

Course > Unit 4 Hypothesis testing > Homework 8 > 3. QQ Plots

### 3. QQ Plots

Consider an iid sample  $X_1, X_2, \ldots, X_n \overset{iid}{\sim} \mathbf{P}$  that has been reordered as  $X_{(1)} \leq X_{(2)} \leq \ldots \leq X_{(n)}$  where n is very large. In the problems below, we have chosen a different distribution for  $\mathbf{P}$  and compared the empirical quantiles to the standard Gaussian quantiles using a QQ plot. Recall that

- ullet the **Laplace distribution**  ${
  m Lap}\,(\lambda)$  with parameter  $\lambda>0$  is the continuous probability distribution with density  $f_\lambda=rac{\lambda}{2}e^{-\lambda|x|}$ , and
- the **Cauchy distribution** is the continuous probability distribution with density  $g(x) = \frac{1}{\pi} \frac{1}{1+x^2}$ .

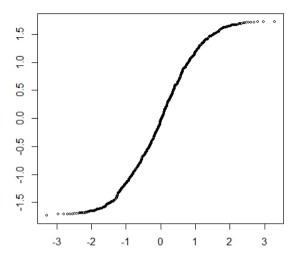
(These were also introduced in Lecture 12.)

For each plot below, match the QQ plot with the correct distribution for  $\mathbf{P}$ . *Hint:* Each possible distribution will be an answer choice exactly once, so you should use the process of elimination.

*Hint:* You may use computational tools to graph the pdf of the possible distributions of  $\bf P$ .

### Matching a Distribution to a QQ Plot I





- igcup Standard normal:  $N\left(0,1
  ight)$
- Cauchy distribution
- $\bigcirc$  Exponential with parameter 1:  $\operatorname{Exp}\left(1\right)$
- lacksquare Uniform on the interval  $[-\sqrt{3},\sqrt{3}]$ :  $\mathrm{Unif}\,[-\sqrt{3},\sqrt{3}]$
- $\bigcirc$  Laplace distribution with parameter  $\sqrt{2}$ :  $\mathrm{Lap}\left(\sqrt{2}
  ight)$

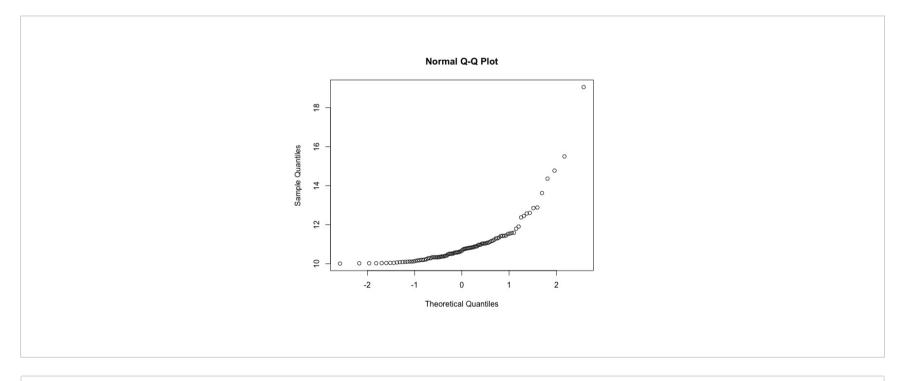


Submit

You have used 1 of 2 attempts

✓ Correct (1/1 point)

## Matching a Distribution to a QQ Plot II



- igcup Standard normal:  $N\left(0,1
  ight)$
- Cauchy distribution
- lacktriangledown Shifted exponential with parameter 2.5:  ${
  m Exp}\,(2.5)+c$  for some c>0

- O Uniform on the interval  $[-\sqrt{3},\sqrt{3}]$ :  $Unif[-\sqrt{3},\sqrt{3}]$
- $\bigcirc$  Laplace distribution with parameter  $\sqrt{2}$ :  $\mathrm{Lap}\left(\sqrt{2}
  ight)$

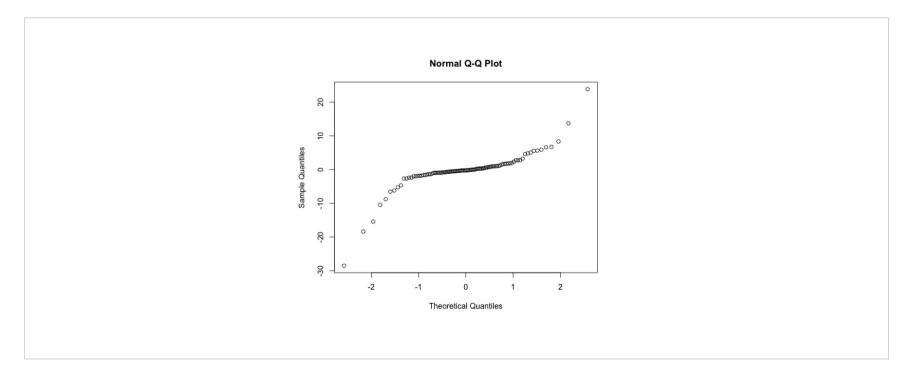


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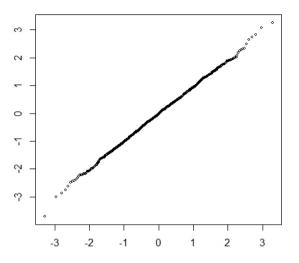
### Matching a Distribution to a QQ Plot III



