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In [1]: from numpy import *
        from matplotlib import pyplot as plt
        %matplotlib inline

#Getting data from file and splitting it into x axis and y axis
def getdata(datafile,delimiter_in_file,header_skipping):
    training_data = genfromtxt(datafile,delimiter=delimiter_in_file,
    skip_header = header_skipping,dtype=str)
    x = [] # x-axis data
    y = [] # y-axis data
    for i in range(0,len(training_data)):
        x.append(float(training_data[i][0]))
        y.append(float(training_data[i][1]))
    return x,y

#Error Finder
#formula : 1/2n{summition from i=1 to n (y[i] - (m * x[i] + b))}
def error(m,b,x,y):
    total_error = 0.0
    for i in range(0,len(x)):
        total_error+= ((m * x[i] + b) - y[i]) ** 2
    return total_error/float(len(x))

#Function by which we can get new values of m and b
#Using gradient descent ( Partial Derivative )
#Having Formula :
# curl/curl{m} = {summition from i = 1 to n of -x[i] * (y[i] - (m * x[i] + b))}
# curl/curl{b} = {summition from i = 1 to n of -(y[i] - (m * x[i] + b))}
def step_gradient(m,b,x,y,learning_rate):
    m_gradient = 0.0 #initial gradient
    b_gradient = 0.0 #initial intercept
    for i in range(0,len(x)):
        m_gradient+=(-x[i] * (y[i]- (m * x[i]) + b))
        b_gradient+=(-(y[i] - ((m * x[i]) + b)))
    #new m using formula of gradient descent
    #new path point = old path point - (alpha) * gradient
    #alpha = learning rate , as what the speed at which we go downwa
rd in graph
    #to find minima
    new_m = m - (learning_rate * (m_gradient)/float(len(x)))
    new_b = b - (learning_rate * (b_gradient)/float(len(x)))
    return new_m,new_b

#running gradient descent upto num of iteration say 10,000 time we g
et
#different m and b and after last we found m and b
def gradient_descent_run(old_m,old_b,num_iterations,x,y,learning_rat
e):
    m = old_m # getting old b
    b = old_b # getting old m
    for i in range(num_iterations):
        #calling step gradient upto num iterations time
        #in this m and b get change again and again upto num iterati
ons
        m,b = step_gradient(m,b,x,y,learning_rate)
    return m,b

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#Test file data to run Test on calculated final m and b
#and predict the y
def test(m,b,x):
    y_new = [] #creating empty list of y_new
    print()
    for i in range(0,len(x)):
        #appending y_new list with y_new = mx+b have x input and y output
        y_new.append(m * x[i] + b)
    return y_new

def train(datafile,delimiter_in_file,skiping_header,num,alpha):

    #Getting X and Y values from File of training data
    x,y = getdata(datafile,delimiter_in_file,skiping_header)
    m_initial = 0 #initial slope
    b_initial = 0 #initial intercept
    num_iterations = num #num of iterations
    learning_rate = alpha #learning rate
    print()
    print('Training Data Scatter Plot')
    plot_graph(x,y) #plotting Training Data
    print()
    print('Starting Linear Regression with m = '+str(m_initial)+' b = '+str(b_initial)+' error = ' + str(error(m_initial,b_initial,x,y)))
    print('Starting...')
    print()
    m,b = gradient_descent_run(m_initial,b_initial,num_iterations,x,y,learning_rate)
    print()
    print('Ending Linear Regression with m = '+str(m)+' b = '+str(b)+' error = ' + str(error(m,b,x,y)))
    print()
    print('Plotting Best Fit Line')
    plot_final_line(m,b) #Plotting Best Fit Line
    return m,b,error(m,b,x,y)

#plotting Scatter Graph Function
def plot_graph(x,y):
    print('Scatter Plot')
    plt.scatter(x,y)
    plt.show()

#plotting Best Fit Line Function
def plot_final_line(m,b):
    print('Printing Best fit Line')
    x = []
    y = []
    for i in range(0,100):
        x.append(float(i))
    for i in range(0,len(x)):
        y.append(m * x[i] + b)
    plt.plot(x,y)
    plt.show()

def run(trainfile,testfile,delimiter,skip_header,num,alpha):
    #getting m , b ,error from training data main function
    m,b,e = train(trainfile,delimiter,skip_header,num,alpha)
    #getting x and y from test data file

