

# LeetCode Cheatsheet

- From <https://jwl-7.github.io/leetcode-cheatsheet/>

## Big O

### Time/Space Complexity

Instant:  $O(1)$  Logarithmic:  $O(\log n)$  Linear:  $O(n)$  Linearithmic:  $O(n \log n)$   
Quadratic:  $O(n^2)$  Cubic:  $O(n^3)$  Exponential:  $O(2^n)$  Factorial:  $O(n!)$

### Data Structure Operations

Data Structure

Time Complexity

Space Complexity

Average

Worst

Worst

Access

Search

Insertion

Deletion

Access

Search

Insertion

Deletion

Array

$O(1)$

$O(n)$

$O(n)$

$O(n)$

$O(1)$

$O(n)$

$O(n)$

$O(n)$

$O(n)$

Stack

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

Queue

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

Linked List

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

Doubly Linked List

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

$O(n)$

$O(1)$

$O(1)$

$O(n)$

Skip List

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(n)$

$O(n)$

$O(n)$

$O(n)$

$O(n \log(n))$

Hash Table

$O(1)$

$O(1)$

$O(1)$

$O(1)$

$O(n)$

$O(n)$

$O(n)$

$O(n)$

$O(n)$

$O(n)$

$O(n)$

Binary Search Tree

$O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(n)$   
 $O(n)$   
 $O(n)$   
 $O(n)$   
 $O(n)$

Cartesian Tree

N/A  
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
N/A  
 $O(n)$   
 $O(n)$   
 $O(n)$   
 $O(n)$

B-Tree

$O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(\log(n))$   
 $O(n)$

Red-Black Tree

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(n)$

Splay Tree

N/A

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

N/A

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(n)$

AVL Tree

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(n)$

KD Tree

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(n)$

Average

Worst

Worst

Quick Sort

$O(n \log(n))$

$O(n \log(n))$

$O(n^2)$

$O(\log(n))$

Merge Sort

$O(n \log(n))$

$O(n \log(n))$

$O(n \log(n))$

$O(n)$

Tim Sort

$O(n)$

$O(n \log(n))$

$O(n \log(n))$

$O(n)$

Heap Sort

$O(n \log(n))$

$O(n \log(n))$

$O(n \log(n))$

$O(1)$

Bubble Sort

$O(n)$

$O(n^2)$

$O(n^2)$

$O(1)$

Insertion Sort

$O(n)$

$O(n^2)$

$O(n^2)$

$O(1)$

Selection Sort

$O(n^2)$

$O(n^2)$

$O(n^2)$

$O(1)$

Tree Sort

$O(n \log(n))$

$O(n \log(n))$

$O(n^2)$

$O(n)$

Shell Sort

$O(n \log(n))$

$O((n \log(n))^2)$

$O((n \log(n))^2)$

$O(1)$

Bucket Sort

O(n+k)  
O(n+k)  
O( $n^2$ )  
O(n)  
Radix Sort  
O(nk)  
O(nk)  
O(nk)  
O(n+k)  
Counting Sort  
O(n+k)  
O(n+k)  
O(n+k)  
O(k)  
Cube Sort  
O(n)  
O(n log(n))  
O(n log(n))  
O(n)

## Array

two pointers: one input, opposite ends

```
def fn(arr):
    ans = 0
    left = 0
    right = len(arr) - 1

    while left < right:
        # TODO: logic with left and right
        if CONDITION:
            left += 1
        else:
            right -= 1

    return ans
```

two pointers: two inputs, exhaust both

```
def fn(arr1, arr2):
    i = 0
    j = 0
    ans = 0

    while i < len(arr1) and j < len(arr2):
        # TODO: logic
        if CONDITION:
            i += 1
        else:
            j += 1

    while i < len(arr1):
        # TODO: logic
        i += 1

    while j < len(arr2):
        # TODO: logic
        j += 1

return ans
```

sliding window

```
def fn(arr):
    n = len(arr)
    window = 0
    left = 0
    ans = 0

    for right in range(n):
        # TODO: add arr[right] to window

        while WINDOW_CONDITION_BROKEN:
            # TODO: remove arr[left] from window
            left += 1

        # TODO: update ans

    return ans
```

prefix sum

```
def fn(arr):
    n = len(arr)
```

```

prefix = [arr[0]]

for i in range(1, n):
    prefix.append(prefix[-1] + arr[i])

return prefix

```

efficient string building

```

def fn(strs: list[str]):
    ans = []

    for char in strs:
        ans.append(char)

    return ''.join(ans)

