8. The K-Means Algorithm: the Specifics

The K-Means Algorithm: the Specifics

And again, looking at this example,

we can see what is the problem.

The problem here is that when we decided, when we randomly

initialized it, we put points which

are very close to each other.

We put two centroids which are very close to each other.

So maybe one intuition from here is

that if we randomly initialize our centers,

we actually may want to spread them around rather than put

them closer together.

And there are algorithms which capture this intuition

and provide you a mechanism for selecting

this random initialization, which results in a better

theoretical guarantees.

But when you are practically trying to do

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Finding the Representative Z

3/3 points (graded)

Find a simplified form of the following equation:

$$\frac{\partial}{\partial z_j} \sum_{i \in \mathbb{C}_j} \left\| x^{(i)} - z_j \right\|^2$$

- [x] $\sum_{i \in \mathbb{C}_j} -2\left(x^{(i)} - z_j\right)$ ✔
- [ ] $-2\left(z_j - \sum_{i \in \mathbb{C}_j} x^{(i)}\right)$
- [ ] $\sum_{i \in \mathbb{C}_j} -\left(x^{(i)} - z_j\right)$
- [ ] $\sum_{i \in \mathbb{C}_j} x^{(i)}$

Now, what is the value of z_j that minimizes the sum?

- [x] $\frac{\sum_{i \in C_j} x^{(i)}}{|C_j|}$ ✔

- [ ] $\sum_{i \in C_j} x^{(i)}$

Regarding update of z_j, which of the following statements is true (select all that apply)?

- [ ] The value of z_j is affected by points $x_i \notin C_j$
- [x] The value of z_j is only affected by points $x_i \in C_j$
- [x] The obtained z_j is the centroid (center of mass assuming each $x^{(i)}$ has equal mass) of the jth cluster

Solution:

Note that

$$z_j = \frac{\sum_{i \in C_j} x^{(i)}}{|C_j|}$$

is the center of mass, or centroid, of the jth cluster.

You have used 1 of 3 attempts

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Answers are displayed within the problem

Impact of Intialization

1/1 point (graded)

Remember that the K-Means algorithm is given by

1. Randomly select $z_1, \ldots, z_k$
2. Iterate
    1. Given $z_1, \ldots, z_k$, assign each $x^{(i)}$ to the closest z_j. i.e., assign each $x^{(i)}$.
    2. Given $C_1, \ldots, C_k$ find the best representatives $z_1, \ldots, z_k$ such that

$$\text{argmin}_{z_1,\ldots,z_k} \sum_{j=1}^{k} \sum_{i \in C_j} \left\| x^{(i)} - z_j \right\|^2$$

Which of the following is true about the initialization and output of the K-Means algorithm? Select all those apply.

- [x] Step 2.1 decreases or does not change the cost of clustering output ✔

- [x] Step 2.2 decreases or does not change the cost of clustering output ✔
- [x] The clustering output that the K-Means algorithm converges to depends on the intialization ✔

✔

Solution:

While steps 2.1 and 2.2 of the algorithm always decreases the cost or keeps it the same at least, the output of the algorithm largely dependes on the intialization of step 1. Thus, in practice, it is wise to make sure that $z_1, \ldots z_k$ are intialized so that they are well spread out. Another alternative is to try multiple initializations and choose the clustering output that appears the most commonly.

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Answers are displayed within the problem

What if K is 1?

1/1 point (graded)
Now, assume that we are given with $K = 1$ as the number of clusters. Now, does initialization matter at all?

(●) No, because cluster assignment does not change in step 2.1 ✔

Yes, because representative selection changes in step 2.2

Solution:

Because if $K = 1$ cluster assignment can never change, initialization does not matter. Also note that the algorithm will converge (have same assignment and same representative from there on) after just 1 iteration.

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Answers are displayed within the problem

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