

# The Quadratic Reciprocity Law (4)

## Eisenstein's Lemma

$P \neq Q$  **odd** prime numbers

$$(-1)^M = \left( \frac{Q}{P} \right)$$

$M = \#$  of lattice points

in the interior of  $\triangle(0,0)-(P,0)-(0,Q)$

with **even** x-coord

# The Quadratic Reciprocity Law (5)

**Example** ( $P=17$ ,  $Q=13$ )

$$M = 52$$

$$(-1)^{52} = 1$$

**13 is QR (mod 17)**

$$13 \equiv 64$$

$$\equiv 8 \times 8 \pmod{17}$$

