

Fertilizer for Gower's Bamboo Growing Company

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Executive Summary

Business Parameters

From the initial parameters, our reference numbers are that one meter of bamboo weighs about 10kg and each kg is worth 12 dollars. We can begin selling bamboo once it has grown up to 3 meters. These numbers were used in the calculations throughout this report and can be changed if the market shifts.

Growth Data

These plots compare the growth of plants in x-grow brand fertilizer and y-grow brand fertilizer. The third plot containing both sets of data marks where plants are eligible to be sold.

If you choose to grow with x fertilizer, your plants will grow faster in the beginning of a 60 day cycle, but the growth rate will begin to decline below the growth rate of y at about 26 days. The plants grown in x or y will come to the same average growth rate and thus same height at 53 days. After 53 days, plants grown with y fertilizer have a higher growth rate for the rest of the duration of the trial experiment. We conclude that there are significant differences in bamboo growth when using the fertilizers from brands x-grow versus y-grow.

Growth Rates

Table 1: Comparing Fertilizers

Characteristic	Fertilizer x	Fertilizer y
Days to 3m	12.7	25.42
Rate of Growth at 3m	0.46	0.232
Optimal Growth Cycle (days)	20.3	48.81
Optimal Choice	Yes	No

The plants grown in x-grow brand fertilizer are eligible for harvest on the 18 hours into the 13th day after planting. Plants grown in y-grow brand fertilizer are eligible for harvest 13 hours into the 26th day after planting. When the plants reach a height of 3 meters, the growth rates of bamboo with fertilizers x and y are, respectively, 0.46 and 0.232 meters per day.

Generally, it is sub-optimal to harvest a plant which is in the middle of a relatively high-growth period, but may be optimal to harvest directly after such a period. The optimal growth cycles are 20.3 and 48.81 days for x and y, respectively. These cycles will yield a profit of 730 and 1,030 dollars for fertilizer x and y, respectively. It is important to note that these cycles are of different duration. For direct comparison, x yields 34 dollars per day and y yields 21 dollars per day on average in an optimal cycle.

1 Decision

Characteristics	x-grow Fertilizer	y-grow Fertilizer	Based
Cost per Plant	1 dollar	1.25 dollar	
Profit per Plant in Optimal Cycle of Growth	690 dollars	1,030 dollars	

on our analysis of the data, we have concluded that x-grow brand fertilizer is the optimal choice if you can harvest repeatedly in 60 days. The cost per plant of fertilizer y (1.25) is negligible compared with the revenue earned from the same plant (1,200). So, we simply disregard this cost of fertilizer without loss of any margin of comparison. The same applies for the cost per plant of fertilizer x (1.00), which in three (optimal) cycles becomes 3 compared with the revenue earned from the same individual physical growth slot (1950). Even though at the end of the full 60 day trial, y is favored, when we include factors like cost of fertilizer (negligible), and length of optimal growing cycle (significantly shorter for x) the clear winner, yielding more dollars per day is fertilizer x.

2 Profits of Scale

We assume the company operates at full capacity to produce 20,000 plants in the 60 day time frame, and has the corresponding turnover of product. We seek to use profit per plant, then scale up to 20,000 plants to get a number that represents profits per 60 days at full capacity.

The one dollar or one dollar twenty-five cents cost is actually quite negligible when compared with the revenue generated by each shoot cycle (1950 and 1200 for x and y respectively). Therefore, we effectively disregard the cost of each brand of fertilizer and focus on the difference in revenue generated by each optimal cycle.

The output of the above code indicates that fertilizers x and y will grow plants that generate revenue of 39 million and 24 million respectively. The 15 million difference between them is the difference of the total marginal benefit from employing fertilizer x as opposed to fertilizer

y.

