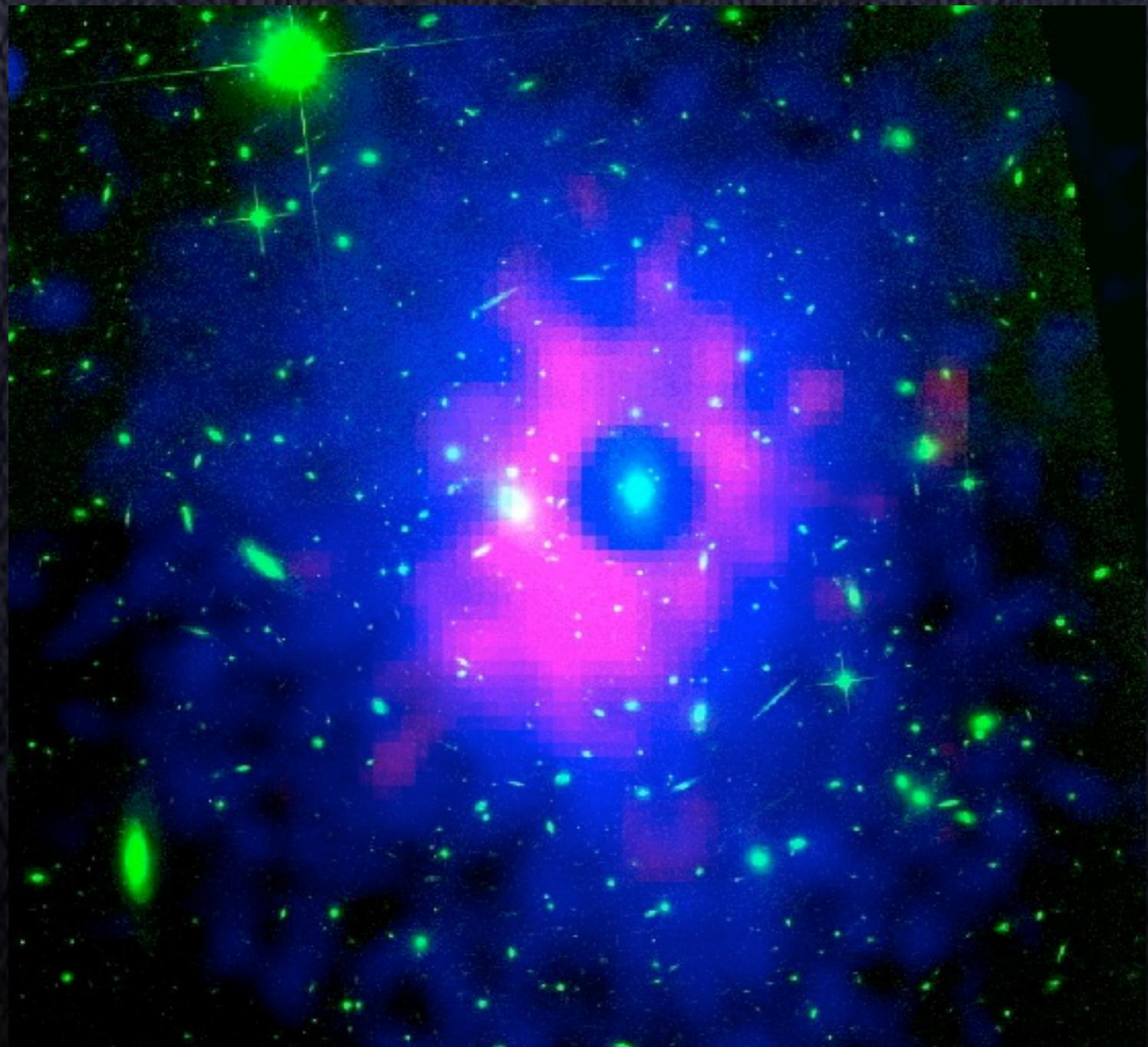


# Probing Cluster Masses with Gravitational Lensing

Sanghamitra Deb  
ANL

**Collaborators:** Prof. David M. Goldberg (Drexel University), Prof. Kristian Pedersen (DARK, Copenhagen), Dr. Andrea Morandi (DARK, Copenhagen & Univ. of Tel Aviv.), Dr. Marceau Limousin (LAM Marseille), Dr. Hakon Dahle (Univ. of Oslo), Dr. Signe Riemer-Sørensen (DARK, Copenhagen), Dr. Catherine Heymans (University of Edinburgh, IfA Royal Observatory), Dr. Reiko Nakajima (UC Berkeley), Dr. Rachel Mandelbaum (Princeton University), Prof. Gary Bernstein (University of Pennsylvania)

# Observing Clusters



galaxies: HST, optical observations

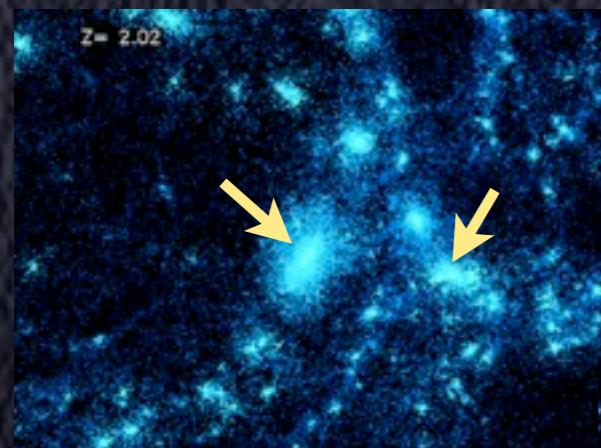
gas: Xray observations

gas: Sunyaev Zeldovich Effect

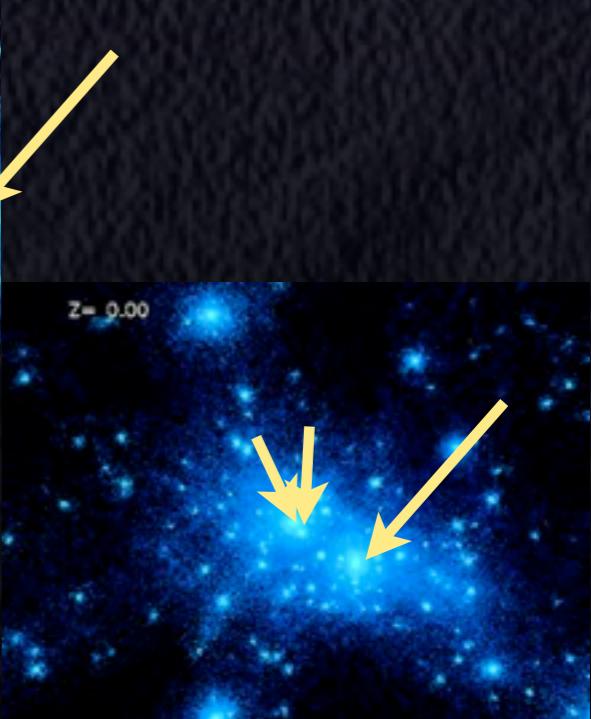
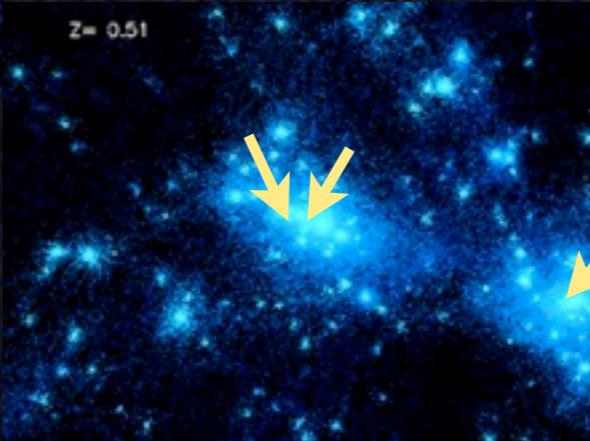
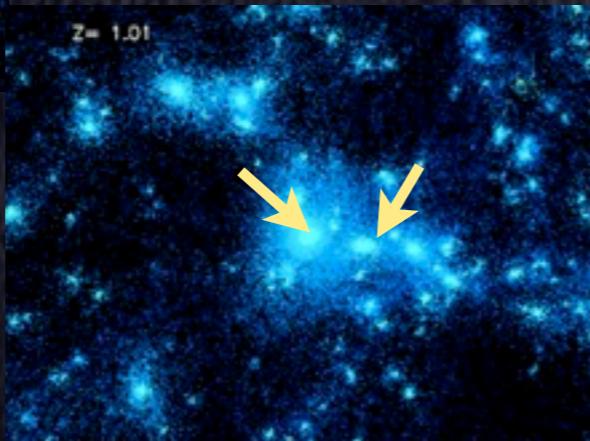
Galaxy Cluster RXJ1347-1145

<http://chile1.physics.upenn.edu/gbtpublic/>

# Substructure: Elliptical Halos

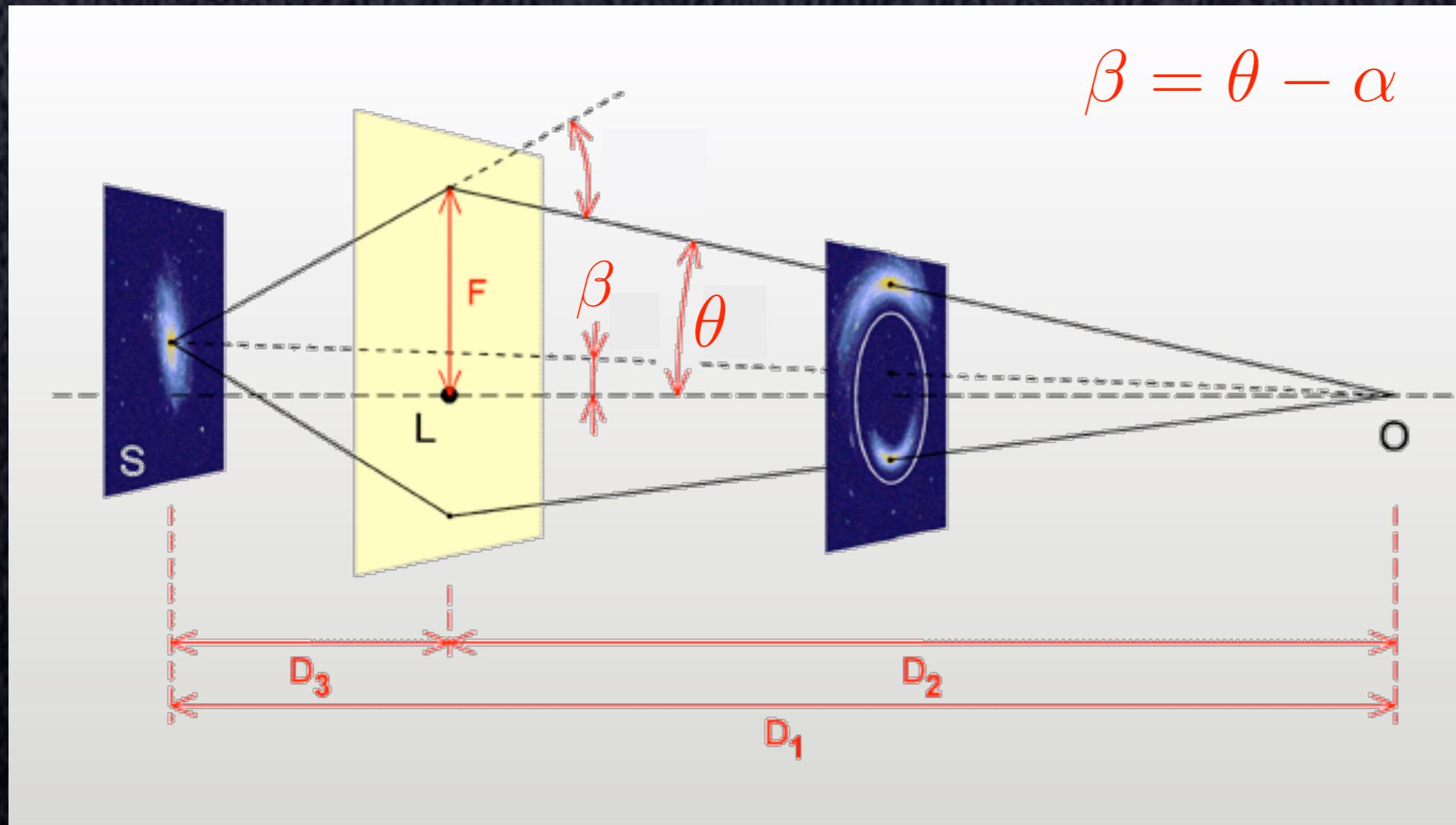


What is the distribution of cluster ellipticity?



How does the distribution and alignment vary with redshift & mass?

