

## AI Intelligence

Artificial  $\rightarrow$  Something created by humans.

Intelligence  $\rightarrow$  ① The ability to solve novel problems.  
② The ability to think like humans.

The ability to act like humans.

↓  
subconscious actions as well.

③ Ability to think rationally (unbiased).

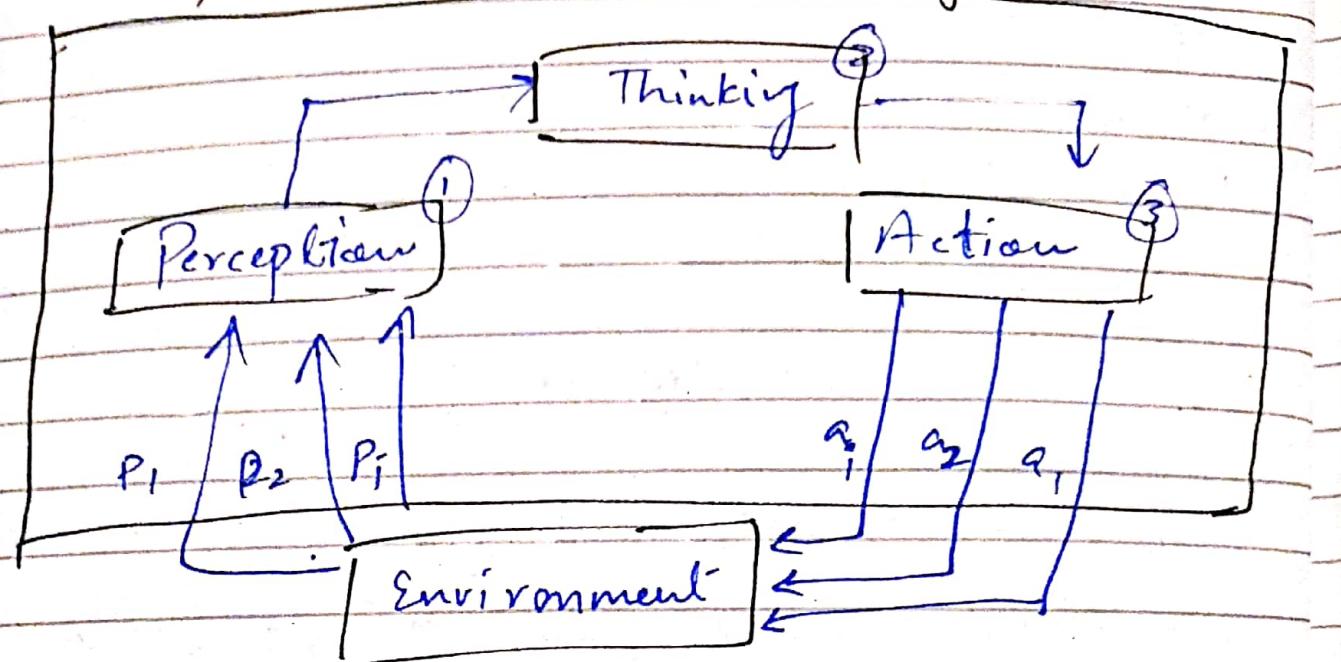
Ability to act rationally.

Rational:- A rational decision is the best possible outcome given the available facts, which is unbiased.  
 $\rightarrow$  performance measure. ↑

AI:- Is to build & understand intelligent entities or agents.

# Model of an agent

Agent"



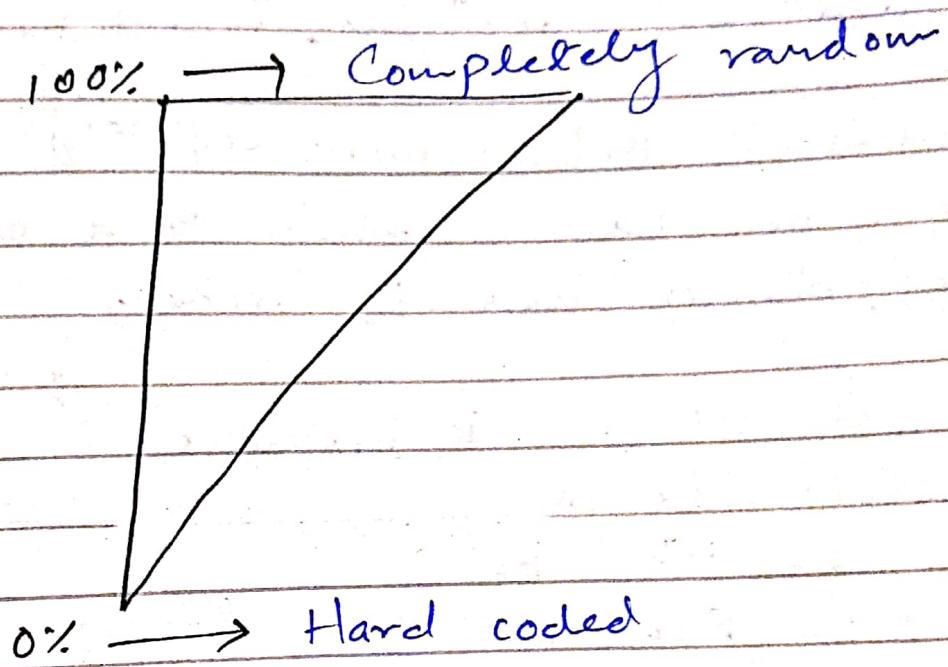
1- Perception:- Receiving input from environment through sensors & maintaining an initial state! (sometimes)  
↳ arrangement of inputs (for now).

2- Thinking:- It is the mapping of perception to action.

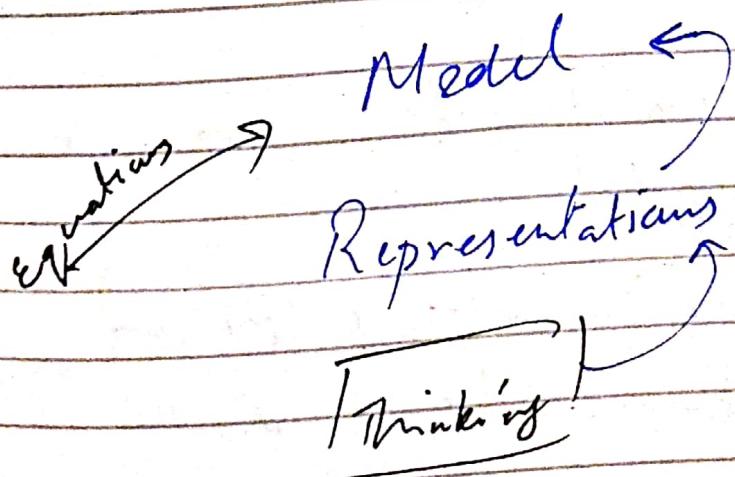
3- Action:- The change by the agent on a environment through actuators.

Example:- light switch is an agent but we know that it's not intelligent. Hence to prove it wrong, we say that there must be some ~~process~~ degree of learning and autonomy.

Autonomy:- It is the extent/degree to which an agent's action are decided by exploring the environment rather than using the designer's provided knowledge.



Learning:- Denotes to changes in the agent's model after experiencing the environment.



## Artificial Intelligence--

Def 1:- (Simple)

AI is an effort for the reproduction of human-like reasoning & intelligent behaviour through computational methods, machines, robots etc.

1)

Machine

Intelligent Behaviour Responding to question E

e.g. The box has a white & a black ball  
The darker ball is broken.

Q :- What is broken?

→ asked from machine

1- The box

2- White ball

3- Black ball

Reasoning:-

e.g. f<sub>1</sub>: All men are mortal  
f<sub>2</sub>: Ali is a man  
Conc: Ali is mortal.

→ AI has 4 types of software/robots

e.g. chess (More focused on actions)

Act like humans	Think like humans
Act rationally	Think rationally

→ How to determine the extent/degree of learning/autonomy?

pandas Series Operations.

Numpy arrays vs.

1) Content → Act like humans' <sup>Meded bewer</sup> <sub>adriaan</sub>

MadinTuring Test → pass if machine <sup>Meded bewer</sup> <sub>adriaan</sub> fools the inter-

Eliza → Program simulating a  
psychotherapist.

e.g. ~

Eliza Q: what is your name?

Aus: My name is Ali.

Human A: what is my name? /

Aus: Your name is Ali. ↗

Syntactic pattern -

My  
██████████

→ Was able to fool over 30%.