3 Appendix

```
1  #Main File
2  import numpy as np
3  import pandas as pd
4  import Build_data_report as BDR
5  import Plot_data_figures as PDF
6
7
8  #User input business parameters
9  x_cost = 1.0
10 y_cost = 1.25
11 dollar_per_kg = 12
12 kg_per_m = 10
13 dollar_per_m = dollar_per_kg*kg_per_m
14 num_plants = 20000
15
16 #x_data = np.loadtxt("x_grow.csv", delimiter=",")
17 #y_data = np.loadtxt("y_grow.csv", delimiter=",")
18 x_data = pd.read_csv("C:/Users/sandy/OneDrive/Documents/Summer 2023/
Computing - 300/Final/x_grow.csv", delimiter=",")
19 y_data = pd.read_csv("C:/Users/sandy/OneDrive/Documents/Summer 2023/
Computing - 300/Final/y_grow.csv", delimiter=",")
20 x_data = np.array(x_data)
21 y_data = np.array(y_data)
22
23 x_data_list_0,x_data_list_1 = BDR.build_data_list(x_data)
24 y_data_list_0,y_data_list_1 = BDR.build_data_list(y_data)
25
26 sell_day_x = BDR.find_sell_day(x_data)
27 sell_day_y = BDR.find_sell_day(y_data)
28 sell_mom_x = BDR.find_sell_moment(x_data,sell_day_x)
29 sell_mom_y = BDR.find_sell_moment(y_data,sell_day_y)
30
31 x_growth_rate = BDR.find_growth_rate(x_data, sell_day_x)
32 y_growth_rate = BDR.find_growth_rate(y_data, sell_day_y)
33 x_growth_rates = BDR.find_growth_rates(x_data)
34 y_growth_rates = BDR.find_growth_rates(y_data)
35 x_max_rate, x_max_rate_day = BDR.find_peak_growth(x_data,
x_growth_rates)
36 y_max_rate, y_max_rate_day = BDR.find_peak_growth(y_data,
y_growth_rates)
37
38 x_optimal_cycle, x_max_profit_per_day = BDR.find_optimal_duration\
39 (x_data,x_cost,dollar_per_m,sell_day_x)
40 y_optimal_cycle, y_max_profit_per_day = BDR.find_optimal_duration\
41 (y_data,y_cost,dollar_per_m,sell_day_y)
42
43
```

```

44     profit_data_x, cycles_x = BDR.find_profit_data(x_data,sell_day_x,
dollar_per_m,x_cost)
45     profit_data_y, cycles_y = BDR.find_profit_data(y_data,sell_day_y,
dollar_per_m,y_cost)
46
47     x_max_profit, x_optimal_cycles = BDR.find_actual_profit(x_data, \
48         sell_day_x, dollar_per_m, x_cost)
49     y_max_profit, y_optimal_cycles = BDR.find_actual_profit(y_data, \
50         sell_day_y, dollar_per_m, y_cost)
51     x_total_profit = x_max_profit*num_plants
52     y_total_profit = y_max_profit*num_plants
53
54     if x_total_profit > y_total_profit:
55         total_saved_money = round((x_total_profit - y_total_profit),2)
56     if y_total_profit > x_total_profit:
57         total_saved_money = round((y_total_profit - x_total_profit),2)
58     if y_total_profit == x_total_profit:
59         total_saved_money = 0
60
61     x_profit_data,x_cycles = BDR.find_profit_data(x_data,sell_day_x,
dollar_per_m,x_cost)
62     y_profit_data,y_cycles = BDR.find_profit_data(y_data,sell_day_y,
dollar_per_m,y_cost)
63
64     report_x_profit = BDR.report_million(BDR.find_mantissa(
x_total_profit))
65     report_y_profit = BDR.report_million(BDR.find_mantissa(
y_total_profit))
66     report_total_profit = BDR.report_million(BDR.find_mantissa(
total_saved_money))
67
68     #Plotting data report:
69
70     #Plots curve fit for data
71     PDF.plot_curve_fit_x(x_data_list_0,x_data_list_1)
72     PDF.plot_curve_fit_y(y_data_list_0,y_data_list_1)
73
74     #Plots data as line segment seperately
75     PDF.plot_x_data(x_data_list_0,x_data_list_1)
76     PDF.plot_y_data(y_data_list_0,y_data_list_1)
77
78     #Plots both sets together
79     PDF.plot_x_y_data(x_data_list_0,x_data_list_1,y_data_list_0,
y_data_list_1)
80     #Plots together with 3m mark
81     PDF.plot_sell_day(x_data_list_0,x_data_list_1,y_data_list_0,
y_data_list_1)
82
83     #Plots growth rates by day
84     PDF.plot_growth_rate(x_data_list_0,x_data_list_1,y_data_list_0,
y_data_list_1,x_growth_rates,y_growth_rates)
85
86     #Plots growth per cycle
87     PDF.make_barchart_x(x_profit_data,x_cycles)

