

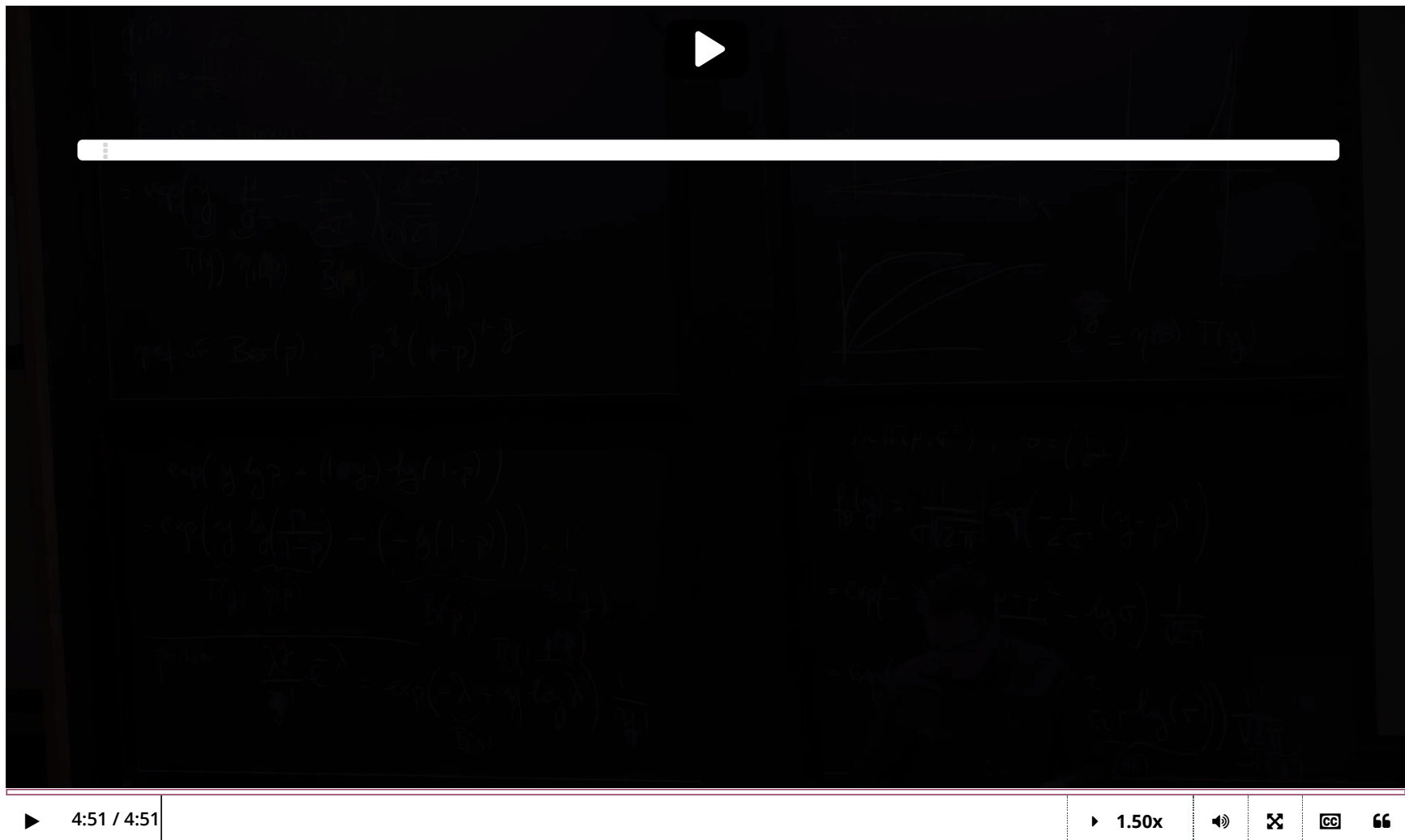


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8. Exponential Family: Discrete
> Examples

8. Exponential Family: Discrete Examples

Example: Bernoulli and Poisson Distribution



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The Binomial Distribution as an Exponential Family

3/3 points (graded)

Recall that the binomial distribution with parameters n and p is governed by

$$P(Y = y) = \binom{n}{y} p^y (1-p)^{n-y}.$$

Let n be some known number, say $n = 1000$. Then the pmf is

$$f_p(y) = \binom{1000}{y} p^y (1-p)^{1000-y}.$$

Write this as an exponential family of the form

$$f_p(y) = h(y) \exp(\eta(p) T(y) - B(p)) \quad \text{where } h(y) = \binom{1000}{y},$$

then enter $\eta(p)$, $T(y)$ and $B(p)$ below. To get unique answers, use 1 as the coefficient of y in $T(y)$.

$\eta(p) =$ ✓ Answer: ln(p/(1-p))

$T(y) =$ ✓ Answer: y

$B(p) =$ ✓ Answer: -1000*ln(1-p)

STANDARD NOTATION

Solution:

We can write $f_p(y)$ as

$$f_p(y) = \binom{1000}{y} e^{\ln p^y (1-p)^{1000-y}} = \binom{1000}{y} e^{y \ln p + (1000-y) \ln(1-p)} = \binom{1000}{y} e^{y \ln \frac{p}{1-p} - (-1000 \ln(1-p))}.$$

From this, we match up terms to get that $\eta(p) = \ln \frac{p}{1-p}$, $T(y) = y$, and $B(p) = -1000 \times \ln(1-p)$.

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i Answers are displayed within the problem

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