Euclid's Elements

Book I

If Euclid did not kindle your youthful enthusiasm, you were not born to be a scientific thinker.

Albert Einstein

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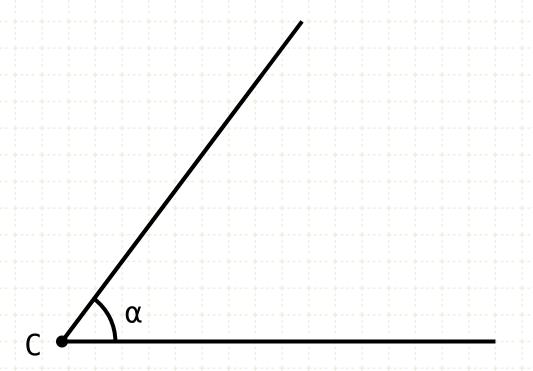


Proposition 23 of Book I

To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



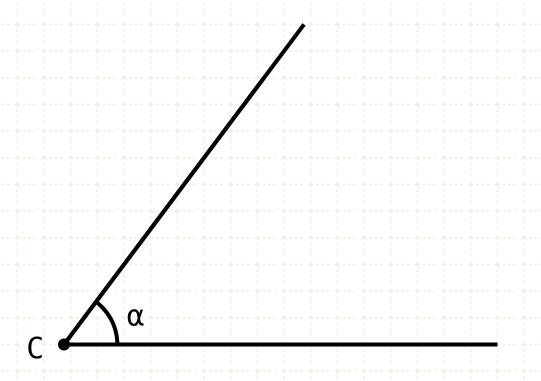
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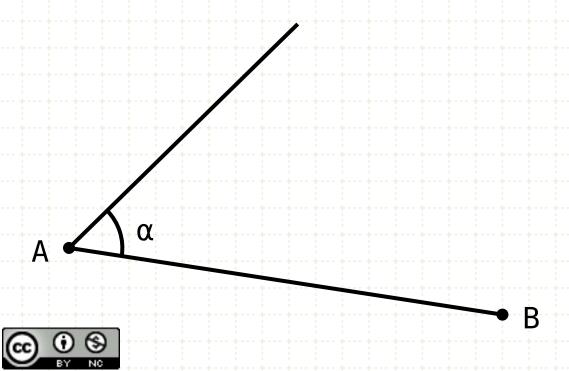


In other words

Given an angle and a line AB

To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



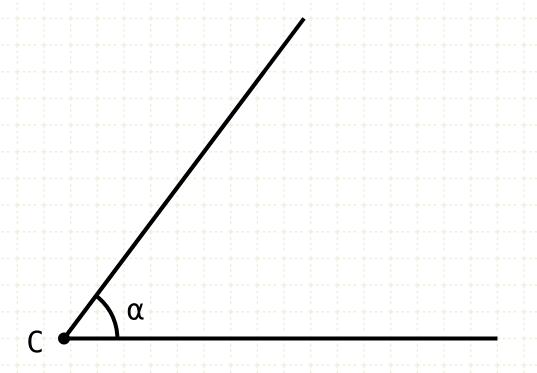


In other words

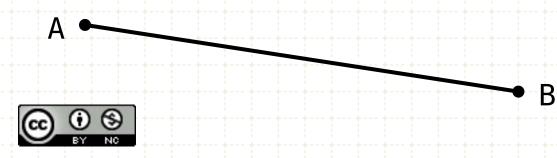
Given an angle and a line AB

Draw a new line on point A such that it forms an angle equivalent to the original

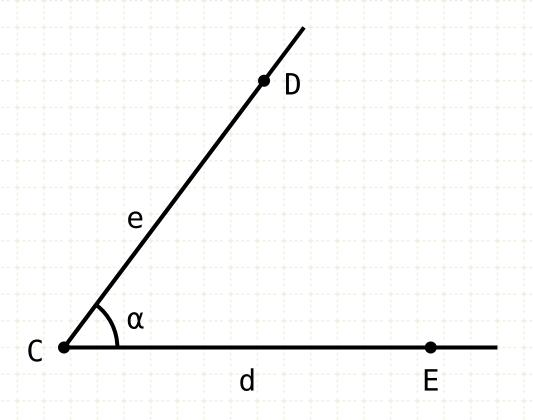
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Construction

