Euclid's Elements

Book I

If Euclid did not kindle your youthful enthusiasm, you were not born to be a scientific thinker.

Albert Einstein

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Proposition 1 of Book I To construct an equilateral triangle on a given finite straight line.



Proposition 1 of Book I To construct an equilateral triangle on a given finite straight line.

Construction:

Start with line segment AB



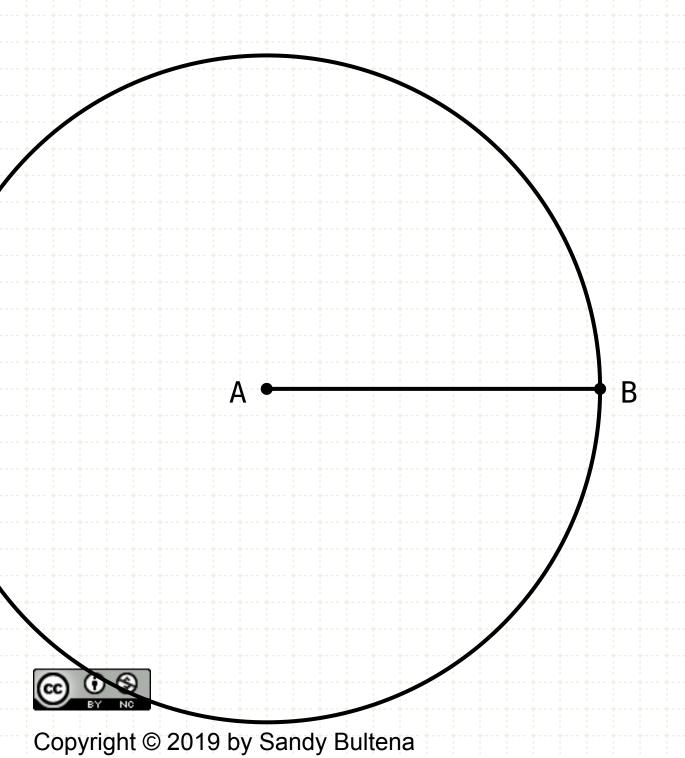


To construct an equilateral triangle on a given finite straight line.

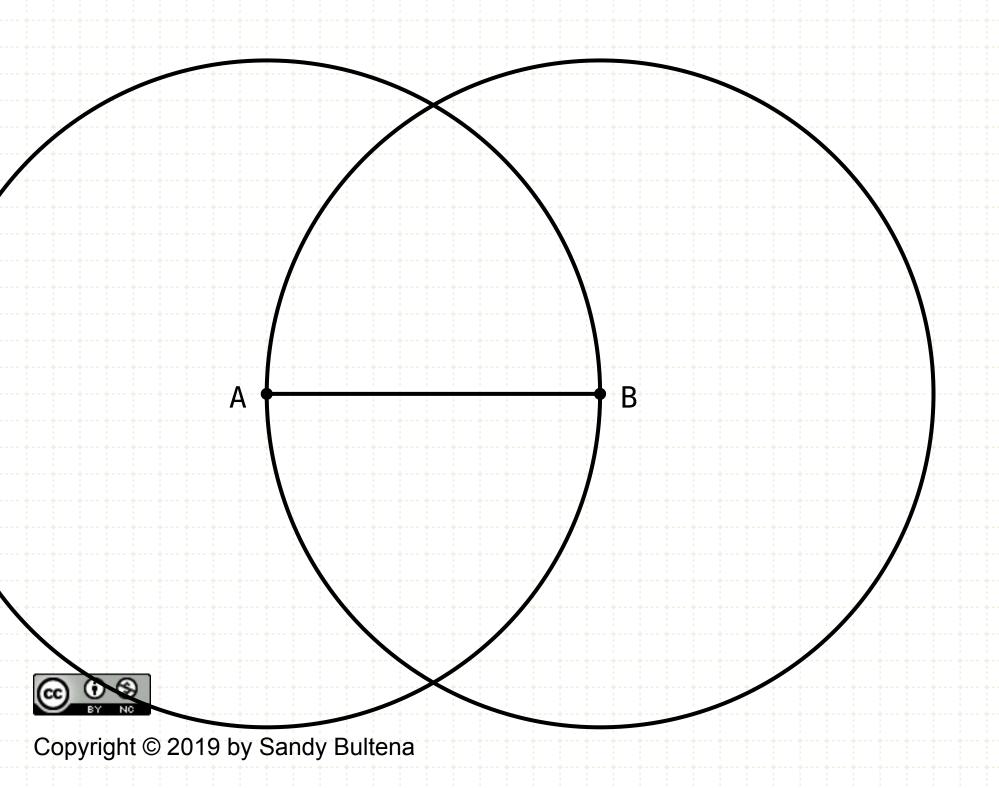
Construction:

Start with line segment AB

Create a circle with center A and radius AB



To construct an equilateral triangle on a given finite straight line.