```

## Hash Map

find number of subarrays that fit an exact criteria

```

from collections import defaultdict

def fn(arr, k):
    counts = defaultdict(int)
    counts[0] = 1
    ans = curr = 0

    for num in arr:
        # TODO: logic to change curr
        ans += counts[curr - k]
        counts[curr] += 1

    return ans

```

## sliding window

```

def fn(arr):
    window = set()
    ans = 0
    left = 0

    for right, ELEMENT in enumerate(arr):
        # TODO: add arr[right] to window

        while WINDOW_CONDITION_BROKEN:

```

```

# TODO: remove arr[left] from window
left += 1

# TODO: update ans

return ans

```

## Linked List

fast and slow pointer

```

def fn(head):
    slow = head
    fast = head
    ans = 0

    while fast and fast.next:
        # TODO: logic
        slow = slow.next
        fast = fast.next.next

    return ans

```

reverse linked list

```

def fn(head):
    prev = None
    curr = head

    while curr:
        nxt = curr.next
        curr.next = prev
        prev = curr
        curr = nxt

    return prev

```

## Stack

monotonic increasing stack

```

def fn(arr):
    stack = []
    ans = 0

    for num in arr:
        while stack and stack[-1] > num:

```

```

# TODO: logic
stack.pop()
stack.append(num)

return ans

monotonic decreasing stack

def fn(arr):
    stack = []
    ans = 0

    for num in arr:
        while stack and stack[-1] < num:
            # TODO: logic
            stack.pop()
            stack.append(num)

    return ans

```

## Binary Tree

### DFS (recursive)

```

def dfs(root):
    if not root:
        return

    ans = 0

    # TODO: logic
    dfs(root.left)
    dfs(root.right)

    return ans

```

### DFS (iterative)

```

def dfs(root):
    stack = [root]
    ans = 0

    while stack:
        node = stack.pop()
        # TODO: logic
        if node.left:
            stack.append(node.left)

```

```

        if node.right:
            stack.append(node.right)

    return ans

BFS

from collections import deque

def fn(root):
    que = deque([root])
    ans = 0

    while que:
        current_length = len(que)
        # TODO: logic for current level
        for _ in range(current_length):
            node = que.popleft()
            # TODO: logic
            if node.left:
                que.append(node.left)
            if node.right:
                que.append(node.right)

    return ans

```

## Graph

### DFS (recursive)

```

def fn(graph):
    def dfs(node):
        ans = 0
        # TODO: logic
        for neighbor in graph[node]:
            if neighbor not in seen:
                seen.add(neighbor)
                ans += dfs(neighbor)

    return ans

seen = {START_NODE}

return dfs(START_NODE)

```

### DFS (iterative)

```
def fn(graph):
    stack = [START_NODE]
    seen = {START_NODE}
    ans = 0

    while stack:
        node = stack.pop()
        # TODO: logic
        for neighbor in graph[node]:
            if neighbor not in seen:
                seen.add(neighbor)
                stack.append(neighbor)

    return ans
```

### BFS

```
from collections import deque
```

```
def fn(graph):
    que = deque([START_NODE])
    seen = {START_NODE}
    ans = 0

    while que:
        node = que.popleft()
        # TODO: logic
        for neighbor in graph[node]:
            if neighbor not in seen:
                seen.add(neighbor)
                que.append(neighbor)

    return ans
```

### Dijkstra (shortest path)

```
from heapq import heappop, heappush
```

```
def dijkstras(graph: list[list[tuple[int, int]]], source: int) -> list[int]:
    n = len(graph)
    distances = [float('inf')] * n
    distances[source] = 0
    heap = [(0, source)]
```

```

while heap:
    curr_dist, node = heappop(heap)

    if curr_dist > distances[node]:
        continue

    for neighbor, weight in graph[node]:
        dist = curr_dist + weight

        if dist < distances[neighbor]:
            distances[neighbor] = dist
            heappush(heap, (dist, neighbor))

return distances

```

### Bellman-Ford (shortest path)

```

def bellman_ford(n: int, edges: list[tuple[int, int, int]], source: int) -> list[int]:
    distances = [float('inf')] * n
    distances[source] = 0

    for _ in range(n - 1):
        for u, v, w in edges:
            if distances[u] != float('inf') and distances[u] + w < distances[v]:
                distances[v] = distances[u] + w

    for u, v, w in edges:
        if distances[u] != float('inf') and distances[u] + w < distances[v]:
            return []

    return distances

```

### Kahn (topological sort)

```

from collections import defaultdict, deque

def kahn_topological_sort(graph: dict[int, list[int]]) -> list[int]:
    result = []
    indegree = defaultdict(int)

    for vertices in graph.values():
        for v in vertices:
            indegree[v] += 1