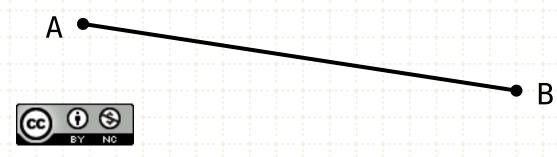


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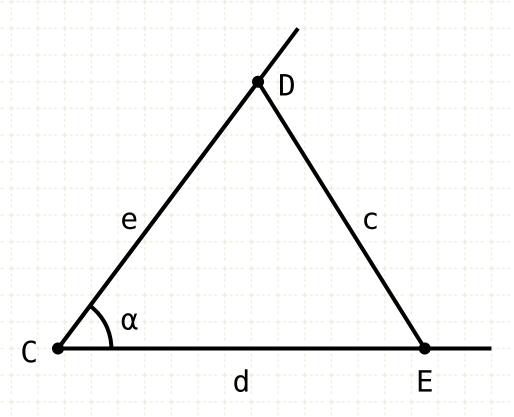


Construction

Define points D and E at random on the two lines defining the angle



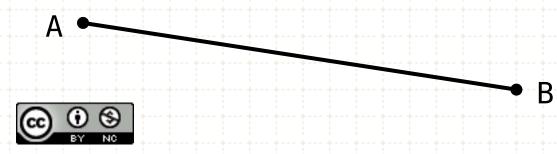
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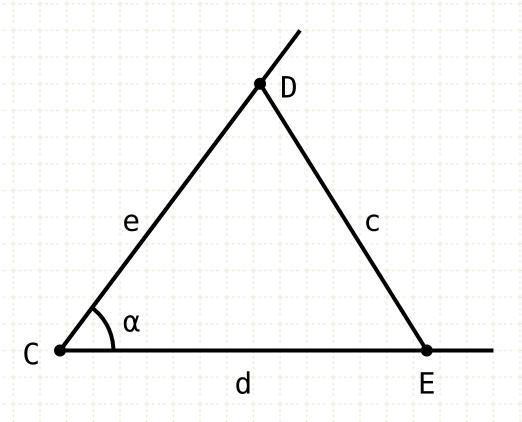
Construction

Define points D and E at random on the two lines defining the angle

Construct triangle DCE by constructing the line DE



To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



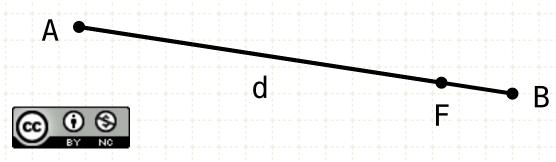
$$AF = CE$$

Construction

Define points D and E at random on the two lines defining the angle

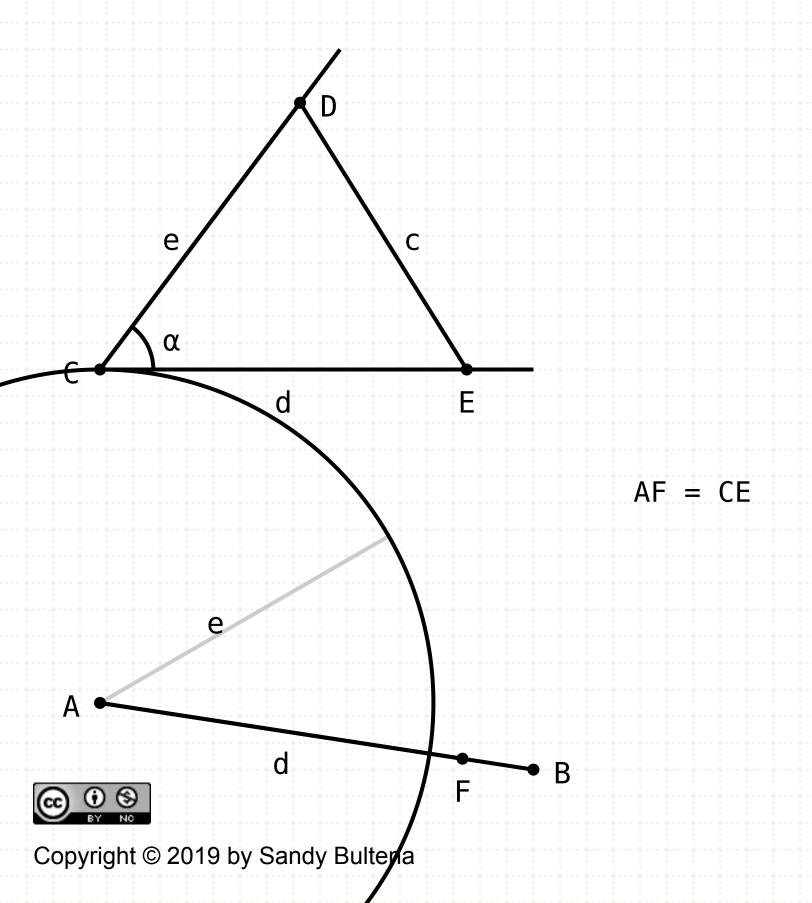
Construct triangle DCE by constructing the line DE
Copy this triangle onto line segment AB, using the methods described in I-22