CAPTCHA → also a Turing test

Eugene Gom - → Ukrainian boy chat

Turing limitations include judges set.

Verbal cloze → Answer the question by adapting the asked question & responding into the same context.

→ Machines lack understanding.

A better Turing Test -

→ MCQs. to avoid verbal  
daggers.

(Most difficult) -  
symbolic web. Relate different  
concepts

2) Think like humans. Modelling  
of thoughts that are human-like.  
eg: Be able to process symbols/  
symbolic knowledge (def, theorems etc).

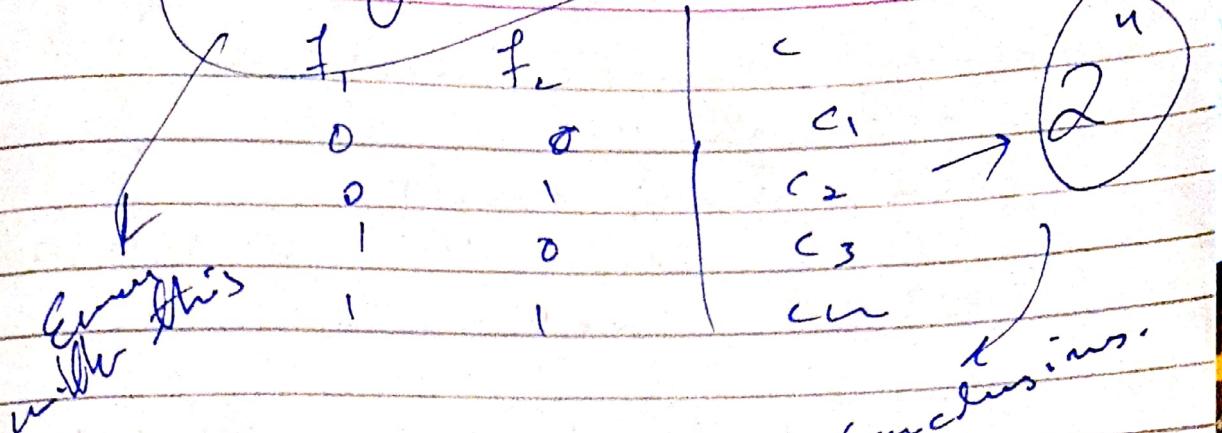
Cognitive Science Approach  
→ Reverse Engineer,

Humans have neurons that are  
connected to 10,000 other neurons  
per <sup>an</sup> avg. Hence, an incredible  
amount/degree of parallelism.  
Problems, emotions, b.ness etc.

3) Think Rationally - Idealized  
way of thinking. (logistics/rati-  
onal approach)

Problems - computational  
complexity, etc.

## Binary facts



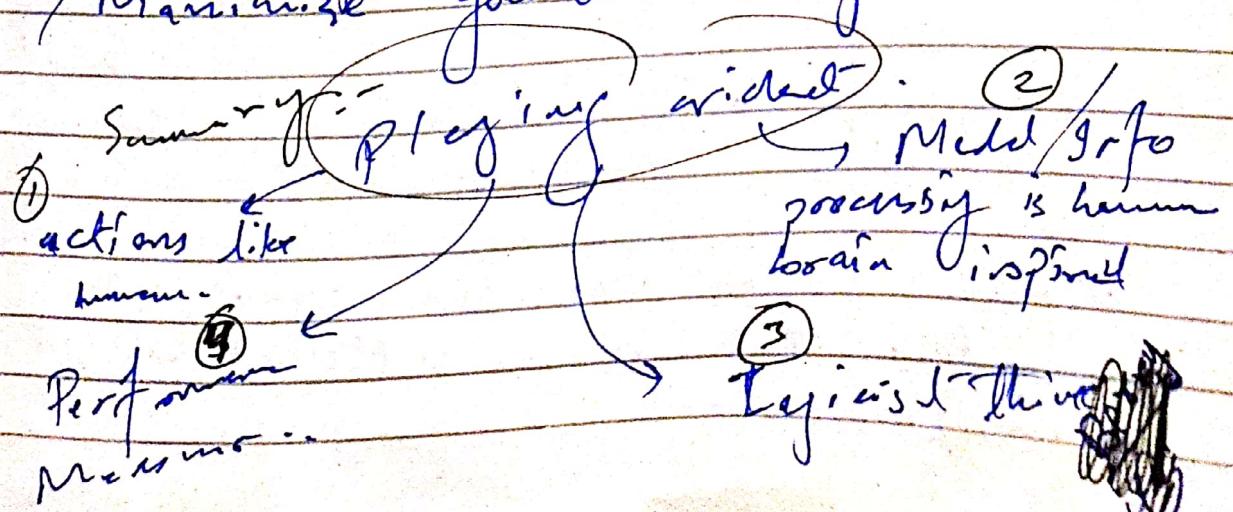
2. Describing real world (Not every fact will be binary). / not 100% true etc.

3. Rational behavior without logic e.g. (reflex)

4. Deciding with uncertainty

4) Act Rationally (easier way):

→ Act optimally to action goals  
/ maximize your utility -



What AI system cannot do?

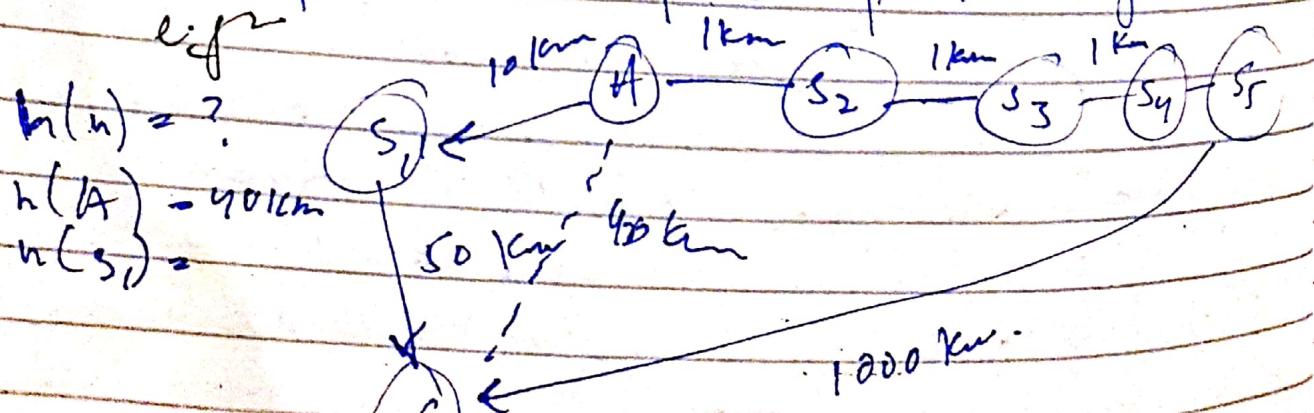
- understanding natural language -
- surfing web.
- comment on arbitrary score.

→ const. laws of a language itself. # of atoms in Universe  $\sim 10^{80}$ .  
Chess Mates =  $10^{120}$   
Go game =  $10^{360}$

- Beating Go game by player.
- Construct plans in dynamic real-time domains.
- Refocus attention in complex environments.
- Perform life-long learning.

// End of chapter.

