## Bit Provenance, Graph-IR Compiling, Physics-Aware Simulation, and a Modular Neural Network Framework for Python

#### **Executive Summary**

This project is a **research harness** for building and comparing geometric/physics-aware learning systems without tying everything to a heavyweight runtime. It offers (a) a backend-agnostic tensor layer; (b) a graph IR that compiles OOP code and dataflow into scheduled DAGs; (c) a physics-based discrete-time system ("dt\_system") for step-wise, adaptive simulation; (d) ASCII and OpenGL renderers for rapid truth-checking; and (e) a path toward **bit-level provenance** and **universal translation** via a minimal operator set. Most components are **theoretical prototypes**—useful, inspectable, and intended for small, reproducible demonstrations rather than production.

#### 1) Rationale: Decouple Exploration from Heavy Runtimes

Typical stacks couple research to a specific framework/hardware footprint. Here, the **AbstractTensor** layer targets **pure Python**, **NumPy**, **Torch**, **JAX**, and experimental **C/OpenGL** routes—so you can explore ideas with small local demos and, when needed, switch to GPU or cloud without rewriting the system. [1][2] Backends are swappable at module boundaries, which keeps the experiments coherent across the codebase.

#### 2) Architecture at a Glance

- Tensor & Autograd Core a backend-agnostic tensor API with a "whiteboard-style" VJP engine to collect residuals and compute vector-Jacobian products across ticks. This favors inspectability and deterministic debugging over black-box speed.^[3][4]
- dt\_system a discrete-time, adaptive super-stepping loop: multiple simulators progress within a frame using micro-steps bounded by local error/ε controls. This supports step-wise continuity: the learning loop sees stable, per-tick states even when internal modules contain discontinuities or mixed rates.^[5][6]
- Graph IR & Transmogrifier OOP constructs are lowered to a graph IR, scheduled as a DAG, and, when useful, embedded in a physical relaxation metaphor (springs/repulsors) to find efficient orderings or allocations. This is the "universal translator" path: bit-level primitives → IR → scheduled program.^[7][8][9]
- Rendering ascii\_diff (engine) + ascii\_render (demo) for terminal-first visualization, plus OpenGL for richer views; both connect to the same state dictionaries for trustworthy introspection.^[10][11]
- Bit-Provenance a design track that traces how bits flow and mix through operators,

#### 3) Backends and Deployment

The framework can run on:

- **Pure Python** (slow but fully transparent)
- NumPy and Torch (fast prototyping; Torch for GPU)
- JAX (cloud-friendly transformations)
- OpenGL shader paths for select rendering/simulation loops^[10]
- C via CFFI with a planned Zig-assisted build for a compact dynamic library (work-in-progress)^[2]
- A longer-term **SSA-compiled** route for fully static binaries^[8]

This mix supports **cheap**, **fluent exploration**: start small on CPU, switch backends when necessary, and keep the same graph-level contracts.

#### 4) Bit-Provenance and the Minimal Operator Set

The compiler stack distinguishes several levels of description:

• OOP → SSA → Scheduled DAG → Minimal Operator Set.

The "minimal set" is where universal translatability emerges: a small repertoire of bit-level primitives (e.g., add/sub/mul/xor, shifts, masks) that can be reliably mapped onto any backend or device.^[7][9] With that, you can skim/simplify/unroll at each lowering stage to optimize for speed, memory, or energy, and still maintain provenance (which bit/region influenced which result). This enables program triage (which parts must be accurate/fast) and energy-aware policies down to the bit flip level.^[12]

# 5) Physics-Aware System Relaxation (for Efficiency and Continuity)

Rather than baking a single global  $\Delta t$ , **dt\_system** lets each simulator advance at its **own micro-step** within a frame, guided by **error metrics** and **step controllers** (e.g., PI-style dt control).^[5][6] This eases the pain of discontinuities:

- Step-wise continuity for NN training: if an internal module has hard thresholds or mixed-rate behavior, the controller can subdivide that sub-step until its state is numerically consistent. The outer learning loop still sees a coherent per-tick state trajectory—so gradients computed with the whiteboard VJP remain meaningful, even when the internals are not strictly smooth.
- Differentiable "stand-in" signals: physics nodes can act as surrogate functions (n-D

differentiable approximations) where analytic gradients are hard or missing.

