

## MITx: 6.041x Introduction to Probability - The Science of Uncertainty



Unit 0:
Overview

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# Problem 1: Defective coin

(3/3 points)

A defective coin minting machine produces coins whose probability of Heads is a random variable  $oldsymbol{Q}$  with PDF

$$f_Q(q) = egin{cases} 3q^2, & ext{if } q \in [0,1], \ 0, & ext{otherwise}. \end{cases}$$

A coin produced by this machine is tossed repeatedly, with successive tosses assumed to be independent. Let  ${m A}$  be the event that the first toss of this coin results in Heads, and let  ${m B}$  be the event that the second toss of this coin results in Heads.

1.

$$\mathbf{P}(A) = \boxed{3/4}$$

(Your answer should be a number.)

2. Find the conditional PDF of  $m{Q}$  given event  $m{A}$ . Express your answer in terms of  $m{q}$  using standard notation .

For 
$$0 \leq q \leq 1$$
,  $f_{Q|A}(q) = igg|$  4\*q^3

3

$$\mathbf{P}(B \mid A) = \boxed{4/5}$$

(Your answer should be a number.)

You have used 2 of 2 submissions

Printable problem set available here .

### DISCUSSION

Click "Show Discussion" below to see discussions on this problem.

### Unit overview

Lec. 14: Introduction to **Bayesian inference** Exercises 14 due Apr 06, 2016 at 23:59 UT 🗗

Lec. 15: Linear models with normal noise

Exercises 15 due Apr 06, 2016 at 23:59 UT @

### **Problem Set 7a**

Problem Set 7a due Apr 06, 2016 at 23:59 UTC

Lec. 16: Least mean squares (LMS) estimation Exercises 16 due Apr 13, 2016 at 23:59 UT 🗗

Lec. 17: Linear least mean squares (LLMS) estimation

Exercises 17 due Apr 13, 2016 at 23:59 UT (2)

#### Problem Set 7b

Problem Set 7b due Apr 13, 2016 at 23:59 UTC

Solved problems

Additional theoretical material

**Unit summary** 

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