

<u>Help</u>

sandipan_dey ~

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☆ Course / Week 11: Orthogonal Projection, Low Rank Approximation,... / 11.3 Orthonorm...

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11.3.6 Solving the Linear Least-Squares Problem via QR Factorization

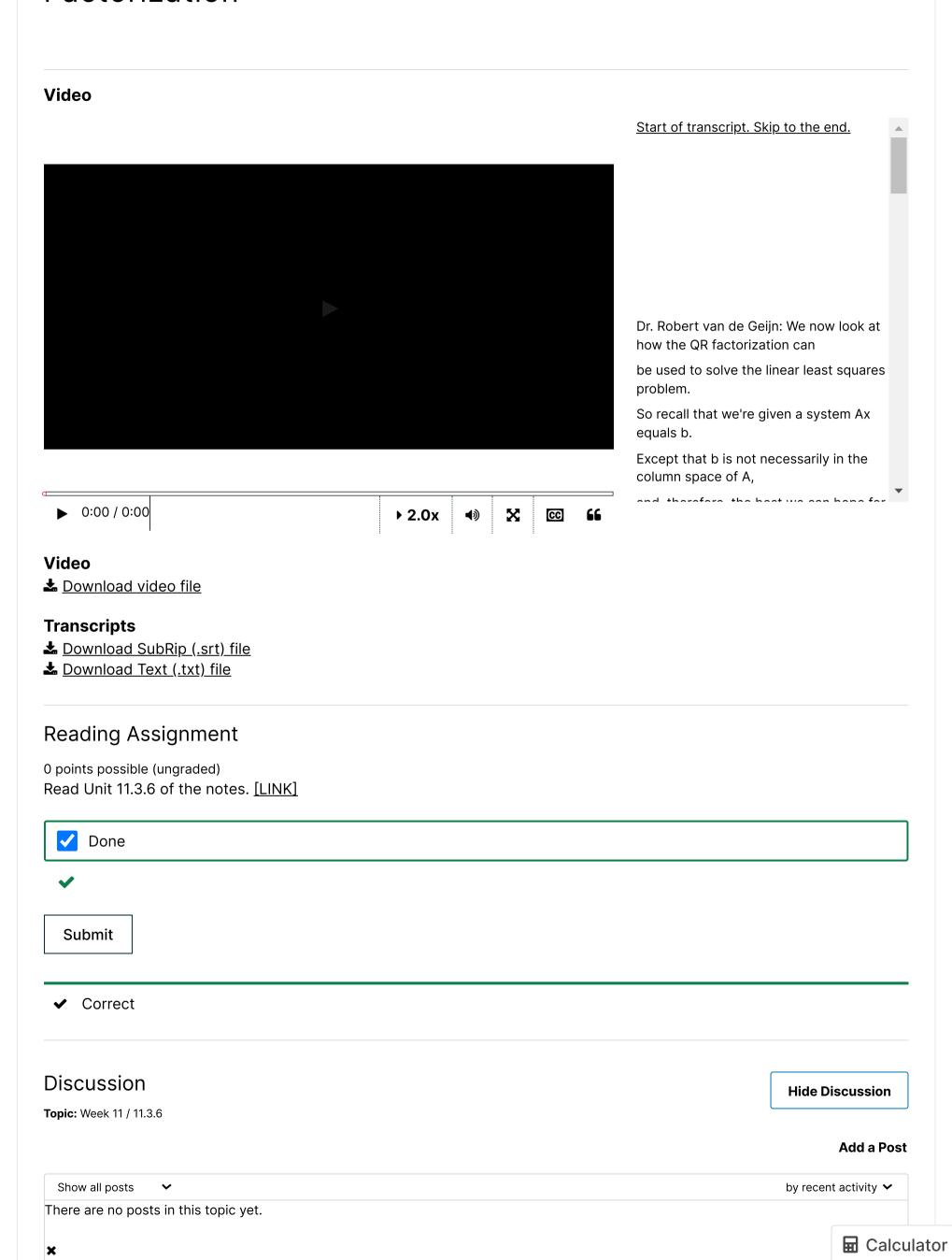
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Week 11 due Dec 22, 2023 21:12 IST Completed

11.3.6 Solving the Linear Least-Squares Problem via QR Factorization



Homework 11.3.6.1

4/4 points (graded)

In Homework 11.3.4.1 you were asked to consider $A=egin{pmatrix}1&0\\0&1\\1&1\end{pmatrix}$ and compute an orthonormal basis for $\mathcal{C}(A)$.