A working demonstration of this posture shows up in **Transmogrifier**: take a program graph, bind it to a **spring/repulsor** layout in a spherical domain, and let relaxation reveal efficient schedules or colocations; encode those back into the compiler for cache-friendly execution.^[8][14]

#### 6) From Simple to Complex Neural Networks—Graph-Native

Neural layers here are **graph-first** modules: small linear blocks, PCA-like adapters, and activation layers that plug into AbstractTensor and the autoautograd tape. Hooks allow per-layer logging/visual panels, and rendering is pluggable (terminal or OpenGL) for fast **concept-to-screen** cycles.^[15][16]

A targeted research direction is **geometrically aware layers** (e.g., Riemannian or Laplace-Beltramiguided operators) that **avoid lossy projections** by operating **in the manifold** rather than flattening to 2D/3D first. This area is intentionally fluid and rapidly prototyped.

#### 7) File-Structure Highlights (What lives where)

- docs/—design notes (e.g., fused program IR, DT-graph design, abstract NN hooks). Good starting points for reviewers.^[17]
- src/common/
  - double\_buffer/ ping-pong and worker-safe buffering primitives (demos included).^[18]
  - dt\_system/ dt\_graph, engine\_api, dt\_controller, dt\_solver, spectral\_dampener, and mechanics/integrator subpackages. This is the time-stepping backbone.^[5][6][19]
  - tensors/—AbstractTensor, autoautograd (whiteboard runtime), backends, and NN building blocks; design docs (EXPLAINER.md, etc.).^[1][3][15]
  - quad\_buffer/ and index\_composer/ supplemental buffering/indexing utilities.^[20][21]
- src/rendering/
  - ascii\_diff/ the actual ASCII engine: framebuffer, kernel classifier, presets, demos (clock/benchmark).^[10]
  - ascii render/ thin demo wrapper around ascii diff.^[11]
  - opengl\_render/—API and threaded renderer stubs for GL-based visualization.^[22]
- src/compiler/
  - bitops.py & bitops\_translator.py bit-level primitives and their translation to graph nodes; supports the "minimal operator set" route.^[7][9]

- ssa\_builder.py, process\_graph\_helper.py lowering from higher-level forms to SSA and scheduled graphs.^[8]
- src/transmogrifier/
  - graph/—graph builders and compilers: BitTensorMemoryGraph, ProcessGraph, GraphDeepCompiler.^[8][14]
  - cycle\_unroller.py, operator\_defs.py, solver\_types.py loop unrolling, operator signatures, and core node/edge types for schedulers.^[22][23][24]
- src/bitbitbuffer/ bit-level ring buffers, indexing, masking, and helpers; foundation for provenance.^[25]
- tests/— extensive but evolving coverage across autograd, dt\_system, rendering, and compiler subsystems. Expect some failures during refactors.

**Reality check**: Transmogrifier "almost works"—its compilers and schedulers largely run, but **correctness** depends on **cell-sim/dt\_system** semantics stabilizing. Likewise, ascii render defers to ascii diff for real work.

#### 8) Current Status and Risks

- Maturity: prototypes across the board; many modules are intentionally partial.
- Interdependence: changes must be meticulously propagated.
- **Backends**: C/GL paths are **promising** but **incomplete**; Torch/JAX remain the most practical compute engines today.
- **Autograd**: the whiteboard VJP is ideal for **small**, **inspectable** runs; large-scale performance depends on future backends and optimized tapes.

#### **Footnotes (Repository Pointers)**

- [1] src/common/tensors/README.md backend-agnostic goals and interfaces.
- [2] src/common/tensors/accelerator backends/c backend.py+
- .../c backend/AGENTS.md CFFI design and Zig-assisted build stubs.
- [3] src/common/tensors/autoautograd/whiteboard\_runtime.py whiteboard VJP, residual/tape mechanics.
- [4] src/common/tensors/backward\_registry.py backward op registrations and policies.
- [5] src/common/dt system/dt.py dt loop primitives and integration points.
- [6] src/common/dt\_system/dt\_controller.py adaptive/PI step controllers and dt scaling.
- [7] src/compiler/bitops.py minimal bit-level operator repertoire.
- [8] src/compiler/ssa\_builder.py, src/compiler/process\_graph\_helper.py—IR lowering and SSA construction.

