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Introduction to Computational Science and Engineering

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4.3.6 Problem Set: p-norm approximation of minimums and maximums

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Because use of min and max functions causes discontinuous derivatives, we will instead use a *p*-norm approximation of these functions. Specifically, consider a vector *v* which has *K* entries, *v* = [*v*₀, *v*₁, . . . , *v*_{*K*−1}]. Then define the following *p*-norms:

$$\mathbf{pmin}(v) = \left[\frac{1}{K} \sum_{k=0}^{K-1} |v_k|^{-p} \right]^{-1/p}$$

(4.48)

$$\mathbf{pmax}(v) = \left[\frac{1}{K} \sum_{k=0}^{K-1} |v_k|^p \right]^{1/p}$$

(4.49)

Note that as *p* → ∞, then **pm**in(*v*) → **min**(*v*) and **pm**ax(*v*) → **max**(*v*).

In our particular problem, we wish to use the combination of **min max** in our objective function. Specifically, for the power between *N_u* users and *N_b* bases, this objective using *p*-norms can be shown to be:

$$J_p = - \left\{ \frac{1}{N^u} \sum_j \left[\frac{1}{N^b} \sum_i (P_{ij})^p \right]^{-1} \right\}^{-1/p}$$

(4.50)

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Eq. 4.50 Where does the exponent of -1
stp2004

2



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