Heuristics -- give additional info to A\* to speed up the algorithm



## Chapter # 02

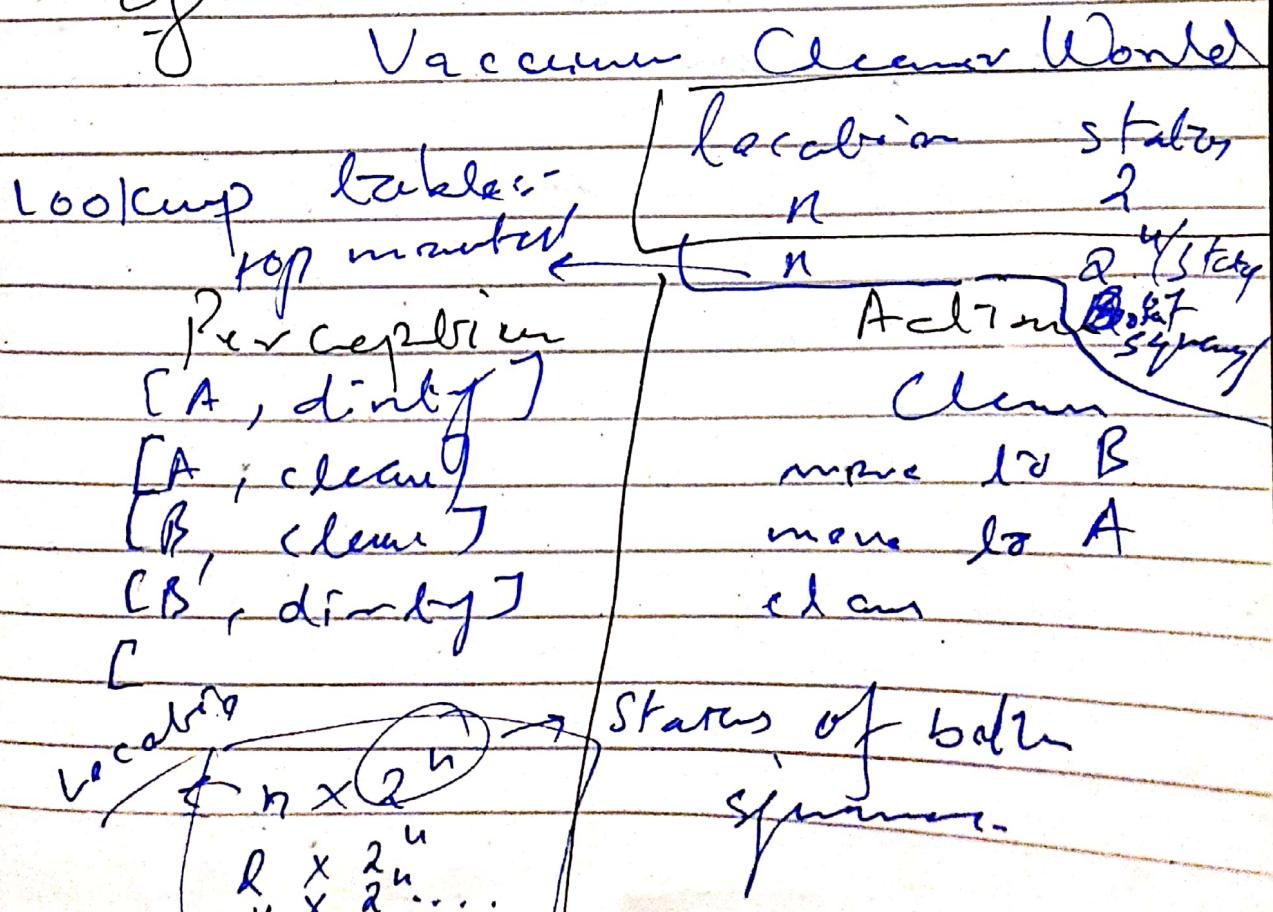
Agent - (Another Def) :-

- ① Sensed in some environment.
- ② Autonomous (sense environment & related to it).
- ③ Flexible
  - a. Reactive (responsive)
  - b. Proactive
  - c. Social

Agent Function -- A Program

→ maps from percept histories into actions.

e.g:-



# Agent Environments

## Rational Agents

### Rationality

- 1 Performance Measure
- 2 Prior knowledge of environment
- 3 Actions that can be performed
- 4 Agent's percept sequence to date

Percept Sequence -- Series of perceptions.

\* To design a rational agent we need to specify its PEAS (Performance measure, Environment, Actions, Sensors).

Rational agent  $\rightarrow$  Selection of action  $\uparrow$  to maximize performance measure for each percept sequence.

# Rationality vs. Omiscience

Omnipotent - All powerful.

→ Perfect agent

Omniscient - (only a concept)

An agent is omniscient if it sees everything.

e.g. knowing all  $^{10^{120}}$  states for chess.

## vs Rationality

e.g.

In cards game, don't know others' cards.

→ Best action in given situation (Not perfect).

## Specifying Task Environment

→ Task environment problems have rational agents as solutions

e.g. = Automated ~~Floor~~ Taxi

↳ must contain PEAS

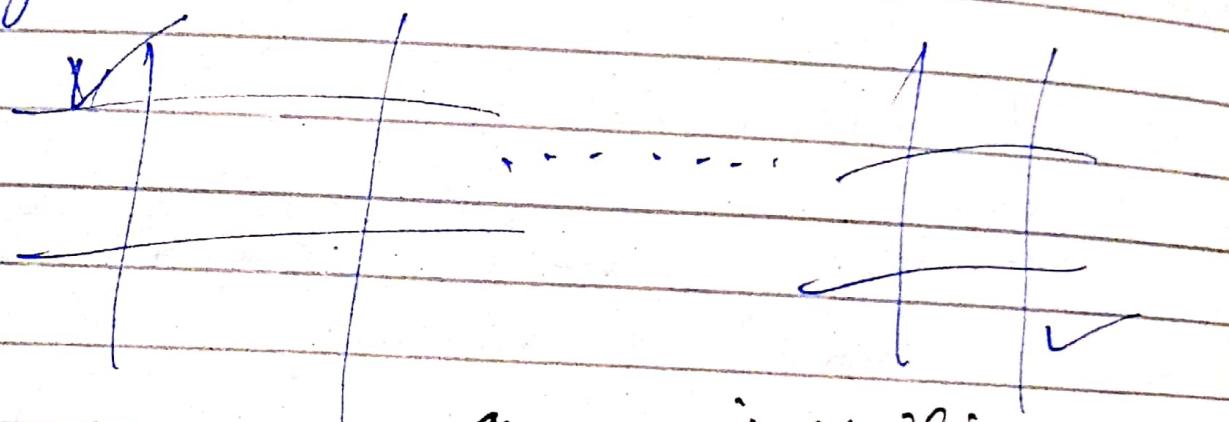
# Rational Tic Tac Toe Agent

e.g.

initial state →

~~a, ——, b~~

Agent 1 (X)



Performance Measures → ~~Planning~~ of possibilities

wining, only legal moves etc

Environment -

→ The environment will be the board / ~~area~~ game play area.

Actuators Hand with a pen.

Sensors: Camera / Angle sensors

State - An abstract representation of the environment by retaining all relevant information.

e.g. In the case of Tic Tac Toe the abstract representation of the initial state can be a  $3 \times 3$  2D Array which is empty.

## Types of Environments -

① Fully observable vs partially observable -

(All state variables)

Fully observable - If an agent's sensor provide all relevant details necessary for taking a rational decision then the environment is fully observable.

② Deterministic vs. stochastic

③ Episodic vs. Sequential

④ Static vs. dynamic

⑤ Discrete vs. continuous

⑥ Single agent vs. multi-agent

⑦ Known vs. unknown

## Stochastic vs Deterministic

↳ you're on a bus stop & the arrival of passengers at the stop is stochastic.  
(Random for you) & it can follow some distribution but it's still random.

↳ the next state of the environment if it can be fully determined by choosing an action - is called deterministic.

↳ when you perform an action in tic-tac-toe you'll know the next state. (deterministic)

## Episodic vs. Sequential

↳ choice of action depends on <sup>only the</sup> current perception only.  
e.g. - spam filter of email.

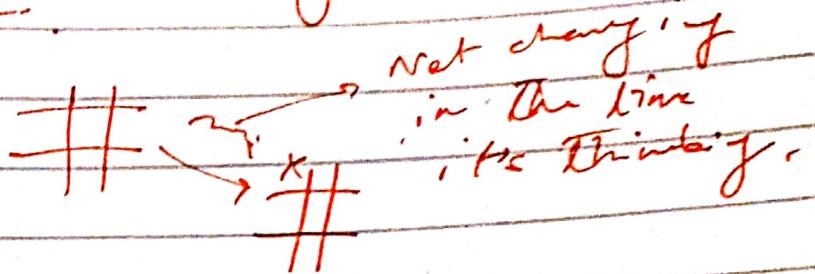
∴ pac man is sequential.

→ Tic-tac-toe is episodic as well as sequential.

## Static vs. Dynamic :-

→ The environment (relevant details) does not change while the agent is thinking to take an action.

e.g.-



→ Opposite of static is dynamic

e.g:-

autonomous cars.

\* → Semi-dynamics → static environment but there is a time factor of blitz chess.

that changes the agent's performance.

## Discrete vs. Continuous --

→ finite values      infinite values

When an agent perceives. The number of possibilities for these scalar variables is finite vs. infinite is continuous.

e.g. environmental values for autonomous cars is infinite so it is continuous.

→ Does the environment provide a fixed number of distinct percepts, actions, and its environment states?

~~no~~ state  
of board  
in chess game

Turn the slicing wheel to  $0.1^\circ, 0.01^\circ, 0.001^\circ$   
continuous

Vacuum cleaner in a confined environment is discrete vs. if it's in an everchanging environment is dynamic continuous.

