

find out the no. of spanning tree possible



asked in [Algorithms](#) May 2, 2015

11,350 views

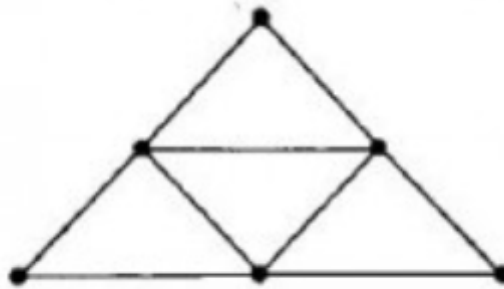
edited Aug 7 by [soujanyareddy13](#)



How many spanning trees are possible from the graph given below?



12



A. 24


B. 34

C. 44

D. 54



[Gunjan Rathore](#) 3.5k views

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3 Comments

[Shubham Sharma 2](#) commented Feb 5, 2017



Explain how u calculate number of graph with 3 length cycle.

 0 

[Rohit Pandey](#) commented Aug 31, 2018



@digvijay Pandey

The no of cycle of length 3 is 4



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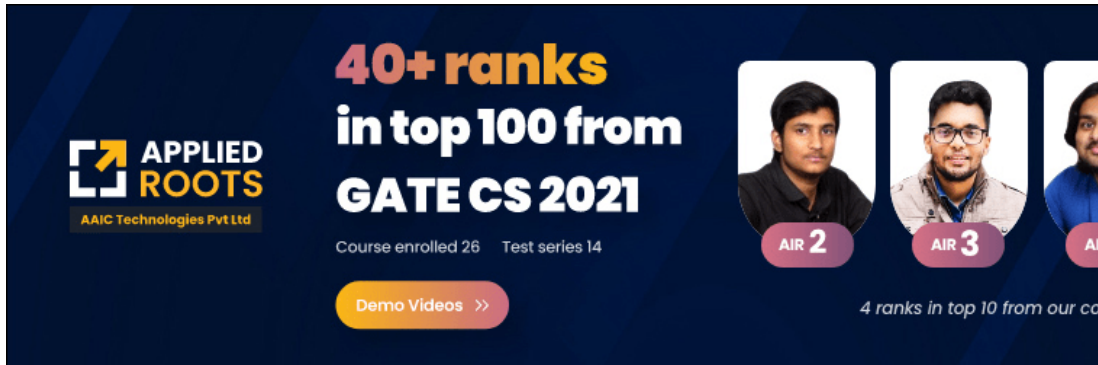


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check out this <https://gateoverflow.in/202571/spanning-tree>

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2 Answers



total 9 edges and 6 vertices..

9

for spanning tree we need 6 vertices and 5 edges..

no of graphs with 5 edges : $9C_5$



no of graph with 3 length cycle (may be disconnected) = select any cycle of length 3 (select any small triangle) and then out of 6 vertices select any 2..

= $(6C_2) \times 3 + 12$ (for middle triangle) = 57

find no of 4 length cycle = select 4 length cycle and for rest 1 edge select those edges which doesn't produces 3 length cycle..

= $4 + 4 + 4 = 12$

no of 5 length cycle = 3

total spanning tree = $126 - (57 + 12 + 3)$

= $126 - 72$

= 54

answered May 2, 2015



Digvijay Pandey



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but it is a 6×6 matrix it would be very lengthy to go by above approach?

 0 

Neha Sisodiya commented Jul 12, 2015

Can explain it in detail I m not getting it how the combinations r made.

 0 

Rachit Saxena commented Dec 9, 2015

Hi, thanks a lot for your response, but I am having trouble understanding the combinations to calculate the number of cycles. Could you elaborate more?

 0 

mcjoshi commented Aug 23, 2016

Please elaborate ??

 0 

Akhilesh Yadav 1 commented Dec 28, 2016

@ Digvijay Pandey

How possible no. of subgraph with the middle triangle is 12? Shouldn't this be $6C2$? please explain.

 2 

papesh commented May 4, 2017

@Akhilesh Yadav since, if we select the middle triangle, now we need to select more two edges, there are 3 ways to select two edges such that it will build another triangle which is already taken into account. so $15 - 3 = 12$

 1 

Chirag arora commented Jan 9, 2018

If combination forming for this question is getting difficult for someone...then...you can go with Kirchoff's algorithm also...the only disadvantage is it gets lengthy...but if you are fast with determinant calculations...then...this algo is simple and best!