```

```

que = deque([node for node in graph if not indegree[node]])

while que:
    node = que.popleft()
    result.append(node)

    for neighbor in graph[node]:
        indegree[neighbor] -= 1

        if not indegree[neighbor]:
            que.append(neighbor)

return result if len(result) == len(graph) else []

```

### Kruskal (mst)

```

def kruskal_mst(n: int, edges: list[tuple[int, int, int]]) -> list[tuple[int, int, int]]:
    mst = []
    uf = UnionFind(n)
    edges.sort()

    for w, u, v in edges:
        if not uf.connected(u, v):
            uf.union(u, v)
            mst.append((w, u, v))

    return mst

```

### Prim (mst)

```
from heapq import heappop
```

```

def prim_mst(n: int, edges: list[tuple[int, int, int]]) -> list[tuple[int, int, int]]:
    mst = []
    uf = UnionFind(n)
    edges.sort()

    while edges:
        w, u, v = heappop(edges)

        if not uf.connected(u, v):
            uf.union(u, v)
            mst.append((w, u, v))

    return mst

```

## Floyd-Warshall (shortest path)

```
def floyd_marshall(n: int, edges: list[tuple[int, int, int]]) -> list[list[int]]:
    V = len(graph)
    dist = [row[:] for row in graph]

    for k in range(V):
        for i in range(V):
            for j in range(V):
                if dist[i][k] != float('inf') and dist[k][j] != float('inf'):
                    dist[i][j] = min(dist[i][j], dist[i][k] + dist[k][j])

    for i in range(V):
        if dist[i][i] < 0:
            return None # Or raise an exception

    return dist
```

## Heap

find top k elements

```
from heapq import heappop, heappush

def fn(arr, k):
    heap = []

    for num in arr:
        # TODO: logic to push onto heap according to problem's criteria
        heappush(heap, (CRITERIA, num))

        if len(heap) > k:
            heappop(heap)

    return [num for num in heap]
```

## Binary Search

binary search

```
def fn(arr, target):
    left = 0
    right = len(arr) - 1

    while left <= right:
        mid = (left + right) // 2
```

```

    if arr[mid] == target:
        # TODO: logic
        return
    if arr[mid] > target:
        right = mid - 1
    else:
        left = mid + 1

return left

```

duplicate elements, left-most insertion point

```

def fn(arr, target):
    left = 0
    right = len(arr)

    while left < right:
        mid = (left + right) // 2

        if arr[mid] >= target:
            right = mid
        else:
            left = mid + 1

    return left

```

duplicate elements, right-most insertion point

```

def fn(arr, target):
    left = 0
    right = len(arr)

    while left < right:
        mid = (left + right) // 2

        if arr[mid] > target:
            right = mid
        else:
            left = mid + 1

    return left

```

greedy (minimum)

```

def fn(arr):
    def check(x):

```

```

    return BOOLEAN

left = MINIMUM_POSSIBLE_ANSWER
right = MAXIMUM_POSSIBLE_ANSWER

while left <= right:
    mid = (left + right) // 2

    if check(mid):
        right = mid - 1
    else:
        left = mid + 1

return left

greedy (maximum)

def fn(arr):
    def check(x):
        return BOOLEAN

left = MINIMUM_POSSIBLE_ANSWER
right = MAXIMUM_POSSIBLE_ANSWER

while left <= right:
    mid = (left + right) // 2

    if check(mid):
        left = mid + 1
    else:
        right = mid - 1

return right

```

## Backtracking

### backtracking

```

def backtrack(curr, OTHER_ARGUMENTS...):
    if (BASE_CASE):
        # TODO: modify answer
        return

ans = 0

for (ITERATE_OVER_INPUT):
    # TODO: modify current state

```

```

        ans += backtrack(curr, OTHER_ARGUMENTS...)
        # TODO: undo modification of current state

    return ans

```

## Dynamic Programming

### DP top-down

```

def fn(arr):
    @cache
    def dp(STATE):
        if BASE_CASE:
            return 0
        return RECURRENCE_RELATION(STATE)

    return dp(STATE_FOR_WHOLE_INPUT)

```

### DP bottom-up

```

def fn(arr):
    if BASE_CASE:
        return 0

    dp = [BASE_CASE] * (STATE_FOR_WHOLE_INPUT + 1)

    for STATE in range(SMALLEST_SUBPROBLEM, STATE_FOR_WHOLE_INPUT + 1):
        if BASE_CASE:
            dp[STATE] = BASE_CASE
        else:
            dp[STATE] = RECURRENCE_RELATION(STATE)

    return dp[STATE_FOR_WHOLE_INPUT]