```

```

88     PDF.make_barchart_y(y_profit_data,y_cycles)
89
90
91     #Printing report set up for x and y grow brand fertilizer
92
93     #Prints sell day information
94     print(f'We can sell bamboo shoots grown with x fertilizer after \
95           {int(sell_day_x)} days and roughly {int(sell_mom_x)} hours after
planting.')
```

```

96     print(f'\nWe can sell bamboo shoots grown with y fertilizer after \
97           {int(sell_day_y)} days and roughly {int(sell_mom_y)} hours after
planting.')
```

```

98
99     #Prints groth rates
100    print(f'\n\nThe growth rate of bamboo grown with x fertilizer at \
101          point of sell is {BDR.find_mantissa(x_growth_rate)} meters per day.'
```

```

102    )
103    print(f'\n\nThe growth rate of bamboo grown with y fertilizer at \
104          point of sell is {BDR.find_mantissa(y_growth_rate)} meters per day.'
```

```

105    )
106
107    #Printing max rates and analysis of optimal cycles
108    print(f'\n\nFertilizer x results in a peak growth rate of {BDR.
find_mantissa(x_max_rate)} meters per day on day {round(x_max_rate_day)
}')
109    print(f'\n\nFertilizer y results in a peak growth rate of {BDR.
find_mantissa(y_max_rate)} meters per day on day {round(y_max_rate_day)
}.'
```

```

110
111    #Paragraph specific to this data and visual analysis. Not valid for
new data.
112    print('\nIf you choose to grow with x fertilizer, your plants will \
113          grow faster in the beginning of a 60 day cycle, but the growth \
114          rate will begin to decline at about 26 days. After about 30 days, \
115          both sets will be growing at roughly the same rate. At this \
116          point, plants grown with y fertilizer will begin to grow faster. \
117          Both plant sets will come to the same average growth rate and \
118          thus same height at 53 days, after which y fertilizer grown \
119          plants have a faster average growth rate.')
```

```

120
121    #Prints optimal cycle days and max profit in that cycle
122    print(f'\n\nThe maximum profit per {BDR.find_mantissa(
x_optimal_cycle)} days, the optimal cycle, per plant \
123          grown in x fertilizer will be {BDR.find_mantissa(
x_max_profit_per_day*x_optimal_cycle)} dollars.')
```

```

124    print(f'\n\nThe maximum profit per {BDR.find_mantissa(y_optimal_cycle)
} days, the optimal cycle, per plant \
125          grown in y fertilizer will be {BDR.find_mantissa(
y_max_profit_per_day*y_optimal_cycle)} dollars.')
```

```

126
127    #Prints the optimal choice
128    print(f'\n\nThe maximum profit per {BDR.find_mantissa(
y_optimal_cycle)} \