Single agent vs. Multiagent =

→ An environment in which the agent does not have to interact with other agents

e.g., Parc-picking robot.

Known vs. Unknown =

→ This is more related to the environment rules.

→ The rules of the environment, (the transition model) are known then it's a known environment

e.g., chess, rules of movement  
Ex: Deterministic

unknown e.g. Rovers, humans  
on moon.

## Artificial Intelligence (V-Imp)

→ Machine Learning.

Categories = of algorithms:

- ① Supervised Learning
- ② Unsupervised "
- ③ Reinforcement "

→ Data in this content is also called Examples. features

	$f_1$	$f_2$	$f_3$	$f_n$	Label
Example 1	7ft	Blue	black	-	Not Hafer
Example 2	5.8ft	Brown	Brown	-	Hafer
:	5.7ft	"	"	-	Hafer
Example n					

height → eye colour → complexion etc.

Supervised Learning:-

→ If we have examples + features + labels.

Unsupervised Learning - if Clustering

→ Examples + features.

Reinforcement Learning -

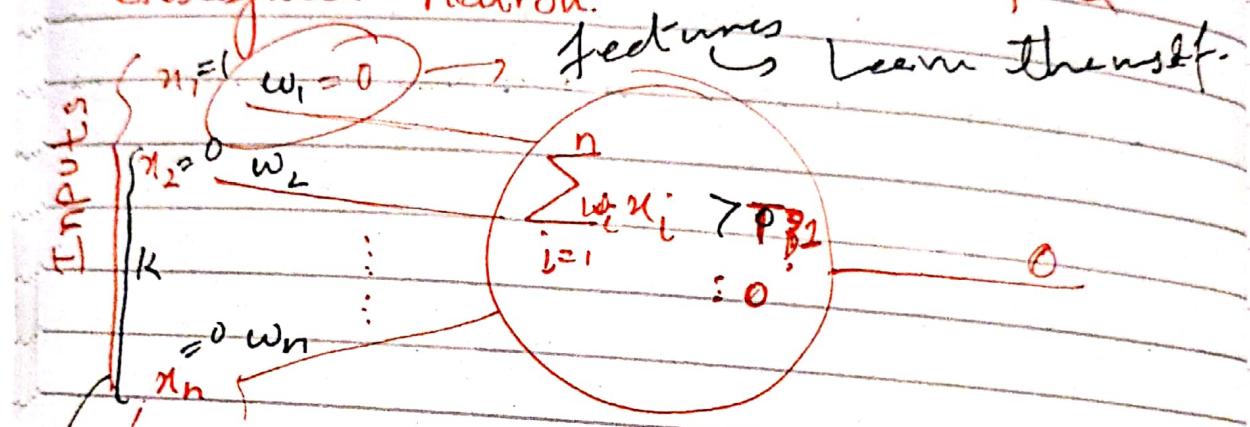
→ Examples + features + feedback / .....

*full� auto* → learn from  
on their own

1) Neural Networks - Type of supervised learning  
(examples, features, labels)

i) Model of a perceptron:-

→ Perceptron is the model of a biological neuron.



→ We can use this to set only the weights of the relevant perceived Inputs/States/Examples/Signals state.

(Depends upon the context).

These can be:-

- ① Binary
- ② Real values
- ③ Vectors

but numerical

values. e.g. A, B, C, d, z.

→ If there are sentences/words  
then those are encoded into numerical values.

$$w_1 x_1 + w_2 x_2 + \dots + w_n x_n > f$$

Variables

constant

0.25  
0.5  
0.75  
0.

→ Let  $T = w_0$

$$-w_0 + w_1x_1 + w_2x_2 + \dots + w_nx_n > 0$$

e.g. if  $w_0 = 7$  & since  $w_0$  is a variable, we can remove the minus sign & replace  $w_0$  with  $-7$ .

$$w_0 = 1$$

$$\Rightarrow w_0 - 1 + w_1x_1 + w_2x_2 + \dots + w_nx_n > 0$$

$$\Rightarrow w_0 \cancel{w_0} + w_1x_1 + w_2x_2 + \dots + w_nx_n > 0$$

→ Bias Input:

$$x_0 = 1 \quad (\text{Bias Input})$$

Binary classification

$$w_0 = 4$$

$$x_1 = 1 \quad w_1 = 1$$

$$x_2 = 1 \quad w_2 = 1$$

$$x_3 = 0 \quad w_3 = 1$$

$$x_4 = 1 \quad w_4 = 1$$

$$x_5 = 1 \quad w_5 = 1$$

$$\sum_{i=0}^5 w_i x_i > 0 ?$$

Example 1

1
1
1
1

Complete white line

Dataset  
Example 2

1
1
0

partial

white line

1
1
0
0

Correct result with this weight vector

feature for  $x_0$

1	4	1	1	1	1	1
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# Perception Learning Algorithm

AND Function

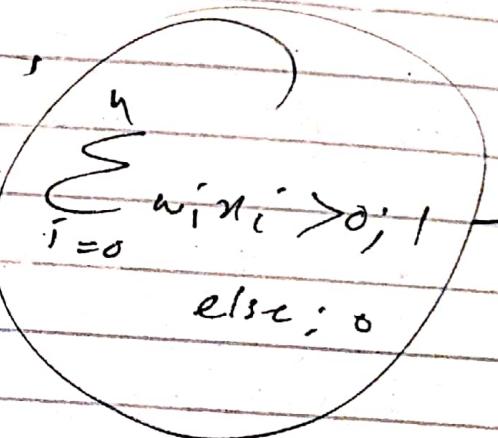
dataset:

$$x_0 = 1 \quad w_0 =$$

$$x_1 = \quad w_1 =$$

$$x_2 = \quad w_2 =$$

	$x_1$	$x_2$	$t$
E1	0	0	0
E2	0	1	0
E3	1	0	0
E4	1	1	1



$$w = [-1, 1, 1]$$

$$\begin{aligned} -1 & 0 1 = 0 \\ -1 & 0 0 = -1 \\ -1 & 1 0 = 0 \\ -1 & 1 1 = 1 \end{aligned}$$

→ In order to generate weight vector automatically, we can use the algorithm.

Steps ..

- ① Initialize all weights to random values (Real & Numerical value).
- ② Until all outputs of all training examples are correct.  
G while ( $\text{Error } != 0$ )

$$\text{Error} = \sum_{d \in D} |t_d - o_d| \quad \xrightarrow{\text{absolute error}}$$

$$(\quad)^2 \rightarrow \text{square error}$$

$$v_0 = 0, w_1 = 0.1, w_2 = 0.2$$

while ( $\text{Error} \neq 0$ ) {

$$\Delta w_0 = 0 \quad \Delta w_1 = 0 \quad \Delta w_2 = 0$$

For Example 1:-

$\Rightarrow$  weight change new  $w_1, w_2 / \theta | e$

$$\Delta w_i = w_i + \eta(t-o)x_i \quad | \quad \begin{matrix} \theta \\ 0 \\ 0 \end{matrix} \quad | \quad \begin{matrix} 0 \\ 0 \\ 0 \end{matrix}$$

Usually  $\eta$  learning rate (controls the pace of learning)

$$\Delta w_0 = 0 + 0.1(0-0)1 = 0$$

$\hookrightarrow$  weight change of  $w_0 = 0$

$$\Delta w_1 = 0 + 0.1(0-0)0 = 0$$

$$\Delta w_2 = 0 + 0.1(0-0)0 = 0$$

For Example 2:-

$$\Delta w_0 = 0 + 0.1(0-1)1 = -0.1$$

$$\Delta w_1 = 0 + 0.1(0-1)0 = 0$$

$$\Delta w_2 = 0 + 0.1(0-1)1 = -0.1$$

For Example 3:

$$\Delta w_0 = -0.1 + 0.1(0-1) \rightarrow -0.2$$

$$\Delta w_1 = 0 + 0.1(0-1) \rightarrow -0.1$$

$$\Delta w_2 = -0.1 + 0.1(0-1) \rightarrow -0.1$$

For Example 4: No change if input is 0.

$$\Delta w_0 = -0.2 + 0.1(0-1) \rightarrow -0.2$$

$$\Delta w_1 = -0.1$$

$$\Delta w_2 = -0.1$$

→ No change cuz  $t-0=0$

$t = 0$  out.

$$w_i = w_i^* + \Delta w_i$$

$$w_0 = 0 + (-0.2)$$

$$w_0 = -0.2$$

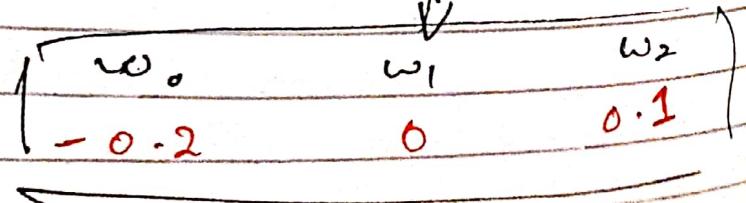
$$w_1 = 0.1 + (-0.1)$$

$$w_1 = 0$$

$$w_2 = 0.2 + (-0.1)$$

$$w_2 = 0.1$$

weights  
Vi, Vj, Vk



$$\begin{array}{r}
 -0.2 + 1 = 0.8 \\
 -0.2 - 0.2 = -0.4 \\
 -0.2 + 0.1 = -0.1
 \end{array}$$

$x_1$	$x_2$	$t$	$o$	
0	0	0	0	✓
0	1	0	0	✓
1	0	0	0	✓
1	1	0	1	X

Error = 25%

One iteration = epoch.