```

### Kadane (max-sum subarray)

```

def kadane(arr: list[int]) -> int:
    curr_sub = max_sub = arr[0]

    for num in arr[1:]:
        curr_sub = max(curr_sub + num, num)
        max_sub = max(max_sub, curr_sub)

    return max_sub

```

## Bit Manipulation

test kth-bit

```
def test_kth_bit(num: int, k: int) -> bool:  
    return num & (1 << k) != 0
```

set kth bit

```
def set_kth_bit(num: int, k: int) -> int:  
    return num | (1 << k)
```

clear kth bit

```
def clear_kth_bit(num: int, k: int) -> int:  
    return num & ~(1 << k)
```

toggle kth bit

```
def toggle_kth_bit(num: int, k: int) -> int:  
    return num ^ (1 << k)
```

get rightmost bit

```
def get_rightmost_set_bit(num: int) -> int:  
    return num & -num
```

count set bits

```
def count_set_bits(num: int) -> int:  
    return bin(num).count('1')
```

multiply by  $2^k$

```
def multiply_by_power_of_two(num: int, k: int) -> int:  
    return num << k
```

divide by  $2^k$

```
def divide_by_power_of_two(num: int, k: int) -> int:  
    return num >> k
```

check if number is power of 2

```
def is_power_of_two(num: int) -> bool:  
    return (num & (num - 1)) == 0
```

swap two variables

```
def swap_variables(num1: int, num2: int) -> tuple:
    num1 ^= num2
    num2 ^= num1
    num1 ^= num2
    return num1, num2
```

## Matrix

create / copy

```
def fn(matrix: list[list[int]]):
    r = len(matrix)
    c = len(matrix[0])

    create_matrix = [[0 for _ in range(c)] for _ in range(r)]
    copy_matrix = [row[:] for row in matrix]
```

diagonals / anti-diagonals

```
def fn(matrix: list[list[int]]):
    r = len(matrix)
    c = len(matrix[0])

    main_diagonal = [matrix[i][i] for i in range(min(r, c))]
    anti_diagonal = [matrix[i][-i] for i in range(min(r, c))]
```

rotate / transpose

```
def fn(matrix: list[list[int]]):
    r = len(matrix)
    c = len(matrix[0])

    transpose_tuple = zip(*matrix)
    transpose = [list(row) for row in transpose_tuple]
    rotate_left = transpose[::-1]
    rotate_right = [row[::-1] for row in transpose]
```

## Data Structures

array

```
from typing import Any
```

```
class Array:
    def __init__(self, size: int) -> None:
```

```

        self.size = size
        self.data = [None] * size

    def __getitem__(self, index: int) -> Any:
        return self.data[index]

    def __setitem__(self, index: int, value: Any) -> None:
        self.data[index] = value

    def __len__(self) -> int:
        return len(self.data)

    def __repr__(self) -> str:
        return repr(self.data)

```

### hash map

```
from typing import Any
```

```

class HashMap:
    def __init__(self) -> None:
        self.size = 100000
        self.bucket = [None] * self.size

    def _hash(self, key: int) -> int:
        return hash(key) % self.size

    def __setitem__(self, key: int, value: Any) -> None:
        self.bucket[self._hash(key)] = value

    def __getitem__(self, key: int) -> Any:
        return self.bucket[self._hash(key)]

    def __delitem__(self, key: int) -> None:
        self.bucket[self._hash(key)] = None

```

### linked list

```
from typing import Any
```

```

class ListNode:
    def __init__(self, data: Any) -> None:
        self.data = data
        self.next = None

```

```

def __repr__(self) -> str:
    return f'[{self.data}]'

class LinkedList:
    def __init__(self) -> None:
        self.head = None

    def append(self, data: Any) -> None:
        if not self.head:
            self.head = ListNode(data)
            return

        curr = self.head

        while curr.next:
            curr = curr.next

        curr.next = ListNode(data)

    def delete(self, data: Any) -> None:
        if not self.head:
            return

        if self.head.data == data:
            self.head = self.head.next
            return

        prev = None
        curr = self.head

        while curr:
            if curr.data == data:
                prev.next = curr.next
                return

            prev = curr
            curr = curr.next

    def reverse(self) -> None:
        prev = None
        curr = self.head

        while curr:
            nxt = curr.next

```

```

        curr.next = prev
        prev = curr
        curr = nxt

    self.head = prev

    def __repr__(self) -> str:
        if not self.head:
            return 'None'

        nodes = []
        node = self.head

        while node:
            nodes.append(repr(node))
            node = node.next

        return ' -> '.join(nodes) + ' -> None'

doubly linked list

from typing import Any

class ListNode:
    def __init__(self, data: Any) -> None:
        self.data = data
        self.prev = None
        self.next = None

    def __repr__(self) -> str:
        return f'{self.data}'


class DoublyLinkedList:
    def __init__(self) -> None:
        self.head = None

    def append(self, data: Any) -> None:
        if not self.head:
            self.head = ListNode(data)
            return

        curr = self.head

        while curr.next:

```

```

        curr = curr.next

    new_node = ListNode(data)
    curr.next = new_node
    new_node.prev = curr

def delete(self, data: Any) -> None:
    if not self.head:
        return

    if self.head.data == data:
        self.head = self.head.next
        if self.head:
            self.head.prev = None
        return

    curr = self.head
    while curr:
        if curr.data == data:
            prev_node = curr.prev
            prev_node.next = curr.next
            if curr.next:
                curr.next.prev = prev_node
            return
        curr = curr.next

def reverse(self) -> None:
    curr = self.head
    prev = None

    while curr:
        nxt = curr.next
        curr.next = prev
        curr.prev = nxt
        prev = curr
        curr = nxt

    self.head = prev

def __repr__(self) -> str:
    if not self.head:
        return 'None'

    nodes = []
    curr = self.head

```

```

        while curr:
            nodes.append(repr(curr))
            curr = curr.next

    return ' <-> '.join(nodes) + ' <-> None'

binary tree

from typing import Any

class TreeNode:
    def __init__(self, data: Any) -> None:
        self.data = data
        self.left = None
        self.right = None

class BinaryTreeNode:
    def __init__(self) -> None:
        self.root = None

    def insert(self, data: Any) -> None:
        if not self.root:
            self.root = TreeNode(data)
        else:
            self.insert_node(self.root, data)

    def insert_node(self, node: TreeNode | None, data: Any) -> TreeNode:
        if not node:
            return TreeNode(data)

        if not node.left:
            node.left = TreeNode(data)
        elif not node.right:
            node.right = TreeNode(data)
        else:
            node.left = self.insert_node(node.left, data)

    return node

    def __repr__(self) -> str:
        return 'Empty tree' if not self.root else self._print_tree(self.root, '', True)

    def _print_tree(self, node: TreeNode | None, prefix: str, is_left: bool) -> str:
        if node is None:

```

```

        return ''

    result = ''
    result += self._print_tree(node.right, prefix + ('    ' if is_left else '   '), False)
    result += prefix + ('    ' if is_left else '   ') + str(node.data) + '\n'
    result += self._print_tree(node.left, prefix + ('    ' if is_left else '   '), True)

    return result
}

binary search tree

from typing import Any

class TreeNode:
    def __init__(self, data: Any) -> None:
        self.data = data
        self.left = None
        self.right = None

class BinarySearchTree:
    def __init__(self) -> None:
        self.root = None

    def insert(self, data: Any) -> None:
        if not self.root:
            self.root = TreeNode(data)
        else:
            self.insert_node(self.root, data)

    def insert_node(self, node: TreeNode | None, data: Any) -> None:
        if data < node.data:
            if not node.left:
                node.left = TreeNode(data)
            else:
                self.insert_node(node.left, data)
        else:
            if not node.right:
                node.right = TreeNode(data)
            else:
                self.insert_node(node.right, data)

    def __repr__(self) -> str:
        return 'Empty tree' if not self.root else self._print_tree(self.root, '', True)

```

```

def _print_tree(self, node: TreeNode | None, prefix: str, is_left: bool) -> str:
    if node is None:
        return ''

    result = ''
    result += self._print_tree(node.right, prefix + ('    ' if is_left else '   '), False)
    result += prefix + ('    ' if is_left else '   ') + str(node.data) + '\n'
    result += self._print_tree(node.left, prefix + ('    ' if is_left else '   '), True)

    return result

graph

class Graph:
    def __init__(self) -> None:
        self.graph = {}

    def add_vertex(self, vertex: str) -> None:
        if vertex not in self.graph:
            self.graph[vertex] = []

    def add_edge(self, a: str, b: str) -> None:
        self.add_vertex(a)
        self.add_vertex(b)
        self.graph[a].append(b)
        self.graph[b].append(a)

    def get_neighbors(self, vertex: str) -> list[str]:
        return self.graph.get(vertex, [])

    def __repr__(self) -> str:
        output = ''

        for vertex, neighbors in self.graph.items():
            output += f'{vertex} - {` - `}.join(neighbors)\n'

        return output

union find

class UnionFind:
    def __init__(self, n: int) -> None:
        self.root = list(range(n))

    def find(self, a: int) -> int:
        return a if a == self.root[a] else self.find(self.root[a])