```

```

128     days, the optimal cycle, per plant grown in y fertilizer will be \
129     {BDR.find_mantissa(y_max_profit_per_day*y_optimal_cycle)} dollars.')}
130     if x_max_profit_per_day > y_max_profit_per_day:
131         print("\nOptimal fertilizer choice is x because it yields more \
132         dollars per day and in the long run pays off.")
133     if y_max_profit_per_day > x_max_profit_per_day:
134         print("\nOptimal fertilizer choice is y because it yields more \
135         dollars per day and in the long run pays off.")
136     if x_max_profit_per_day == y_max_profit_per_day:
137         print("\nBoth fertilizers are equivalent in optimal profit.")
138
139     #Notes irrelevant cost
140     print('\nNote that the cost per plant is negligible because the
profit is roughly one thousand times larger than the cost.')}
141
142     #Prints final data analysis
143     print(f'\n\nAfter {len(x_data)} days as {int(BDR.find_mantissa(
x_optimal_cycles))} \
144     cycle(s) of {int(BDR.find_mantissa(len(x_data)/x_optimal_cycles))}
days in \
145     fertilizer x, the profit per plant is {BDR.find_mantissa(
x_max_profit)}. \
146     Therefore, the total profit for all {num_plants} plants at a time \
147     is {report_x_profit}.')}
148
149     print(f'\n\nAfter {len(y_data)} days as {int(BDR.find_mantissa(
y_optimal_cycles))} \
150     cycle(s) of {int(BDR.find_mantissa(len(y_data)/y_optimal_cycles))}
days in \
151     fertilizer y, the profit per plant is {BDR.find_mantissa(
y_max_profit)}. \
152     Therefore, the total profit for all {num_plants} plants at a time \
153     is {report_y_profit}.')}
154
155     print(f'\nFinally, the total profit saved from using the optimal \
156     fertilizer is {report_total_profit}')}
157

```

```

1
2 #Build_data_report File for functions
3 import numpy as np
4 import math
5
6 #For rounding later on:
7 def find_mantissa(num):
8     scale = int(round(np.log10(num),0))-3
9     mantissa = int(round(num/10**scale,0))
10    rounded_num = mantissa*10**scale
11    rounded_num = round(rounded_num,3)
12    return rounded_num
13
14 def report_million(num):
15     if num >= 1000000:
16         num = int(num/1000000)
17         return f'{num} Million'
18     if num < 1000000:
19         return num
20
21 #Build data report
22 def build_data_list(data):
23     data_list_0 = []
24     data_list_1 = []
25     for i in range(len(data)):
26         data_list_0.append(data[i][0])
27         data_list_1.append(data[i][1])
28     return data_list_0,data_list_1
29
30 #Finds day eligible for selling
31 def find_sell_day(data):
32     for i in range(len(data)):
33         if data[i][1] >= 3.0:
34             max_day = data[i][0]
35             min_day = data[i-1][0]
36             grow_max = data[i][1]
37             grow_min = data[i-1][1]
38             mom_at_3 = ((grow_max-3)*max_day+(3-grow_min)*min_day)/(
grow_max-grow_min)
39             return mom_at_3
40             raise Exception("Did not reach 3 meters in observed duration.
Expand duration or adjust expected height.")
41
42 def find_sell_moment(data,sell_day):
43     extra = sell_day - int(sell_day)
44     extra = 24*extra
45     extra = round(extra,0)
46     return extra
47
48 def find_growth_rate(data, sell_day):
49     for i in range(len(data)):
50         if data[i][0] >= sell_day:
51             dh = data[i+1][1] - data[i-1][1]

```

```

52         dt = data[i+1][0] - data[i-1][0]
53         rate = dh/dt
54         return rate
55
56     def find_growth_rates(data):
57         growth_rates = []
58         dh0 = data[1][1] - data[0][1]
59         dt0 = data[1][0] - data[0][0]
60         growth_rates.append(dh0/dt0)
61         dh1 = data[2][1] - data[0][1]
62         dt1 = data[2][0] - data[0][0]
63         growth_rates.append(dh1/dt1)
64         dh2 = data[4][1] - data[0][1]
65         dt2 = data[4][0] - data[0][0]
66         growth_rates.append(dh2/dt2)
67         for i in range(3, len(data)-3):
68             dh = data[i+3][1] - data[i-3][1]
69             dt = data[i+3][0] - data[i-3][0]
70             growth_rates.append(dh/dt)
71         dhe = data[len(data)-1][1] - data[len(data)-5][1]
72         dte = data[len(data)-1][0] - data[len(data)-5][0]
73         growth_rates.append(dhe/dte)
74         dhe = data[len(data)-1][1] - data[len(data)-3][1]
75         dte = data[len(data)-1][0] - data[len(data)-3][0]
76         growth_rates.append(dhe/dte)
77         dhe = data[len(data)-1][1] - data[len(data)-2][1]
78         dte = data[len(data)-1][0] - data[len(data)-2][0]
79         growth_rates.append(dhe/dte)
80         return growth_rates
81
82     def find_peak_growth(data, growth_rates):
83         new_max_rate = 0
84         for i in range(len(growth_rates)):
85             max_rate = new_max_rate
86             if growth_rates[i] > max_rate:
87                 max_rate = growth_rates[i]
88                 max_day = data[i][0]
89             new_max_rate = max_rate
90         return max_rate, max_day
91
92     def find_optimal_duration(data, cost, dollar_per_m, sell_day):
93         t_max = len(data)
94         profit = []
95         max_day = 0
96         new_max = 0
97         for i in range(int(round(sell_day, 0)), t_max):
98             max_profit = new_max
99             profit.append((data[i][1]*dollar_per_m-cost)/data[i][0])
100             new_max = max(profit)
101             if new_max > max_profit:
102                 max_day = data[i][0]
103         return max_day, max_profit
104
105     def find_actual_profit(data, sell_day, dollar_per_m, cost):