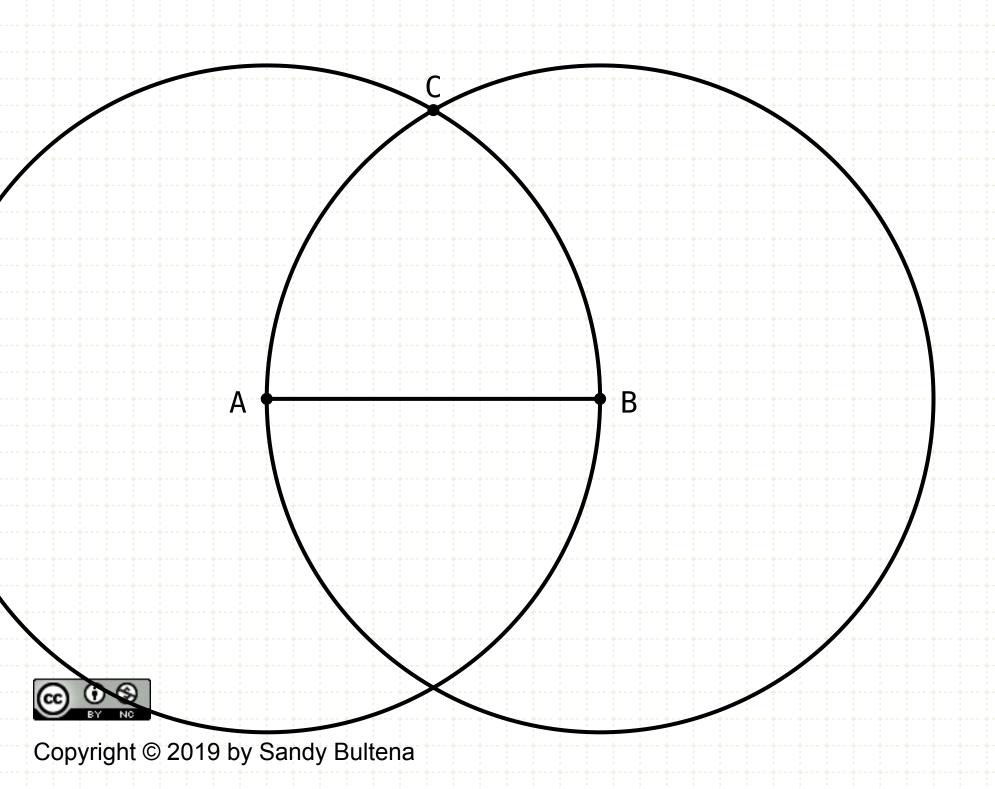
Construction:

Start with line segment AB

Create a circle with center A and radius AB

Create a circle with center B and radius AB

To construct an equilateral triangle on a given finite straight line.



Construction:

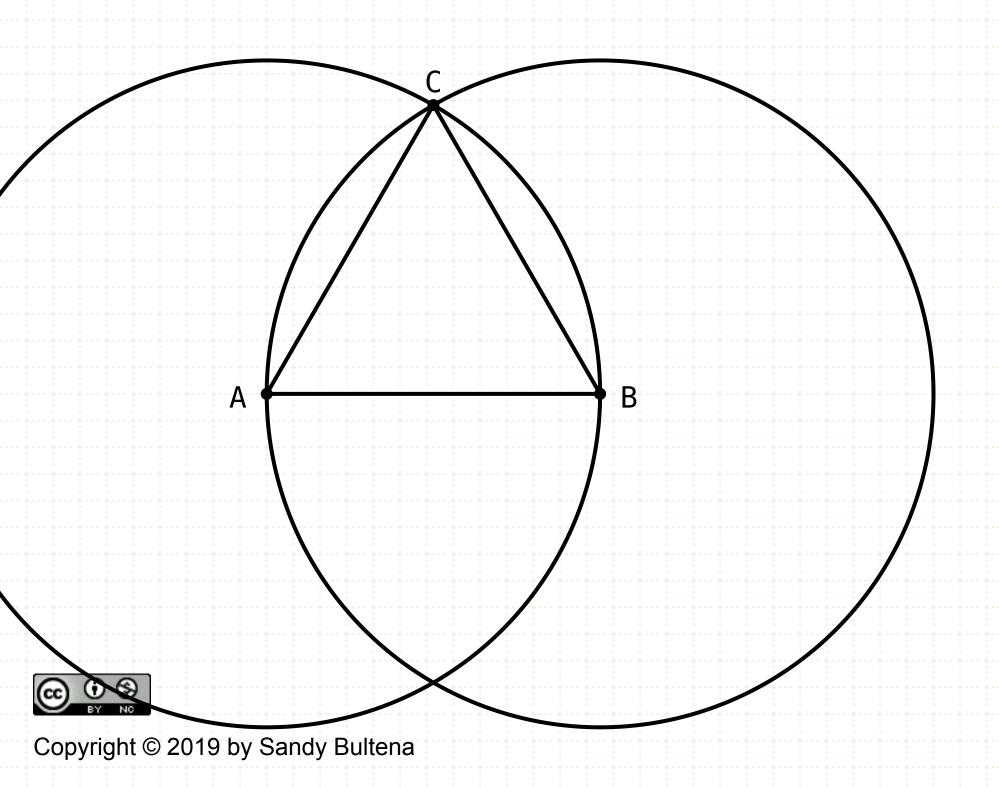
Start with line segment AB

Create a circle with center A and radius AB

Create a circle with center B and radius AB

Label the intersection point C

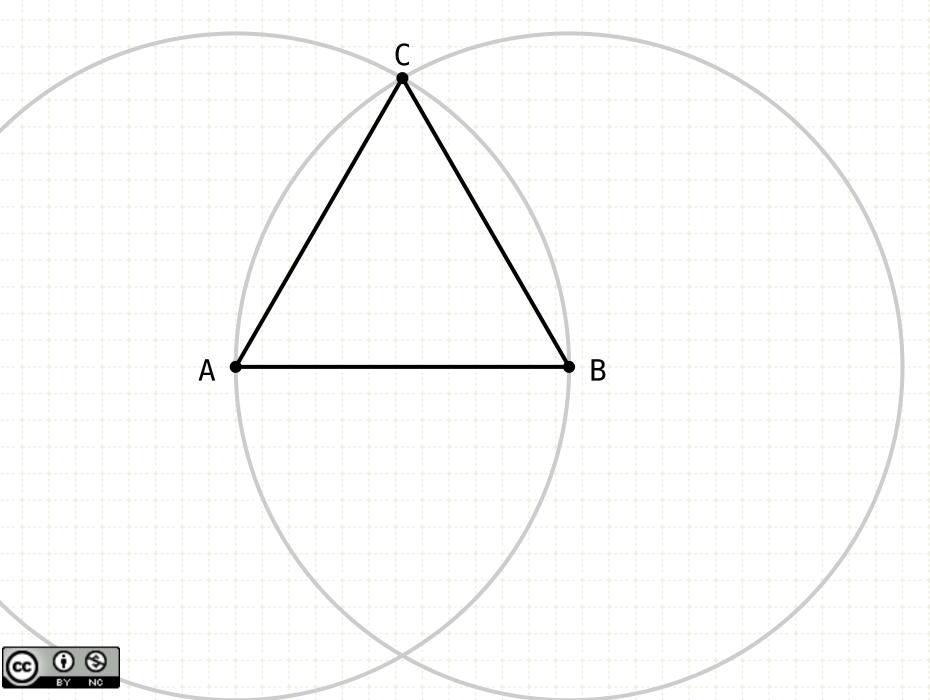
To construct an equilateral triangle on a given finite straight line.



Construction:

Start with line segment AB
Create a circle with center A and radius AB
Create a circle with center B and radius AB
Label the intersection point C
Create line AC and CB

To construct an equilateral triangle on a given finite straight line.