```

```

def union(self, a: int, b: int) -> None:
    self.root[self.find(a)] = self.find(b)

def connected(self, a: int, b: int) -> bool:
    return self.find(a) == self.find(b)

def __repr__(self) -> str:
    n = len(self.root)
    lines = []
    components = {}

    for i in range(n):
        root = self.find(i)

        if root not in components:
            components[root] = []

        components[root].append(i)

    for component in components.values():
        lines.append(' - '.join(f'({node})' for node in component))

    return '\n'.join(lines)

union find optimized

class UnionFind:
    def __init__(self, n: int) -> None:
        self.root = list(range(n))
        self.rank = [1] * n

    def find(self, a: int) -> int:
        return a if a == self.root[a] else self.find(self.root[a])

    def union(self, a: int, b: int) -> None:
        root_a = self.find(a)
        root_b = self.find(b)

        if root_a != root_b:
            if self.rank[root_a] < self.rank[root_b]:
                self.root[root_a] = root_b
            elif self.rank[root_a] > self.rank[root_b]:
                self.root[root_b] = root_a
            else:
                self.root[root_b] = root_a

```

```

        self.rank[root_a] += 1

    def connected(self, a: int, b: int) -> bool:
        return self.find(a) == self.find(b)

    def __repr__(self) -> str:
        n = len(self.root)
        lines = []
        components = {}

        for i in range(n):
            root = self.find(i)

            if root not in components:
                components[root] = []

            components[root].append(i)

        for component in components.values():
            lines.append(' - '.join(f'({node})' for node in component))

        return '\n'.join(lines)

trie

class TrieNode:
    def __init__(self) -> None:
        self.children = {}
        self.is_word = False

class Trie:
    def __init__(self) -> None:
        self.root = TrieNode()

    def build(self, words: list[str]) -> None:
        for word in words:
            self.insert(word)

    def insert(self, word: str) -> None:
        node = self.root

        for char in word:
            if char not in node.children:
                node.children[char] = TrieNode()
            node = node.children[char]

```

```

        node.is_word = True

    def search(self, word: str) -> bool:
        node = self.root

        for char in word:
            if char not in node.children:
                return False
            node = node.children[char]

        return node.is_word

    def starts_with(self, prefix: str) -> bool:
        node = self.root

        for char in prefix:
            if char not in node.children:
                return False
            node = node.children[char]

        return True

    def collect_words(self, node: TrieNode, prefix: str) -> list[str]:
        words = []

        if node.is_word:
            words.append(prefix)

        for char, child_node in node.children.items():
            words.extend(self.collect_words(child_node, prefix + char))

        return words

    def __repr__(self) -> str:
        return 'Trie:\n' + self._print_trie(self.root)

    def _print_trie(self, node: TrieNode | None, level: int = 0, prefix: str = '') -> str:
        output = ''
        prefix_str = '    ' * level + prefix

        if not node:
            return output

        if node.is_word:
            output += prefix_str + '    ' + '(*)' + '\n'


```

```

        for i, (char, child_node) in enumerate(node.children.items()):
            is_last = i == len(node.children) - 1
            marker = ' ' if is_last else ' '
            output += prefix_str + marker + char + '\n'
            output += self._print_trie(child_node, level + 1, ' ' if not is_last else ' ')

    return output

```

### Min Heap

```

class MinHeap:
    def __init__(self):
        # The heap is stored internally as a list
        self.heap = []

    def _get_parent_index(self, index):
        # Parent of index k is at (k-1)//2
        return (index - 1) // 2

    def _get_left_child_index(self, index):
        # Left child of index k is at 2*k + 1
        return 2 * index + 1

    def _get_right_child_index(self, index):
        # Right child of index k is at 2*k + 2
        return 2 * index + 2

    def _swap(self, i, j):
        # Helper function to swap two elements in the list
        self.heap[i], self.heap[j] = self.heap[j], self.heap[i]

    def _heapify_up(self, index):
        """
        Moves the element up the tree until the min-heap property is satisfied.
        Used after insertion.
        """
        parent_index = self._get_parent_index(index)
        # While we are not at the root and the current element is smaller than its parent
        while index > 0 and self.heap[index] < self.heap[parent_index]:
            self._swap(index, parent_index)
            index = parent_index
            parent_index = self._get_parent_index(index)

    def _heapify_down(self, index):
        """

