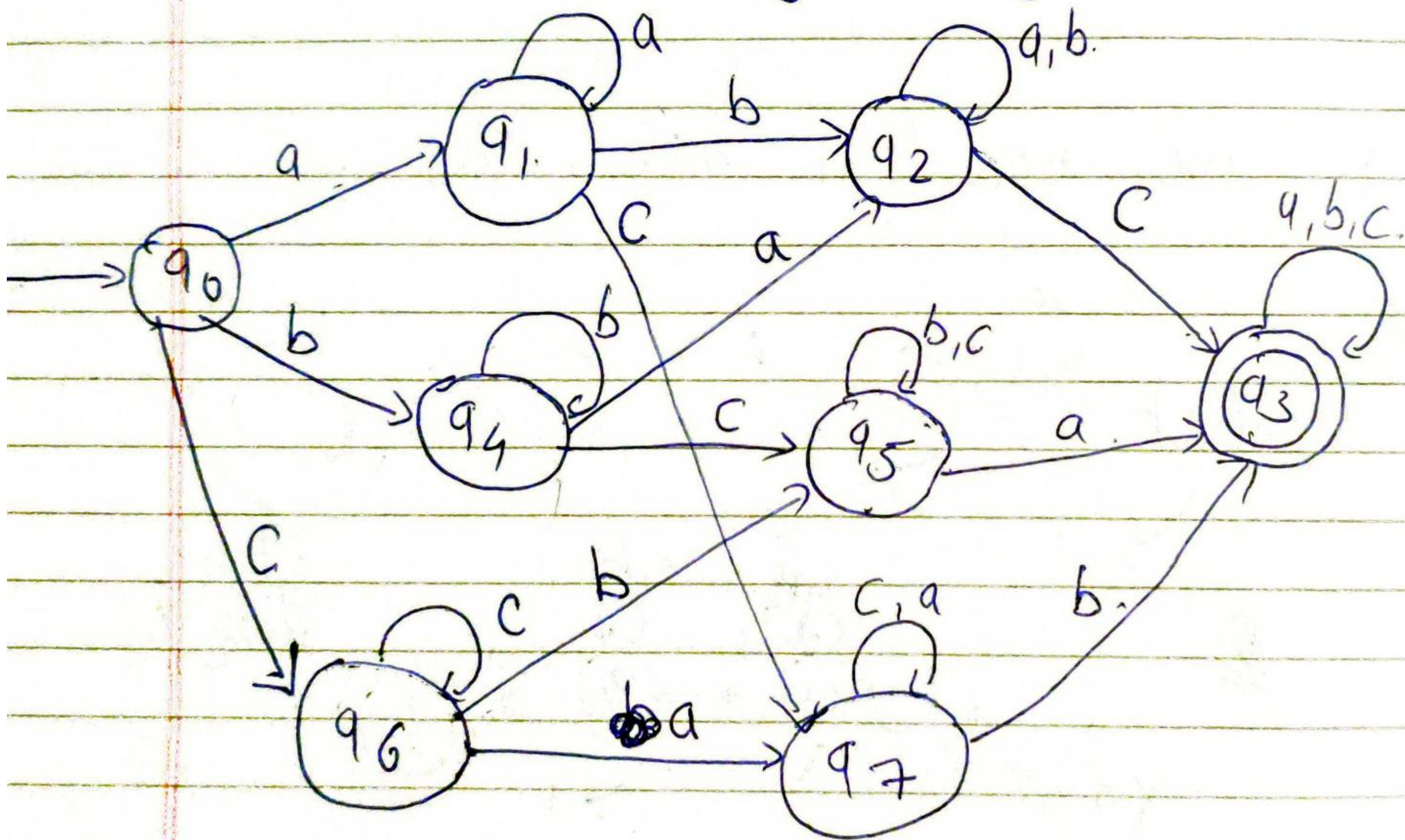


Spring 2014

Q.1 → Give the

→ Given!

input =

 $\Sigma = \{a, b, c\}$ $L_1 = \{w: w \text{ contains at least one } a, \text{ one } b \text{ and one } c \text{ in any order}\}$ 

2) - prove that following ...

→ ~~for~~ prove the language is not ~~not~~ context free using pumping lemma.

Use steps below to prove ~~EF~~ above using pumping lemma.

→ 1) Assume that language (L) is context free.

2) It has to have a pumping length (p) .

3) All strings longer than p can be pumped $|S| \geq p$

4) Now, find a string ' s ' in A such that $|S| \geq p$.

5) Divide S into u, v, x, y, z .

6) Show that

$uv^i x y^i z \notin A$ for some i .

7) Then consider the ways that S can be divided into $u v x y z$.

$$u v^i x y^i z$$

8) Show that none of these can satisfy all 3 pumping lemma conditions at same time.

that are

1) $u^i \cdot v \cdot x \cdot y^i \cdot z$ is in A for every $i \geq 0$

$$2) |v y| > 0$$

$$3) |v x y| \leq p.$$

9) S cannot be pumped == contradiction.

$L = \{ w : w \text{ containing the same no. of } a's, b's \text{ and } c's \text{ in any order} \}$
 $a^N \neq b^N, c^N$

1) Assume, L is context free

2) L must have a pumping length p

3) take s such that $s = a^p b^p c^p$.

4) divide 8 into u, v, x, y, z .

take $p = 4$.

So, $S = a^4 b^4 c^4$

case 1

u, v, x, y, z each contain only one type of symbol

$a a a a \quad b b b b \quad c c c c$
 $u \quad \underbrace{\quad}_v \quad \underbrace{\quad}_x \quad \underbrace{\quad}_y \quad \underbrace{\quad}_z$

$u v^i x y^i z \quad (i = 2)$

$u v^2 x y^2 z$

$a a a a a \quad a b b b b \quad c c c c c$
 $u \quad \underbrace{\quad}_{v^2} \quad \underbrace{\quad}_x \quad \underbrace{\quad}_y \quad \underbrace{\quad}_z$

$a^6 b^4 c^5 \neq L$

here no. of ~~a's~~ a's, b's & c's are not equal.

This does not belong to language L given.

as, this condition is not satisfied
it is not context free.

$\therefore L$ is not context free.

case II.

a a a a b b b b c c c c
u v x y z

$u v^i x y^i z \quad (i = 2)$

a a a a b b a a b b b b b c c c c $\notin L$

as pattern ~~$a^n b^n$~~ $a^n b^n c^n$
is not there in above string.

~~the~~ above string is not in language
and condition 1 fails.
so thus, language L is not context
free.

Q.3 \rightarrow Let $ATM = \{ M, w : \dots \}$

\rightarrow We can show it like for input,

Let $\langle M, w \rangle$ to ATM , we transform it into an input of $TWOTM$.

Let's there be a function f which takes $\langle M, w \rangle$ as input and produce another Turing Machine M_1 as output.

$$f(\langle M, w \rangle) = M_1$$

This M_1 will be the input to $TWOTM$.

Now let's M_1 rejects all ~~other~~ input other than $1, w$.

on input 1 it accepts it and for input w it runs M on w .

So if M_1 in $TWOTM$, means M_1 accepts only 2 strings which imply M must accept w .

Thus, $ATM \leq TWOTM$.