# Gravitational Lensing



**Dimension less  
surface mass  
density**

$$\kappa = \frac{\sum}{\sum_{cr}}$$

**Gravitational Lensing is co-ordinate transformation between the foreground ( $\Theta$ ), and background positions( $\beta$ )**

# Shape Distortions

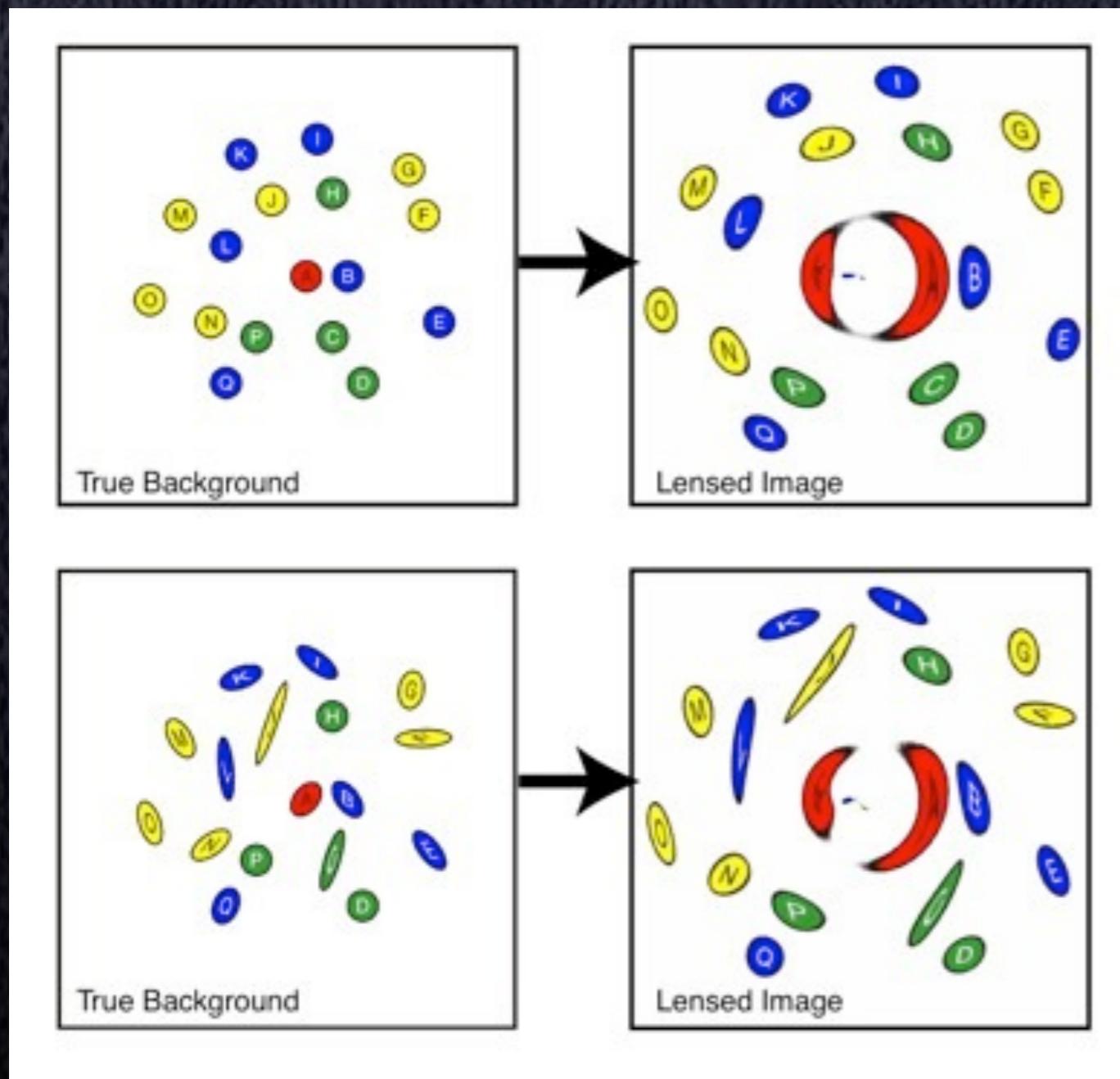
$$\kappa = (\psi_{,11} + \psi_{,22})/2$$

$$\gamma_1 = (\psi_{,11} - \psi_{,22})/2$$

$$\gamma_2 = \psi_{,12}$$

**Distortion Observables are  
Measured Ellipticities.  
For semi-strong regime:  $g = \gamma / (1 - \kappa)$**

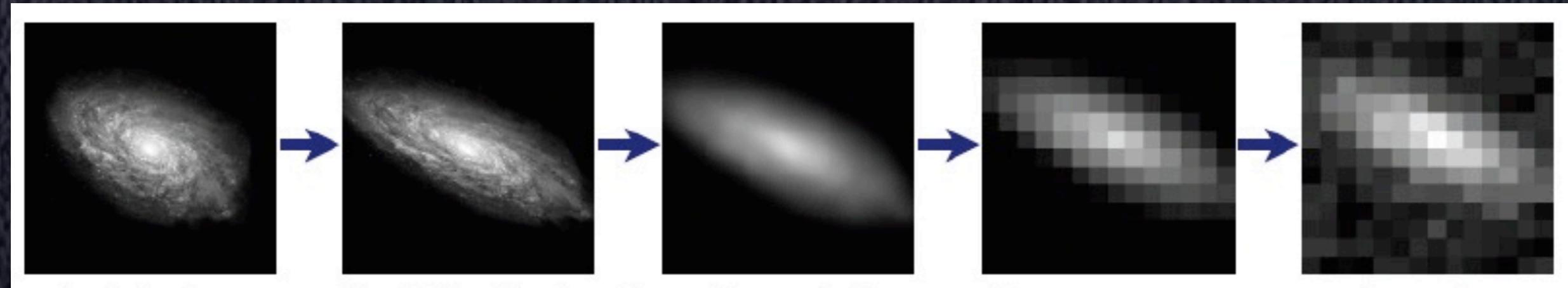
# Weak Lensing



**Weak lensing is a statistical measure of the distortion of background galaxies due to the intervening mass.**

Williamson et al. 2007.

# The shear signal



Intrinsic galaxy  
(shape unknown)

Gravitational lensing  
causes a **shear (g)**

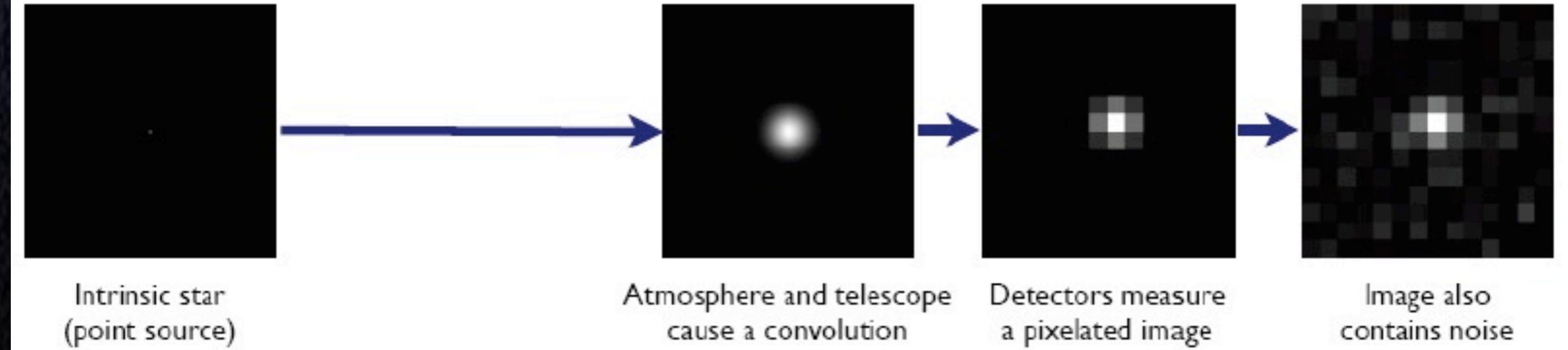
Atmosphere and telescope  
cause a convolution

Detectors measure  
a pixelated image

Image also  
contains noise

**Stars:** Point sources to star images:

PSF



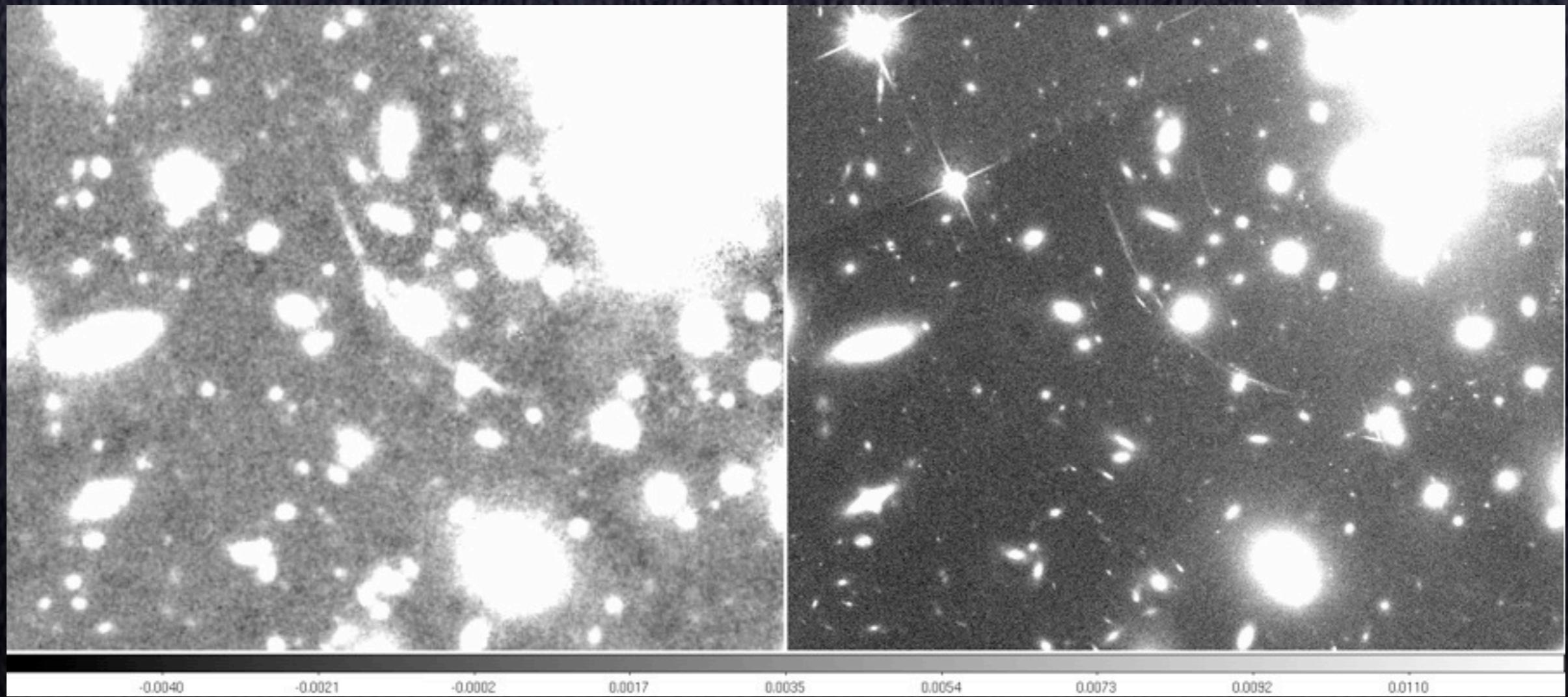
Intrinsic star  
(point source)