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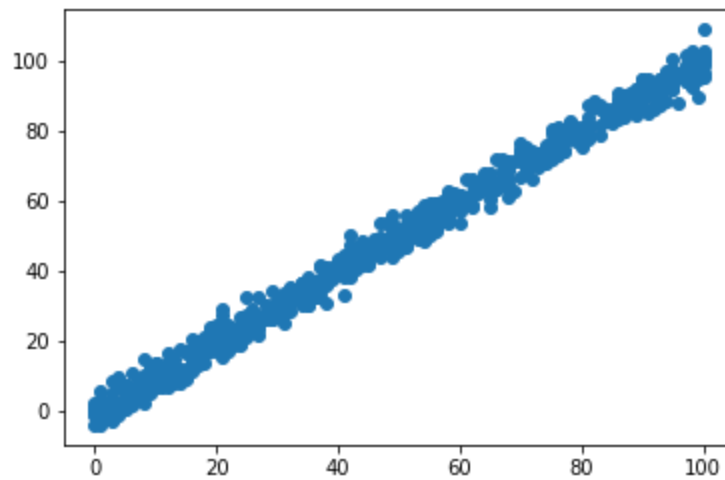
x,y = getdata(testfile,delimiter,skip_header)
#plotting graph of actual dataset in test
print('Ploting actual Data from test file')
plot_graph(x,y)
print()
#Calculating Prediction of y
y_new = test(m,b,x)
print()
#plotting graph of Predicted y with actual x
print('Ploting Predicted data of Y ')
plot_graph(x,y_new)
print()
#printing y actual and corresponding to its y_new
for i in range(0,len(y)):
    print('Y actual = ' + str(y[i]),end = ' | ')
    print('Y Predicted = ' + str(y_new[i]))
print()
print('Ending Linear Regression with m = '+str(m)+' b = '+str(b)
+' error = ' + str(e))
print()

# -----Main----- #

run('data/train.csv','data/test.csv',',',',',1,5000,0.0001)

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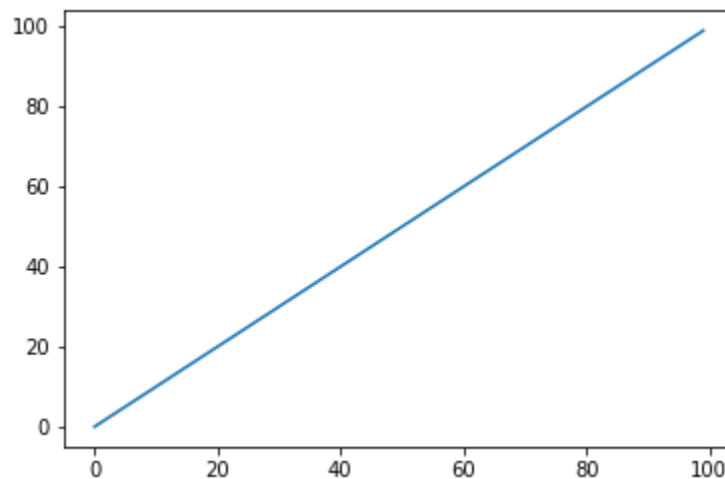
Training Data Scatter Plot  
Scatter Plot



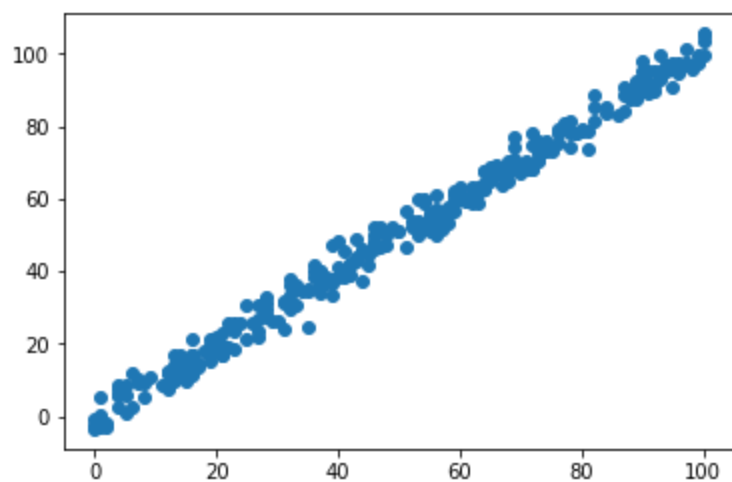
Starting Linear Regression with  $m = 0$   $b = 0$  error = 3336.6524577344949  
Starting...