- Copy length CE to AF (I·2)



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To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



Construction

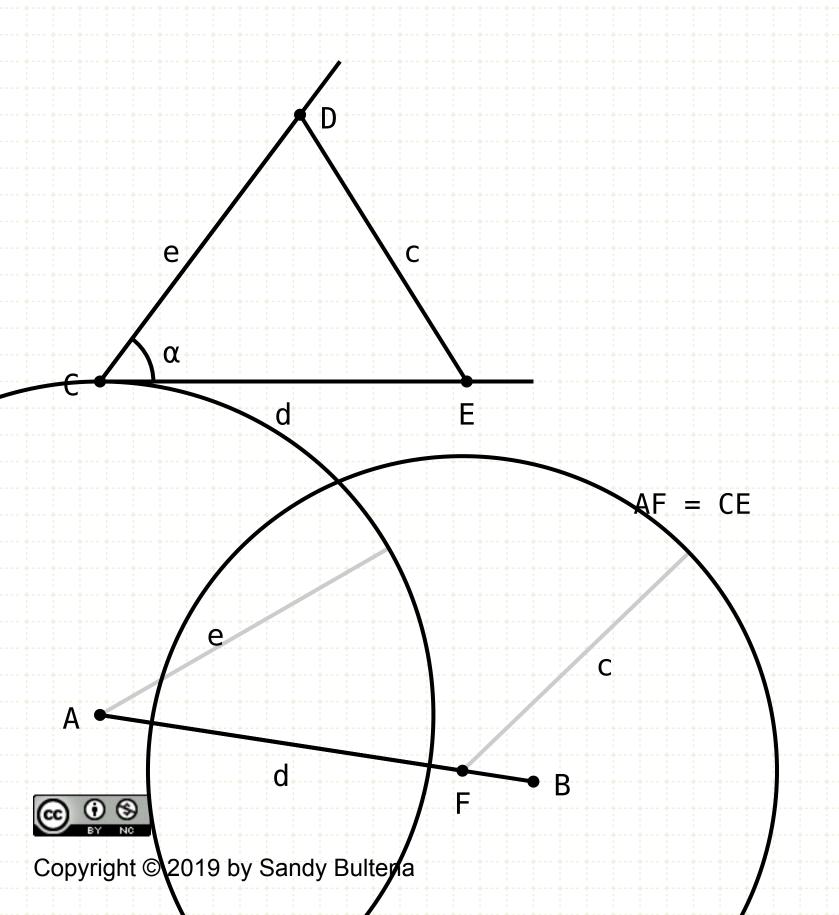
Define points D and E at random on the two lines defining the angle

Construct triangle DCE by constructing the line DE

Copy this triangle onto line segment AB, using the methods described in I-22

- Copy length CE to AF (I·2)
- Copy length CD, start at point A (I·2), and then construct a circle with radius CD

