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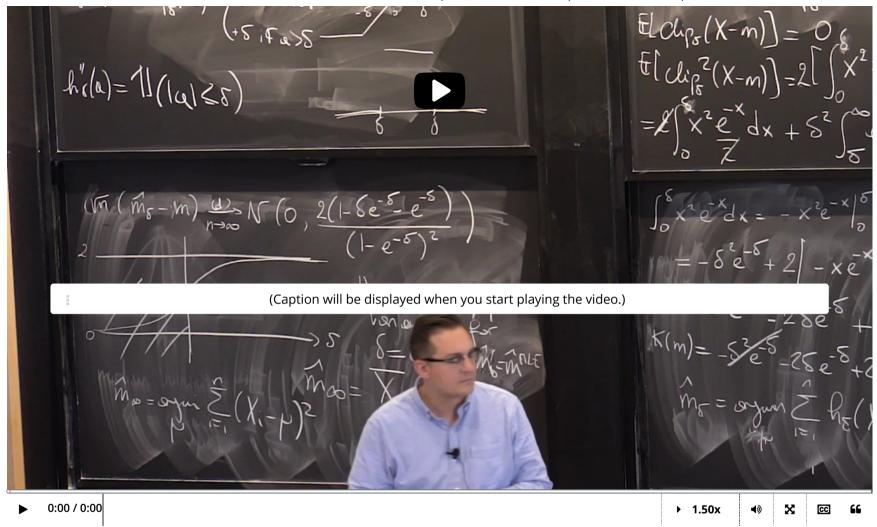
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10. Review of Methods of Estimation Review of Methods of Estimation



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Concept Check: Methods of Estimation I

1/1 point (graded)

Which of the following estimators are defined in terms of an optimization problem? (Choose all that apply.)

✓ Maximum likelihood estimator.
 ✓ Method of moments estimator.
 ✓ M-estimator.

Solution:

The correct responses are "Maximum likelihood estimator." and "M-estimator." The MLE is defined by maximizing the log-likelihood, and an M-estimator is defined by minimizing a loss function. However, the method of moments estimator is constructed by solving a system of equations, so this response is not correct.

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You have used 1 of 2 attempts

• Answers are displayed within the problem

Concept Check: Methods of Estimation II

1/1 point (graded)

All three method of estimation studied in this unit: maximum likelihood estimation, the method of moments, and M-estimation, lead to asymptotically normal estimators if certain technical conditions are satisfied.

In general, an asymptotically normal estimator $\hat{\theta}_n$ can be used to construct a confidence interval for an unknown parameter.

What quantity related to the estimator $\hat{\theta}$ determines the length of an asymptotic confidence interval at level 95%? (Assume that you use the plug-in method and that n is very large.)

- lacksquare The asymptotic variance of $\hat{ heta}_n$.
- igcup The rate of convergence of $\hat{ heta}_n$ to the normal distribution $\mathcal{N}\left(0,1
 ight)$.
- igcup The mean of $\hat{ heta}_n$.



Solution:

The correct response is "The asymptotic variance of $\hat{\theta}_n$," as we demonstrate below. Consider an asymptotically normal estimator $\widehat{\theta_n}$, which satisfies

$$\sqrt{n}\left(\widehat{ heta_n}- heta
ight) \stackrel{(d)}{ \longrightarrow \infty} \mathcal{N}\left(0,\sigma^2
ight)$$

for some asymptotic variance $\sigma^2>0$. Let $q_{lpha/2}$ denote the lpha/2-quantile of a standard Gaussian. Then we have that

$$P\left(\sqrt{n}rac{\left|\widehat{ heta_n}- heta
ight|}{\sigma}\geq q_{lpha/2}
ight)\stackrel{n o\infty}{-\!\!\!-\!\!\!-\!\!\!-\!\!\!-}lpha$$

which implies that

$$P\left(heta
otin \left[\widehat{ heta_n} - q_{lpha/2}rac{\sigma}{\sqrt{n}}, \widehat{ heta_n} + q_{lpha/2}rac{\sigma}{\sqrt{n}}
ight]
ight) \stackrel{n o\infty}{-\!\!\!-\!\!\!-\!\!\!-\!\!\!-\!\!\!-\!\!\!-} lpha.$$

Therefore, using the plug-in method, we have that

$$P\left(heta
otin \left[\widehat{ heta_n} - q_{lpha/2} rac{\widehat{\sigma}}{\sqrt{n}}, \widehat{ heta_n} + q_{lpha/2} rac{\widehat{\sigma}}{\sqrt{n}}
ight]
ight) \stackrel{n o\infty}{-\!\!\!-\!\!\!\!-\!\!\!\!-\!\!\!\!-} lpha,$$

Setting lpha=0.05 , we have that

$$\mathcal{I} := \left[\widehat{ heta_n} - q_{lpha/2} rac{\widehat{\sigma}}{\sqrt{n}}, \widehat{ heta_n} + q_{lpha/2} rac{\widehat{\sigma}}{\sqrt{n}}
ight]$$

If n is very large, we have that $\widehat{\sigma}_n \approx \sigma$, so the length of $\mathcal I$ is approximately $2q_{0.025}\sigma/\sqrt{n}$. That is, the length depends only on the $\alpha/2$ quantile, the sample size, and the asymptotic variance. Therefore, "The rate of convergence of $\widehat{\theta}_n$ to the normal distribution $\mathcal N$ (0,1)." and "The mean of $\widehat{\theta}_n$." are incorrect responses.

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You have used 1 of 2 attempts

1 Answers are displayed within the problem

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