

MITx: 6.041x Introduction to Probability - The Science of Uncertainty

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Problem 5: LLMS estimation with random sums

(4/4 points)

Let N be a geometric r.v. with mean 1/p; let A_1,A_2,\ldots be a sequence of i.i.d. random variables, all independent of N, with mean 1 and variance 1; let B_1,B_2,\ldots be another sequence of i.i.d. random variable, all independent of N and of A_1,A_2,\ldots , also with mean 1 and variance 1. Let $A=\sum_{i=1}^N A_i$ and $B=\sum_{i=1}^N B_i$.

1. Find the following expectations using the law of iterated expectations. Express each answer in terms of \boldsymbol{p} using standard notation .

$$\mathbf{E}[AB] = \boxed{(2-p)/p^2}$$

$$\mathbf{E}[NA] = \boxed{(2-p)/p^2}$$

2. Let $\hat{N}=c_1A+c_2$ be the LLMS estimator of N given A. Find c_1 and c_2 in terms of p.

$$c_1 = \boxed{ ext{ 1-p} }$$

$$c_2 = \boxed{ 1 }$$

You have used 2 of 2 submissions

DISCUSSION

Click "Show Discussion" below to see discussions on this problem.

Unit overview

Lec. 14: Introduction to Bayesian inference Exercises 14 due Apr 06, 2016 at 23:59 UT &

Lec. 15: Linear models with normal noise Exercises 15 due Apr 06, 2016 at 23:59 UT

Problem Set 7a
Problem Set 7a due
Apr 06, 2016 at 23:59
UTC

Lec. 16: Least mean squares (LMS) estimation Exercises 16 due Apr 13, 2016 at 23:59 UT

Lec. 17: Linear least mean squares (LLMS) estimation Exercises 17 due Apr

Exercises 17 due Apr 13, 2016 at 23:59 UT

Problem Set 7b

Problem Set 7b due Apr 13, 2016 at 23:59 UTC

Solved problems

Additional theoretical material

Unit summary

 Unit 8: Limit theorems and classical statistics

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