```

```

Moves the element down the tree until the min-heap property is satisfied.
Used after removal of the root.
"""
min_index = index
while True:
    left_child_index = self._get_left_child_index(index)
    right_child_index = self._get_right_child_index(index)
    heap_size = len(self.heap)

    # Check left child
    if (left_child_index < heap_size and
        self.heap[left_child_index] < self.heap[min_index]):
        min_index = left_child_index

    # Check right child
    if (right_child_index < heap_size and
        self.heap[right_child_index] < self.heap[min_index]):
        min_index = right_child_index

    # If the current node is the smallest among its children/itself, we stop
    if min_index == index:
        break

    # Otherwise, swap and continue heapifying down
    self._swap(index, min_index)
    index = min_index

def insert(self, value):
    """Adds a new element to the heap."""
    self.heap.append(value)
    # Maintain heap property by moving the new element up
    self._heapify_up(len(self.heap) - 1)

def extract_min(self):
    """Removes and returns the smallest element (root) from the heap."""
    if self.is_empty():
        return None
    if len(self.heap) == 1:
        return self.heap.pop()

    # Swap the root with the last element
    root = self.heap[0]
    self.heap[0] = self.heap.pop()
    # Maintain heap property by moving the new root down
    self._heapify_down(0)
    return root

```

```

def peek(self):
    """Returns the smallest element without removing it."""
    if self.is_empty():
        return None
    return self.heap[0]

def is_empty(self):
    """Checks if the heap is empty."""
    return len(self.heap) == 0

def size(self):
    """Returns the number of elements in the heap."""
    return len(self.heap)

def __str__(self):
    return str(self.heap)

```

## Sorting Algorithms

### bubble sort

- Should never used

```

def bubble_sort(arr: list) -> None:
    n = len(arr)

    for i in range(n):
        swapped = False

        for j in range(0, n - i - 1):
            if arr[j] > arr[j + 1]:
                arr[j], arr[j + 1] = arr[j + 1], arr[j]
                swapped = True

        if not swapped:
            break

```

### selection sort

```

def selection_sort(arr: list) -> None:
    n = len(arr)

    for i in range(n):
        min_i = i

        for j in range(i + 1, n):

```

```

        if arr[j] < arr[min_i]:
            min_i = j

        if min_i != i:
            arr[i], arr[min_i] = arr[min_i], arr[i]

```

### insertion sort

```

def insertion_sort(arr: list) -> None:
    n = len(arr)

    for i in range(1, n):
        key = arr[i]

        while i > 0 and key < arr[i - 1]:
            arr[i] = arr[i - 1]
            i -= 1

        arr[i] = key

```

### shell sort

```

def shell_sort(arr: list) -> None:
    n = len(arr)
    gaps = [701, 301, 132, 57, 23, 10, 4, 1]

    for gap in gaps:
        for i in range(gap, n):
            tmp = arr[i]
            j = i

            while j >= gap and arr[j - gap] > tmp:
                arr[j] = arr[j - gap]
                j -= gap

            if j != i:
                arr[j] = tmp

```

### merge sort

- Should used for LeetCode because it runs faster than quick sort

```

def merge_sort(arr: list) -> list:
    n = len(arr)

    if n <= 1:
        return arr

```

```

mid = n // 2
left = merge_sort(arr[:mid])
right = merge_sort(arr[mid:])

return merge(left, right)

def merge(left: list, right: list) -> list:
    output = []

    while left and right:
        min_num = left.pop(0) if left[0] <= right[0] else right.pop(0)
        output.append(min_num)

    output.extend(left)
    output.extend(right)

    return output

```

### quick sort

```

def quick_sort(arr: list) -> list:
    n = len(arr)

    if n <= 1:
        return arr

    pivot = arr[n // 2]
    left = [x for x in arr if x < pivot]
    right = [x for x in arr if x > pivot]

    return quick_sort(left) + [pivot] + quick_sort(right)

```

### timsort

```

def tim_sort(arr: list) -> list:
    n = len(arr)
    min_run = 32

    for start in range(0, n, min_run):
        end = min(start + min_run - 1, n - 1)
        insertion_sort(arr, start, end)

    size = min_run

```

```

while size < n:
    for left in range(0, n, 2 * size):
        mid = min(n - 1, left + size - 1)
        right = min((left + 2 * size - 1), (n - 1))
        arr[left : right + 1] = merge(arr[left : mid + 1], arr[mid + 1 : right + 1])
    size *= 2

return arr

def insertion_sort(arr: list, left: int, right: int) -> None:
    for i in range(left + 1, right + 1):
        key = arr[i]

        while i > 0 and key < arr[i - 1]:
            arr[i] = arr[i - 1]
            i -= 1

        arr[i] = key

def merge_sort(arr: list) -> list:
    n = len(arr)

    if n <= 1:
        return arr

    mid = n // 2
    left = merge_sort(arr[:mid])
    right = merge_sort(arr[mid:])

    return merge(left, right)

def merge(left: list, right: list) -> list:
    output = []

    while left and right:
        min_num = left.pop(0) if left[0] <= right[0] else right.pop(0)
        output.append(min_num)

    output.extend(left)
    output.extend(right)

    return output