Atmosphere and telescope  
cause a convolution

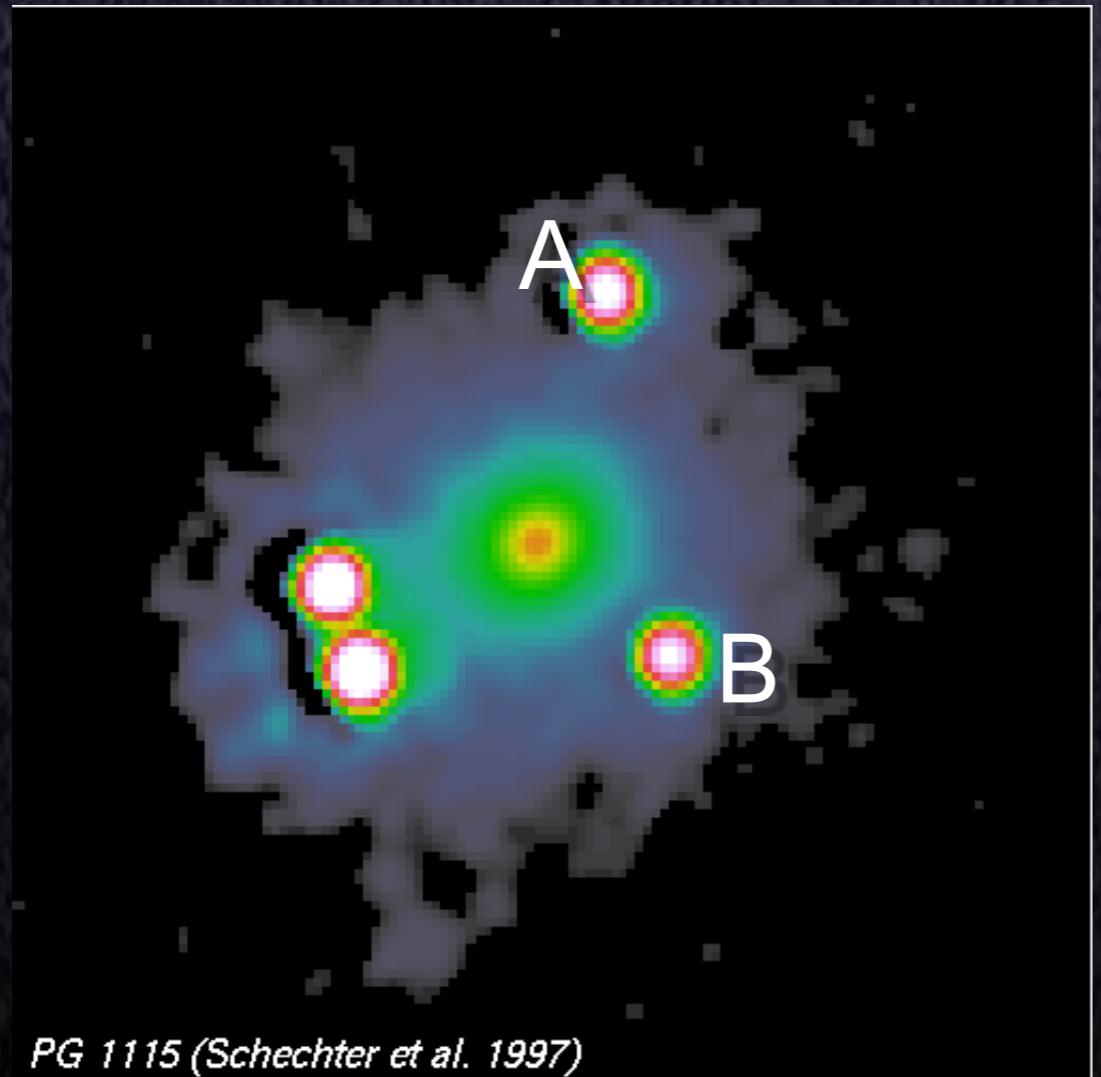
Detectors measure  
a pixelated image

Image also  
contains noise

# Comparison of Space vs Ground: A1689



# Strong Lensing

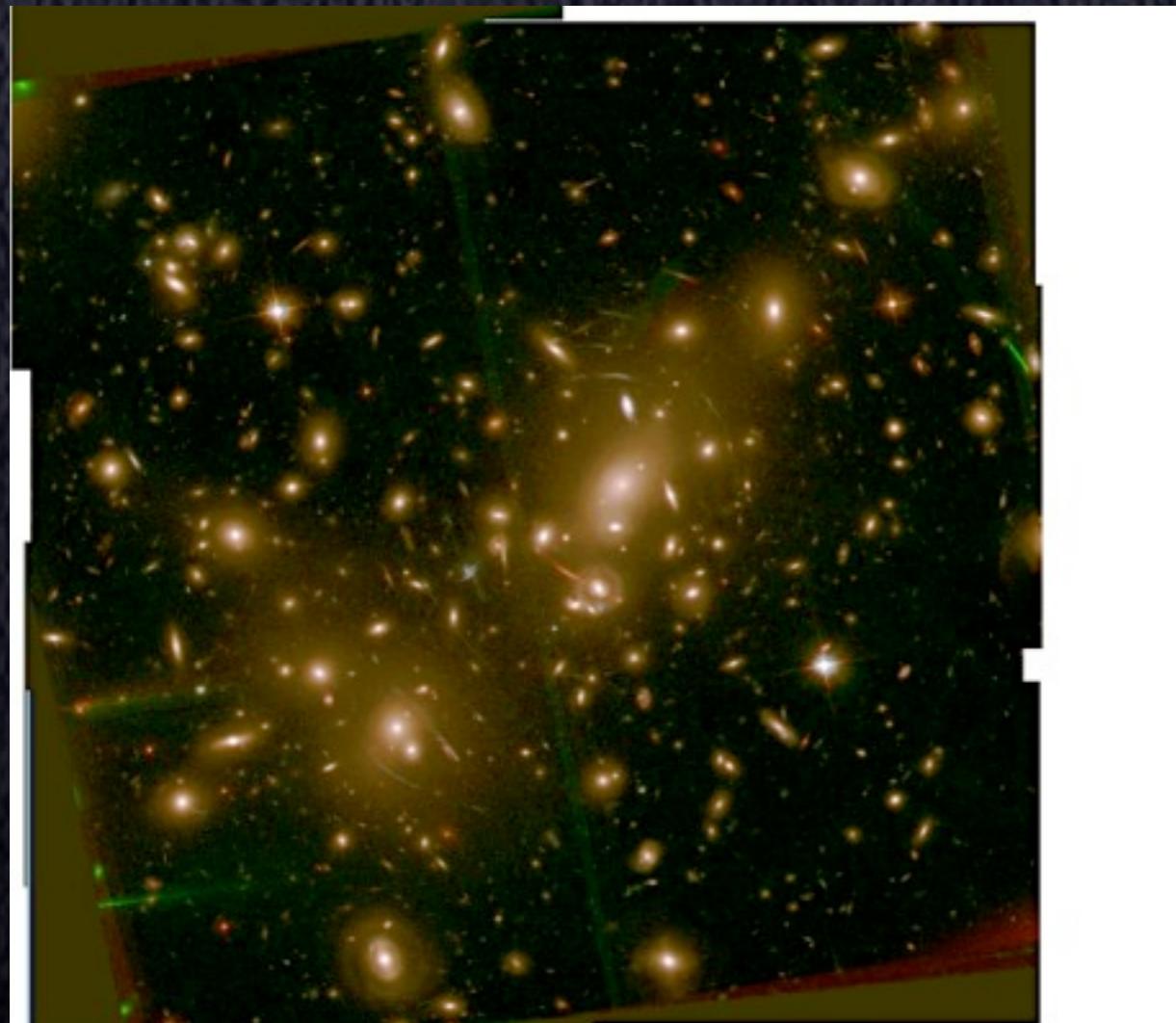


PG 1115 (Schechter et al. 1997)

$$\alpha_i = \psi_{,i}$$

$$\alpha_A - \alpha_B = \theta_A - \theta_B$$

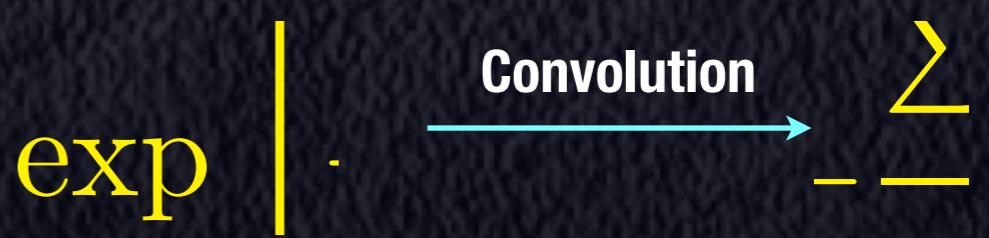
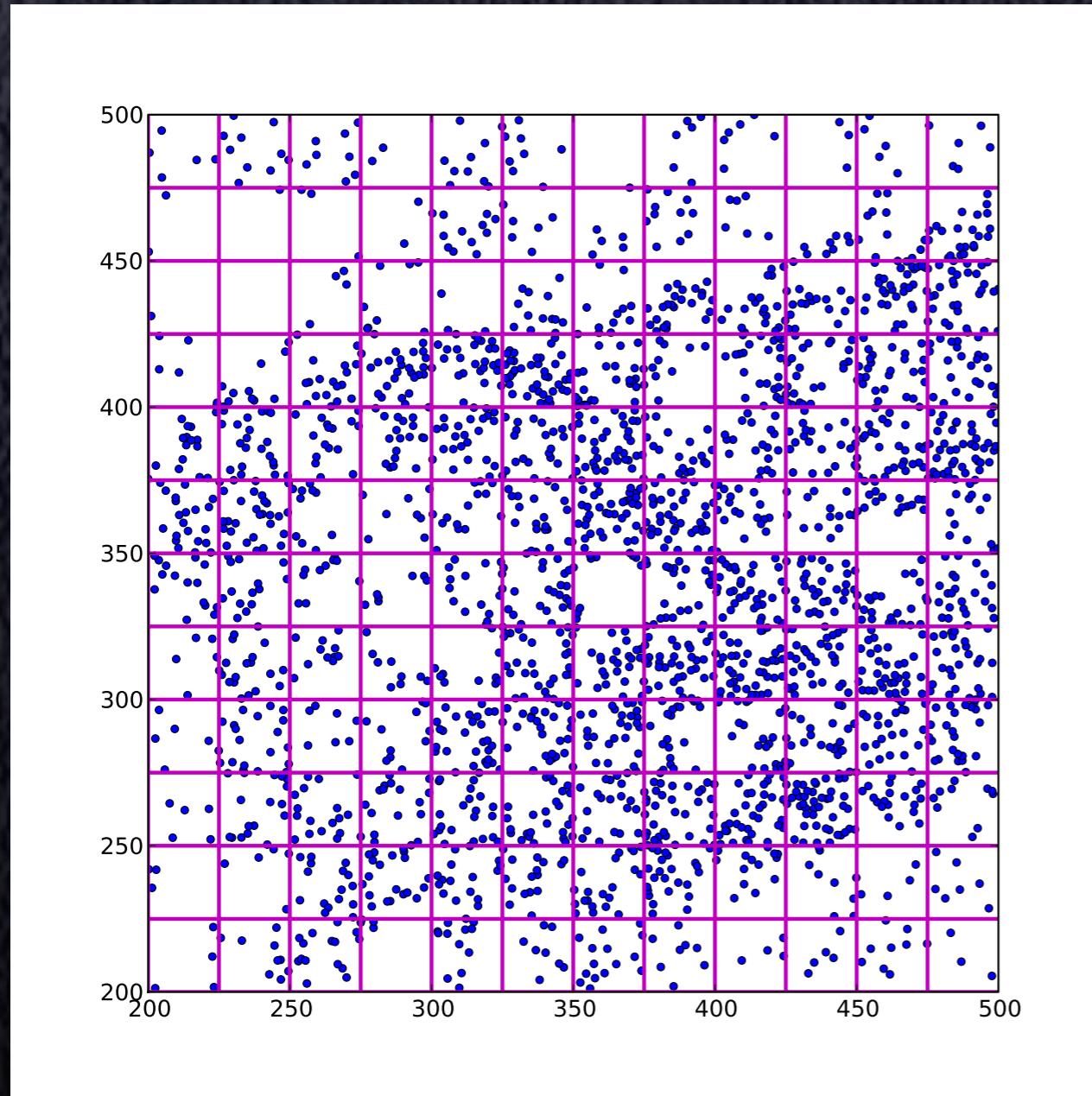
# Parametric technique



**Assumption: Light traces mass**

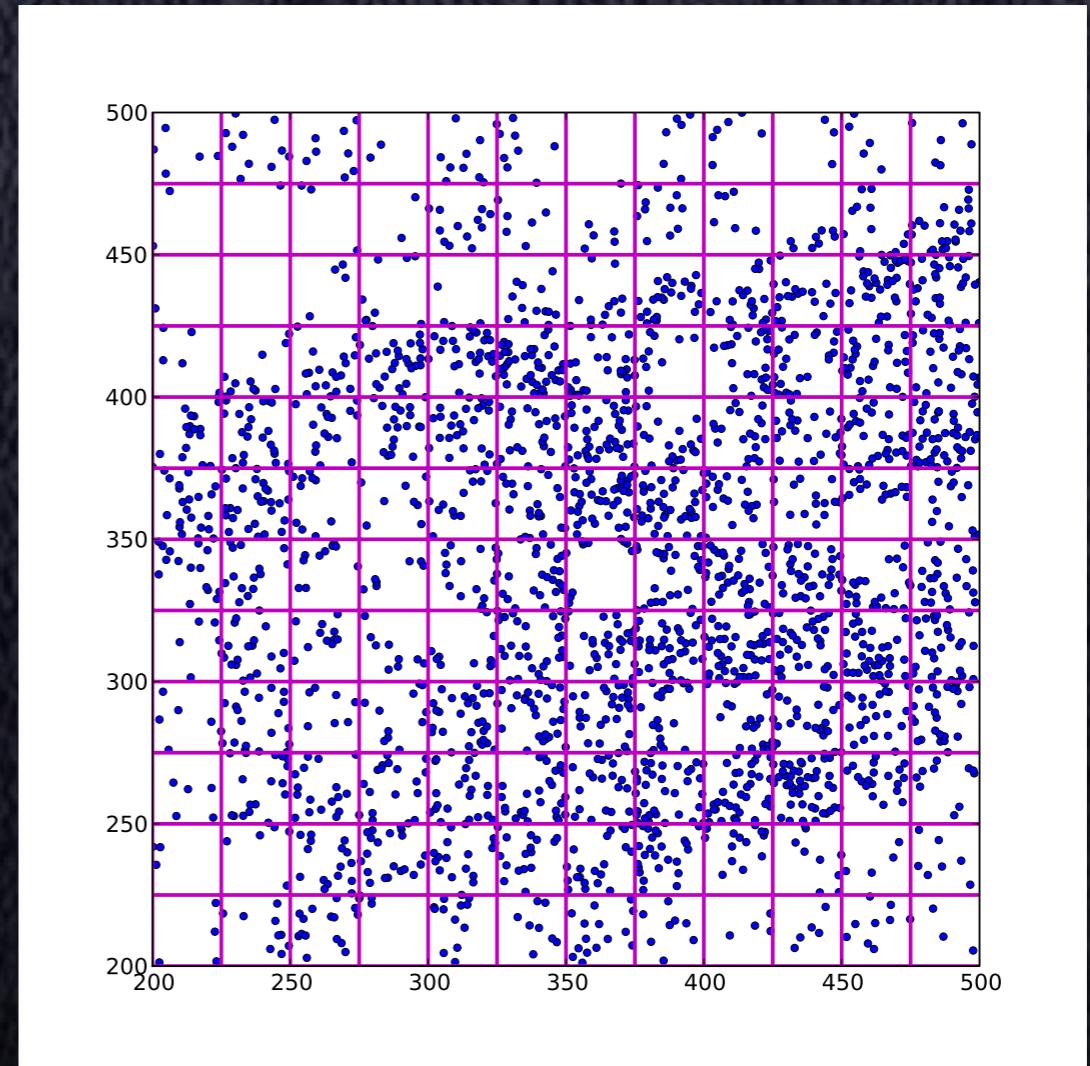
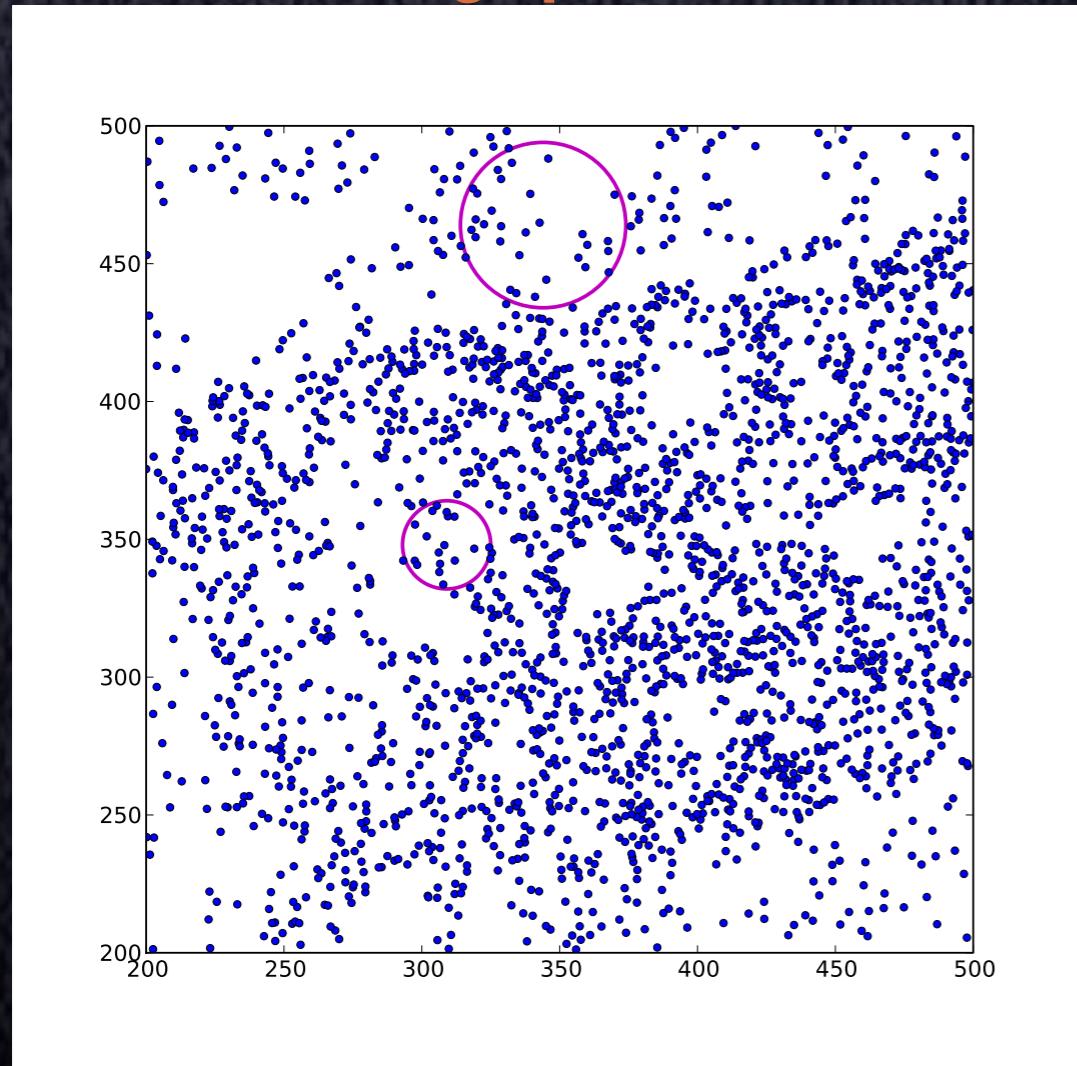
- Place galaxy sized halos at the location of Cluster Members.
- Have one or more dark matter halos with free parameters that are fit from data.