→ Every iteration will reduce the error. Still not converged. But it's going towards convergence.

→ All examples 1-3 will be 0. ( $T=0$ )

Example 4:

$$\Delta w_0 = 0 + 0.1(1-0) = 0.1$$

$$\Delta w_1 = 0 + 0.1(1-0) = 0.1$$

$$\Delta w_2 = 0 + 0.1(1-0) = 0.1$$

$x_1$	$x_2$	$t$	$w_0 = 0.1$	$w_1 = 0.1$	$w_2 = 0.2$	$-0.1 = -0.1$
0	0	0	0	0	0	$-0.1 + 0.2 = 0.1$
0	1	0	0	0	0	$-0.1 + 0.1 = 0$
1	0	0	0	0	0	$-0.1 + 0.2 = 0.1$
1	1	0	0	0	0.2	

Error = 25%

$$w_0 = -0.1 \quad w_1 = 0.1 \quad w_2 = 0.2$$

E2:

$$\Delta w_0 = 0 + 0.1(0-1)|_1 = -0.1$$

$$\Delta w_1 = 0 + 0.1(0-1)|_0 = 0$$

$$\Delta w_2 = 0 + 0.1(0-1)|_1 = -0.1$$

$$w_0 = -0.1 + (-0.1) = -0.2$$

$$w_1 = 0.1 + 0 = 0$$

$$w_2 = 0.2 + (-0.1) = 0.1$$

$$\frac{-0.2}{-0.2+0.1} = 0.1$$

$x_1$	$x_2$	$y$	$\hat{y}$
0	0	0	0
0	1	0	0 ✓
1	0	0	0 ✓
1	1	0	0 ✓

4th Epoch

~~bad~~ ~~good~~ Error = 25%

E4:-

$$\Delta w_0 = 0 + 0.1(1-0)|_1 = 0.1$$

$$\Delta w_1 = 0 + 0.1(2-0)|_1 = 0.1$$

$$\Delta w_2 = 0 + 0.1(1-0)|_1 = 0.1$$

$w_0 = -0.1$	$x_1$	$x_2$	$y$	$\hat{y}$
$w_1 = 0.2$	0	0	0	0
$w_2 = 0.2$	0	1	0	1 X
	1	0	0	1 X
	1	1	1	1 X

Error = 50%

5<sup>th</sup> Epoch -

$\Delta w_0 :$   
⋮

← → Delta Rule / Gradient Descent Rule

$$\rightarrow \text{Error} = \sum_{d \in D} |t_d - o_d| \quad \begin{matrix} \hookrightarrow \text{1st order derivative} \\ \hookrightarrow \text{absolute error} \end{matrix}$$

Sometimes absolute does not capture the variation.

$$\hookrightarrow \text{for the variation} \rightarrow = \sum_{d \in D} |t_d - o_d|^2 \quad \begin{matrix} \text{2} \\ \hookrightarrow \text{to capture variation} \end{matrix}$$

$$\rightarrow \text{Mean squared error} \quad \begin{matrix} \hookrightarrow \frac{1}{N} \sum_{d \in D} |t_d - o_d|^2 \end{matrix}$$

→ Half squared error (Mathematical convenience)

$$\hookrightarrow = \frac{1}{2} \sum_{d \in D} |t_d - o_d|^2.$$

$$\Rightarrow \boxed{\text{O}_d} = \sum_{i=0}^n w_i x_i = w_0 n_0 + w_1 n_1 + \dots + w_n n_n$$

\* → To compute change in  $w_i$ ,

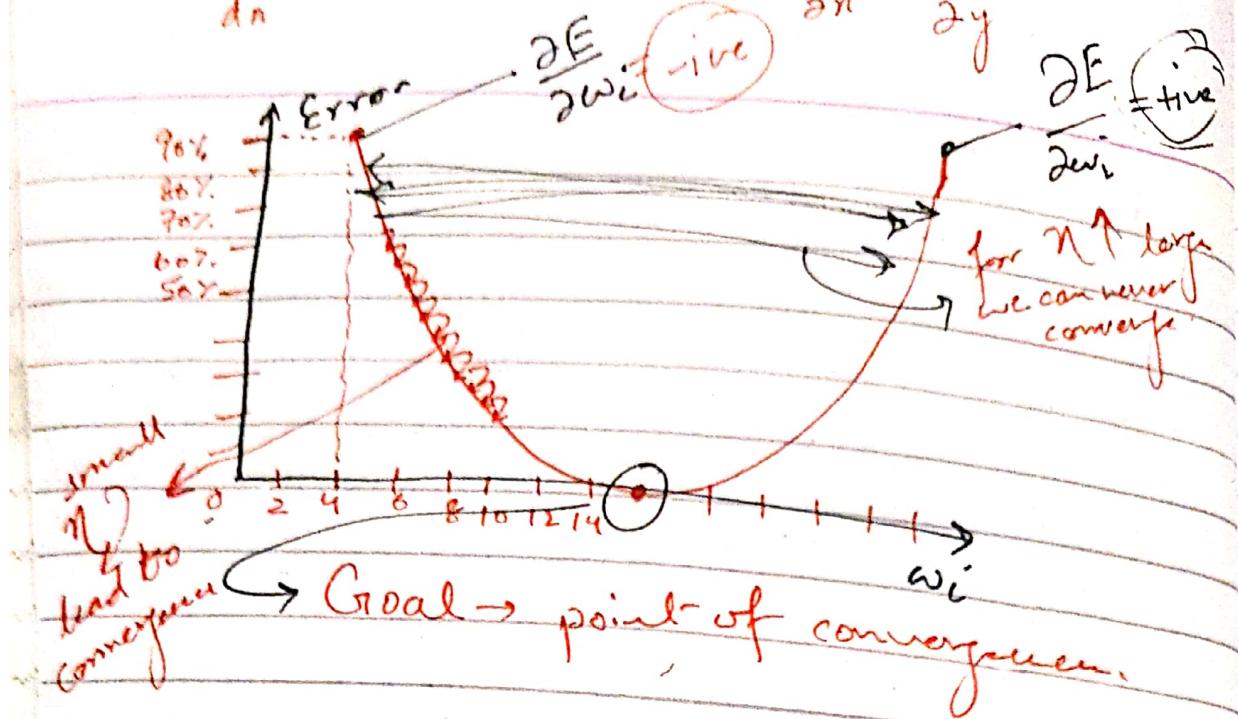
$$\Delta w_i = -\eta \cdot \frac{\partial E}{\partial w_i} \quad \begin{matrix} \text{slope of error} \end{matrix}$$

$$y = x^2 + 2x + 3$$

$$\frac{dy}{dx}$$

$$z = xy^2 + 2x^2 + y$$

$$z' = \frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} + y$$



$w$

$\rightarrow$  Independent  $\downarrow$  = Dependant inc.  $E$  slope

$\rightarrow$  Independent  $\downarrow$  = Dependant time.

$\Delta w_i = -\eta \cdot \frac{\partial E}{\partial w_i}$  Gradient

Hyper parameter  $\eta$  (learning rate)

So if slope is negative then  $w_i$  should increase.

$\rightarrow$  Keep  $\eta$  small, so that movement is small.

Hyper-parameter :-

① Hit & try

② Validation dataset

Using the data-set, we will get the  $\eta$ .