To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



Construction

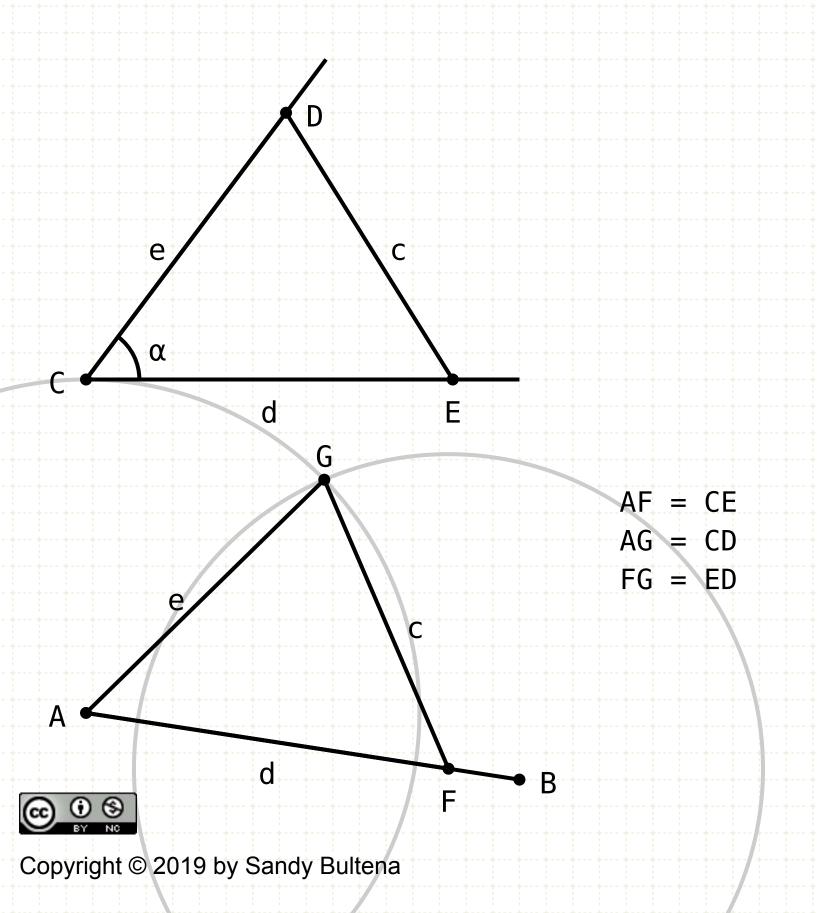
Define points D and E at random on the two lines defining the angle

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- Copy length CE to AF (I·2)
- Copy length CD, start at point A (I·2), and then construct a circle with radius CD
- Copy length DE, start at point F (I·2), and then construct a circle with radius DE

To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



Construction

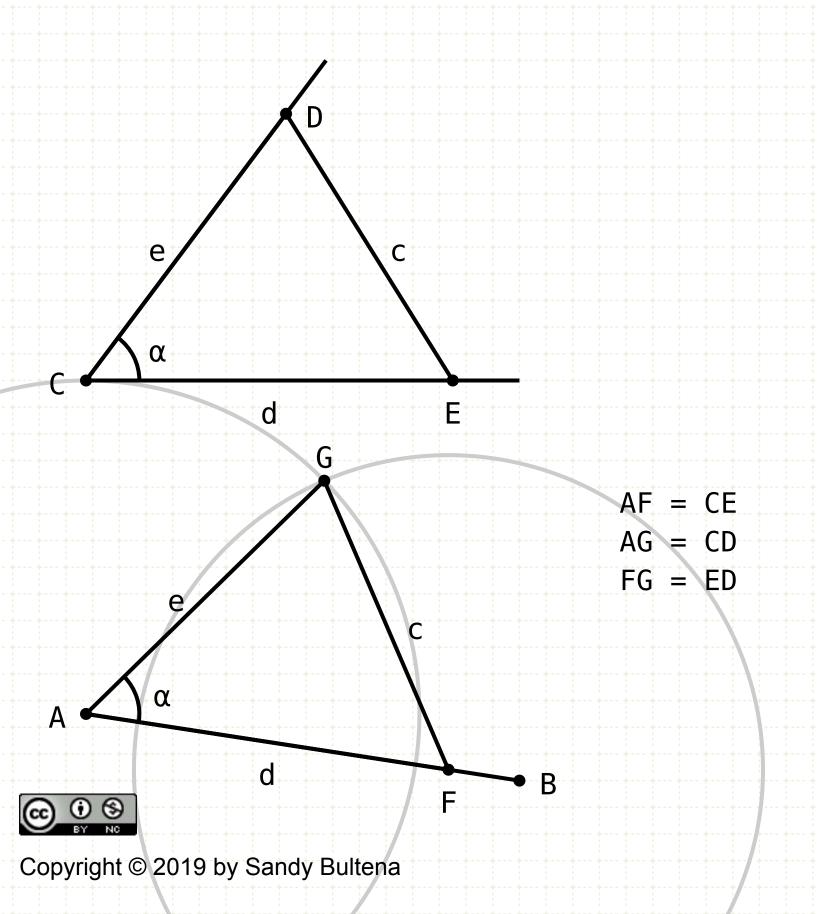
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- Copy length CE to AF (I-2)
- Copy length CD, start at point A (I·2), and then construct a circle with radius CD
- Copy length DE, start at point F (I·2), and then construct a circle with radius DE
- Construct triangle AFG, where G is the intersection of the two circles

