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10. Review of Methods of Estimation

Review of Methods of Estimation

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Concept Check: Methods of Estimation I

1/1 point (graded)

Which of the following estimators are defined in terms of an optimization problem? (Choose all that apply.)

☒ Maximum likelihood estimator.

☐ Method of moments estimator.

☒ M-estimator.



Solution:

The correct responses are "Maximum likelihood estimator." and "M-estimator." The MLE is defined by maximizing the log-likelihood, and an M-estimator is defined by minimizing a loss function. However, the method of moments estimator is constructed by solving a system of equations, so this response is not correct.

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You have used 1 of 2 attempts

 Answers are displayed within the problem

Concept Check: Methods of Estimation II

1/1 point (graded)

All three method of estimation studied in this unit: maximum likelihood estimation, the method of moments, and M-estimation, lead to asymptotically normal estimators if certain technical conditions are satisfied.

In general, an asymptotically normal estimator $\hat{\theta}_n$ can be used to construct a confidence interval for an unknown parameter.

What quantity related to the estimator $\hat{\theta}$ determines the length of an asymptotic confidence interval at level 95%? (Assume that you use the plug-in method and that n is very large.)

☒ The asymptotic variance of $\hat{\theta}_n$.

☐ The rate of convergence of $\hat{\theta}_n$ to the normal distribution $\mathcal{N}(0, 1)$.

☐ The mean of $\hat{\theta}_n$.



Solution:

The correct response is "The asymptotic variance of $\hat{\theta}_n$," as we demonstrate below. Consider an asymptotically normal estimator $\hat{\theta}_n$, which satisfies

$$\sqrt{n}(\hat{\theta}_n - \theta) \xrightarrow[n \rightarrow \infty]{(d)} \mathcal{N}(0, \sigma^2)$$

for some asymptotic variance $\sigma^2 > 0$. Let $q_{\alpha/2}$ denote the $\alpha/2$ -quantile of a standard Gaussian. Then we have that

$$P\left(\sqrt{n} \frac{|\hat{\theta}_n - \theta|}{\sigma} \geq q_{\alpha/2}\right) \xrightarrow{n \rightarrow \infty} \alpha$$

which implies that

$$P\left(\theta \notin \left[\hat{\theta}_n - q_{\alpha/2} \frac{\sigma}{\sqrt{n}}, \hat{\theta}_n + q_{\alpha/2} \frac{\sigma}{\sqrt{n}}\right]\right) \xrightarrow{n \rightarrow \infty} \alpha.$$

Therefore, using the plug-in method, we have that

$$P\left(\theta \notin \left[\widehat{\theta}_n - q_{\alpha/2} \frac{\widehat{\sigma}}{\sqrt{n}}, \widehat{\theta}_n + q_{\alpha/2} \frac{\widehat{\sigma}}{\sqrt{n}}\right]\right) \xrightarrow{n \rightarrow \infty} \alpha,$$

Setting $\alpha = 0.05$, we have that

$$\mathcal{I} := \left[\widehat{\theta}_n - q_{\alpha/2} \frac{\widehat{\sigma}}{\sqrt{n}}, \widehat{\theta}_n + q_{\alpha/2} \frac{\widehat{\sigma}}{\sqrt{n}}\right]$$

If n is very large, we have that $\widehat{\sigma}_n \approx \sigma$, so the length of \mathcal{I} is approximately $2q_{0.025}\sigma/\sqrt{n}$. That is, the length depends only on the $\alpha/2$ quantile, the sample size, and the asymptotic variance. Therefore, "The rate of convergence of $\widehat{\theta}_n$ to the normal distribution $\mathcal{N}(0, 1)$." and "The mean of $\widehat{\theta}_n$." are incorrect responses.

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i Answers are displayed within the problem

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