TsinghuaX: 60240013x Combinatorial Mathematics

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H1 (1/1 point)
1) Please calculate the number of positive integers which are smaller than 10000 and contain "1"
3439
3439
Answer: 3439
2) Please calculate the number of positive integers which are smaller than 10000 and contain "0" $$
2619

Answer: 2619

2619

EXPLANATION

1) Solution 1: Smaller than 10000, the positive interger which does not contain '1' can be seen as a 4 digit number, except 0000. Therefore, there is $9\times9\times9\times9-1=6560$. Therefore, those numbers which contains '1' is: 9999-6560=3439,

Solution 2: The number of all 4 digit number are 10^4 , the 4 digit number which does not contain 1 is 9^4 , the 4 digit number which contains 1 is the difference between the two: $10^4 - 9^4 = 3439$

- 2) "Contain 0" and "Contain 1" are not same with each other, for example '0019' contains '1' but does not contain '0' in format of natural numbers. You may need to pay attention on that, in the combination exercise, it contains similar kinds of implicit rules you may need to pay attention to.
- 1 digit number which does not contain '0' is 9 of them, 2 digit numbers we have 9^2 , 3 digit number we have 9^3 , 4 digit number contains 9^4 , the positive number which is smaller than 1000 that does not contains 0 contains: $9 + 9^2 + 9^3 + 9^4 = (9^5 1)/(9 1) = 7380$. Therefore, the positive number which is smaller than 10000 that contains '0' is: 9999 7380 = 2619

Final Check	Save	Hide Answer	You have used 2 of 3 submissions

H2 (2/2 points)

Find the number of shortest path from O to P

1) If the path must pass through point A

560

Answer: 560

2) If the path must pass through path AB

350

350

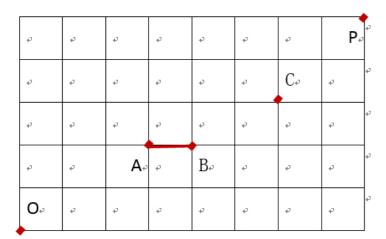
Answer: 350

3) If the path must pass through point A and point C

240

240

Answer: 240



EXPLANATION

1) Complete in 2 steps O(0,0)->A(3,2), A(3,2)->P(8,5); according to multiplication rules:

C(3+2,2)*C(3+5,3)=560

2) Complete in 2 steps O(0,0)->A(3,2),B(4,2)->P(8,5), according to multiplication rules:

C(3+2,2)*C(3+4,3)=350

3) Complete in 3 steps: O(0,0)->A(3,2),A(3,2)->C(6,3),C(6,3)->P(8,5),

According to multiplication rules,

C(3+2,2)*C(3+1,1)*C(2+2,2)=240

Check Save

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H3 (1/1 point)

For the case of giving fruits to 3 children, in total there are 12 identical apples, each child may at least have a fruit, it contains ____ types of ways.

55

Answer: 55

[EXPLANATION]

Set the fruit giving away for ith child as

 $x_i, x_i \geq 1, x_1 + x_2 + x_3 = 12, let y_1 = x_1 - 1, y_2 = x_2 - 1, y_3 = x_3 - 1, y_1 + y_2 + y_3 = 9, y_i \leq 0$ The non-negative integer solution number is C(9+3-1,9)=55.

Think About: The number of non-negative integer solution number of $x_1+x_2+x_3=12, and x_1\leq 5, x_2\leq 8, x_3\leq 5$

Final Check

Save

Hide Answer

You have used 1 of 2 submissions

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