

## MITx: 6.041x Introduction to Probability - The Science of Uncertainty

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Lec. 4: Counting

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### **Problem Set 3**

Problem Set 3 due Feb 24, 2016 at 23:59 UTC

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# Problem 1: Alice and Bob's card game

(2/2 points)

Alice plays the following game with Bob. First, Alice randomly chooses a set of 4 cards out of a 52-card deck, memorizes them, and places them back into the deck. (Any set of 4 cards is equally likely.) Then, Bob randomly chooses 8 cards out of the same deck. (Any set of 8 cards is equally likely.) Assume that the choice of 4 cards by Alice and the choice of 8 cards by Bob are independent.

What is the probability that all 4 cards Alice chose were also among the 8 cards chosen by Bob?



 $\frac{\binom{48}{4}}{\binom{52}{4}}$ 

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#### Answer:

Let us fix the 4 cards that Alice gets. Since 4 cards are fixed, Bob must choose 4 more cards out of 48 remaining cards, so the total number of possible hands for Bob that include all of Alice's cards is  $\binom{48}{4}$ . The total number of possible choices of 8 cards for Bob is  $\binom{52}{8}$ . Thus, the probability is  $\binom{48}{4}/\binom{52}{8}$ .

You have used 1 of 2 submissions

Printable problem set available here.

## DISCUSSION

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Final Exam

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