



[Course](#) > [Unit 6 Linear Regression](#) > [Homework 10 Linear regression](#) > 2. Polynomial Regression

2. Polynomial Regression

Suppose that we observe ten points $(X_1, Y_1), \dots, (X_{10}, Y_{10})$ where $X_1 = 1, X_2 = 2, \dots, X_{10} = 10$. We believe that the data is governed by a polynomial relationship:

$$Y_i = \beta_0 + \beta_1 X_i + \beta_2 X_i^2 + \epsilon_i$$

where ϵ_i are i.i.d. $\mathcal{N}(0, \sigma^2)$, and $\sigma^2 = 0.1$.

(a)

1/1 point (graded)

Treat the expression for Y_i on the right hand side as a linear function of 1, X_i and X_i^2 , plus the noise variable ϵ .

What is the design matrix \mathbb{X} ? Recall that the desired setup for linear regression in this course is $\mathbf{Y} = \mathbb{X}\beta + \epsilon$, where both β and ϵ are column vectors, so carefully consider what the size of the matrix \mathbb{X} is.

(Enter your answer as a matrix. For instance, to enter the 3×2 matrix $\begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}$, type `[[1,2],[3,4],[5,6]]`. Your answer may be a large matrix.)

$\mathbb{X} =$



STANDARD NOTATION

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You have used 1 of 4 attempts

✓ Correct (1/1 point)

(b)

1/1 point (graded)

Calculate the matrix $\mathbb{X}^T \mathbb{X}$. Since the values of each X_i happen to be integers, your answer should also have integer entries.

(Enter your answer as a matrix. For instance, to enter the 3×2 matrix $\begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}$, type `[[1,2],[3,4],[5,6]]`.)

$\mathbb{X}^T \mathbb{X} =$

`[[10,55,385],[55,385,3025],[385,3025,25333]]`



STANDARD NOTATION

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You have used 1 of 3 attempts

✓ Correct (1/1 point)

(c)

3/3 points (graded)

Calculate the least squares estimator $\hat{\beta}$ for $\beta = (\beta_0, \beta_1, \beta_2)$ given the data:

| | | | | | | | | | | |
|-----|---|---|---|---|----|----|----|----|----|----|
| x | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| y | 1 | 3 | 5 | 8 | 11 | 14 | 18 | 21 | 25 | 28 |

Round each entry of your final answer to the nearest 0.01.

$\hat{\beta}_0 =$ ✓

$\hat{\beta}_1 =$ ✓

$\hat{\beta}_2 =$ ✓

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You have used 1 of 3 attempts

✓ Correct (3/3 points)

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