```

### heap sort

```
def heap_sort(arr: list) -> list:
    n = len(arr)

    for i in range(n // 2 - 1, -1, -1):
        heapify(arr, n, i)
    for i in range(n - 1, 0, -1):
        arr[i], arr[0] = arr[0], arr[i]
        heapify(arr, i, 0)

    return arr

def heapify(arr: list, n: int, i: int) -> None:
    largest = i
    left = 2 * i + 1
    right = 2 * i + 2

    if left < n and arr[left] > arr[largest]:
        largest = left
    if right < n and arr[right] > arr[largest]:
        largest = right
    if largest != i:
        arr[i], arr[largest] = arr[largest], arr[i]
        heapify(arr, n, largest)
```

### counting sort

```
def counting_sort(arr: list) -> list:
    max_num = max(arr)
    min_num = min(arr)
    count_range = max_num - min_num + 1
    count = [0] * count_range
    output = [0] * len(arr)

    for num in arr:
        count[num - min_num] += 1

    for i in range(1, count_range):
        count[i] += count[i - 1]

    for num in arr[::-1]:
        output[count[num - min_num] - 1] = num
        count[num - min_num] -= 1

    return output
```

```

bucket sort

def bucket_sort(arr: list) -> list:
    num_buckets = 10
    min_num = min(arr)
    max_num = max(arr)
    bucket_size = (max_num - min_num) / num_buckets
    buckets = [[] for _ in range(num_buckets)]

    for num in arr:
        index = min(int((num - min_num) / bucket_size), num_buckets - 1)
        buckets[index].append(num)

    return [num for bucket in buckets for num in sorted(bucket)]


radix sort

def radix_sort(arr: list) -> None:
    max_val = max(arr)
    exp = 1

    while max_val // exp > 0:
        counting_sort(arr, exp)
        exp *= 10

def counting_sort(arr: list, exp: int) -> None:
    n = len(arr)
    output = [0] * n
    count = [0] * 10

    for i in range(n):
        idx = arr[i] // exp
        count[idx % 10] += 1

    for i in range(1, 10):
        count[i] += count[i - 1]

    i = n - 1

    while i >= 0:
        idx = arr[i] // exp
        output[count[idx % 10] - 1] = arr[i]
        count[idx % 10] -= 1
        i -= 1

    for i in range(n):

```

```

        arr[i] = output[i]

cubesort

def cube_sort(arr: list, processors: int) -> None:
    n = len(arr)
    subarrays = []
    subarray_size = n // processors

    for i in range(processors):
        subarray = arr[i * subarray_size : (i + 1) * subarray_size]
        subarrays.append(subarray)

    for subarray in subarrays:
        subarray.sort()

    for dimension in range(processors.bit_length() - 1):
        for i in range(processors):
            partner = i ^ (1 << dimension)
            if i < partner:
                merged = subarrays[i] + subarrays[partner]
            else:
                merged = subarrays[partner] + subarrays[i]
            merged.sort()
            subarrays[i] = merged[:subarray_size]
            subarrays[partner] = merged[subarray_size:]

    arr[:] = [num for subarray in subarrays for num in subarray]

```

bogo sort

```
import random
```

```

def bogo_sort(arr: list) -> None:
    target = sorted(arr)

    while arr != target:
        random.shuffle(arr)

```

pancake sort

```

def pancake_sort(arr: list) -> None:
    n = len(arr)

    for size in reversed(range(2, n + 1)):
        max_idx = find_max_index(arr, size)

```

```

        if max_idx != size - 1:
            flip(arr, max_idx)
            flip(arr, size - 1)

def flip(arr: list, i: int) -> None:
    left = 0

    while left < i:
        arr[left], arr[i] = arr[i], arr[left]
        left += 1
        i -= 1

def find_max_index(arr: list, n: int) -> int:
    max_idx = 0

    for i in range(n):
        if arr[i] > arr[max_idx]:
            max_idx = i

    return max_idx

sleep sort

def pancake_sort(arr: list) -> None:
    n = len(arr)

    for size in reversed(range(2, n + 1)):
        max_idx = find_max_index(arr, size)

        if max_idx != size - 1:
            flip(arr, max_idx)
            flip(arr, size - 1)

def flip(arr: list, i: int) -> None:
    left = 0

    while left < i:
        arr[left], arr[i] = arr[i], arr[left]
        left += 1
        i -= 1

def find_max_index(arr: list, n: int) -> int:
    max_idx = 0

    for i in range(n):

```

```
if arr[i] > arr[max_idx]:  
    max_idx = i  
  
return max_idx
```