- [9] src/compiler/bitops translator.py mapping from bit ops to graph primitives.
- [10] src/rendering/ascii\_diff/ framebuffer, kernel classifier, presets, demos (e.g., clock demo.py, benchmark demo.py).
- [11] src/rendering/ascii render/ demo wrapper (demo ascii render.py).
- [12] src/bitbitbuffer/ + src/bitbitbuffer/helpers/ buffers, indexers, slices, streams (provenance foundations).
- [13] docs/FUSED PROGRAM IR.md notes toward a common IR surface.
- [14] src/transmogrifier/graph/graph\_deep\_compiler.py, graph\_express2.py, graph/memory\_graph/— graph builders and deep compiler.
- [15] src/common/tensors/abstract\_nn/ small NN blocks (linear\_block.py, pca layer.py) and adapters.
- [16] src/common/tensors/abstract nn/hooks.py hook panel and training-time events.
- [17] docs/dt\_graph\_design.md, docs/abstract\_nn\_hooks.md high-level design notes.
- [18] src/common/double buffer/ base/core/lock/workers and demos.
- [19] src/common/dt\_system/engine\_api.py, dt\_graph.py, dt\_solver.py, spectral dampener.py orchestration/graphing.
- [20] src/common/quad buffer/ quad buffer.py, tribuffer.py.
- [21] src/common/index\_composer/indexcomposer.py.
- [22] src/rendering/opengl render/—API, threaded renderer stubs.
- [23] src/transmogrifier/cycle unroller.py loop unrolling strategies.
- [24] src/transmogrifier/operator defs.py,
- src/transmogrifier/solver types.py operator signatures and node/edge types.
- [25] src/bitbitbuffer/helpers/bitbitindex.py, .../bitbitslice.py,
- .../rawspan.py, etc.

#### Appendix: Notes on "Step-Wise Continuity"

Why it helps: Many real systems are piecewise or event-driven. For training, it's enough that each outer tick's state lies on a consistent, low-error manifold—even if the tick internally required 3→30 micro-steps. The dt controller contracts/inflates those micro-steps until local criteria are satisfied; the autograd tape then differentiates through the sequence of stable sub-states, insulating parameter updates from internal discontinuities. This is the practical bridge between clean gradients and messy simulators.

### Sources & Selected Readings (Annotated)

**Purpose.** This page curates key, peer-reviewed (and a few influential preprint) works that ground the project's aims: geometry-aware learning, graph-native representations, physics-structured training, operator learning, and constraint-aware layers. Each entry has a brief, plain-language note on what it contributes and how it informs this framework.

#### A. Field Overviews (context for geometry in ML)

[1] Bronstein, Bruna, Cohen, Veličković. Geometric Deep Learning: Grids, Groups, Graphs, Geodesics, and Gauges (2021).

What it says: A broad map of how modern ML should respect the structure of data—symmetries, graphs, and manifolds—not just raw arrays.

Why it matters here: Validates a design where geometry is first-class and modules stay portable across backends while preserving structure.

[2] Bronstein, Bruna, LeCun, Szlam, Vandergheynst. *Geometric Deep Learning: Going Beyond Euclidean Data* (2016/2017).

What it says: Early, influential survey of learning on graphs and manifolds.

Why it matters here: Motivates a graph-native IR and manifold-aware layers as default building blocks, not afterthoughts.

#### **B.** Symmetry-Respecting Models (equivariance)

[3] Weiler & Cesa. General E(2)-Equivariant Steerable CNNs (NeurIPS 2019).

What it says: Convolutional layers that "do the right thing" under 2D rotations/reflections by design. Why it matters here: Template for symmetry-aware kernels that plug into a unified tensor API.

[4] Finzi, Stanton, Izmailov, Wilson. *LieConv* (ICML 2020).