In Homework 11.3.5.1 you were then asked to compute the QR factorization of that matrix. Of course, you could/should have used the results from Homework 11.3.4.1 to save yourself calculations. The result was the following factorization A=QR:

$$\left(egin{array}{c|c} 1 & 0 \ 0 & 1 \ 1 & 1 \end{array}
ight) = \left(egin{array}{c|c} rac{1}{\sqrt{2}} \begin{pmatrix} 1 \ 0 \ 1 \end{pmatrix} & rac{\sqrt{2}}{\sqrt{3}} \begin{pmatrix} -rac{1}{2} \ 1 \ rac{1}{2} \end{pmatrix} \end{array}
ight) \left(egin{array}{c|c} \sqrt{2} & rac{1}{\sqrt{2}} \ \hline 0 & rac{\sqrt{3}}{\sqrt{2}} \end{array}
ight)$$

Now, compute the "best" solution (in the linear least-squares sense), $\hat{\boldsymbol{x}}$, to

$$egin{pmatrix} 1 & 0 \ 0 & 1 \ 1 & 1 \end{pmatrix} egin{pmatrix} \chi_0 \ \chi_1 \end{pmatrix} = egin{pmatrix} 1 \ 1 \ 0 \end{pmatrix}.$$

(This is the same problem as in Homework 10.4.2.1.)

$$u = Q^T b = \begin{bmatrix} 1/\operatorname{sqrt}(2) & \checkmark & \operatorname{Answer: 1/\operatorname{sqrt}(2)} \\ \frac{1}{\sqrt{2}} & \\ 1/\operatorname{sqrt}(6) & \checkmark & \operatorname{Answer: sqrt}(2)/(2 * \operatorname{sqrt}(3)) \\ \frac{1}{\sqrt{6}} & \\ \end{bmatrix}$$

$$\left(egin{array}{c} rac{1}{\sqrt{2}} \left(egin{array}{c} 1 \ 0 \ 1 \end{array}
ight) & rac{\sqrt{2}}{\sqrt{3}} \left(egin{array}{c} -rac{1}{2} \ 1 \ rac{1}{2} \end{array}
ight) \end{array}
ight)^T \left(egin{array}{c} 1 \ 1 \ 0 \end{array}
ight) = \left(egin{array}{c} rac{1}{\sqrt{2}} \ rac{\sqrt{2}}{2\sqrt{3}} \end{array}
ight)$$

• The solution to $R\hat{x}=u$ is

$$\hat{x} = \begin{bmatrix} 1/3 \\ \frac{1}{3} \\ 1/3 \\ \frac{1}{3} \end{bmatrix}$$
Answer: 1/3

Answer: 1/3

$$\left(egin{array}{c|c} \sqrt{2} & rac{1}{\sqrt{2}} \ \hline 0 & rac{\sqrt{3}}{\sqrt{2}} \end{array}
ight) \left(egin{array}{c} \hat{\chi}_0 \ \hat{\chi}_1 \end{array}
ight) = \left(egin{array}{c} rac{1}{\sqrt{2}} \ rac{\sqrt{2}}{2\sqrt{3}} \end{array}
ight)$$

■ Calculator

or

 $egin{pmatrix} \hat{\chi}_0 \ \hat{\chi}_1 \end{pmatrix} = egin{pmatrix} 1/3 \ 1/3 \end{pmatrix}$

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