Euclid's Elements

Book I

If Euclid did not kindle your youthful enthusiasm, you were not born to be a scientific thinker.

Albert Einstein

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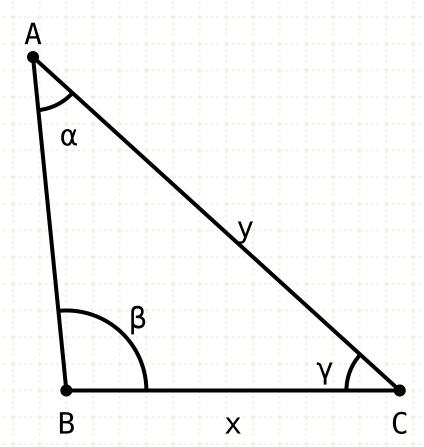
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Proposition 18 of Book I A greater side of a triangle is opposite a greater angle.



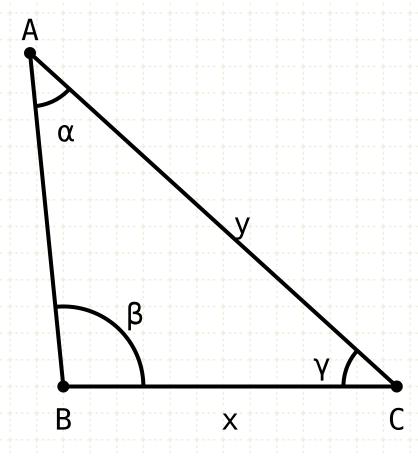
A greater side of a triangle is opposite a greater angle.



In other words

Given a triangle ABC

A greater side of a triangle is opposite a greater angle.

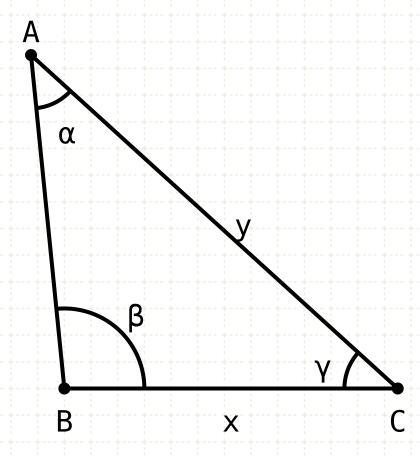


Given a triangle ABC

If line AC is greater than BC, then angle ABC is greater than BAC

$$y > x \Rightarrow \beta > \alpha$$

A greater side of a triangle is opposite a greater angle.



In other words

Given a triangle ABC

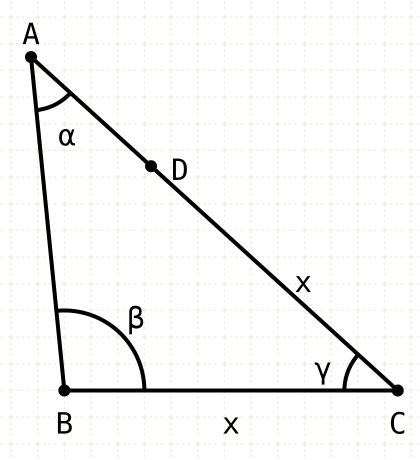
If line AC is greater than BC, then angle ABC is greater than BAC

Proof

AC > BC



A greater side of a triangle is opposite a greater angle.



Given a triangle ABC

If line AC is greater than BC, then angle ABC is greater than BAC

Proof

Create point D on line AC, such that CD equals BC

$$AC > BC$$
 $DC = BC$

A greater side of a triangle is opposite a greater angle.

In other words

Given a triangle ABC

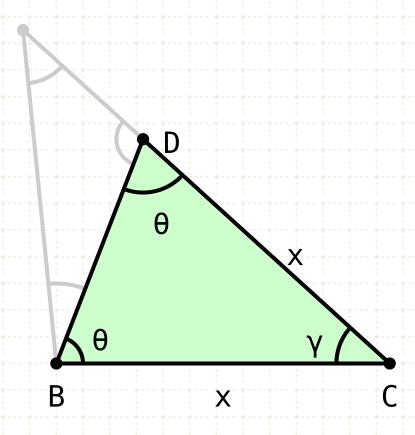
If line AC is greater than BC, then angle ABC is greater than BAC

Proof

Create point D on line AC, such that CD equals BC Create line BD

The angle CDB is an exterior angle to triangle ADB, thus angle CDB is greater than angle DAB (I-16)

A greater side of a triangle is opposite a greater angle.



$$AC > BC$$
 $DC = BC$
 $\theta > \alpha$

In other words

Given a triangle ABC

If line AC is greater than BC, then angle ABC is greater than BAC

Proof

Create point D on line AC, such that CD equals BC Create line BD

The angle CDB is an exterior angle to triangle ADB, thus angle CDB is greater than angle DAB (I·16)

The triangle BCD is an isosceles triangle, thus angles CDB and DBC are equal (I·5)

A greater side of a triangle is opposite a greater angle.

AC > BC
DC = BC

$$\theta > \alpha$$

 $\beta > \theta > \alpha$

In other words

Given a triangle ABC

If line AC is greater than BC, then angle ABC is greater than BAC

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Angle ABC is greater than angle DBC, so angle ABC is greater than angle BAC

A greater side of a triangle is opposite a greater angle.

In other words

Given a triangle ABC

If line AC is greater than BC, then angle ABC is greater than BAC

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Angle ABC is greater than angle DBC, so angle ABC is greater than angle BAC

 $\theta > \alpha$

 $\beta > \theta > \alpha$

∠ABC > ∠BAC

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