What it says: Convolutions equivariant to continuous Lie groups; one recipe across many symmetry groups.

Why it matters here: Encourages a small set of primitive operations the IR can preserve while retargeting to different domains.

[5] Cohen, Weiler, Kicanaoglu, Welling. *Gauge-Equivariant CNNs & Icosahedral CNN* (ICML 2019). What it says: Layers that are consistent on curved domains (spheres/meshes) via local frames ("gauges").

Why it matters here: Direct precedent for manifold-native layers that run on spherical/mesh data without lossy flattening.

[6] Fuchs, Worrall, Fischer, Welling. SE(3)-Transformer (NeurIPS 2020).

What it says: Self-attention that's rigid-motion equivariant in 3D.

Why it matters here: A path toward attention modules that stay physically consistent in 3D scenes.

[7] Thomas et al. *Tensor Field Networks* (2018, preprint).

What it says: Uses spherical harmonics to handle vectors/tensors with rotation awareness.

Why it matters here: Connects natural "typed" features (scalars/vectors) to spectral methods used

elsewhere in the stack.

[8] Satorras, Hoogeboom, Welling. *E(n)-Equivariant GNNs* (ICML 2021).

What it says: Lightweight equivariant message-passing without heavy tensor representations.

Why it matters here: A pragmatic default for symmetry-aware graph layers.

[9] Cohen, Geiger, Weiler. A General Theory of Equivariant CNNs on Homogeneous Spaces (NeurIPS 2019).

What it says: A unifying mathematical frame for equivariant CNNs.

Why it matters here: Helps specify what the compiler must not break when lowering high-level models to IR.

[10] Batzner et al. NequIP (Nature Communications 2022).

What it says: Strong accuracy and data efficiency using E(3)-equivariant networks in atomistic modeling.

Why it matters here: Evidence that symmetry priors reduce data needs—useful when experiments are small or expensive.

#### C. Physics-Structured Learning (conservation & mechanics)

[11] Greydanus, Dzamba, Yosinski. Hamiltonian Neural Networks (NeurIPS 2019).

What it says: Learn a Hamiltonian so rollouts conserve energy/momentum by construction.

Why it matters here: Shows how architectural structure can stabilize learning in dynamical systems.

[12] Cranmer et al. Lagrangian Neural Networks (ICLR 2020 workshop/related).

What it says: Learn a Lagrangian and derive dynamics from it.

Why it matters here: Complements the above with an alternative, principled route to physics-aware layers.

[13] Lutter, Ritter, Peters. Deep Lagrangian Networks (DeLaN) (ICLR 2019).

What it says: Enforce Euler-Lagrange structure for better generalization in control tasks.

Why it matters here: Signals how to combine structure with gradient-based training in practice.

#### D. Operator Learning & PDE Surrogates

[14] Raissi, Perdikaris, Karniadakis. *Physics-Informed Neural Networks (PINNs) (J. Comput. Phys.* 2019).

What it says: Use PDE residuals directly in the loss to guide learning.

Why it matters here: Lets data and physics work together when ground truth is scarce.

[15] Lu et al. DeepONet (Nature Machine Intelligence 2021).

What it says: Learn mappings between function spaces (operators), not just numbers.

Why it matters here: A flexible way to drop in learned "mini-solvers" beside traditional simulators.

[16] Kovachki et al. Neural Operator (JMLR 2023).

What it says: A comprehensive treatment of operator learning with discretization-invariant goals.

Why it matters here: Theory scaffolding for portable operator blocks across meshes/resolutions.

[17] Li et al. Fourier Neural Operator (FNO) (NeurIPS 2021; arXiv 2020).

What it says: Learn PDE solution maps in Fourier space; fast and mesh-agnostic.

Why it matters here: Aligns with spectral/FFT features and offers a strong candidate kernel for future acceleration.

#### E. Learned Simulators on Graphs/Meshes

[18] Sanchez-Gonzalez et al. Learning to Simulate with Graph Networks (ICML 2020).

What it says: Particle/graph-based simulators trained directly from rollouts.

Why it matters here: A natural fit for graph IR and multi-rate stepping.

