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Chapter 3

3.1 Determine whether the signal is periodic or not. If the signal is periodic, determine the fundamental period.

(a) $x[n] = \cos\left(\frac{\pi n}{8}\right)$

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$$x[n] = \cos\left(\frac{\pi n}{8}\right) = \cos\left(\frac{\pi(n+N_1)}{8}\right)$$

$$= \cos\left(\frac{\pi n}{8} + \frac{\pi N_1}{8}\right)$$

$$\frac{\pi N_1}{8} = 2\pi k. \quad \therefore N_1 = 16.$$

the signal is periodic with $N_1 = 16$

(c) $x[n] = \sin\left(\frac{2\pi n}{3}\right) + \cos\left(\frac{\pi n}{3}\right)$

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$$x[n] = \sin\left(\frac{2\pi n}{3}\right) + \cos\left(\frac{\pi n}{3}\right)$$

$$= \sin\left(\frac{2\pi(n+N_1)}{3}\right) + \cos\left(\frac{\pi(n+N_2)}{3}\right)$$

$$= \sin\left(\frac{2\pi n}{3} + \frac{2\pi N_1}{3}\right) + \cos\left(\frac{\pi n}{3} + \frac{\pi N_2}{3}\right)$$

$$\frac{2\pi N_1}{3} = 2\pi k. \quad \therefore N_1 = 3.$$

$$\frac{\pi N_2}{3} = 2\pi k. \quad \therefore N_2 = 6.$$

$$N = \text{LCM}(3, 6) = 6.$$

the signal is periodic with $N = 6$.

3.2 Determine whether it is energy signal or power signal. Calculate the corresponding energy or average power.

(a) $x[n] = (-0.5)^n u[n]$

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$$x[n] = (-0.5)^n u[n] \quad \text{Energy signal.}$$

$$E = \sum_{n=-\infty}^{\infty} |(-0.5)^n u[n]|^2 = \sum_{n=0}^{\infty} (-0.5)^{2n}$$

$$= \sum_{n=0}^{\infty} (0.25)^n = \frac{1}{1-0.25} = \frac{4}{3}$$

(c) $x[n] = u[n-1] - u[n-7]$

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$x[n] = u[n-1] - u[n-7]$ Energy signal

$$E = \sum_{n=-\infty}^{\infty} |u[n-1] - u[n-7]|^2$$

$$= \sum_{n=1}^6 (1)^2 = 6.$$

3.3 Draw the following signals.

(a) $x[n] = \delta[-n]$

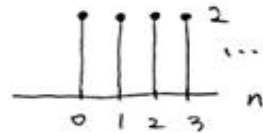
(c) $x[n] = 2u[n-1]$

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$x[n] = \delta[-n]$



$x[n] = 2u[n-1]$



3.4 Express the following pulse signals in terms of unit step function either in summing form or in product form.

(a) $x[n] = \begin{cases} 1 & \text{for } 3 \leq n \leq 7 \\ 0 & \text{otherwise} \end{cases}$

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$x[n] = \begin{cases} 1 & \text{for } 3 \leq n \leq 7 \\ 0 & \text{otherwise} \end{cases}$



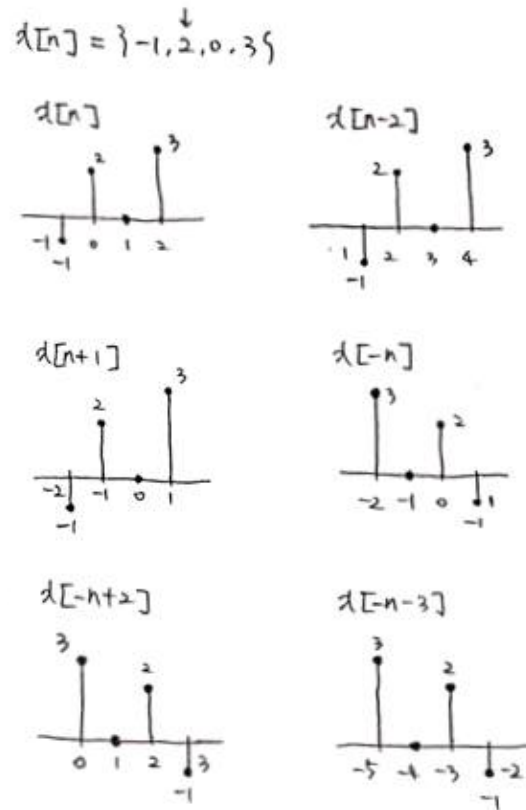
$$x[n] = u[n-3] - u[n-8]$$

$$= u[n-3] u[-n+7]$$

3.5 For given a discrete sequence $x[n] = \{-1, 2, 0, 3\}$, sketch the following discrete signals.

- (a) $x[n]$
- (b) $x_1[n] = x[n-2]$
- (c) $x_2[n] = x[n+1]$
- (d) $x_3[n] = x[-n]$
- (e) $x_4[n] = x[-n+2]$
- (f) $x_5[n] = x[-n-3]$

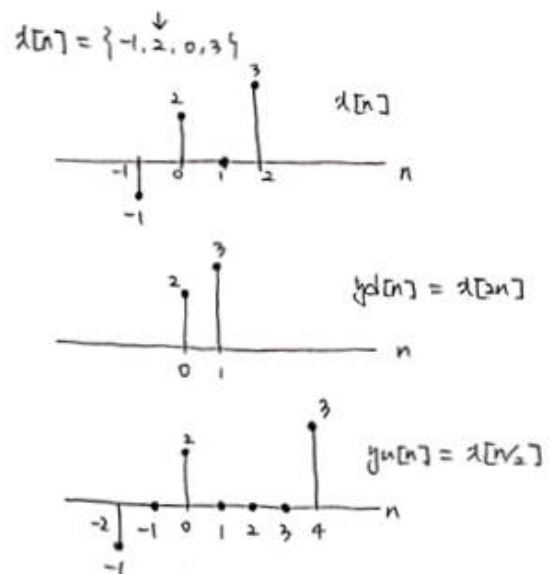
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3.6 For given a discrete sequence $x[n] = \{-1, 2, 0, 3\}$, sketch the following discrete signals.

- (a) $x[n]$ down-sampled by 2 signal
 $y_d[n] = x[2n]$
- (b) $x[n]$ up-sampled by 2 signal
 $y_u[n] = x\left[\frac{n}{2}\right]$

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3.7 An analog sinusoid signal $x(t) = \cos(2\pi(2000)t)$ is sampled to get the discrete signal by Nyquist-Shannon sampling theory.

(a) What is the bandwidth of the analog signal?

$$\rightarrow f_{\max} = \text{Bandwidth} = 2000$$

(b) What is the Nyquist sampling rate?

$$\rightarrow \text{Nyquist sampling rate } f_s = 2 * \text{Bandwidth} = 4000$$

3.8 An analog sinusoid signal $x(t) = \cos(2\pi(2000)t) + \cos(2\pi(3000)t)$ is sampled to get the discrete signal by Nyquist-Shannon sampling theory.

(a) What is the bandwidth of the analog signal?

$$\rightarrow f_{\max} = \text{Bandwidth} = 3000$$

(b) What is the Nyquist sampling rate?

$$\rightarrow \text{Nyquist sampling rate } f_s = 2 * \text{Bandwidth} = 6000$$

3.9 In general, an analog speech is quantized to 8bits/sample. How much is the quantizer SNR in dB for this condition?

$$\rightarrow \text{SNR(dB)} = 6.02N + 1.76\text{dB}$$

$$= 6.02 * 8 + 1.76 = 49.92\text{dB}$$