Ending Linear Regression with  $m = 0.99892060904202362$   $b = -0.0037952402952288961$  error = 7.8922376235243767

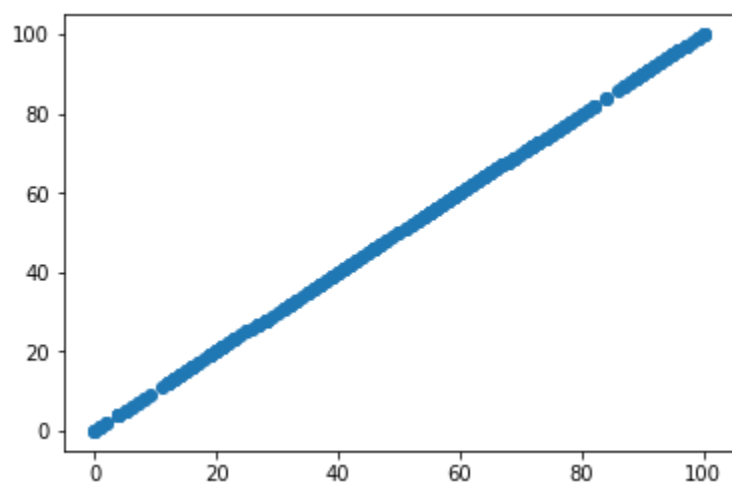
Plotting Best Fit Line  
Printing Best fit Line



Plotting actual Data from test file  
Scatter Plot



Plotting Predicted data of Y  
Scatter Plot



Y actual = 79.775152009999999 | Y Predicted = 76.91309165594059  
Y actual = 23.177278869999999 | Y Predicted = 20.973537549587267  
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Y actual = 9.2411389770000003 | Y Predicted = 11.983252068209055  
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Y actual = 9.2816997529999998 | Y Predicted = 6.9886490229989358  
Y actual = 103.52661620000001 | Y Predicted = 99.888265663907134  
Y actual = 47.410067249999997 | Y Predicted = 47.94439399372191  
Y actual = 42.038357730000001 | Y Predicted = 41.950870339469766  
Y actual = 96.11982476 | Y Predicted = 95.892583227739038  
Y actual = 38.057664080000002 | Y Predicted = 38.954108512343694  
Y actual = 105.4503788 | Y Predicted = 99.888265663907134  
Y actual = 88.803069109999996 | Y Predicted = 86.902297746360816  
Y actual = 15.493011409999999 | Y Predicted = 13.981093286293101  
Y actual = 12.42624606 | Y Predicted = 13.981093286293101  
Y actual = 40.007095980000003 | Y Predicted = 36.956267294259646  
Y actual = 5.6340309020000001 | Y Predicted = 4.9908078049148887  
Y actual = 87.369389310000003 | Y Predicted = 87.901218355402847  
Y actual = 89.73951993 | Y Predicted = 90.897980182528912  
Y actual = 66.614996430000005 | Y Predicted = 64.926044347436303  
Y actual = 72.913885300000004 | Y Predicted = 73.916329828814511  
Y actual = 57.191035059999997 | Y Predicted = 55.935758866058094  
Y actual = 11.217104770000001 | Y Predicted = 15.978934504377149  
Y actual = 0.67607674900000003 | Y Predicted = 4.9908078049148887  
Y actual = 28.15668543 | Y Predicted = 27.965981812881431  
Y actual = 95.395800300000005 | Y Predicted = 91.896900791570943  
Y actual = 52.054907030000003 | Y Predicted = 45.946552775637862  
Y actual = 59.708645769999997 | Y Predicted = 53.937917647974047  
Y actual = 36.792247619999998 | Y Predicted = 38.954108512343694

