

### MITx: 6.041x Introduction to Probability - The Science of Uncertainty



Unit 0: Overview

- EntranceSurvey
- Unit 1: Probability models and axioms
- Unit 2: Conditioning and independence
- Unit 3: Counting
- Unit 4: Discrete random variables
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### Unit overview

# Lec. 8: Probability density functions

Exercises 8 due Mar 16, 2016 at 23:59 UT

Lec. 9: Conditioning on an event; Multiple r.v.'s

Exercises 9 due Mar 16, 2016 at 23:59 UT Unit 5: Continuous random variables > Lec. 10: Conditioning on a random variable; Independence; Bayes' rule > Lec 10 Conditioning on a random variable Independence Bayes rule vertical6

■ Bookmark

## Exercise: Stick-breaking

(3/3 points)

Consider the same stick-breaking problem as in the previous clip, and let  $\ell=1$ . Recall that  $f_{X,Y}(x,y)=1/x$  when  $0\leq y\leq x\leq 1$ .

a) Conditioned on Y=2/3, the conditional PDF of X is nonzero when  $a \leq x \leq b$ . Find a and b.

b) On the range found in part (a), the conditional PDF  $f_{X|Y}(x \mid 2/3)$  is of the form  $cx^d$  for some constants c and d. Find d.

$$d = \begin{bmatrix} -1 \end{bmatrix}$$
 Answer: -1

#### Answer:

- a) Since the joint PDF is nonzero only for  $0 \le y \le x \le 1$ , it follows that given that Y = 2/3, X ranges on the interval [2/3, 1].
- b) As a function of x, the conditional PDF has the same functional form (within a normalizing constant) as the joint PDF, and so it is of the form c/x, from which we conclude that d=-1.

You have used 1 of 2 submissions

Lec. 10: Conditioning on a random variable; Independence; Bayes' rule

Exercises 10 due Mar 16, 2016 at 23:59 UT

Standard normal table

Solved problems

Problem Set 5 Problem Set 5 due Mar 16, 2016 at 23:59 UT

**Unit summary** 

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