 & 0 \\ 2 & 1 \end{pmatrix}} \overset{B}{\left( \begin{array}{ccc} 2 & 3 & -1 \\ 1 & -2 & -1 \end{array} \right)} = \begin{pmatrix} -1 & 9 & 2 \\ 0 & 0 & 0 \\ 5 & 4 & -3 \end{pmatrix}$$

$\uparrow 3 \times 2$ 
 $2 \times 3$ 
 $3 \times 3$

(g) Which of the three algorithms for computing  $C := AB$  do parts (d)-(f) illustrate? (Circle the correct one.)

- Matrix-matrix multiplication by columns.
- Matrix-matrix multiplication by rows.
- Matrix-matrix multiplication via rank-1 updates.