# Grid Based Lensing



# Particle Based Lensing

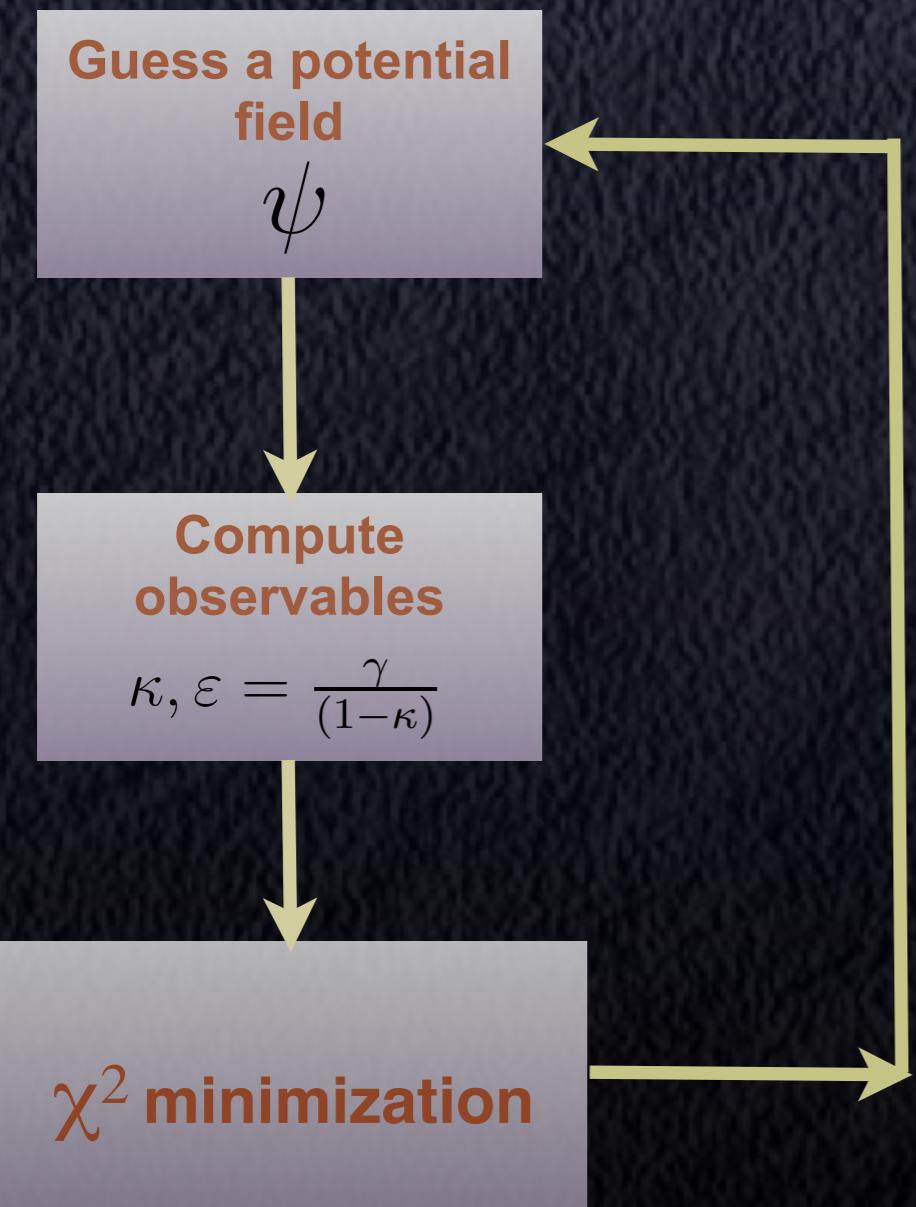
Particles-> lensed  
image positions



- Variable Resolution with the same complexity as finite differencing on a regular grid.
- No empty grid cells.

# Reconstruction Procedure

Keep Iterating ...



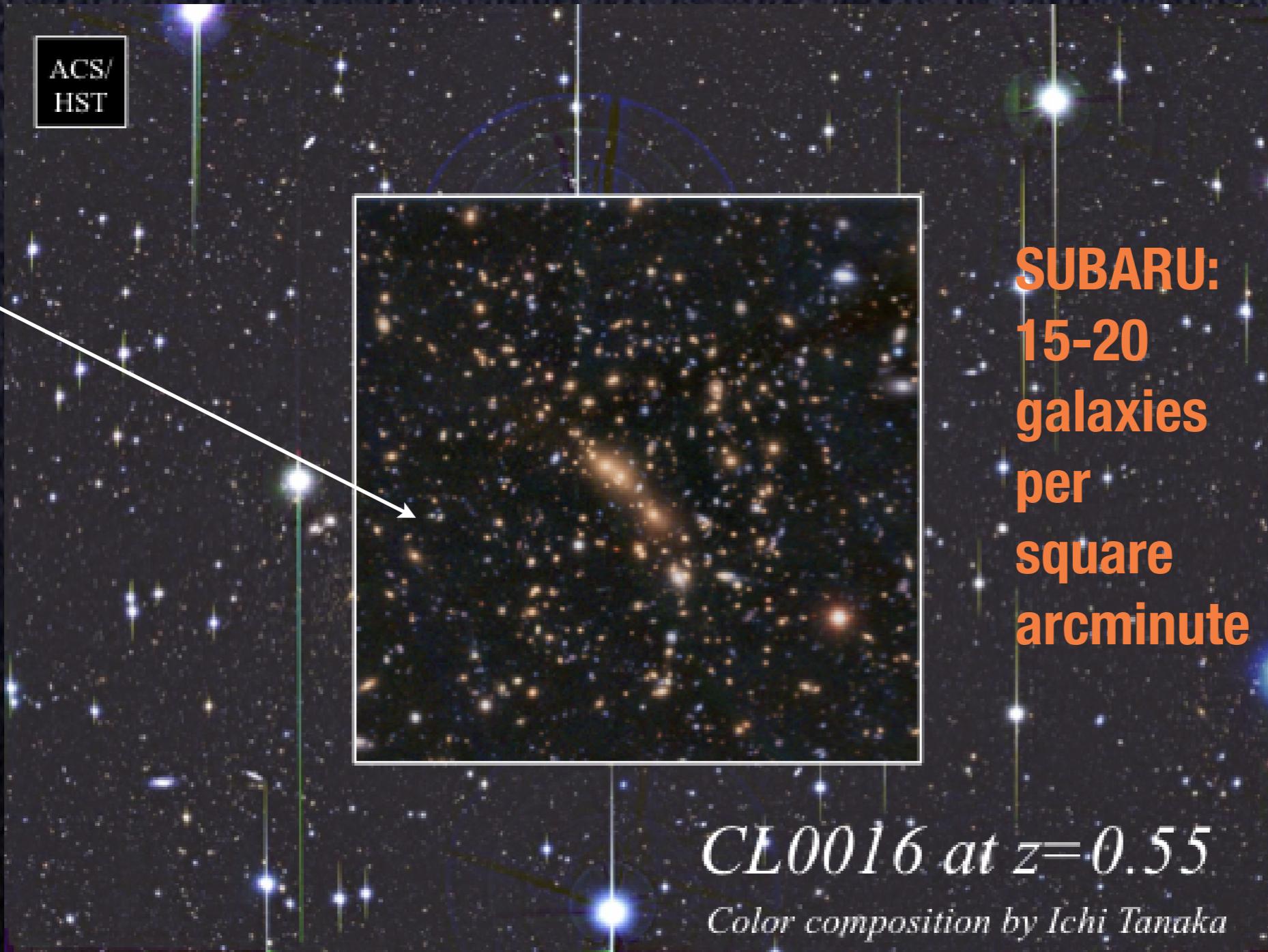
$$\chi_{\text{weak}}^2 = \sum_i \frac{\left[ \varepsilon_i - \frac{\gamma_i}{(1-\kappa_i)} \right]^2}{\sigma_i^2}$$

In case of weak lensing, a  $\chi_w^2$  like this will fit best to noisy data

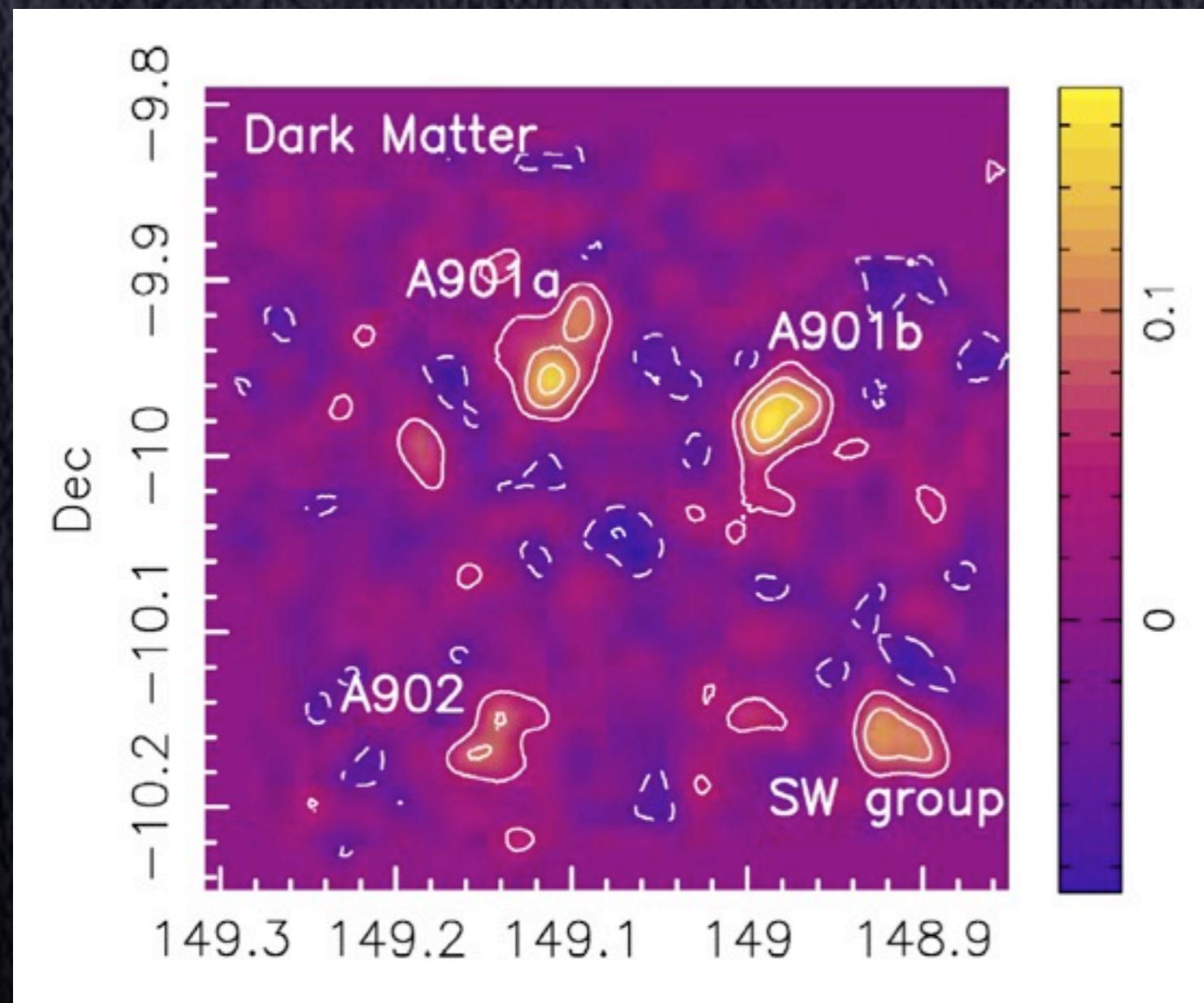
**Smoothing the ellipticity field before minimization and using the full covariance matrix in the minimization**

# Heterogeneous Datasets

HST:  
50-60  
galaxies  
per  
square  
arcminute



# Abell 901/902

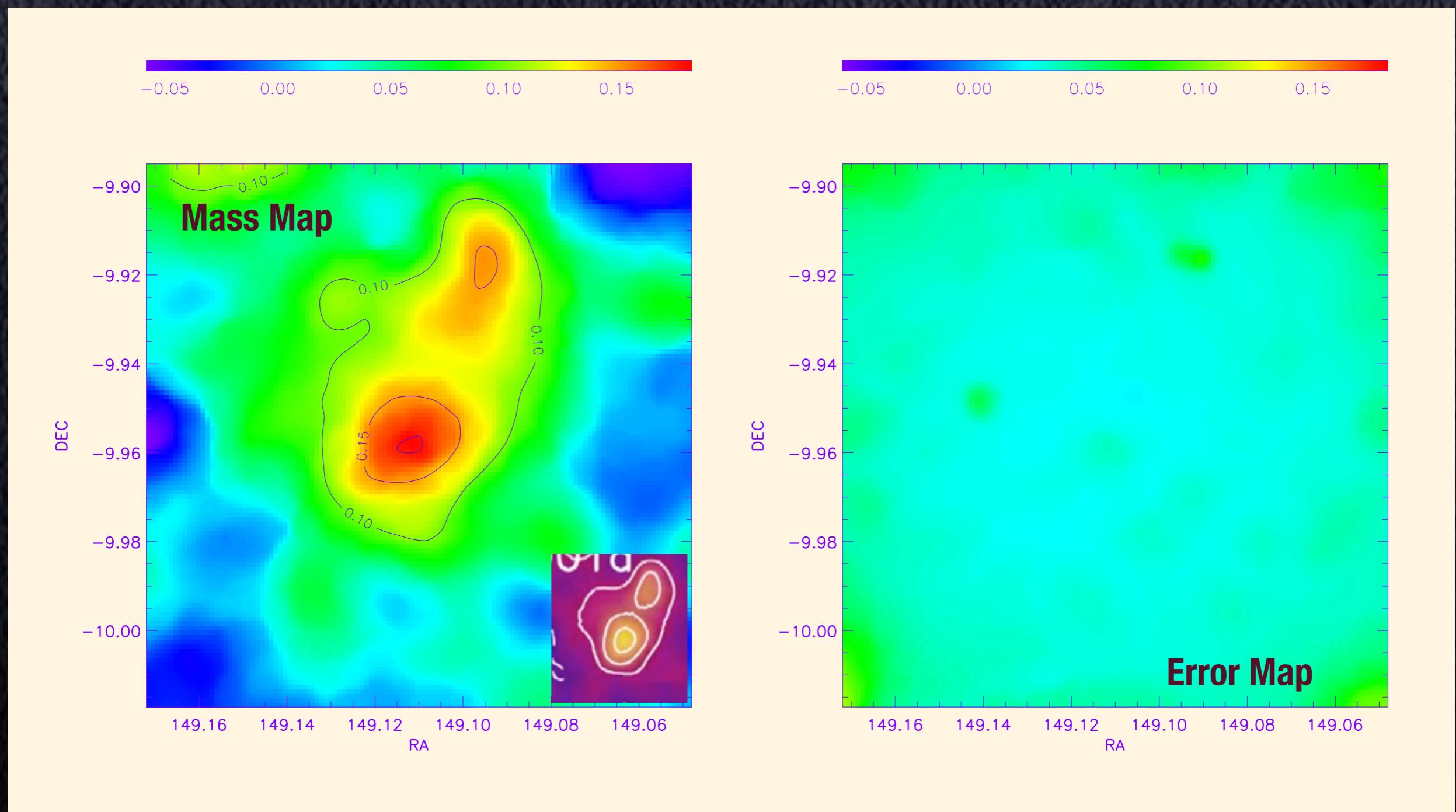


0.5 degree<sup>2</sup> fov  
STAGES HST  
survey  
60,000 background  
images.