(open research issue)

Play error derivation -

~~Δw<sub>i</sub>~~

$$\frac{\partial E}{\partial w_i} = \frac{1}{2} \sum_{d \in D} |t_d - o_d|^2$$

⇒ Since  $o_d$  is fn of  $w_i$

$$\frac{\partial E}{\partial w_i} = \frac{1}{2} \sum_{d \in D} |t_d - o_d|^{2-1} \cdot \frac{\partial}{\partial w_i} |t_d - o_d|$$
$$\Rightarrow \sum_{d \in D} |t_d - o_d| \cdot [o - (x_i)] = o + o(x_i)$$

$$\frac{\partial E}{\partial w_i} = \sum_{d \in D} (t_d - o_d)(-x_i)$$

$$\Delta w_i = -\eta \sum_{d \in D} (t_d - o_d)(-x_i)$$

$$\Delta w_i = \eta \sum_{d \in D} (t_d - o_d)(x_i)$$

$$\Delta w_i = \Delta w_i' + \eta (t_d - o_d) x_i'$$

came from here

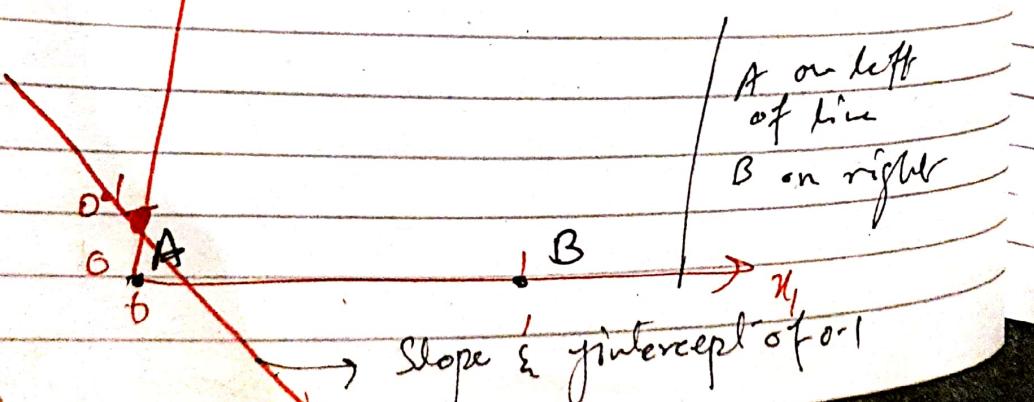
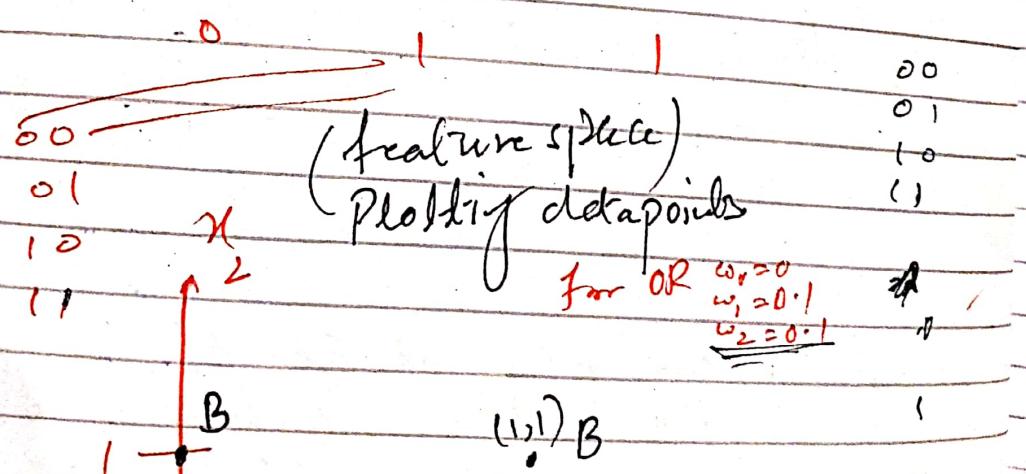
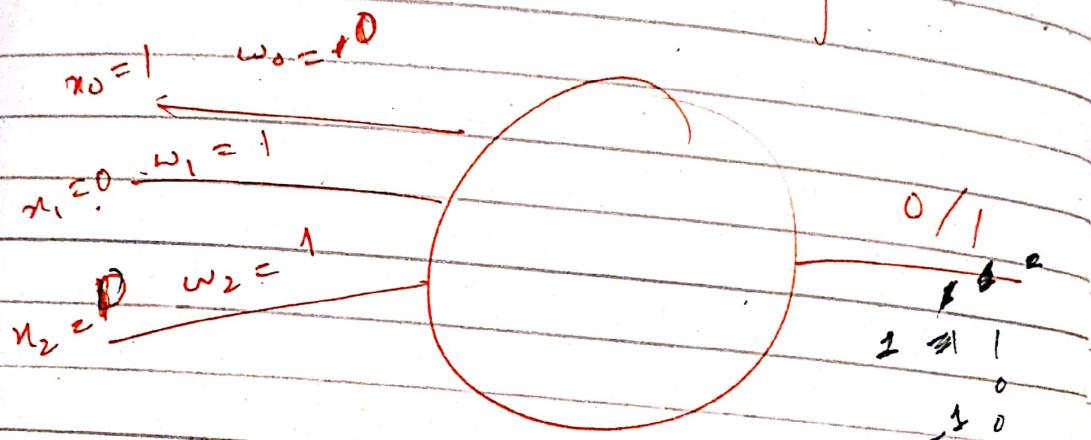
(Raw data features)

→ why Neural Networks:-

① Linearly separable data

Example:-

	$x_1$	$x_2$	$J$	Label
E <sub>1</sub>	0	0	0	A
E <sub>2</sub>	0	1	1	B
E <sub>3</sub>	1	0	1	B
E <sub>4</sub>	1	1	0	A



XOR

↳ XOR

Equation of line  $\rightarrow y = ax + b$

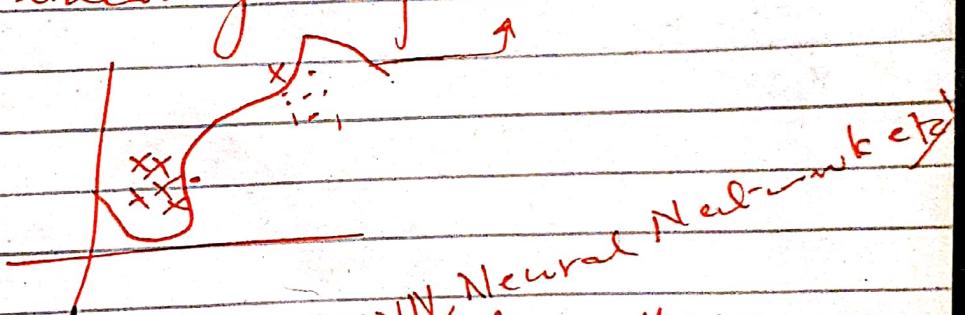
$$y = ax + b$$

slope  $a$

intercept  $b$

→ If you can separate the data points using line then the data is called linearly separable data. (2 classes of data).

Non linearly separable data



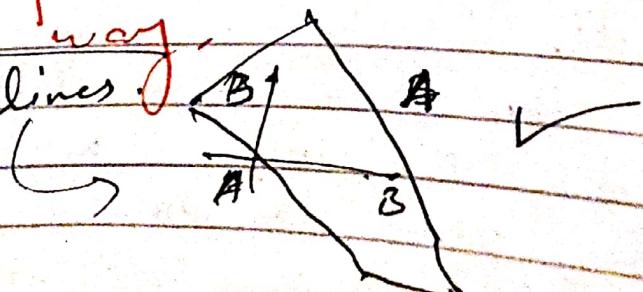
\* classifier:- (KNN, Neural Network)

→ A classifier is a function that partitions the feature space into disjoint categories.

vs. Cluster (Prediction labels not given)

→ XOR is not linearly separable. Hence, we cannot solve this problem using line function. We need some other way.

