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### 3. Simple Testing

Let  $X_1, \dots, X_n$  be i.i.d.  $\mathcal{N}(\theta, 1)$ . Consider testing

$$H_0 : \theta = 0 \quad \text{v.s.} \quad H_1 : \theta = 1.$$

(a)

2/2 points (graded)

What would a Type 1 error be in this test?

☒ Rejecting  $H_0$  when  $\theta = 0$

☐ Not Rejecting  $H_0$  when  $\theta = 0$

☐ Rejecting  $H_0$  when  $\theta = 1$

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☐ Not rejecting  $H_0$  when  $\theta = 1$



What would a Type 2 error be in this test?

☐ Rejecting  $H_0$  when  $\theta = 0$

☐ Not Rejecting  $H_0$  when  $\theta = 0$

☐ Rejecting  $H_0$  when  $\theta = 1$

☒ Not rejecting  $H_0$  when  $\theta = 1$



Submit

You have used 1 of 1 attempt

(b)

1/1 point (graded)

Suppose that the rejection region of a test  $\psi$  has the form  $R = \{\bar{X}_n : \bar{X}_n > c\}$ . Find the smallest  $c$  such that  $\psi$  has level  $\alpha$ .

(If applicable, type **abs(x)** for  $|x|$ , **Phi(x)** for  $\Phi(x) = \mathbf{P}(Z \leq x)$  where  $Z \sim \mathcal{N}(0, 1)$ , and **q(alpha)** for  $q_\alpha$ , the  $1 - \alpha$  quantile of a standard normal variable.)

$c \geq$

q(alpha)/sqrt(n)



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You have used 3 of 3 attempts

✓ Correct (1/1 point)

(c)

2/2 points (graded)

Suppose that the test  $\psi$  has level  $\alpha = 0.05$ . What is the power of  $\psi$ ?

(If applicable, type **abs(x)** for  $|x|$ , **Phi(x)** for  $\Phi(x) = \mathbf{P}(Z \leq x)$  where  $Z \sim \mathcal{N}(0, 1)$ , and **q(alpha)** for  $q_\alpha$ , the  $1 - \alpha$  quantile of a standard normal variable, e.g. enter **q(0.01)** for  $q_{0.01}$ .)

Power of  $\psi$ :

1-Phi(q(0.05)-sqrt(n))



What does the power of  $\psi$  approach as  $n \rightarrow \infty$ ?

$\lim_{n \rightarrow \infty}$  Power =

1



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You have used 1 of 3 attempts

✓ Correct (2/2 points)

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## which test statistics in 3-c

 question posted a day ago by [denizstij](#)

i am not sure exactly which test's power we need to estimate in 3-c. is it test of:

1)  $H_0 : \theta = 0; H_1 : \theta = 1 \Rightarrow \psi = \mathbf{1}\{|\bar{X}_n| > s\}$  the test mentioned 3-a (i assume)

2)  $\psi = \mathbf{1}\{\bar{X}_n > c\}$  ; namely the test mentioned in 3-b

as far as i see, 3-a and 3-b imply different tests. or is my understanding wrong; namely both tests are same in 3-a and 3-b ?

if my approach is wrong, any hint on 3-c please?

Thanks

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1 response

**[samc1031](#)**

a day ago

Part (a) does not specify a rejection region (the answers for that part don't depend on what that region is)

you are right... rejection region of 3-b worked... thanks ...

 posted a day ago by [denizstij](#)

Hi @denizstij, would you please mark @samc1031's answer with a green check? This will help us navigate the forum more efficiently!

 posted about 23 hours ago by [ya\\_mukhin](#) (Staff)

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