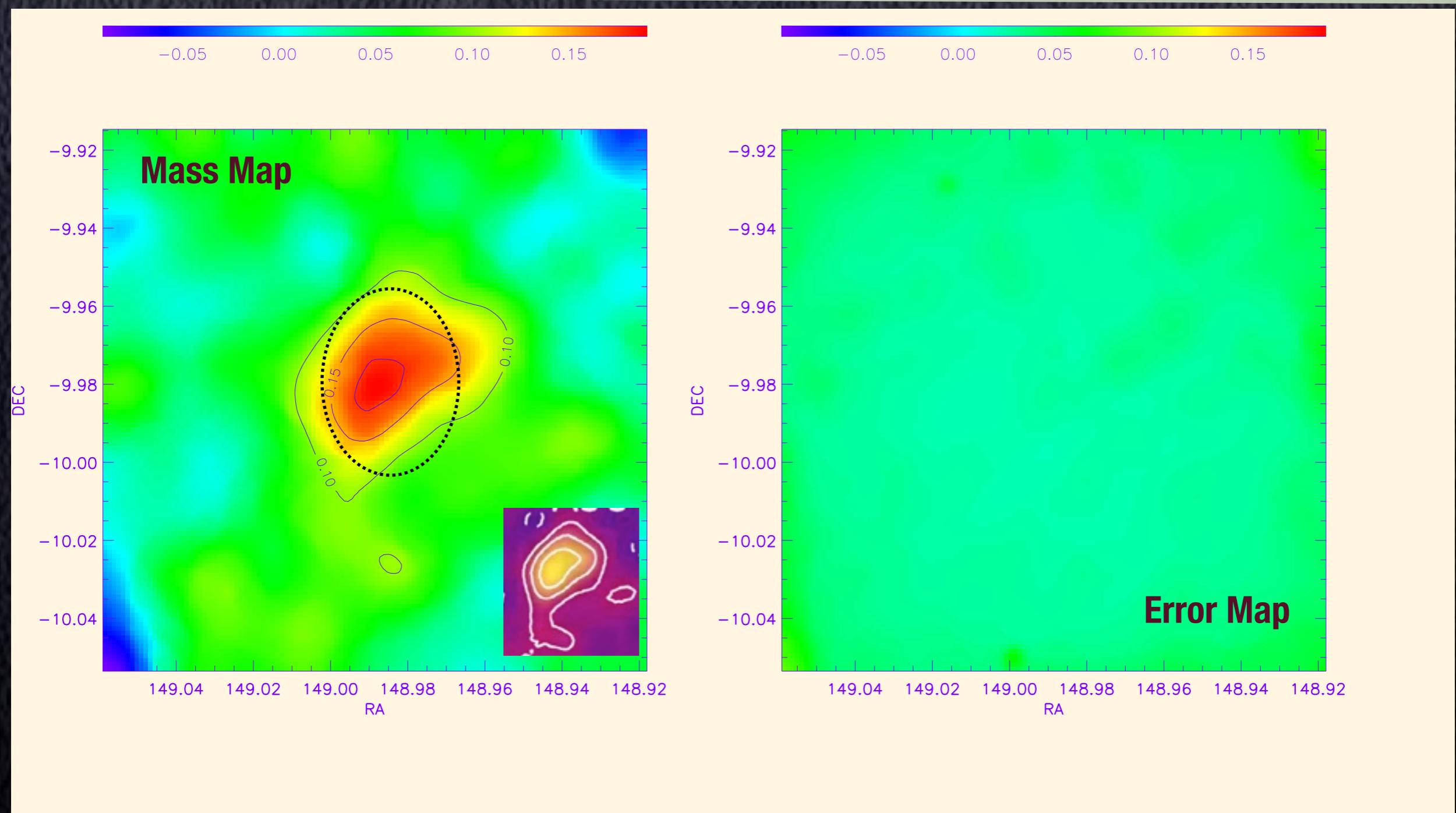
Heymans et. al. 2008.