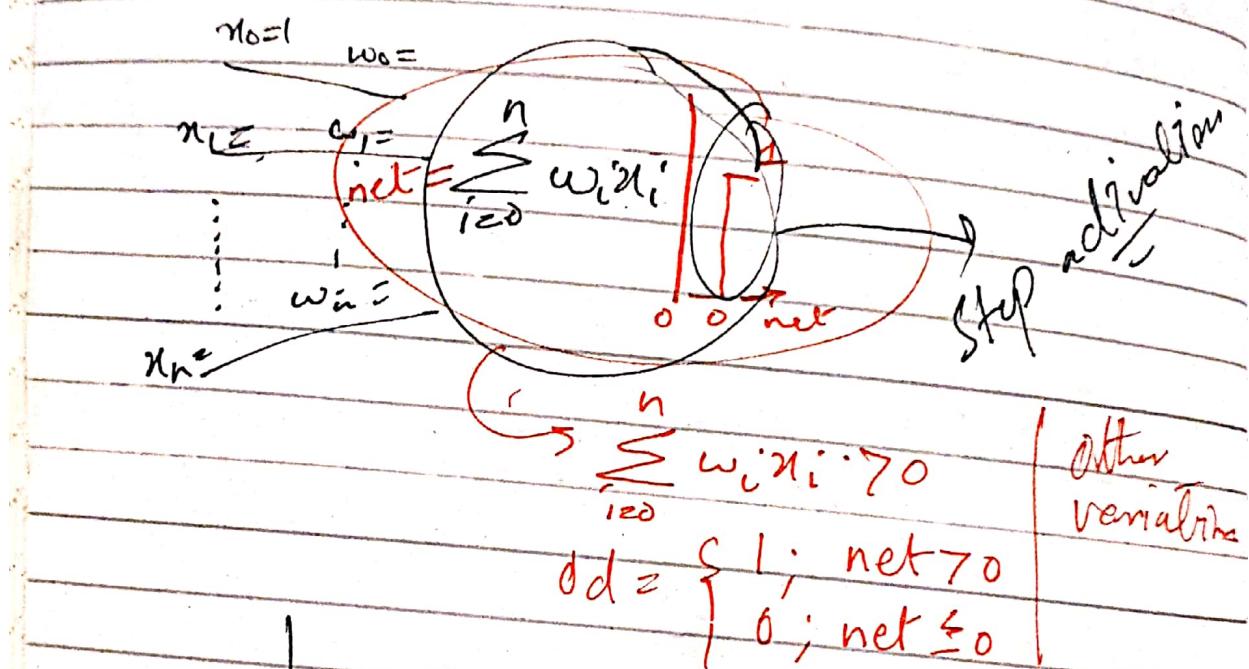
① Multiple lines



# Machine Learning

→ Non-linear activation functions

- ① Sigmoid function
- ② Tangent Hyperbolic function
- ③ ReLU function
- ④ Leaky ReLU func
- ⋮      ⋮



\* → Use multiple lines for non-linearly separable data. But you can have more freedom in the data space use a function that has curves (non-linearly activated) such as sigmoid.

multiple perceptrons learn an AND data because linearly separable

perceptron can learn an OR data

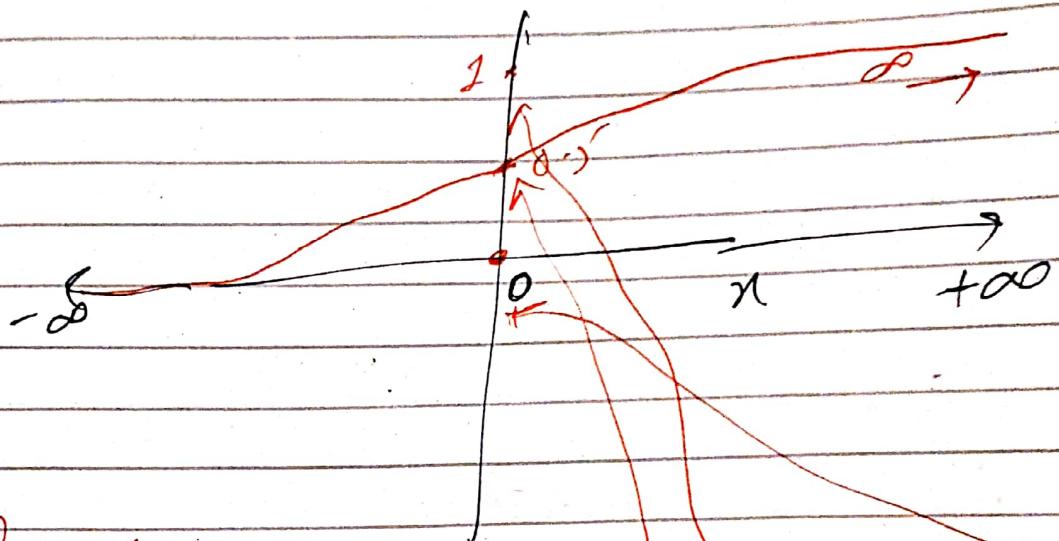
(curve) to sigmoid

① Sigmoid fn:-

$$f(x) = \frac{1}{1 + e^{-x}}$$

$$y = \frac{1}{1 + e^{-x}}$$

$$y = \frac{1}{1 + e^{-x}}$$



Put  $x = \infty$ :

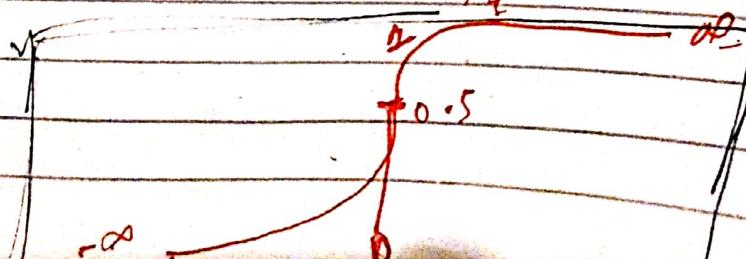
$$y = \frac{1}{1 + e^{-\infty}} = \frac{1}{1 + 0} = \frac{1}{1} = 1 \quad (0)$$

Put  $x = 0$ :

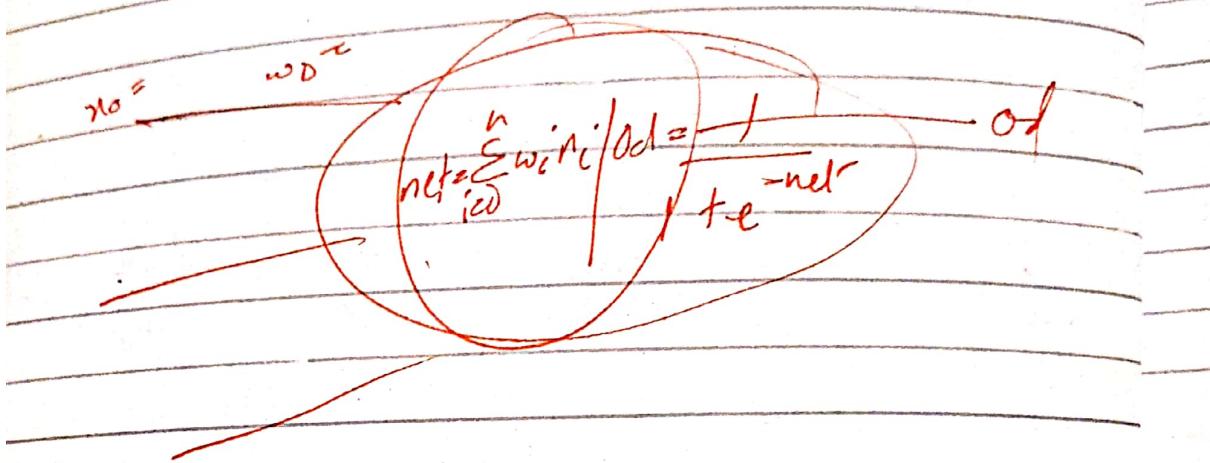
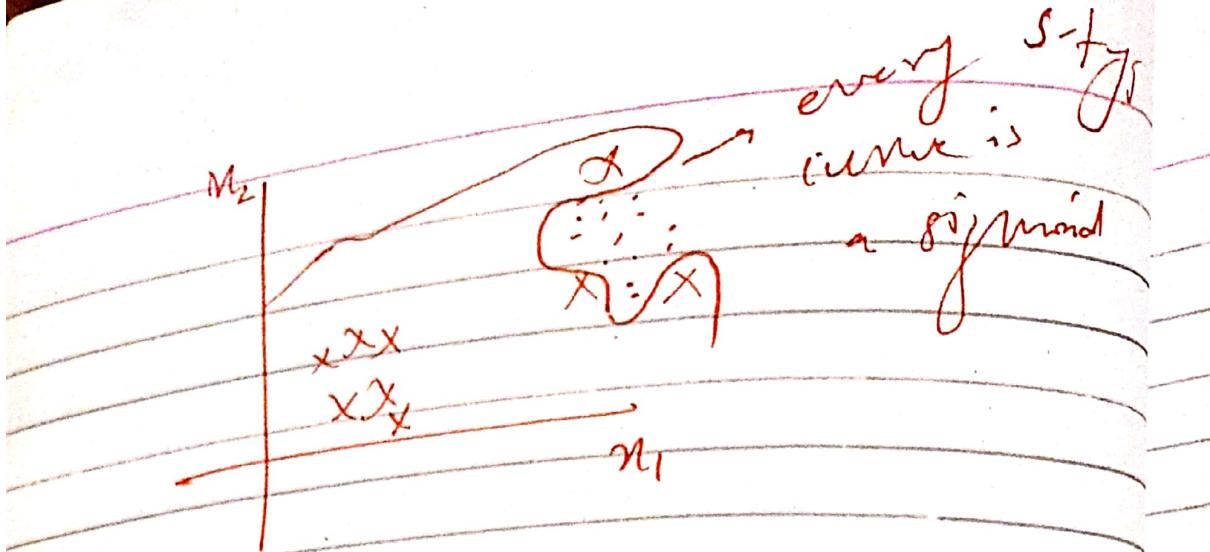
$$y = \frac{1}{1 + 1} = \frac{1}{2} = 0.5 \quad (0.5)$$

