

#### MITx: 6.008.1x Computational Probability and Inference

Heli



**Bookmarks** 

- Introduction
- ▼ 1. Probability and Inference

# Introduction to Probability (Week 1)

Exercises due Sep 22, 2016 at 02:30 IST

### Probability Spaces and Events (Week 1)

Exercises due Sep 22, 2016 at 02:30 IST

#### Random Variables (Week 1)

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### Jointly Distributed Random Variables (Week 2)

Exercises due Sep 29, 2016 at 02:30 IST

# Conditioning on Events (Week 2)

Exercises due Sep 29, 2016 at 02:30 IST

1. Probability and Inference > Independence Structure (Week 3) > Exercise: Mutual vs Pairwise Independence

■ Bookmark

### Exercise: Mutual vs Pairwise Independence

(1/1 point)

(A)

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Suppose random variables  $\boldsymbol{X}$  and  $\boldsymbol{Y}$  are independent, where  $\boldsymbol{X}$  is 1 with probability 1/2, and -1 otherwise. Similarly,  $\boldsymbol{Y}$  is also 1 with probability 1/2, and -1 otherwise. In this case, we say that  $\boldsymbol{X}$  and  $\boldsymbol{Y}$  are identically distributed since they have the same distribution (remember, just because they have the same distribution doesn't mean that they are the same random variable — here  $\boldsymbol{X}$  and  $\boldsymbol{Y}$  are independent!). Note that often in this course, we'll be seeing random variables that are independent and identically distributed (i.i.d.).

Suppose we have another random variable Z that is the product of X and Y, i.e., Z=XY.

Select all of the following that are true:

- $lacklossymbol{arphi}$  The distributions  $p_X$ ,  $p_Y$ , and  $p_Z$  are the same.  $\checkmark$
- lacktriangledown The joint distributions  $p_{X,Y}$ ,  $p_{X,Z}$ , and  $p_{Y,Z}$  are the same.  $\checkmark$
- $ot\hspace{-1em} 
  ot\hspace{-1em} 
  ot\hspace{-1em} 
  ot\hspace{-1em} X,Y,$  and Z are pairwise independent.  $ot\hspace{-1em} 
  ot\hspace{-1em} 
  ot\hspace{-1em}$
- lacksquare X, Y, and Z are mutually independent.

#### Homework 1 (Week 2)

Homework due Sep 29, 2016 at 02:30 IST

#### **B**

### Inference with Bayes' Theorem for Random Variables (Week 3)

Exercises due Oct 06, 2016 at 02:30 IST

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# Independence Structure (Week 3)

Exercises due Oct 06, 2016 at 02:30 IST



#### Homework 2 (Week 3)

Homework due Oct 06, 2016 at 02:30 IST

# Notation Summary (Up Through Week 3)

### Mini-project 1: Movie Recommendations (Week 3)

Mini-projects due Oct 13, 2016 at 02:30 IST



#### **Solution:**

The fastest way to solve this problem is to realize that it's actually the same problem as in the previous video where we had X and Y independent and identically distributed as  $\operatorname{Bernoulli}(1/2)$ , and Z was the exclusive-or (XOR) of X and Y. All we did was slightly change the labels of the outcomes to get this problem! Notice that Z takes on value -1 precisely when X and Y are different, and 1 otherwise. Hopefully that should sound like XOR. Basically -1 is what used to be 1, and 1 is what used to be 0. The problem is otherwise the same and the identical reasoning used in the video can be used here, so we won't actually spell out the solution again in detail (it's in the video!).

As a reminder, you can check that  $p_X$ ,  $p_Y$ , and  $p_Z$  are each going to have 1/2-1/2 chance of being either 1 or -1, so they have the same distribution, and when we look at any pair of the random variables, they are going to appear independent with (1, 1), (1, -1), (-1, 1), and (-1, -1) equally likely so the pairs of random variables also have the same distribution. However, as before, when we look at all three random variables, they are not mutually independent!

You have used 2 of 5 submissions

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