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ApurvaDubey Update hmm\_robot\_toy\_example.py

3b62089 2 days ago

1 contributor

85 lines (59 sloc) 3.38 KB

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```
1  ## Suppose you send your robot, Inquisition, to Mars. Unfortunately, it gets stuck in a canyon while landing and most of its sensors break.
2  ## Every hour, it tries to move forward by one area (i.e. from Area 1 to Area 2, or Area 2 to Area 3). It succeeds with probability
3  ## and fails with probability. If it fails, it stays where it is. If it is in Area 3, it always stays there (and waits to be rescued).
4  ##
5  ## The temperature sensor still works. Every hour, we get a binary reading telling us whether the robot's current environment is hot or col
6  ## We have no idea where the robot initially got stuck.
7  ##
8  ## Let's construct an HMM for this problem
9
10 import numpy as np
11
12 #####
13 # Inputs
14
15 # Emission probabilities
16 em_idx= {'hot':0, 'cold':1} # this dictionary is to be able to map observed state back to the index in the 'emission' matrix
17 emission = np.array([[1,0],[0,1],[1,0]])
```

```
18
19 # Transition probabilities
20 transition = np.array([[0.25,0.75,0],[0,0.25,0.75],[0,0,1]])
21
22 # Prior Distribution
23 prior = np.array([1/3.0,1/3.0,1/3.0])
24
25 # Observations
26 observations = ['hot','cold','hot']
27 #####
28
29 #####
30 # parameters for forward/backward algorithm
31 alpha = np.zeros(shape=(3,3)) # timesteps x hidden states
32 beta = np.zeros(shape=(3,3)) # timesteps x hidden states
33
34 print "Initial value of alpha and beta"
35 print alpha, '\n', beta
36
37 # initialize alpha and beta
38 alpha[0] = prior
39 beta[2] = 1.0/len(observations)
40
41 #####
42 print "Running forward algorithm"
43
44 # Go forward
45 for i in range(len(observations)-1):
46
47     alpha[i+1] = np.matrix(np.array(alpha[i]) # prior message
48                             * np.array(emission[:,em_idx[observations[i]]])) * np.matrix(transition)
49                             # emission probability x transition probability
50
51     alpha[i+1] = alpha[i+1]/sum(list(alpha[i+1])) # normalize
52
```

```
53     print "Iteration : " + str(i) + "\n" + str(alpha)
54
55 print "Final alpha is: \n -----"
56 print alpha
57
58 # Go backward
59 print "Running backward algorithm"
60 for i in range(len(observations)-2,-1,-1):
61
62     beta[i] = np.matrix(np.array(beta[i+1]) # prior message
63                         * np.array(emission[:,em_idx[observations[i+1]]])) * np.transpose(np.matrix(transition))
64     # emission probability x transition probability
65
66     beta[i] = beta[i]/sum(list(beta[i])) # normalize
67
68 print "Final beta is: \n -----"
69 print beta
70 #####
71
72 #####
73 print "Calculating marginals"
74
75 marginals = np.zeros(shape=(3,3)) # timesteps x hidden states
76
77 for i,obs in enumerate(observations):
78
79     marginals[i] = (alpha[i]) * (beta[i]) * np.array(emission[:,em_idx[obs]]) # martignal = alpha x beta x emission probability
80     marginals[i] = marginals[i]/sum(list(marginals[i])) # normalize
81
82 print marginals
83 #####
84
```