Put  $x = -\infty$ :

$$y = \frac{1}{1 + e^{-\infty}} = \frac{1}{1 + 0} = \frac{1}{1} = 0 \quad (0)$$



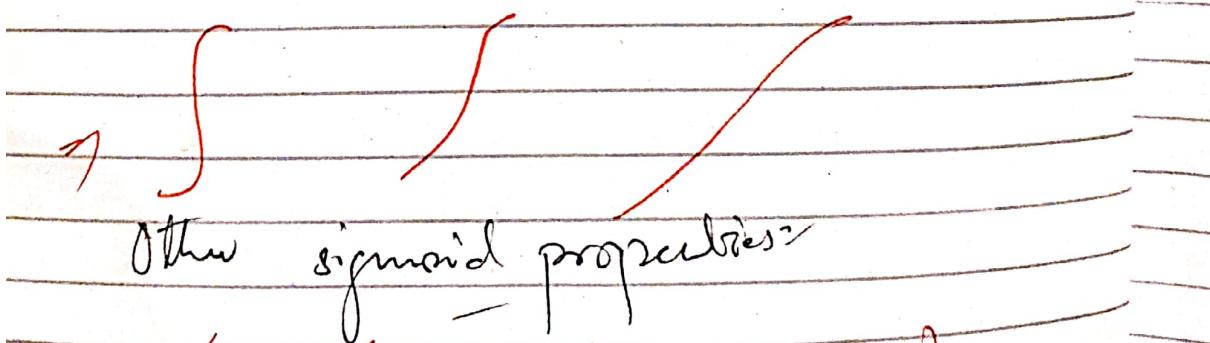
So even if  
So type and  
like be a sig



for more control:

$$f = \frac{1}{1 + e^{-kx}}$$

controls  
skewness



$$1. f' = f(1-f) \text{ (very simple)}$$

$$f'(x) = \frac{0 - (0 - e^{-x})}{(1 + e^{-x})^2}$$

$$= \frac{e^{-x}}{(1 + e^{-x})^2} \Rightarrow \frac{1}{(1 + e^{-x})} \cdot \frac{e^{-x}}{(1 + e^{-x})}$$

$$\Rightarrow \frac{1}{(1+e^{-x})} \cdot \frac{e^{-x} + 1 - 1}{(1+e^{-x})}$$

$$\Rightarrow f\left(\frac{1-1}{1+e^{-x}}\right) = f\left(\frac{1-j}{1+e^{-x}}\right) //$$

→ This will help in  $\Delta w_i = \eta \cdot \frac{\partial E}{\partial w_i}$

Training Rule equation using Sigmoid function:-

$$\Delta w_i = -\eta \cdot \frac{\partial E}{\partial w_i}$$

$$\text{Let } E = \frac{1}{2} \sum_{d \in D} (t_d - o_d)^2$$

$$\frac{\partial E}{\partial w_i} = \frac{1}{2} \cdot \frac{\partial}{\partial w_i} \sum_{d \in D} (t_d - o_d)^2$$

$$= \frac{1}{2} \cdot \frac{\partial}{\partial w_i} \sum_{d \in D} (t_d - o_d) \cdot \frac{\partial}{\partial w_i} (t_d - o_d)$$

$$= \sum_{d \in D} (t_d - o_d) \cdot \frac{\partial}{\partial w_i} (t_d - o_d)(1 - o_d)$$

Since the was <sup>wrt</sup>  
derivative was <sup>wrt</sup>  
wrt <sup>wrt</sup>  $w_i$  but  
was <sup>wrt</sup>  $w_i$   
Now  $\frac{\partial}{\partial w_i}$  this card has  
 $\frac{\partial}{\partial w_i}$  more values.

$$\nabla \sum_{d \in D} (t_d - o_d) \cdot -o_d(1-o_d) \cdot (x_i)$$

$$\frac{\partial E}{\partial w_i} = \sum_{d \in D} (t_d - o_d) \cdot o_d(1-o_d) u_i$$

? slope for sigmoid.

Putting:-

$$\Delta w_i = -\eta \cdot \sum_{d \in D} (t_d - o_d) o_d(1-o_d) u_i$$

G weight change calculation  
method for sigmoid fn

$$\text{Backward equation, } \Delta w_i = -\eta \cdot \frac{\partial E}{\partial w_i}$$

just put in the activation  
fn. you need the equation for.  
Also for different types of fn.

(S-II)

Non-linear  
training data

$n_1$	$x_2$	$j(\text{XOR})$
0	0	0
0	1	1
1	0	1
1	1	0

$$n_1 \oplus x_2 = (n_1, \sqrt{x_2}) \wedge \sim(n_1 \wedge n_2)$$

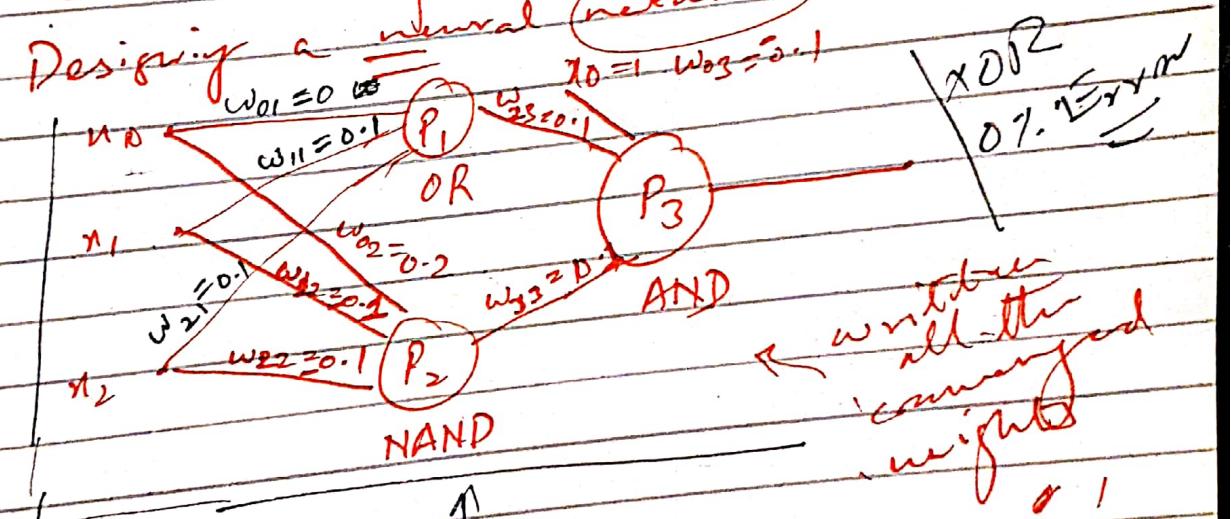
we know  $P_1$

that this is linearly  
separable so we  
can use perceptron 1.

some  
with  
this

by now

Designing a neural network  $\Rightarrow$  linear



width = OR

width = AND

NAND

$$w_0 = 0.2$$

$$w_1 = -0.1$$

$$w_2 = -0.1$$

for this propagation  
back algorithm

$$0 \times 0.1$$

$$1 \times -0.1 + -0.1 - 0.1 = -0.3$$

$$1 \times -0.1 - 0.2 + 0.1 = -0.2$$

$$0 \times 1 = 0.1 = 0$$

for this calculate  $\Delta E$   
width  $(\Delta w_{ij}) = \eta \cdot \Delta E \cdot u_j$