[19] Pfaff et al. MeshGraphNets (2020, arXiv/ML4Eng).

What it says: Mesh-aware GNNs for simulation with adaptive discretization.

Why it matters here: Blueprint for mesh-domain lowering and visual verification.

#### F. Optimization as a Layer (hard constraints inside nets)

[20] Amos, Xu, Kolter. Input-Convex Neural Networks (ICML 2017).

What it says: Architectures guaranteed convex in the right variables.

Why it matters here: Stable "sub-steps" you can embed where guarantees help.

[21] Amos, Kolter. *OptNet* (ICML 2017).

What it says: Differentiate through a quadratic program—optimization as a layer.

Why it matters here: Insert exact constraints without leaving end-to-end training.

[22] Agrawal et al. CVXPY Layers (NeurIPS 2019).

What it says: Disciplined convex programs turned into differentiable layers.

Why it matters here: A practical toolchain for constraint-aware components.

#### **Full Citations**

- 1. Bronstein MM, Bruna J, Cohen T, Veličković P. Geometric Deep Learning: Grids, Groups, Graphs, Geodesics, and Gauges. 2021.
- 2. Bronstein MM, Bruna J, LeCun Y, Szlam A, Vandergheynst P. *Geometric Deep Learning: Going Beyond Euclidean Data*. 2016/2017.
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- 4. Finzi M, Stanton S, Izmailov P, Wilson AG. *Generalizing CNNs for Equivariance to Lie Groups*. ICML, 2020.
- 5. Cohen TS, Weiler M, Kicanaoglu B, Welling M. *Gauge-Equivariant CNNs and the Icosahedral CNN*. ICML, 2019.
- 6. Fuchs FB, Worrall DE, Fischer V, Welling M. SE(3)-Transformers. NeurIPS, 2020.
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- 8. Satorras VG, Hoogeboom E, Welling M. *E(n) Equivariant Graph Neural Networks*. ICML, 2021.

- 9. Cohen TS, Geiger M, Weiler M. A General Theory of Equivariant CNNs on Homogeneous Spaces. NeurIPS, 2019.
- 10.Batzner SL, Musaelian A, Sun L, et al. *E*(3)-equivariant GNNs for Interatomic Potentials. *Nature Communications*, 2022.
- 11. Greydanus S, Dzamba M, Yosinski J. Hamiltonian Neural Networks. NeurIPS, 2019.
- 12. Cranmer M, Greydanus S, Hoyer S, et al. *Lagrangian Neural Networks*. ICLR 2020 workshop/related.
- 13.Lutter M, Ritter C, Peters J. Deep Lagrangian Networks. ICLR, 2019.
- 14. Raissi M, Perdikaris P, Karniadakis GE. *Physics-Informed Neural Networks*. *Journal of Computational Physics*, 2019.
- 15.Lu L, Jin P, Pang G, Zhang Z, Karniadakis GE. DeepONet. Nature Machine Intelligence, 2021.
- 16.Kovachki NB, Li Z, Liu B, et al. Neural Operator. JMLR, 2023.
- 17.Li Z, Kovachki NB, Azizzadenesheli K, et al. *Fourier Neural Operator*. NeurIPS 2021 (arXiv 2020).
- 18. Sanchez-Gonzalez A, Godwin J, Pfaff T, et al. *Learning to Simulate with Graph Networks*. ICML, 2020.
- 19.Pfaff T, Fortunato M, Sanchez-Gonzalez A, Battaglia P. *Learning Mesh-Based Simulation with Graph Networks*. 2020 (arXiv/ML4Eng).
- 20.Amos B, Xu L, Kolter JZ. Input-Convex Neural Networks. ICML, 2017.
- 21.Amos B, Kolter JZ. OptNet: Differentiable Optimization as a Layer in Neural Networks. ICML, 2017.
- 22. Agrawal A, Amos B, Barratt S, et al. *Differentiable Convex Optimization Layers*. NeurIPS, 2019.

**How to read this page:** Start with A/B to see why the system is geometry-native; jump to C/D for physics and operators if you're coming from simulation; visit F when constraints/safety are central.