# A901a

From Deb et al. 2009



# A901b



From Deb et al. 2009

**Axis Ratio      Position angle**

**Non-  
Parametric:**

$$0.37^{+0.1}_{-0.1}$$

$$91.4^{+8.2}_{-8.2}$$

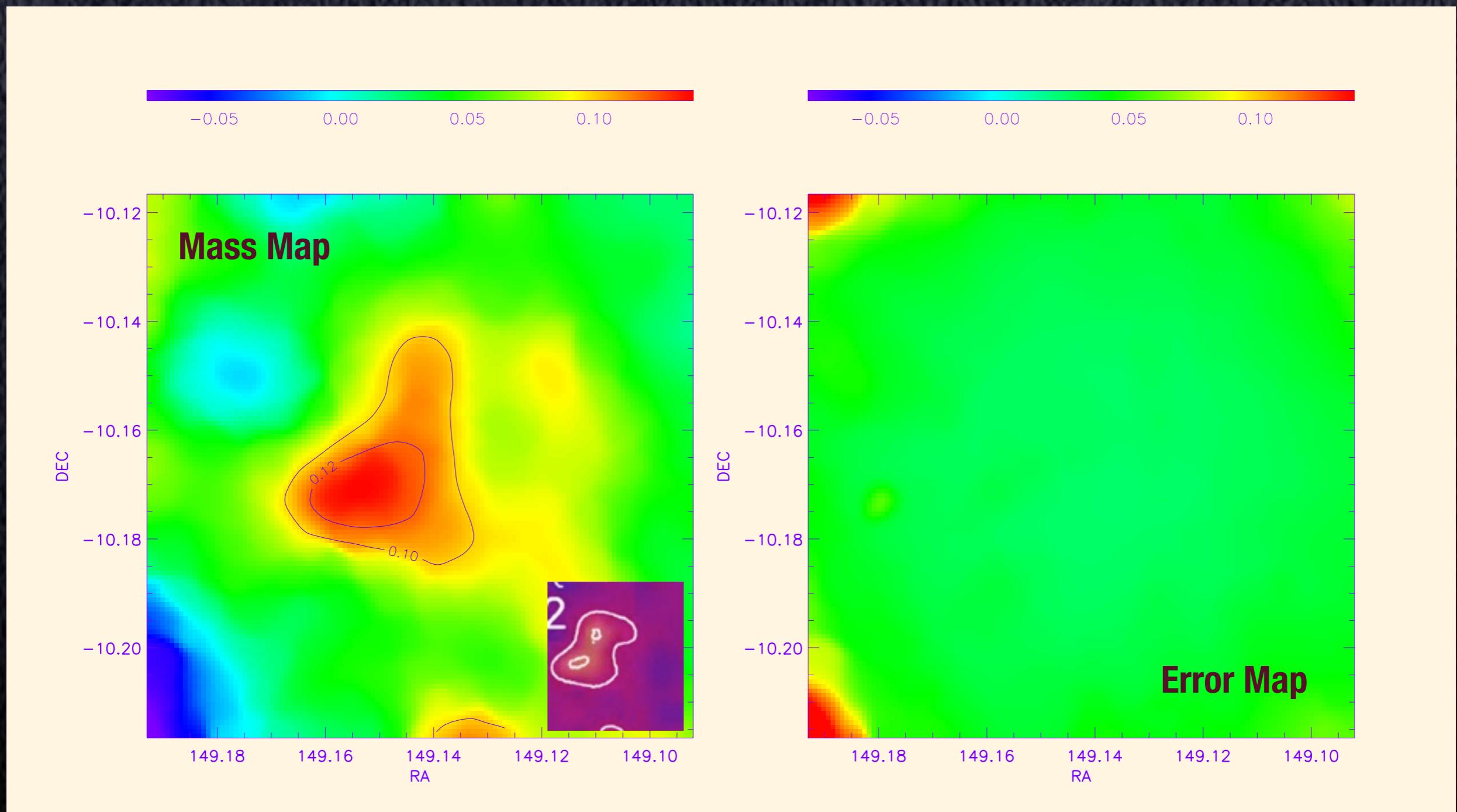
**Parametric:**

$$0.437^{+0.1}_{-0.087}$$

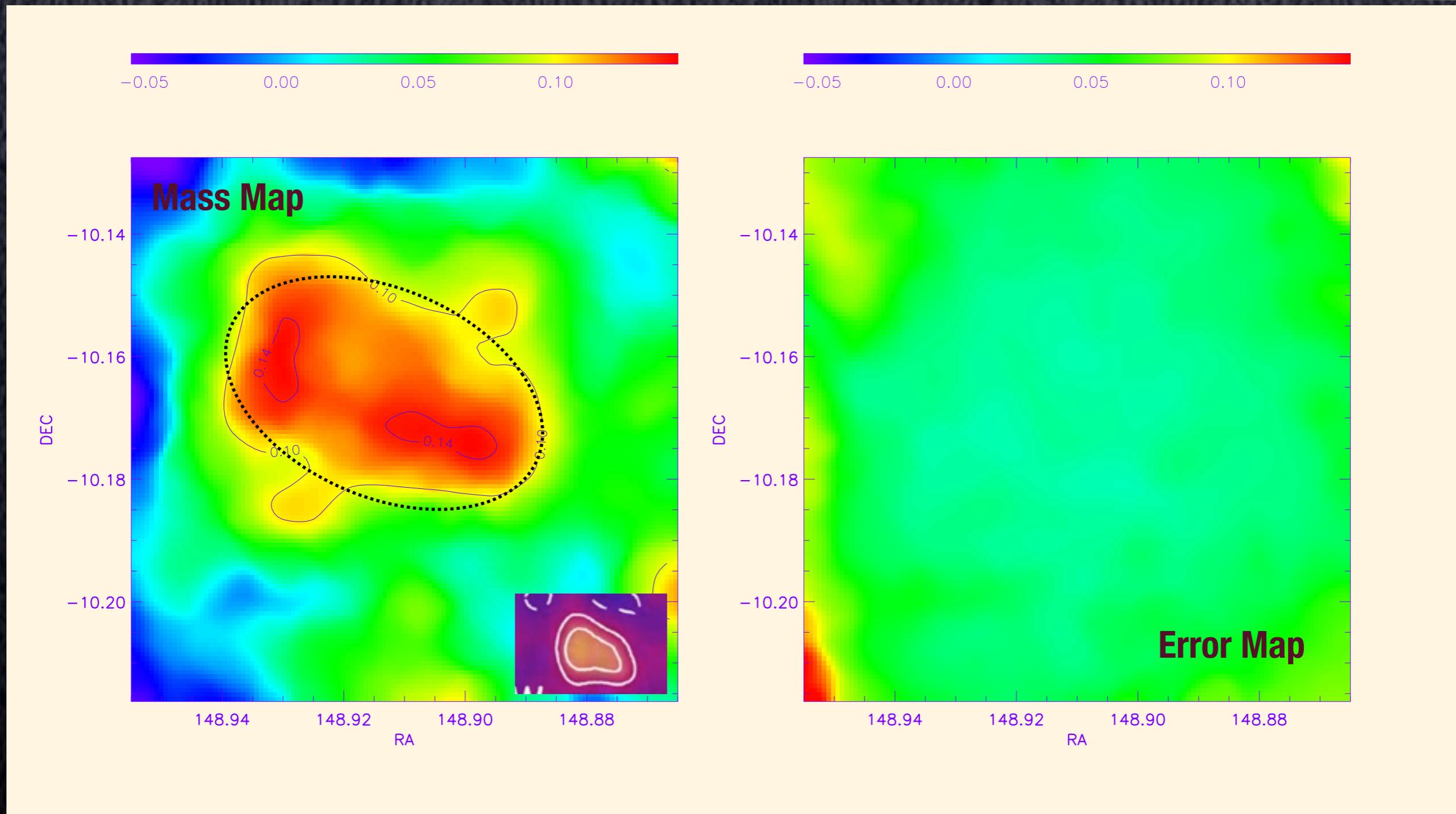
$$90.0^{+2.25}_{-2.25}$$

# A902

From Deb et al. 2009



# Southwest Group



From Deb et al. 2009

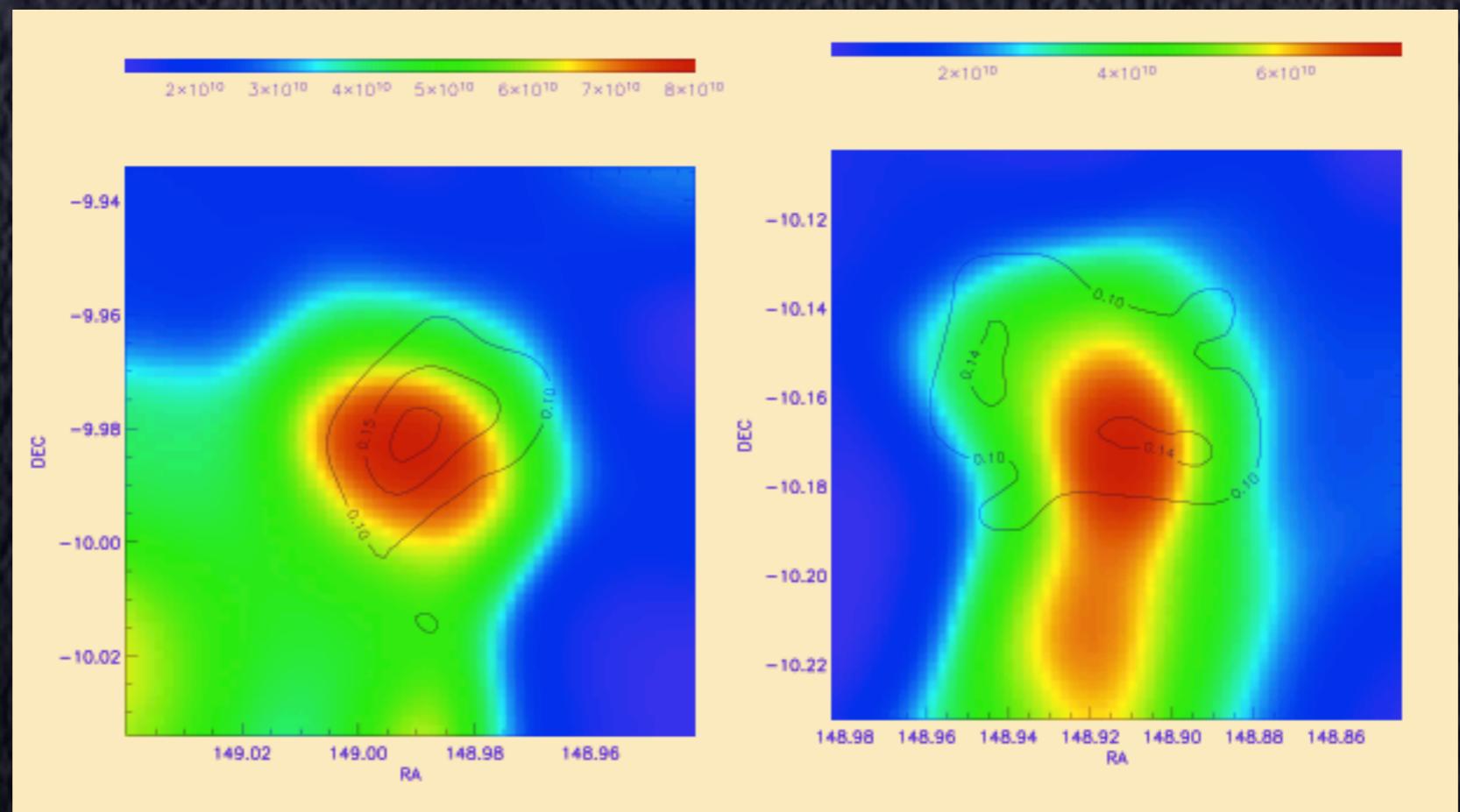
**Axis Ratio      Position angle**

**Non-  
Parametric:**  $0.54^{+0.08}_{-0.09}$      $120.0^{+4.8}_{-4.8}$

**Parametric:**  $0.42^{+0.18}_{-0.12}$      $180.0^{+7.73}_{-5.15}$

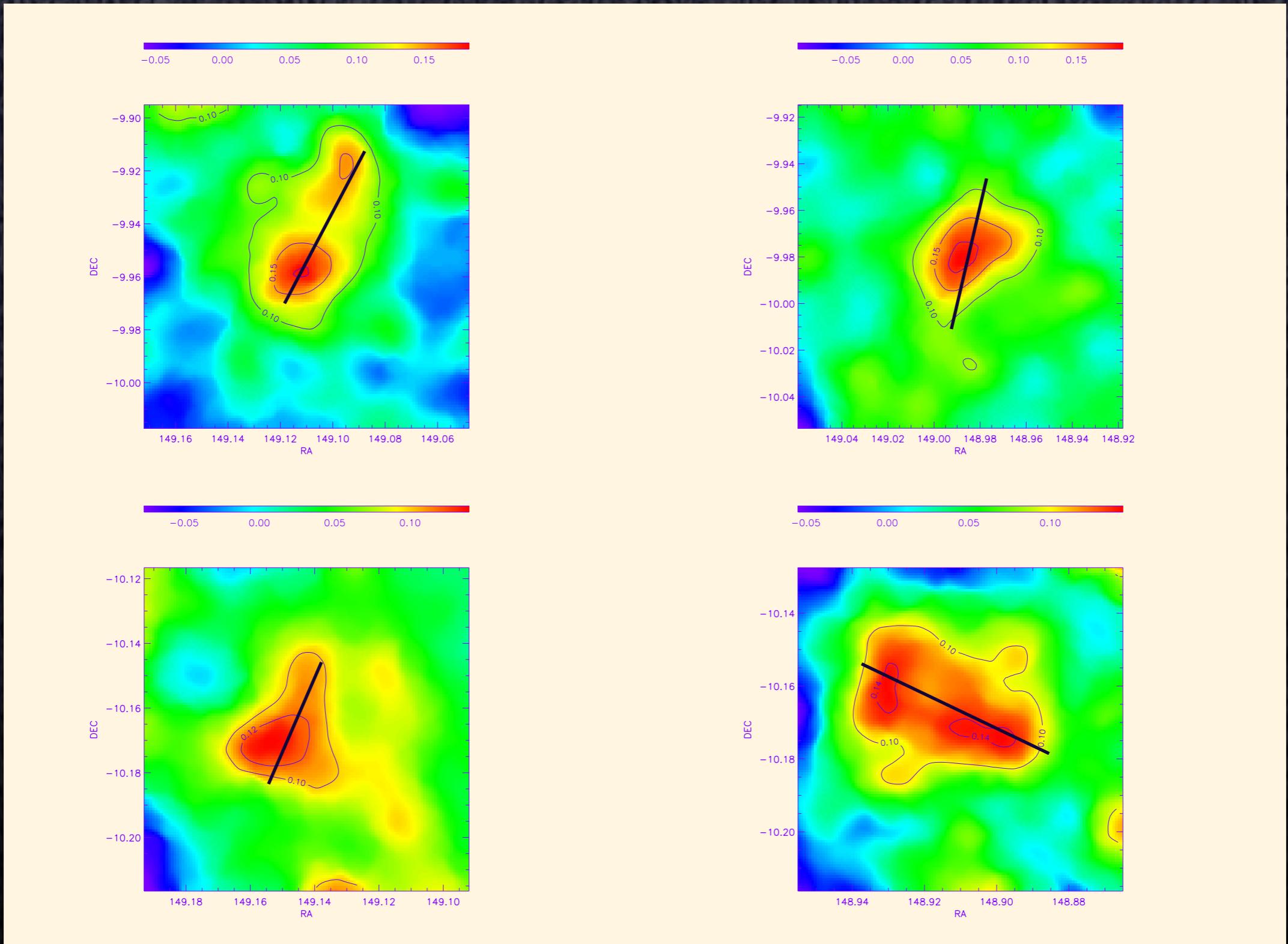
# Dark Matter vs Light

From Deb et al. 2009



# Alignment

From Deb et al. 2009



# Reconstruction Methods

## Parametric: Strong Lensing

GRAVELENS - Keeton et al., 2001

LENSTOOL - Jullo et al., 2007

## Galaxy-Galaxy Lensing

Natarajan et al. 2005

## Hybrid LENSTOOL - Jullo et al., 2009

## Non-Parametric Strong Lensing

Jullo & Kneib 2009,

LENSPERFECT -Coe et al, 2008,2010 (Mesh Free)

## Weak Lensing

Kaiser 1995, Seitz & Schneider 1995-2001

## Strong+Weak Lensing

## Finite Differencing Based

Bradac et al. 2004,

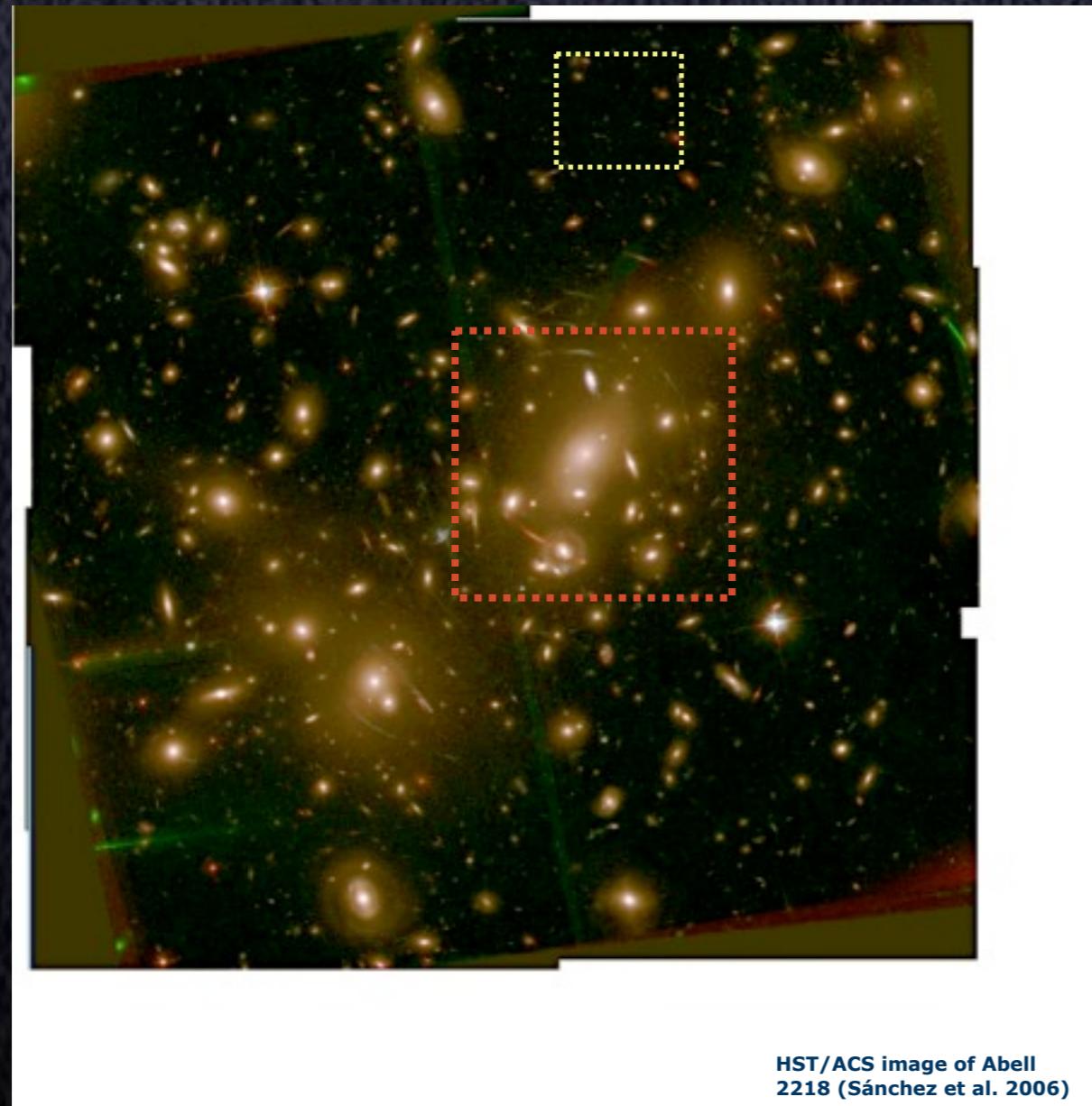
(ADAPTIVE) - Diego et al. , Cacciato et al.

Merten et al., Saha et. al. Pixelens  
and more ....

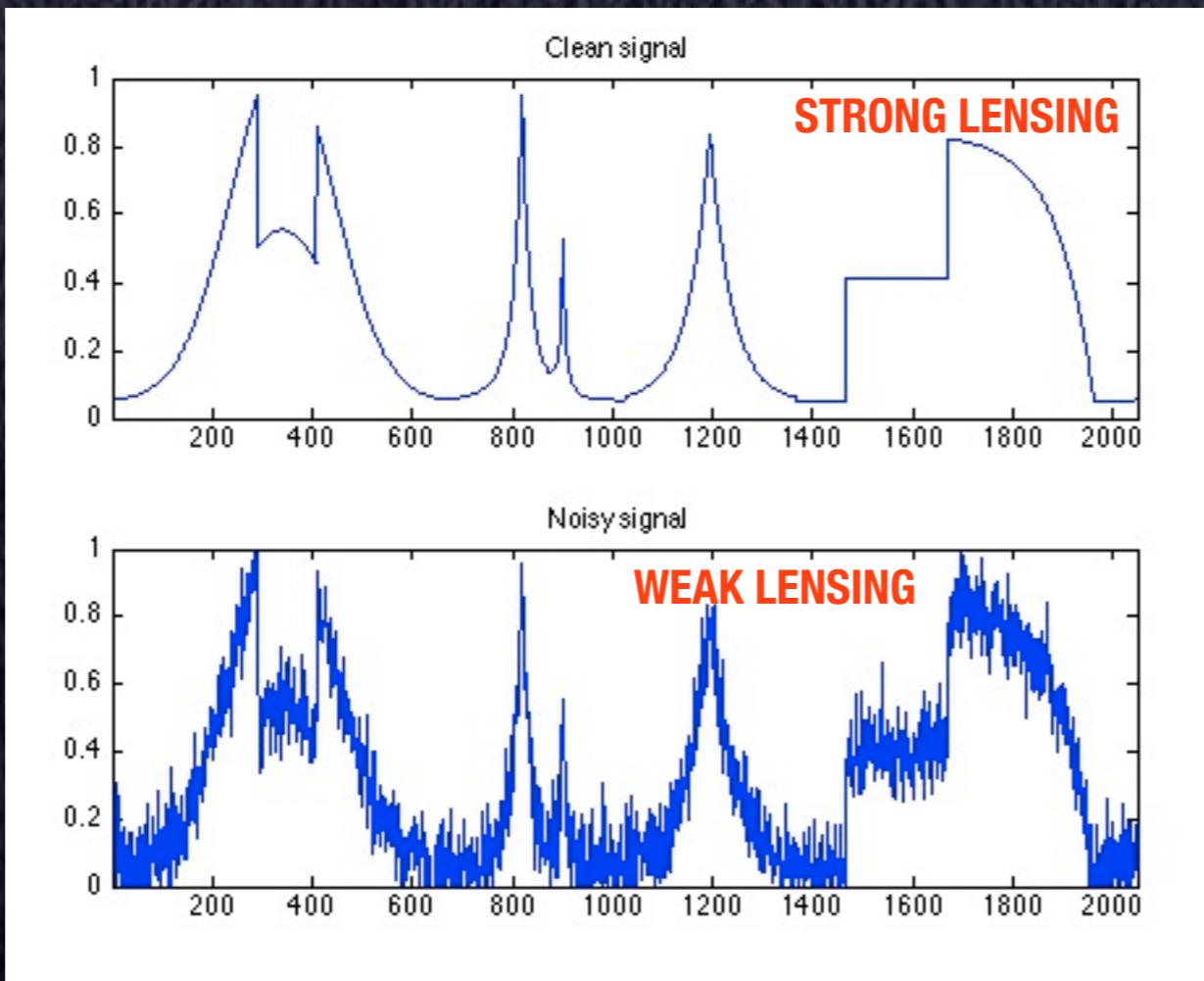
## Mesh-Free Technique Particle Based Lensing (PBL)

