

## MITx: 6.041x Introduction to Probability - The Science of Uncertainty



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- Unit 1: Probability models and axioms
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Unit overview

Lec. 8: Probability density functions

Exercises 8 due Mar 18, 2016 at 23:59 UT

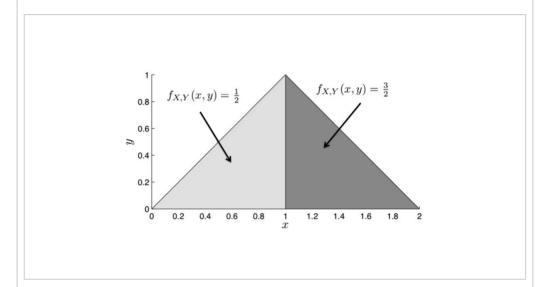
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**■** Bookmark

## Problem 5: A joint PDF on a triangular region

(7/7 points)

This figure below describes the joint PDF of the random variables X and Y. These random variables take values in [0,2] and [0,1], respectively. At x=1, the value of the joint PDF is 1/2.



1. Are  $oldsymbol{X}$  and  $oldsymbol{Y}$  independent?



2. Find  $f_X(x)$ . Express your answers in terms of x using standard notation .

If 
$$0 < x < 1$$
,

$$f_X(x) = \boxed{\hspace{1cm} imes /2 \hspace{1cm}}$$

If 1 < x < 2

Problem 5: A joint PDF on a triangular region | Problem Set 5 | 6.041x Courseware | edX

Exercises 9 due Mar 18, 2016 at 23:59 UT

Lec. 10: Conditioning on a random variable; Independence; Bayes' rule

Exercises 10 due Mar 18, 2016 at 23:59 UT

Standard normal table

Solved problems

## **Problem Set 5**

Problem Set 5 due Mar 18, 2016 at 23:59 UT

**Unit summary** 

 Unit 6: Further topics on random variables

$$f_X(x) = \boxed{3-3*x/2}$$

3. Find  $f_{Y\mid X}(y\mid 0.5)$ .

If 
$$0 < y < 1/2$$
,

$$f_{Y\mid X}(y\mid 0.5)=$$
 2

4. Find  $f_{X\mid Y}(x\mid 0.5)$ .

If 
$$1/2 < x < 1$$
,

$$f_{X\mid Y}(x\mid 0.5)=$$
 1/2

If 
$$1 < x < 3/2$$
,

$$f_{X\mid Y}(x\mid 0.5)=$$
 3/2

5. Let R = XY and let A be the event  $\{X < 0.5\}$ . Evaluate  $\mathbf{E}[R \mid A]$ .

$$\mathbf{E}[R \mid A] = \boxed{1/16}$$

You have used 3 of 3 submissions

## DISCUSSION

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