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9.2.1 Accuracy and Convergence

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MO2.4

MO2.6

As the timestep is decreased, i.e. $\Delta t \rightarrow 0$, we would like our numerical method to better approximate the exact solution to the model equations. Let's define the error in our approximation at timestep n to be:

$$\underline{e}^n \equiv \underline{v}^n - \underline{u}(t^n)$$

(9.1)

Since this is $\underline{u}(t^n)$ is in general an M -dimensional vector of states, then so are \underline{v}^n and \underline{e}^n . We can define the components of this error then,

$$e_m^n = v_m^n - u_m(t^n)$$

(9.2)

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for each $m = 0$ to $M - 1$. Then, to measure the error for the entire simulation (i.e. over all timesteps), we'll take the maximum magnitude,

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$$(e_m)_{\max} = \max_n |e_m^n|$$

(9.3)

Then, in terms of these error definitions, we desire that the maximum error in each state goes to zero as $\Delta t \rightarrow 0$. This concept is known as convergence and is stated mathematically as follows:

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Definition 2 (Convergence).

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While convergence is a clear requirement for a good numerical method, the rate at which the method converges is also important. This rate is known as the order of accuracy.

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Definition 3 (Order of Accuracy).

A method has an order of accuracy of p if, for all m ,



$$(e_m)_{\max} = O(\Delta t^p)$$

as $\Delta t \rightarrow 0$,



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$$(e_m)_{\max} = C\Delta t^p \quad \text{as} \quad \Delta t \rightarrow 0.$$

where C is depends on the method and the