Alexandra Anderson (aea84) CS 4620 a4-Shaders Warmup Exercise

1. Given a viewing direction, how does one compute the reflection direction?

Let  $\vec{v}$  be the viewing direction, pointing outward from the surface, vecr be the reflection direction likewise outward from the surface, and vecn be the normal. We assume all quantities are normalized, and solve for vecr.

We know that  $\vec{v} + \vec{r}$  is parallel to  $\vec{n}$ , because  $\vec{r}$  is the reflection of  $\vec{v}$  across  $\vec{n}$ . And since both starting vectors are normalized,

$$\begin{split} \frac{\vec{v}+\vec{r}}{||\vec{v}+\vec{r}||} &= \vec{n} \\ \vec{v}+\vec{r} &= (||\vec{v}+\vec{r}||)\vec{n} \\ \vec{v}+\vec{r} &= 2(\dot{\vec{v}}\vec{n})\vec{n} \text{ as dot(v, n)} = \text{dot(n, r) and when we sum v + r,} \\ &\text{we equivalently project each onto n, the direction of the final sum, and then add from there} \\ \vec{v}+\vec{r} &= 2(\vec{v}\bullet\vec{n})\vec{n} \\ \vec{r} &= 2(\vec{v}\bullet\vec{n})\vec{n}-\vec{v} \end{split}$$

So, the reflection vector  $\vec{r} = 2(\dot{\vec{vn}})\vec{n} - \vec{v}$