

## MITx: 6.041x Introduction to Probability - The Science of Uncertainty



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## Exercise: The sum of Poisson r.v.'s

(1 point possible)

Consider a Poisson process with rate  $\lambda=1$ . Consider three times that satisfy  $0 < t_1 < t_2 < t_3$ . Let M be the number of arrivals during the interval  $[0,t_2]$ . Let N be the number of arrivals during the interval  $[t_1,t_3]$ . Is the random variable M+N guaranteed to be Poisson?





Answer: No

## Answer:

Because the two time intervals overlap, M and N are not independent and the result in the preceding video does not apply. Consider the extreme case where  $t_1 \approx 0$  and  $t_2 \approx t_3$ . In that case, the two intervals almost coincide, and therefore M=N with high probability. In that case, the PMF of M+N is concentrated on the even integers, which cannot happen for a Poisson PMF.

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Unit overview

Lec. 21: The Bernoulli process

Exercises 21 due May 11, 2016 at 23:59 UTC

Lec. 22: The Poisson process

Exercises 22 due May 11, 2016 at 23:59 UTC

Lec. 23: More on the Poisson process

## You have used 1 of 1 submissions

Exercises 23 due May 11, 2016 at 23:59 UTC

Solved problems

Additional theoretical material

**Problem Set 9** 

Problem Set 9 due May 11, 2016 at 23:59 UTC

**Unit summary** 

Unit 10: Markov chains

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