```



```

106     cycles = int(math.trunc(len(data)/int(round(sell_day,0))))
107     max_profit = 0
108     for i in range(1,cycles+1):
109         days = int(math.trunc(len(data)/i))
110         height = data[days-1][1]
111         profit = height*dollar_per_m - cost
112         if profit*i >= max_profit:
113             max_profit = profit*i
114             optimal_cycles = i
115     return max_profit, optimal_cycles
116
117     #For building a histogram
118     def find_actual_profit_cycles(data,sell_day,dollar_per_m,cost,days):
119         if sell_day > days:
120             raise Exception("The requested duration is shorter than the
121 eligible sell day. Choose a longer duration or different fertilizer.")
122         cycles = int(math.trunc(len(data)/int(round(days,0))))
123         height = data[int(round(days,0))-1][1]
124         profit = cycles*(height*dollar_per_m - cost)
125         return find_mantissa(profit)
126
127     def find_profit_data(data,sell_day,dollar_per_m,cost):
128         num = len(data)
129         nums = [num]
130         profits = []
131         for i in range(2,len(data)):
132             if num/i < sell_day:
133                 break
134             nums.append(num/i)
135         for i in range(len(nums)):
136             profits.append(2*find_actual_profit_cycles(data,sell_day,
137 dollar_per_m,cost,nums[i]))
138     return profits, nums

```

```

1      #Plot_data_figures file for plotting
2      import numpy as np
3      import matplotlib.pyplot as plt
4
5      #Functions made for curve fit.
6      #Will need to change for different data.
7      #constants = sc.optimize.curve_fit(f_y,y_data_list_0,y_data_list_1)
8
9      def f_y(t,x0,x1,x2,x3):
10         f = x0/(1+np.exp(-x1*t+x2))+x3
11         return f
12
13      def f_x(t,x0,x1,x2,x3,x4,x5,x6,x7,x8):
14         f = x0*t**2 + x1*t**3 + x2*t**4 + x3*t + x4 + x5*t**5 + x6*t**6
+ x7*t**7 + x8*t**8
15         return f
16
17      def plot_curve_fit_x(x_data_list_0,x_data_list_1):
18         tx = np.linspace(min(x_data_list_0),max(x_data_list_0),1000)
19         fig1 = plt.figure(1)
20         fig1.suptitle("Measured and Fit Data for x-grow", fontsize=16)
21         plt.plot(x_data_list_0,x_data_list_1)
22         plt.xlabel('Days of Growth')
23         plt.ylabel('Height (m)')
24         plt.scatter(x_data_list_0,x_data_list_1,color='red')
25         plt.plot(tx,f_x(tx,-6.51968382e-02, 1.05973801e-02, -6.73468343
e-04, 2.59080135e-01,
26                 3.55047909e-01, 2.16533793e-05, -3.77703269e-07,
3.41898145e-09,
27                 -1.26162606e-11))
28         labels = ('Measurements','Polynomial Curve Fit')
29         plt.legend(labels)
30
31      def plot_curve_fit_y(y_data_list_0,y_data_list_1):
32         ty = np.linspace(min(y_data_list_0),max(y_data_list_0),1000)
33         fig2= plt.figure(2)
34         fig2.suptitle("Measured and Fit Data for y-grow", fontsize=16)
35         plt.xlabel('Days of Growth')
36         plt.ylabel('Height (m)')
37         plt.scatter(y_data_list_0,y_data_list_1,color='red')
38         plt.plot(ty,f_y(ty,10.70286051, 0.09901738, 3.46901829,
0.09466854))
39         labels = ('Measurements','Logistic Curve Fit')
40         plt.legend(labels)
41
42      #Plot 1 of just x data
43      def plot_x_data(x_data_list_0,x_data_list_1):
44         fig3 = plt.figure(3)
45         fig3.suptitle("Growth with Fertilizer x", fontsize=16)
46         plt.plot(x_data_list_0,x_data_list_1)
47         plt.xlabel('Days of Growth')
48         plt.ylabel('Height (m)')
49