To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



Construction

Define points D and E at random on the two lines defining the angle

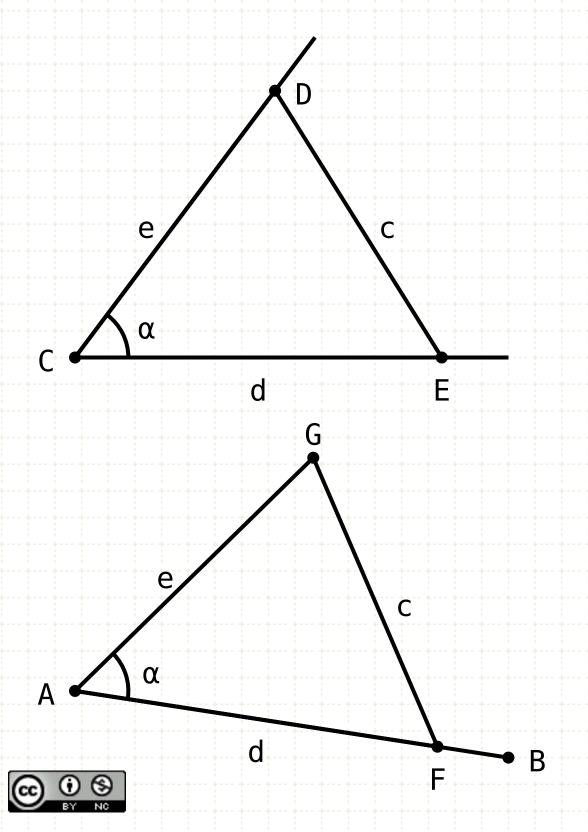
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Angle GAF is equal to DCE

To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



AF = CE AG = CD FG = ED

Construction

Define points D and E at random on the two lines defining the angle

Construct triangle DCE by constructing the line DE

Copy this triangle onto line segment AB, using the methods described in I-22

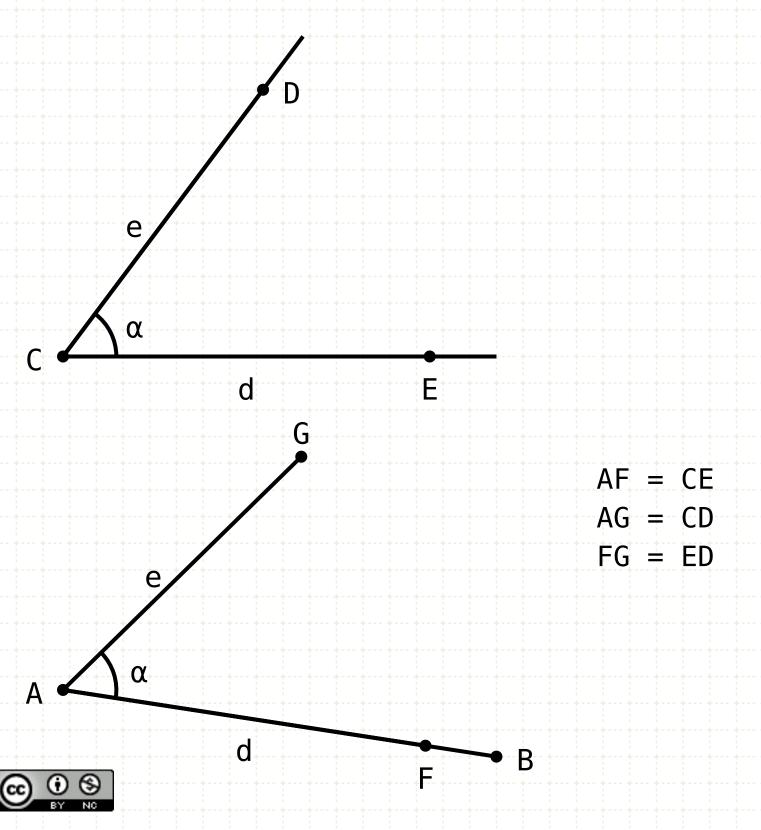
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Angle GAF is equal to DCE

Proof

Two triangles where all three sides are equivalent, have equivalent angles (I-8)

To construct a rectilinear angle equal to a given rectilinear angle on a given straight line and at a point on it.



Construction

Define points D and E at random on the two lines defining the angle

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