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<u>Lecture 7: Hypothesis Testing</u>

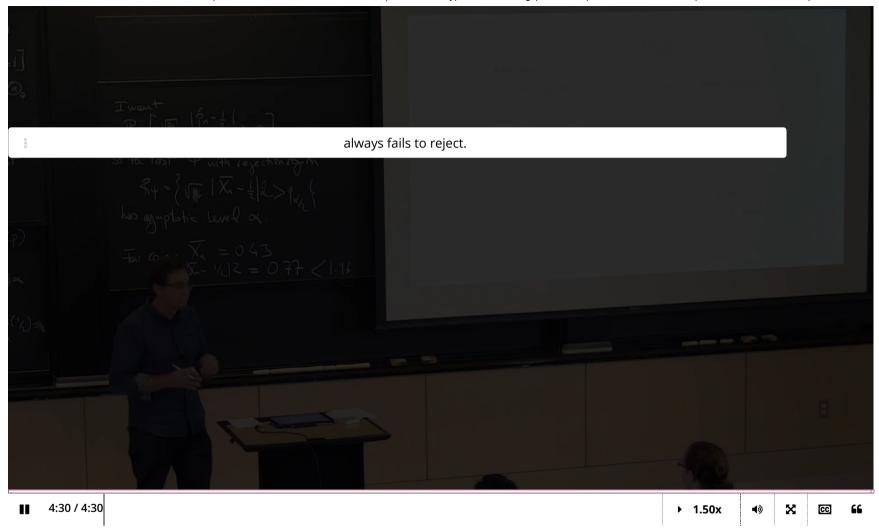
4. Worked Example: Conclusion of a

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> Two-Sided Test

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4. Worked Example: Conclusion of a Two-Sided Test
Conclusion and Comments on the Two-Sided Test for a Bernoulli Experiment



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Rejecting or Failing to Reject the Null Hypothesis I

2/2 points (graded)

In this problem, we will complete the hypothesis testing procedure for testing if a coin is fair.

## Setup as before:

You observe  $X_1,\ldots,X_n\stackrel{i.i.d.}{\sim} \mathrm{Ber}\left(p^*\right)$  (each  $X_i$  models a coin flip) and want to decide if  $p^*=1/2$ . The associated statistical model is  $(\{0,1\},\{\mathrm{Ber}\left(p\right)\}_{p\in(0,1)})$  and the null and alternative hypotheses are

- $H_0: p^* = 1/2$
- $H_1: p^* \neq 1/2$ .

You design the statistical test:

$$\psi_n \; = \; \mathbf{1} \left( T_n > q_{lpha/2} 
ight) \ ext{where} \quad T_n \; = \; \sqrt{n} rac{\left| \overline{X}_n - 0.5 
ight|}{\sqrt{0.5 \left( 1 - 0.5 
ight)}}$$

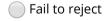
where  $q_{\alpha/2}$  denotes the  $1-\alpha/2$  quantile of a standard Gaussian, and  $\alpha$  is determined by the required level of  $\psi$ . Note the absolute value in  $T_n$  for this two sided test.

## **Questions:**

You flip the coin 200 times and observed 80 Heads. Recall from the problem *Hypothesis Testing: A Sample Data Set of Coin Flips I* in the previous lecture that the value of the test statistics  $T_n$  for this data set is  $T_{200} = 2.83$ .

If the test  $\psi = \mathbf{1}$   $(T_n > q_{\alpha/2})$  is designed to have asymptotic level 5%, would you **reject** or **fail to reject** the null hypothesis  $H_0: p^* = 1/2$  for this data set?







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If instead, the test  $\psi=\mathbf{1}$   $(T_n>q_{lpha/2})$  is designed to have asymptotic level 10%, would you reject or fail to reject  $H_0$  using the same data set?





Fail to reject



## Solution:

• If  $\psi$  is designed to have asymptotic level 5%, this implies that  $\alpha=0.025$ , according to the problem on the problem. By using a table or computational tools, we see that  $q_{0.025}=1.96$ .

In the problem "Hypothesis Testing: A Sample Data Set of Coin Flips I", we computed that  $T_{200}=|-2.82842|\sim 2.83$ . Since  $T_{200}=|-2.82842|>1.96$ , we have  $\psi=1$  and we **reject** the null.

• If instead  $\psi$  has asymptotic level  $\eta$  where  $\eta>\alpha$ , then  $q_{\eta/2}< q_{\alpha/2}$ , i.e. the threshold decreases, leading to  $T_{200}>q_{\eta/2}$ . Therefore, we again reject  $H_0$ .

**Remark:** A test with a smaller (asymptotic) level is more "stringent" than a test of the same form with a greater (asymptotic) level.

Submit

You have used 1 of 1 attempt

**1** Answers are displayed within the problem

Discussion

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