$\bigcirc$ Standard normal: $N\left(0,1 ight)$
Cauchy distribution
$igcup$ Exponential with parameter $1$ : $\operatorname{Exp}\left(1 ight)$
Uniform on the interval $[-\sqrt{3},\sqrt{3}]$ : $\mathrm{Unif}[-\sqrt{3},\sqrt{3}]$
$\bigcirc$ Laplace distribution with parameter $\sqrt{2}$ : $\mathrm{Lap}(\sqrt{2})$
✓
Submit You have used 1 of 2 attempts
✓ Correct (1/1 point)
Matching a Distribution to a CO Plot IV

Matching a Distribution to a QQ Plot IV





- lacksquare Standard normal:  $N\left(0,1
  ight)$
- Cauchy distribution
- $\bigcirc$  Exponential with parameter 1:  $\operatorname{Exp}\left(1\right)$
- O Uniform on the interval  $[-\sqrt{3},\sqrt{3}]$ :  $\mathrm{Unif}\,[-\sqrt{3},\sqrt{3}]$
- igcup Laplace distribution with parameter  $\sqrt{2}$ :  $\mathrm{Lap}\left(\sqrt{2}
  ight)$

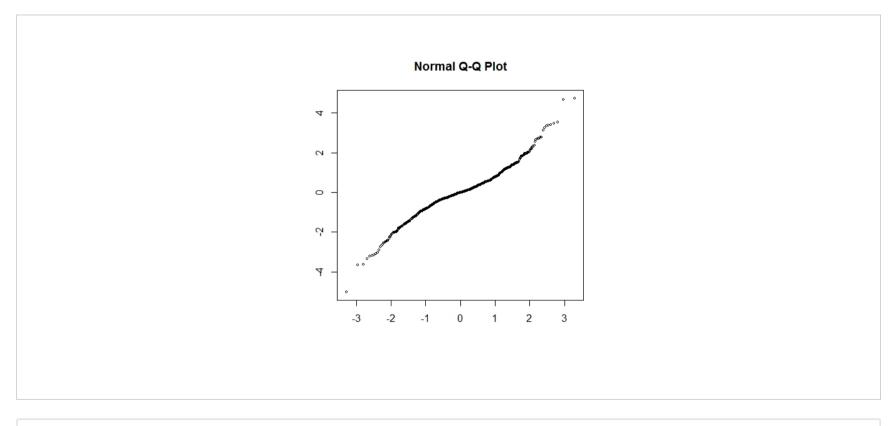


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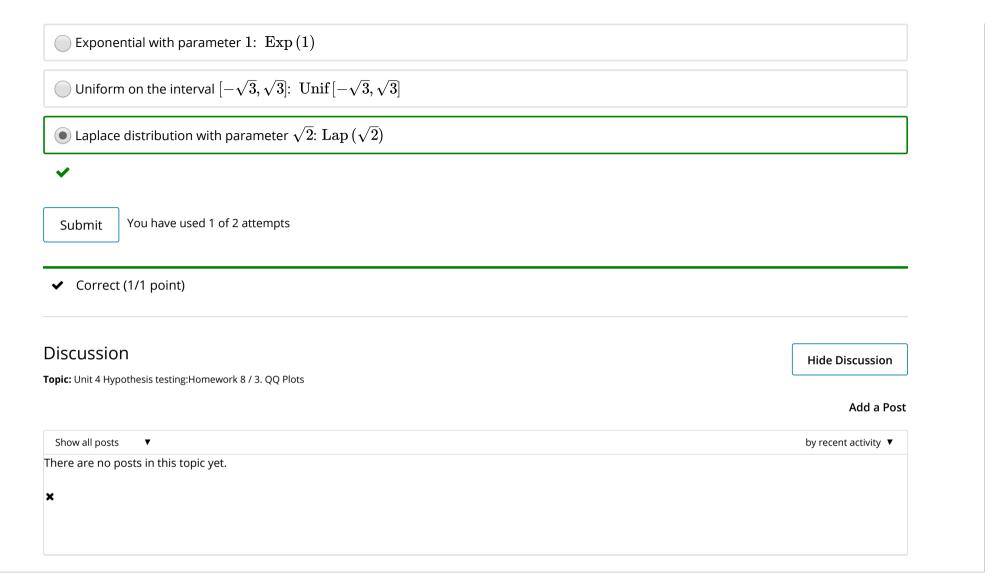
You have used 1 of 2 attempts

✓ Correct (1/1 point)

# Matching a Distribution to a QQ Plot V



- igcup Standard normal:  $N\left(0,1
  ight)$
- Cauchy distribution



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