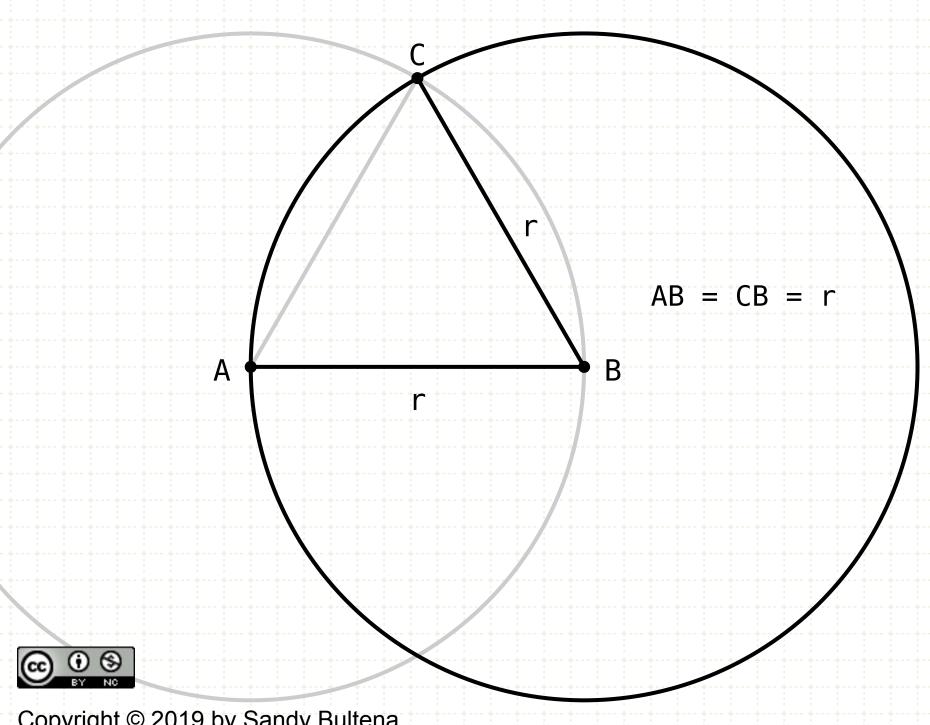


Construction:

Start with line segment AB
Create a circle with center A and radius AB
Create a circle with center B and radius AB
Label the intersection point C
Create line AC and CB

Triangle ABC is an equilateral triangle

To construct an equilateral triangle on a given finite straight line.



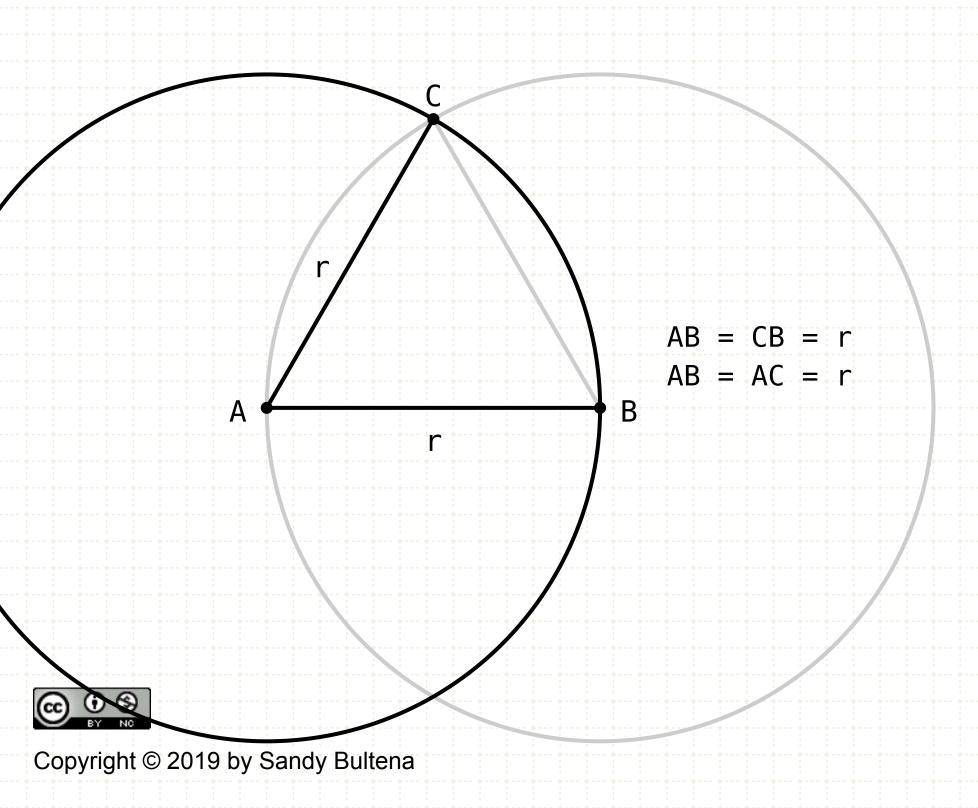
Construction:

Start with line segment AB Create a circle with center A and radius AB Create a circle with center B and radius AB Label the intersection point C Create line AC and CB Triangle ABC is an equilateral triangle

Proof:

AB and CB are radii of the same circle - hence they are equal

To construct an equilateral triangle on a given finite straight line.