Deb et al. ,2008, 2009

# Strong+Weak Lensing: Challenges



# Strong+Weak Lensing



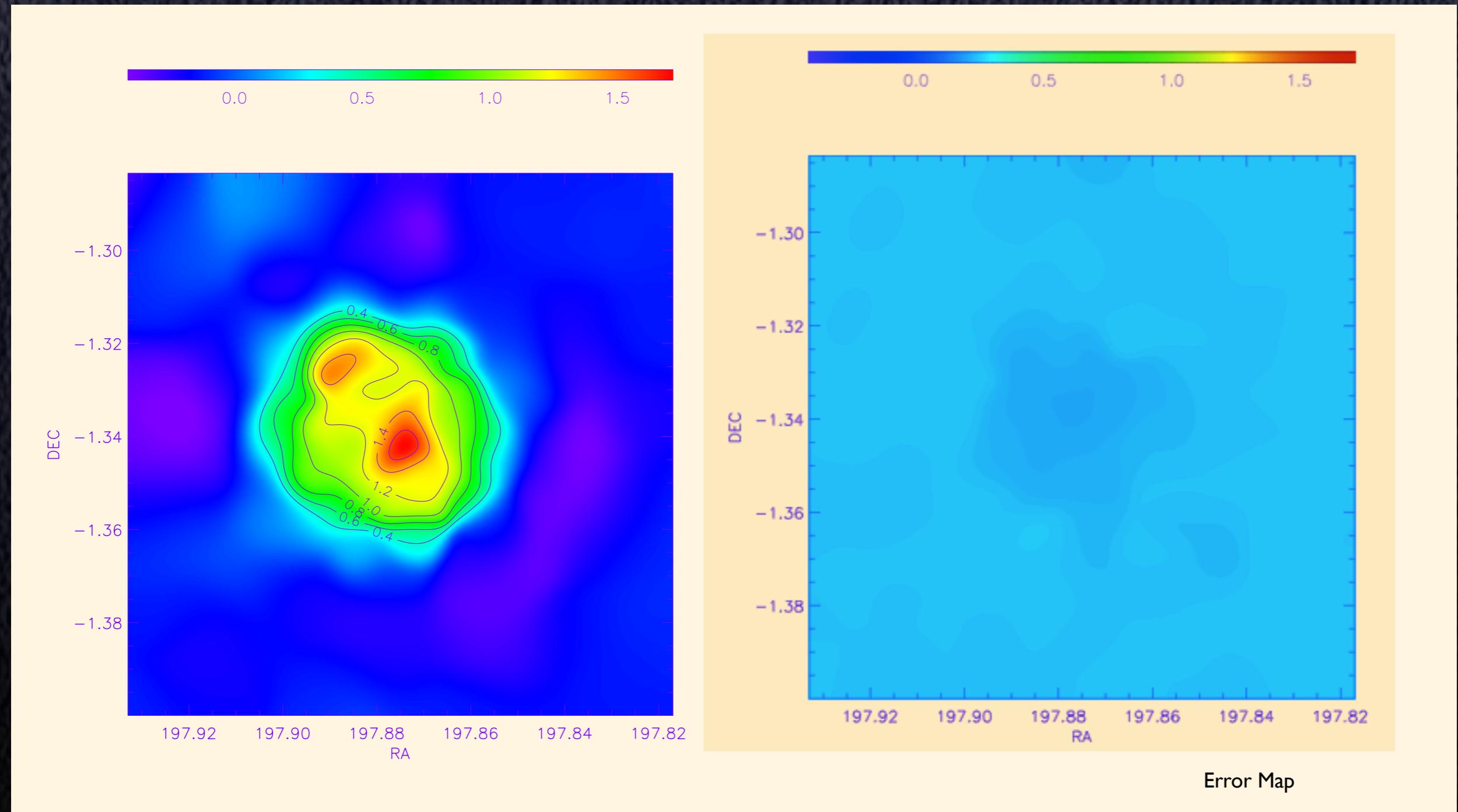
+

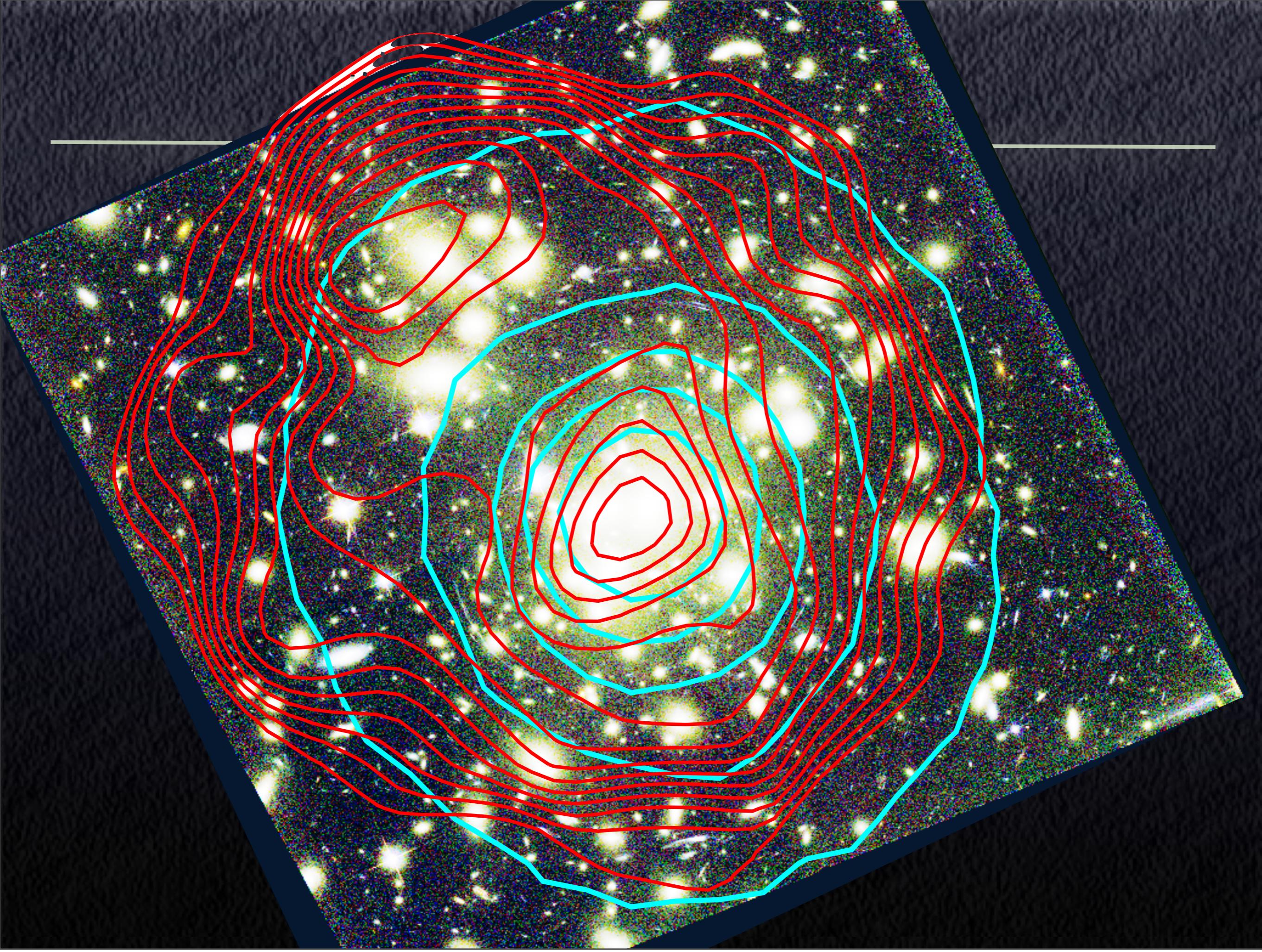
# A1689



<http://chandra.harvard.edu/photo/2008/a1689/>

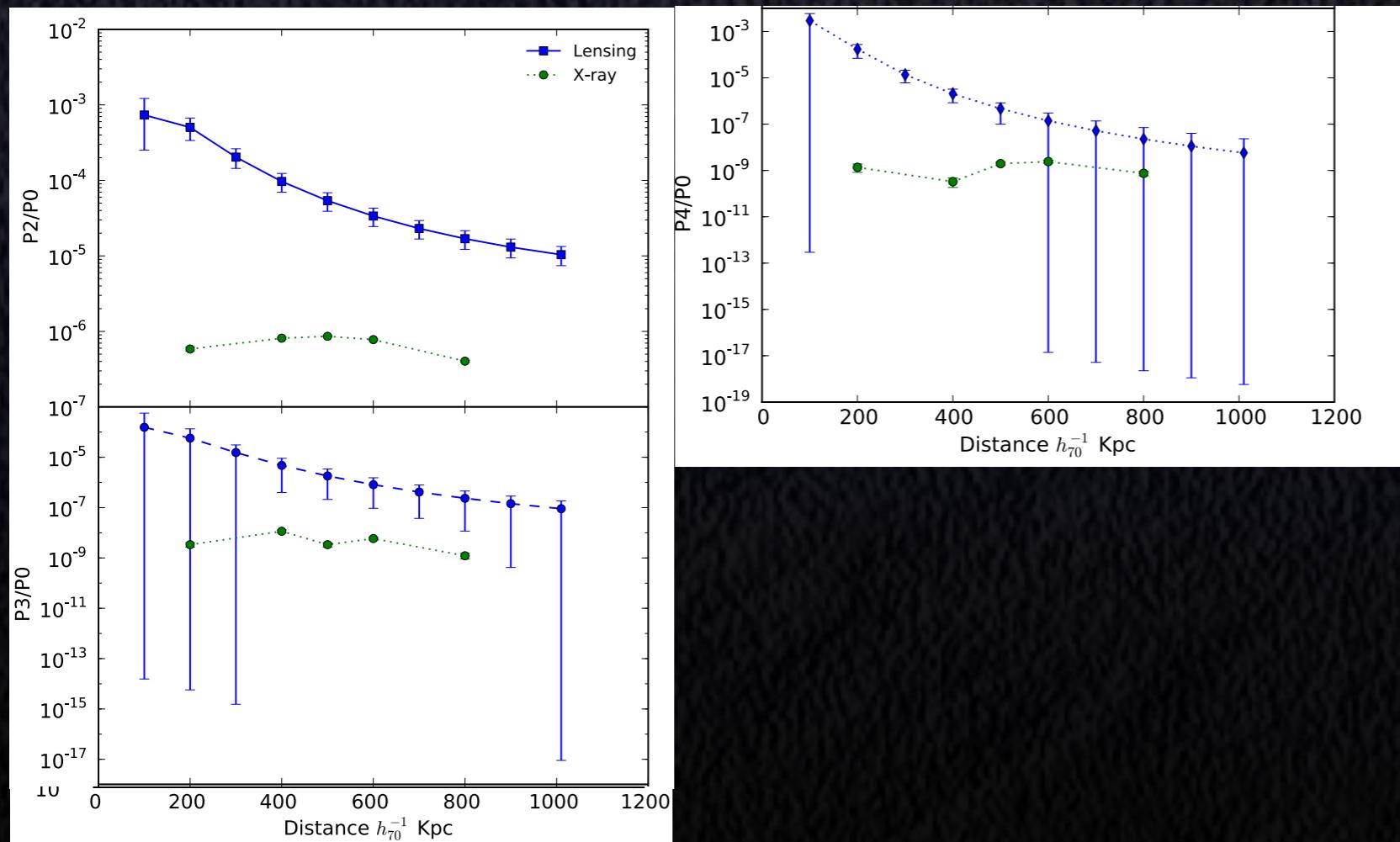
# Mass Map



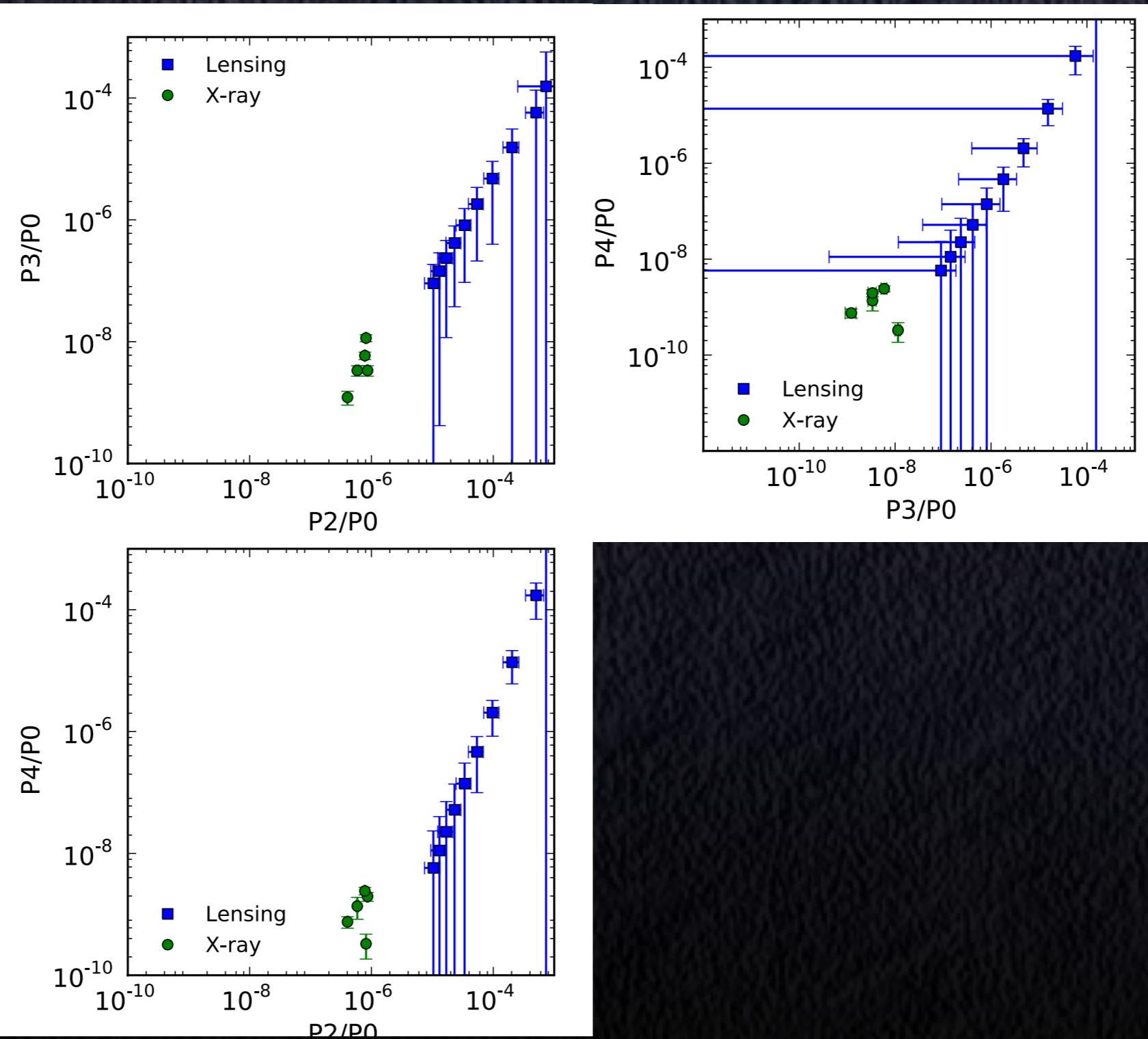


# Power Ratios

Moments of the mass distribution characterize the morphology and substructure in dark matter distribution.

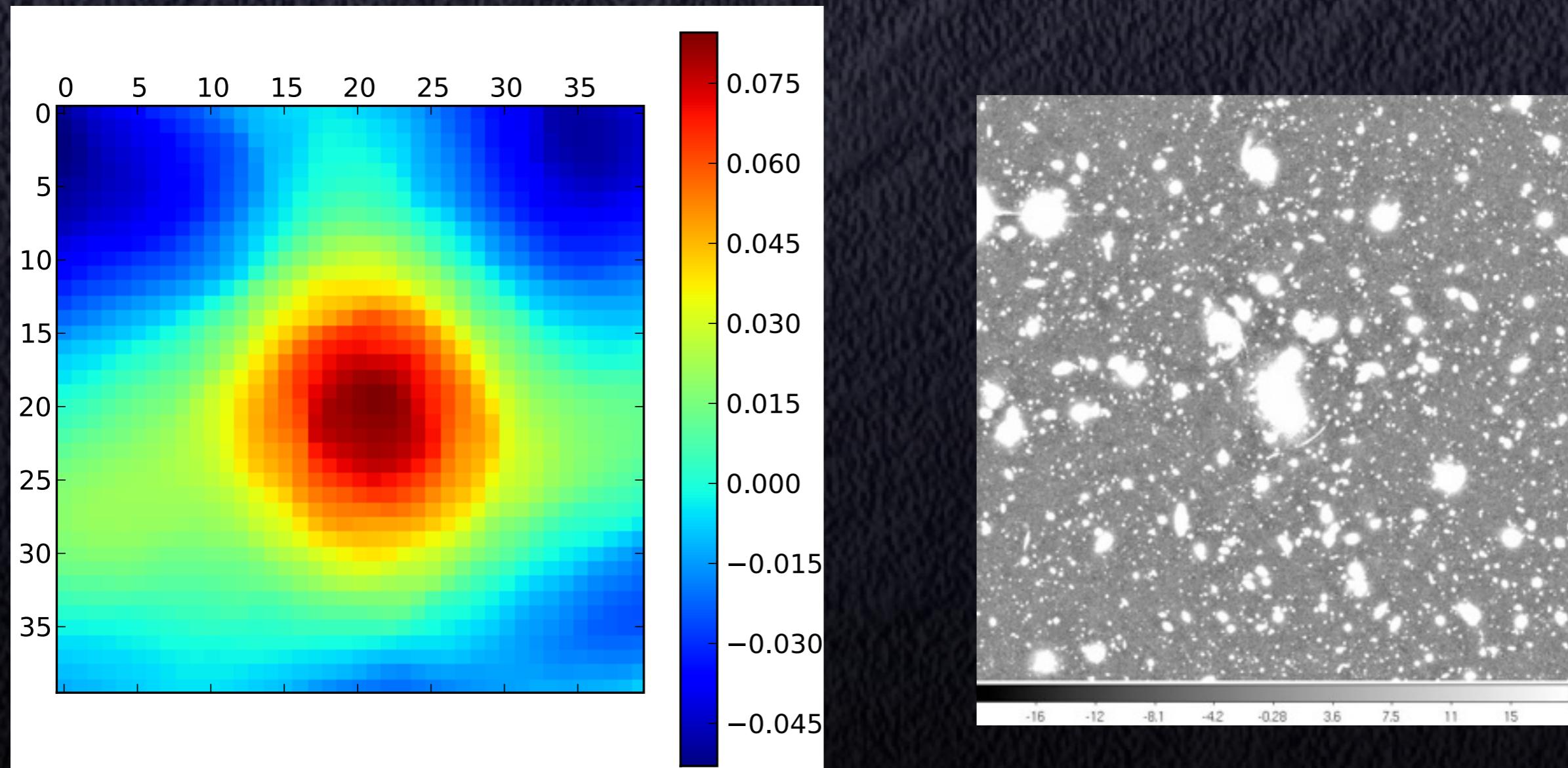


# Cross-Correlations



# Current Research

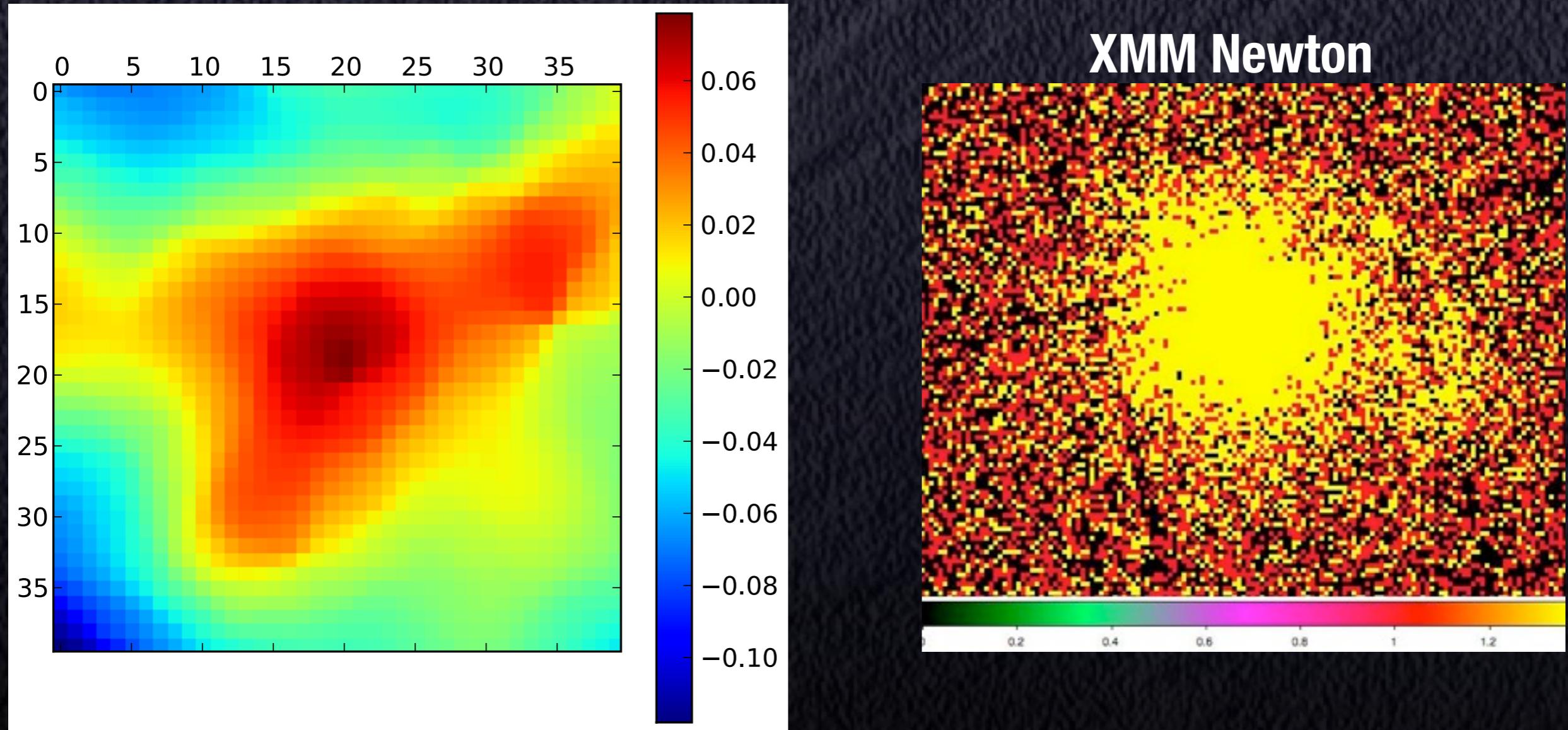
## A2219: Optical vs Lensing mass reconstruction



PRELIMINARY

# Current Research

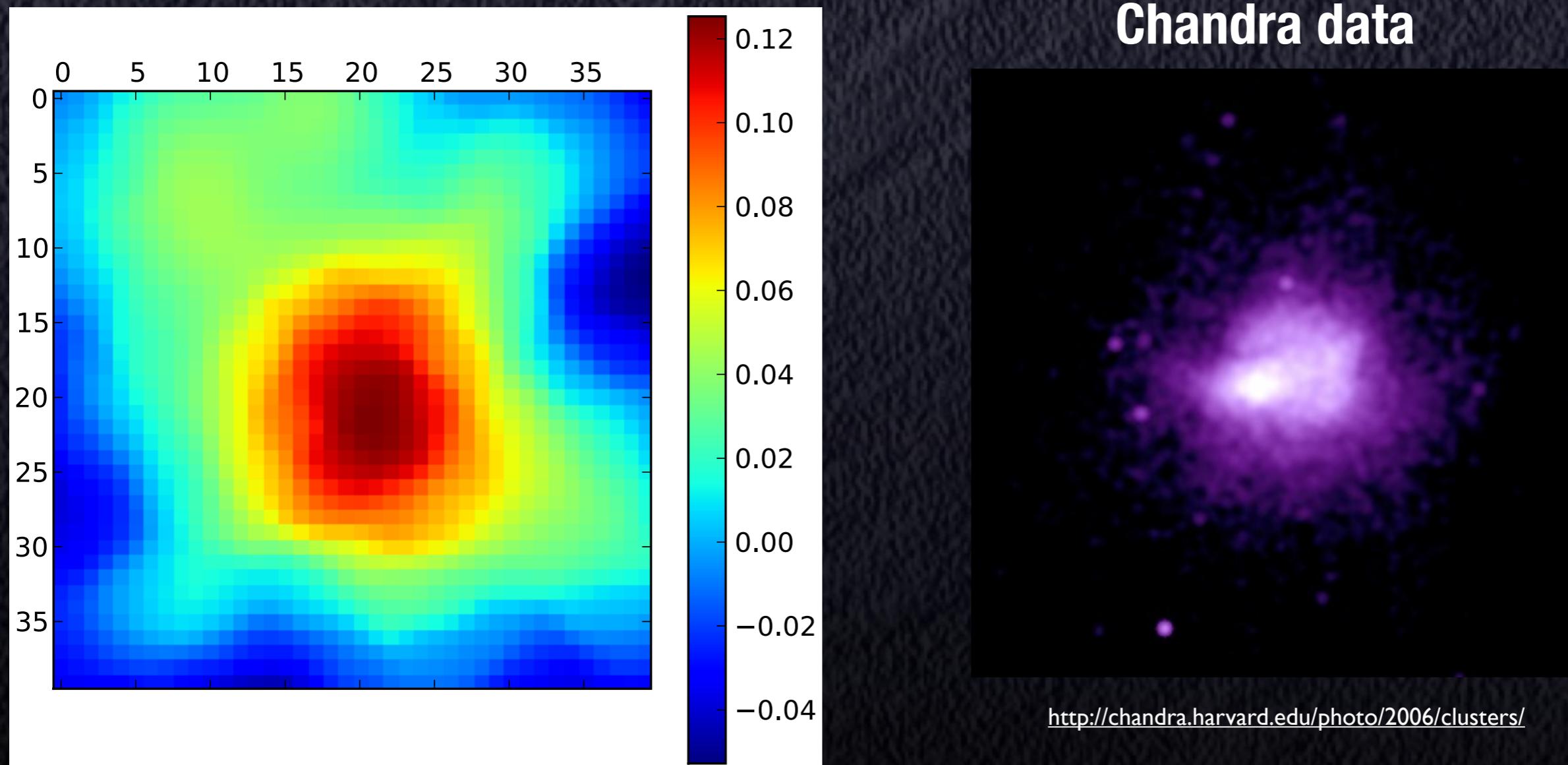
## A2261: X-ray vs Lensing mass reconstruction



PRELIMINARY

# Current Research

## A1914: X-ray vs Lensing mass reconstruction



PRELIMINARY

# Summary

---

## METHOD

Developed a non-parametric mass reconstruction technique “Particle Based Lensing” (PBL).

PBL is applied to compute mass maps of variable resolution and signal-to-noise.

## RESULTS

- \* The **ellipticity** for the light distribution is smaller than the ellipticity of the dark matter distribution for A901b and the Southwest Group.
- \* A901a, A901b and A902 have **strong alignment** whereas the Southwest group is not aligned with the rest of the peaks.
- \* The **gas distribution** of A1689 is **smoother** than the **dark matter distribution**.

## Future Research

Mutiwavelength analysis for a sample of 20 Supermassive Clusters.