```

```

50 #Plot 2 of just y data
51 def plot_y_data(y_data_list_0,y_data_list_1):
52     fig4 = plt.figure(4)
53     fig4.suptitle("Growth with Fertilizer y", fontsize=16)
54     plt.plot(y_data_list_0,y_data_list_1)
55     plt.xlabel('Days of Growth')
56     plt.ylabel('Height (m)')
57
58 #Plot 3 of x and y data
59 def plot_x_y_data(x_data_list_0,x_data_list_1,y_data_list_0,
60 y_data_list_1):
61     fig5 = plt.figure(5)
62     fig5.suptitle("Growth with Fertilizer x and y", fontsize=16)
63     plt.plot(x_data_list_0,x_data_list_1)
64     plt.plot(y_data_list_0,y_data_list_1)
65     plt.xlabel('Days of Growth')
66     plt.ylabel('Height (m)')
67     labels = ('x Fertilizer','y Fertilizer')
68     plt.legend(labels)
69
70 #Plot 4 marks where 3m exists to find when we can sell
71 def plot_sell_day(x_data_list_0,x_data_list_1,y_data_list_0,
72 y_data_list_1):
73     fig6 = plt.figure(6)
74     fig6.suptitle("When We Can Sell", fontsize=16)
75     plt.plot(x_data_list_0,x_data_list_1)
76     plt.plot(y_data_list_0,y_data_list_1)
77     plt.axhline(3,linestyle='--')
78     plt.xlabel('Days of Growth')
79     plt.ylabel('Height (m)')
80     labels = ('x Fertilizer','y Fertilizer','3m Achievement')
81     plt.legend(labels)
82
83 #Plot 5 Growth Rate
84 def plot_growth_rate(x_data_list_0,x_data_list_1,y_data_list_0,
85 y_data_list_1,x_growth_rates,y_growth_rates):
86     fig7 = plt.figure(7)
87     fig7.suptitle("Growth Rates", fontsize=16)
88     plt.plot(x_data_list_0,x_growth_rates)
89     plt.plot(y_data_list_0,y_growth_rates)
90     plt.xlabel('Days of Growth')
91     plt.ylabel('Rate of Growth')
92     labels = ('x Fertilizer','y Fertilizer')
93     plt.legend(labels)
94
95 def make_barchart_x(profit_data,cycles):
96     fig8 = plt.figure(8)
97     fig8.suptitle("60-Day Profit for Each Cycle Duration in x
98 Fertilizer", fontsize=16)
99     plt.bar(cycles,profit_data)
100     plt.xlabel('Cycle Duration in Days')
101     plt.ylabel('Profit per Plant in Ten Thousand Dollars')
102
103 def make_barchart_y(profit_data,cycles):

```

```
100     fig9 = plt.figure(9)
101     fig9.suptitle("60-Day Profit for Each Cycle Duration in y
102     Fertilizer", fontsize=16)
103     plt.bar(cycles,profit_data)
104     plt.xlabel('Cycle Duration in Days')
105     plt.ylabel('Profit per Plant in Ten Thousand Dollars')
```