

e

5. Compute the LU factorization of $A = \begin{pmatrix} -2 & 1 & 0 \\ 6 & -1 & -1 \\ 4 & 2 & -1 \end{pmatrix}$ and use it to solve $Ax = b$, where

$$b = \begin{pmatrix} 0 \\ 6 \\ 10 \end{pmatrix}.$$

You can use any method you prefer to find the LU factorization.

$$\begin{pmatrix} 1 & 0 & 0 \\ 3 & 1 & 0 \\ 2 & 0 & 1 \end{pmatrix} \left(\begin{array}{ccc|c} -2 & 1 & 0 & 0 \\ 6 & -1 & -1 & 6 \\ 4 & 2 & -1 & 10 \end{array} \right)$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -2 & 1 \end{pmatrix} \left(\begin{array}{ccc|c} -2 & 1 & 0 & 0 \\ 0 & 2 & -1 & 6 \\ 0 & 14 & -1 & 10 \end{array} \right)$$

$$\left(\begin{array}{ccc|c} -2 & 1 & 0 & 0 \\ 0 & 2 & -1 & 6 \\ 0 & 0 & 1 & -2 \end{array} \right)$$

$$\begin{aligned} x_0 &= 1 \\ x_1 &= 2 \\ x_2 &= -2 \end{aligned}$$

$$\boxed{\begin{matrix} L & U \\ \begin{pmatrix} 1 & 0 & 0 \\ -3 & 1 & 0 \\ -2 & 2 & 1 \end{pmatrix} & \begin{pmatrix} -2 & 1 & 0 \\ 0 & 2 & -1 \\ 0 & 0 & 1 \end{pmatrix} \end{matrix}}$$

$$2x_1 + (-x_2) = 6$$

$$2x_1 + 2 = 6$$

$$2x_1 = 4$$

$$x_1 = 2$$

$$-2x_0 + x_1 = 0$$

$$-2x_0 + 2 = 0$$

$$-2x_0 = -2$$

$$x_0 = 1$$