For those who are facing difficulty ...with spanning tree questions..

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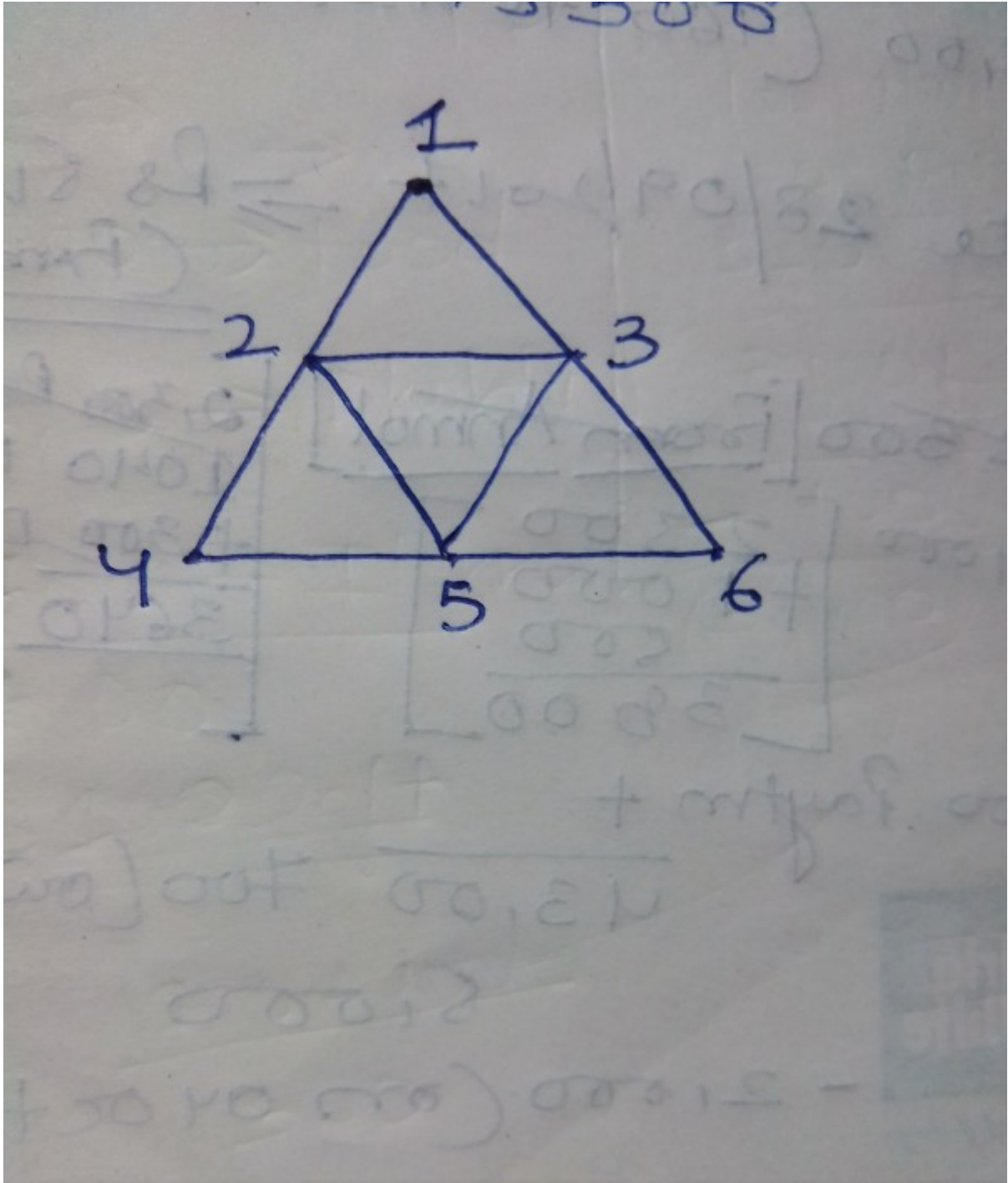


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i have numbered the node.

total edges are 9 .For mst edges will be $v-1=5$

step 1 : total combination

$${}^9C_5=126$$

but this combination contains 3 edges,4edges,5 edges cycle.so subtraction from these must be done.

