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<u>Unit 5 Reinforcement Learning (2</u>

Lecture 17. Reinforcement Learning

Course > weeks)

> 1

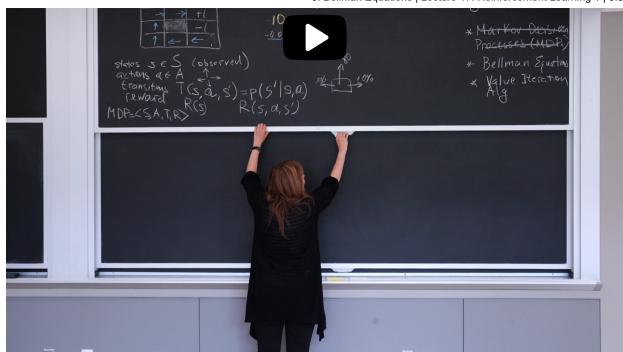
> 6. Bellman Equations

6. Bellman Equations Bellman Equations

Start of transcript. Skip to the end.

So now we will start introducing a tiny bit more notation.

X



Just three.

I promise to discuss Bellman equations.

So the first annotation that I will introduce,

as I already alluded, is called V. V star.

This is the value of state.

What does it mean?

It tells you the value of the expected reward



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In this problem, we work through a numerical example to understand the Bellman equations:

Let there be 4 possible actions, a_1, a_2, a_3, a_4 from a given state s and assume while answering the following problems that the Q^* values are given as below:

$$Q^{st}\left(s,a_{1}
ight) =10Q^{st}\left(s,a_{2}
ight) =-1Q^{st}\left(s,a_{3}
ight) =0Q^{st}\left(s,a_{4}
ight) =11$$

Recall from the lecture that,

$$V^{st}\left(s
ight) =\max_{a}Q^{st}\left(s,a
ight)$$

$$Q^{st}\left(s,a
ight)=\sum_{s^{\prime}}T\left(s,a,s^{\prime}
ight)\left(R\left(s,a,s^{\prime}
ight)+\gamma V^{st}\left(s^{\prime}
ight)
ight)$$

Value function in terms of Q function

1/1 point (graded) Enter the value of $V^{st}\left(s\right)$ below:

11 **✓** Answer: 11

Solution:

Note that $V^{st}\left(s
ight)$ is given by:

$$V^{st}\left(s
ight) =\max_{a}Q^{st}\left(s,a
ight)$$

$$V^*(s) = \max(10, -1, 0, 11) = 11$$

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You have used 1 of 2 attempts

1 Answers are displayed within the problem

Bellman Equation for Q function

1/1 point (graded)

Let s^\prime be a state that can be reached from s by taking the action a_1 . Also assume that

$$T\left(s,a_{1},s^{\prime}
ight)=1R\left(s,a_{1},s^{\prime}
ight)=5\gamma=0.5$$

Enter the value of $V^*\left(s'\right)$ below:

10

✓ Answer: 10

Solution:

Note that since T denotes probabilities, the following must be true:

$$\sum_{s'}T(s,a,s')=1$$

. Also,

$$Q^{st}\left(s,a
ight) = \sum_{s^{\prime}}T\left(s,a,s^{\prime}
ight)\left(R\left(s,a,s^{\prime}
ight) + \gamma V^{st}\left(s^{\prime}
ight)
ight)$$

Since, $T(s,a_1,s')=1$ and $\sum_{s'}T(s,a,s')=1$, we would have $T(s,a_1,s")=0 \quad \forall s"\neq s'$. The above equation would then reduce as follows

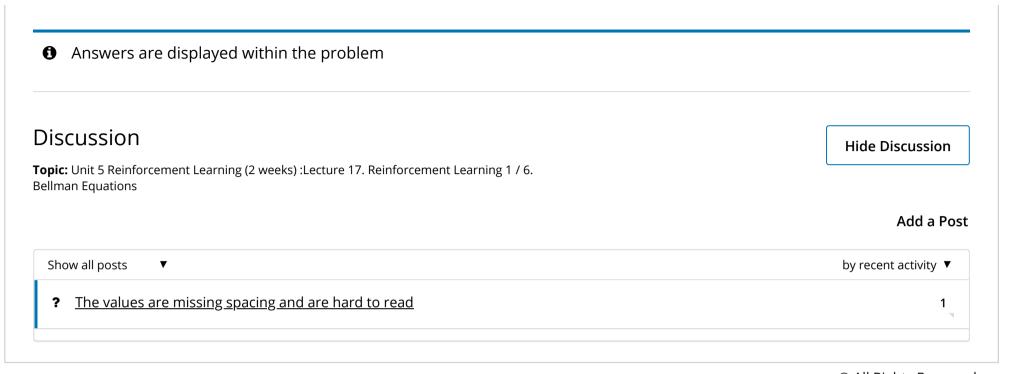
$$Q^{st}\left(s,a_{1}
ight)=T\left(s,a_{1},s^{\prime}
ight)\left(R\left(s,a_{1},s^{\prime}
ight)+\gamma V^{st}\left(s^{\prime}
ight)
ight)$$

$$10 = 1*(5+0.5*V^*(s'))$$

$$V^*\left(s'\right) = 5/0.5 = 10$$

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You have used 2 of 3 attempts



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