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## Arithmetical Symbols

The arithmetical symbols “0”, “1”, “+”, “×” and “^” work exactly as you’d expect: “0” and “1” name the numbers zero and one, respectively, and “+”, “×” and “^” express addition, multiplication and exponentiation, respectively. (To improve readability I will usually write “ $n^m$ ” instead of “ $n \wedge m$ ”.)

Our arithmetical symbols can be combined to form complex symbols. For instance, one can construct the complex symbols “ $0 + 1$ ” and “ $(1 + 1) \times (1 + 1)$ ”, which name the numbers one and four, respectively. For this reason,  $L$  has the expressive resources to name every natural number.

Here is a partial list:

Expression	Abbreviation	Refers to
0	-	number zero
1	-	number one
$(1 + 1)$	2	number two
$((1 + 1) + 1)$	3	number three
$((((1 + 1) + 1) + 1) + 1)$	4	number four
$\vdots$	$\vdots$	$\vdots$

Note the abbreviations in the middle column of the table above. They are not officially part of our language. Instead, they should be thought of as short-hand for the complex symbols to their left. And they’ll make a big difference. For instance, they’ll allow us to write “12” instead of the much more cumbersome:

$$(((((((((((1 + 1) + 1) + 1) + 1) + 1) + 1) + 1) + 1) + 1) + 1) + 1)$$

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