step 2: finding 3 edges cycle

3 edges cycle are (123,245,235,356)- 4 cycles

now for each cycle 2 edges are remaining so choosing those 2 edges will take 6C_2 ways.

$$\text{total}=4*{}^6C_2$$

but if we choose 2 more edges then there may be chances of getting 4 edges cycle.

for example- in cycle 123 if we choose edge 5-3 and 2-5 cycle 1253 is possible,in cycle 235 if we choose 2-4 & 4-5 then 2354 is possible also in same cycle if we choose edge 3-6,5-6 then cycle 2365 is possible.

3 EDGES CYCLE FORMED	EDGES ADDED	4 EDGES CYCLE
123	5-3,2-5	1253
245	2-3,3-5	2354
235 1253	5-4,2-4 or 3-6,5-6 OR 1-2,1-3	2354 OR 2365 OR
356	2-5,2-3	2365

so total 6 (4-edges cycle) will be formed so we must remove this 6 cycles

$$4*{}^6C_2-6=54$$

case 3: finding 4 edges cycle (1253,2453,2563)

choosing the fifth edges will take 5C_1 ways but we have to careful that choosing 5th edges can lead us to 5 edges cycle.

So 3 5EDGES WILL BE FORMED SO WE MUST REMOVE THESE 3 CYCLES $3 \times 5 - 3 = 12$

case 4:choosing 5 edges cycle(231253,253245,532563,421354,521365,236542)

total 6

final answer: $126 - (54 + 12 + 6) = 54$

 answered Nov 9, 2018



adarsh_1997

2 Comments

HeadShot commented Jan 4, 2019 edited Jan 4, 2019 by **HeadShot**
[@adarsh_1997](#)



one doubt :

While considering 5 edge cycles... 3 are actual 5 edge cycles. But the rest what you took are 2 - 3 edge cycles with 1 edge common and which i guess are already covered in 3 edge cycles. isnt it ?

p.s :

I got my mistake :

Its like, even if are repeating the cycles , it is still a different count coz it is formed during different edge count.

is it fine ?



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Answer: 54

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 asked in [Programming](#) Jul 12, 20160 
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 asked in [Operating System](#) Oct 4, 20151 
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 asked in [Algorithms](#) May 3, 20170 
#4

Ace test series question on number of spanning trees possible





 asked in [Algorithms](#) Jan 24, 2019

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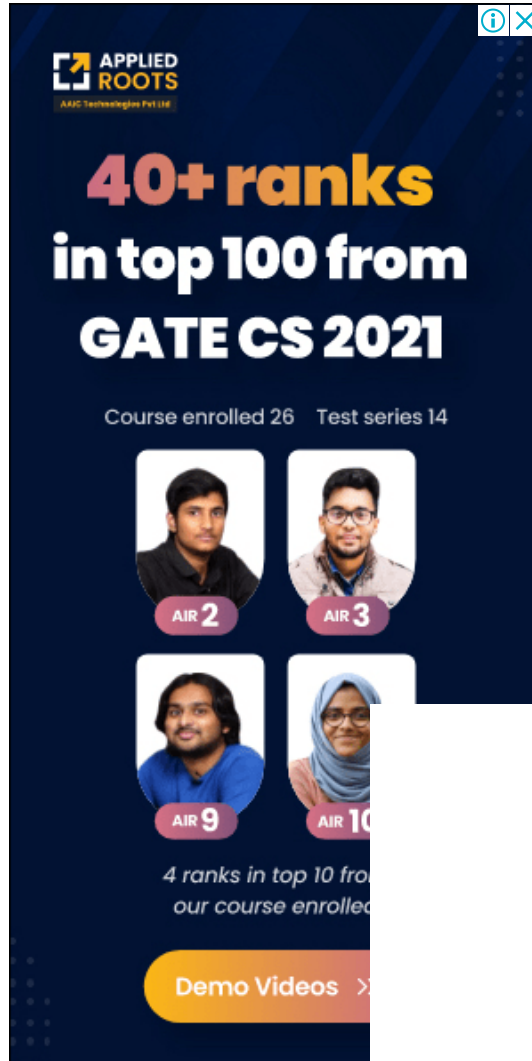
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