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## 4. Solving the homogeneous tuned mass damper system

A tuned mass damper

2/2 points (graded)

Recall that the tuned mass damper system used to reduce the swaying in tall buildings can be modeled by the 4x4 inhomogeneous system.

$$egin{pmatrix} \dot{x}_1 \ \dot{x}_2 \ \dot{y}_1 \ \dot{y}_2 \end{pmatrix} = egin{pmatrix} 0 & 0 & 1 & 0 \ 0 & 0 & 0 & 1 \ rac{-(k_1+k_2)}{m_1} & rac{k_2}{m_1} & rac{-(b_1+b_2)}{m_1} & rac{b_2}{m_1} \ rac{k_2}{m_2} & rac{-k_2}{m_2} & rac{b_2}{m_2} & rac{-b_2}{m_2} \end{pmatrix} egin{pmatrix} x_1 \ x_2 \ y_1 \ y_2 \end{pmatrix} + egin{pmatrix} 0 \ rac{F}{m_1} \ 0 \end{pmatrix}$$

In this problem, we will find the normal modes of the associated homogeneous system,

$$egin{pmatrix} \dot{x}_1 \ \dot{x}_2 \ \dot{y}_1 \ \dot{y}_2 \end{pmatrix} egin{pmatrix} 0 & 0 & 1 & 0 \ 0 & 0 & 0 & 1 \ rac{-(k_1+k_2)}{m_1} & rac{k_2}{m_1} & rac{-(b_1+b_2)}{m_1} & rac{b_2}{m_2} \ rac{b_2}{m_2} & rac{-b_2}{m_2} \end{pmatrix} egin{pmatrix} x_1 \ x_2 \ y_1 \ y_2 \end{pmatrix}.$$

In this problem, we will set

$$m_1 = 1, k_1 = 1, b_1 = 0.001, m_2 = 0.05, k_2 = 1, b_2 = 0.01.$$

The normal modes are real-valued functions that can be written in the form

$$egin{array}{lll} n_1 &=& e^{a_1 t} \cos (\omega_1 t + \phi_1) (c_1 \mathbf{v}_1 + c_2 \mathbf{v}_2) \ n_2 &=& e^{a_2 t} \cos (\omega_2 t + \phi_2) (c_3 \mathbf{v}_3 + c_4 \mathbf{v}_4). \end{array}$$

What are  $\omega_1$  and  $\omega_2$ ? (Let  $\omega_1$  be the term such that  $a_1>a_2$  in the expression above. Use the convention that frequencies are positive numbers.)

Use <u>Matlab Online</u> or other computer system to find the answer. Enter your answer to 4 decimal places in the answer boxes below.

$$\omega_1 = \boxed{0.9747}$$
 $\omega_2 = \boxed{4.5868}$ 

Answer: 0.9747

Answer: 4.5868

## Solution:

Using MATLAB (or your preferred math solver), you will find that the eigenvalues of the associated matrix for the given constants are

$$-0.1050 + 4.5868i \ -0.1050 - 4.5868i \ -0.0005 + 0.9747i \ -0.0005 - 0.9747i$$

The frequencies are the imaginary parts of these eigenvalues. The term  $e^{at}$  in the expression of the normal modes is determined by the eigenvalue where a is the real part of one of the eigenvalues. The eigenvalue with the largest real part is -0.0005 + 0.9747i. Thus

$$\omega_1 = \operatorname{Im} (-0.0005 + 0.9747i) = 0.9747,$$

and

$$\omega_2 = \operatorname{Im} (-0.1050 + 4.5868i) = 4.5868.$$

Submit

You have used 2 of 10 attempts

**1** Answers are displayed within the problem

## 4. Solving the homogeneous tuned mass damper system

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