Y actual = 37.084576980000001 | Y Predicted = 43.948711557553814  
Y actual = 24.184379759999999 | Y Predicted = 30.962743640007503  
Y actual = 67.287253320000005 | Y Predicted = 67.922806174562368  
Y actual = 82.870593999999997 | Y Predicted = 85.903377137318799  
Y actual = 89.899991 | Y Predicted = 89.899059573486895  
Y actual = 36.941731779999998 | Y Predicted = 37.95518790330167  
Y actual = 19.875622419999999 | Y Predicted = 20.973537549587267  
Y actual = 90.714816540000001 | Y Predicted = 94.893662618697007  
Y actual = 61.093677620000001 | Y Predicted = 55.935758866058094  
Y actual = 60.111349580000002 | Y Predicted = 59.93144130222619  
Y actual = 64.832963160000006 | Y Predicted = 64.926044347436303  
Y actual = 81.403817689999997 | Y Predicted = 77.912012264982607  
Y actual = 92.402176859999997 | Y Predicted = 88.900138964444864  
Y actual = 2.576625376 | Y Predicted = 5.9897284139569127  
Y actual = 63.807681719999998 | Y Predicted = 66.923885565520351  
Y actual = 38.67780759 | Y Predicted = 35.957346685217622  
Y actual = 16.82839701 | Y Predicted = 15.978934504377149  
Y actual = 99.786872520000003 | Y Predicted = 99.888265663907134  
Y actual = 44.689134330000002 | Y Predicted = 44.947632166595838  
Y actual = 71.003778240000003 | Y Predicted = 72.917409219772495  
Y actual = 51.573267180000002 | Y Predicted = 56.934679475100118  
Y actual = 19.878464789999999 | Y Predicted = 19.974616940545243  
Y actual = 79.503414950000007 | Y Predicted = 75.914171046898559  
Y actual = 34.588764910000002 | Y Predicted = 33.959505467133575  
Y actual = 55.738346700000001 | Y Predicted = 54.93683825701607  
Y actual = 68.197219050000001 | Y Predicted = 71.918488610730464  
Y actual = 55.816285090000001 | Y Predicted = 54.93683825701607  
Y actual = 9.3914167979999998 | Y Predicted = 7.9875696320409597  
Y actual = 56.014481109999998 | Y Predicted = 55.935758866058094  
Y actual = 77.996947700000007 | Y Predicted = 71.918488610730464  
Y actual = 55.370499529999996 | Y Predicted = 57.933600084142142  
Y actual = 11.89457829 | Y Predicted = 5.9897284139569127  
Y actual = 94.79081712 | Y Predicted = 95.892583227739038  
Y actual = 25.690415460000001 | Y Predicted = 22.971378767671315  
Y actual = 53.520423190000002 | Y Predicted = 57.933600084142142  
Y actual = 18.31396758 | Y Predicted = 22.971378767671315  
Y actual = 21.426377850000002 | Y Predicted = 18.975696331503219  
Y actual = 30.413032820000002 | Y Predicted = 24.969219985755363  
Y actual = 67.681421490000005 | Y Predicted = 63.927123738394286  
Y actual = 17.085478299999998 | Y Predicted = 20.973537549587267  
Y actual = 60.917927069999998 | Y Predicted = 58.932520693184166  
Y actual = 14.99514319 | Y Predicted = 18.975696331503219  
Y actual = 16.749239370000002 | Y Predicted = 15.978934504377149  
Y actual = 41.469238830000002 | Y Predicted = 41.950870339469766  
Y actual = 42.84526108 | Y Predicted = 42.94979094851179  
Y actual = 59.129129740000003 | Y Predicted = 60.930361911268214  
Y actual = 91.308636730000003 | Y Predicted = 91.896900791570943  
Y actual = 8.6733363570000002 | Y Predicted = 10.984331459167031  
Y actual = 39.31485292 | Y Predicted = 40.951949730427742  
Y actual = 5.3136862049999998 | Y Predicted = 0.99512536874679469  
Y actual = 5.4052205180000001 | Y Predicted = 7.9875696320409597  
Y actual = 68.545887899999997 | Y Predicted = 70.919568001688447  
Y actual = 47.334876289999997 | Y Predicted = 45.946552775637862  
Y actual = 54.090636859999996 | Y Predicted = 54.93683825701607  
Y actual = 63.29717058 | Y Predicted = 61.929282520310238  
Y actual = 52.459466880000001 | Y Predicted = 46.945473384679886

Ending Linear Regression with  $m = 0.99892060904202362$   $b = -0.0037952402952288961$  error = 7.8922376235243767