Construction:

Start with line segment AB

Create a circle with center A and radius AB

Create a circle with center B and radius AB

Label the intersection point C

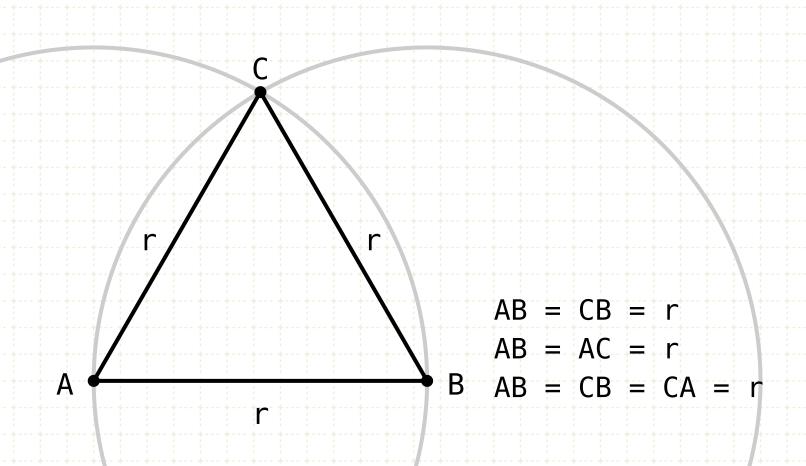
Create line AC and CB

Triangle ABC is an equilateral triangle

Proof:

AB and CB are radii of the same circle - hence they are equal AB and AC are radii of the same circle - hence they are equal

To construct an equilateral triangle on a given finite straight line.



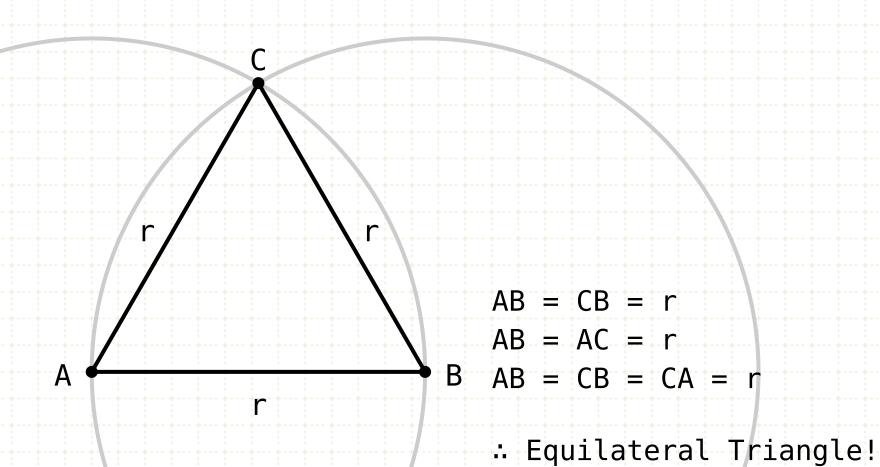
Construction:

Start with line segment AB
Create a circle with center A and radius AB
Create a circle with center B and radius AB
Label the intersection point C
Create line AC and CB
Triangle ABC is an equilateral triangle

Proof:

AB and CB are radii of the same circle - hence they are equal AB and AC are radii of the same circle - hence they are equal If AB equals AC and AB equals CB, then AC equals CB

To construct an equilateral triangle on a given finite straight line.



Construction:

Start with line segment AB
Create a circle with center A and radius AB
Create a circle with center B and radius AB
Label the intersection point C
Create line AC and CB
Triangle ABC is an equilateral triangle

Proof:

AB and CB are radii of the same circle - hence they are equal AB and AC are radii of the same circle - hence they are equal If AB equals AC and AB equals CB, then AC equals CB

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