44 (6) BCA-HE-6016

## 2024

## AUTOMATA THEORY AND LANGUAGES

Paper: BCA-HE-6016

Full Marks: 80

Time: Three hours

The figures in the margin indicate full marks for the questions.

Answer Q. No. 1 and any five from Q. No. 2 to Q. No. 7.

1. Answer the following:

 $1 \times 5 = 5$ 

- An unrestricted language can be accepted by
  - (i) Finite automata
  - (ji) Turing Machine

- (iii) Push Down automata
- (iv) Cellular automata

(b) A language is regular if any only if

- (i) accepted by DFA
  - (ii) accepted by PDA
  - (iii) accepted by LBA
  - (iv) accepted by Turing Machine

Which is the data structure used to implement in Push Down Automata?

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- (i) Link list
- (ii) Queue
- (tji) Stack
  - (iv) Array

14/11/2

The context free grammar defined by ab\* is

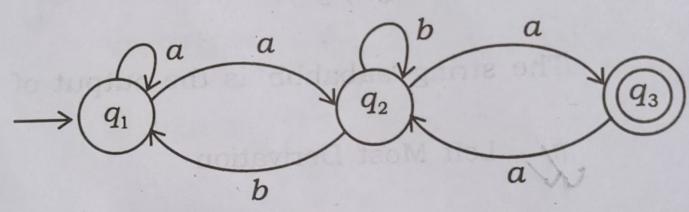
- (i)  $S \rightarrow Sb/a$
- (ii)  $S \rightarrow XY$ ,  $X \rightarrow ax$ ,  $Y \rightarrow by$
- (iii)  $C \rightarrow ss/baa/abb$ ,  $s \rightarrow \varepsilon$
- (iv)  $S \rightarrow as$ ,  $S \rightarrow bs$
- (e) Consider the grammar G with production  $S \rightarrow ass$

$$S \rightarrow b$$

The string 'aababbb' is the output of

- (i) Left Most Derivation
- (ii) Mixed Derivation
  - (iii) Right Most Derivation
  - (iv) All of the above

- 2. (a) Construct deterministic finite automata to recognize odd number of 1's and even number of 0's.
  - Explain the properties of context-free languages.
  - Show that the language:  $L = \{a^i b^i c^i / i > 0\} \text{ is not context free}$
  - 3. following system.



(b) Construct a DFA with reduced states equivalent to the regular expression

4

- Define regular expression with example.
  Show that regular sets are closed under union operation.

  2+3=5
- 4. (a) Eliminate the unit production from the CFG with P given by

$$S \rightarrow Aa/B$$
,  $B \rightarrow a/bb$ ,  $A \rightarrow a/bc/B$  5

(b) Construct a reduced grammar equivalent to the grammar

$$S \rightarrow aAa$$

$$A \rightarrow Sb/bcc/DaA$$

$$C \rightarrow abb/DD$$

$$D \rightarrow aDA, E \rightarrow aC$$

What do you mean by ambiguity of a grammar? What is left most derivation and right most derivation.

If G is the grammar

$$S \rightarrow S + S | S * S | a | b$$

Show that G is ambiguous.

5

- 5. (a) Prove that CFL are closed under union and concatenation operation. 5+5=10
  - (b) Reduce the following grammar G to CNF:

G is 
$$S \rightarrow aAD$$
,  $A \rightarrow aB/bAB$ ,

$$B \rightarrow b, D \rightarrow d.$$

5

6. (a) Construct a PDA to accept the language

$$L = \{a^n b^m / n > m \& n, m > = 0\}$$

- (i) Through empty stack
- (ii) Through final state

4+4=8



Define Push Down Automata. Give the instantaneous description of PDA.

3.5+3.5=7

7. Write short notes on: (any three) 5×3=15

La Turing machine

Pigeonhole principle

(c) Chomsky classification

Way GNF

(e) Pumping Lemma for regular languages

