

- WODEN: A CUDA-enabled package to simulate
- 2 low-frequency radio interferometric data
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#### Software

- Review 🖸
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# Summary

WODEN is designed to simulate the response of a class of telescope known as an interferometer, producing output "visibilities" for a given astrophysical sky model. Simulated observations allow us to test other software packages that are designed to calibrate and analyse real interferometric data, including verifying expected behaviour with known inputs, and trialling new sky modelling techniques. The WODEN sky model can be specified in dirac-delta like functions on the sky (known in the field as "point sources") elliptical Gaussian models, or built out of "shapelet" basis functions (allowing complicated morphologies to be created). Users are able to input a bespoke layout for the interferometer, vary a number of observational parameters including time of day, length of observation and frequency coverage, and select from a number of predefined primary beams which encode the response of the receiving elements of an interferometer. This allows simulations of a number of telescopes to be undertaken. WODEN works with all Stokes I, Q, U, V sky polarisations, simulating telescopes with dual linear polarisations.

The core functionality of WODEN is written in CUDA as interferometric simulations are computationally intensive but embarrassingly parallel. The compute performance of CUDA allows for large-scale simulations to be run including emission from all directions in the sky. This is paramount for interferometers with a widefield of view such as the Murchison Widefield Array (MWA, Tingay et al. (2013)). A Python wrapper is used to take advantage of community packages such as astropy Astropy Collaboration et al. (2018), and to present a user-friendly interface to WODEN. Those simulating MWA observations can use the MWA metafits file to quickly feed in observational parameters to WODEN to match real data.

## Statement of need

- An interferometer creates visibilities V by cross-correlating signals detected between pairs of antennas or dishes (baselines), described by coordinates u,v,w. Each visibility is sensitive to the entire sky, directions of which we describe by the direction cosines l,m,n. The full
- 32 integral can be discretised as

$$V(u_i, v_i, w_i) = \sum_{j} \mathcal{B}(l_j, m_j) I(l_j, m_j) \exp[-2\pi i (u_i l_j + v_i m_j + w_i (n_j - 1))],$$

- where  $u_i,v_i,w_i$  are the visibility coordinates of the  $i^{\rm th}$  baseline,  $l_j,\,m_j,\,n_j$  is the sky position of the  $j^{\rm th}$  component in the sky model,  $I(l_j,m_j)$  is the flux density of that component, and
- $\mathcal{B}(l_i, m_i)$  the instrument beam pattern.



For a telescope like the MWA, the primary beam  $\mathcal{B}(l,m)$  is a complicated pattern on the sky, which is sensitive to emission from directly overhead to all the way down to the horizon. To truly capture the effects of astrophysical foregrounds we therefore have to simulate the entire sky. The MWA Fully Embedded Element (FEE, Sokolowski et al. (2017)) model is currently the most accurate representation of the MWA primary beam, and is incorporated into WODEN.

Under a formalism like the above, that splits the sky into discrete points, pushing  $j>=25\times 10^6$  can be required to achieve the angular resolution required. Furthermore, u,v,w are time and frequency dependent, so to sample in frequency of order 500 times and 100 samples in time, there are of order  $10^{12}$  visibility calculations to make. This makes CUDA acceleration paramount.

Alternative approaches to interferometric simulations exist, such as pyuvsim (which sacrifices speed for excellent precision), and RIMEz (which decomposes the sky into spherical harmonics 47 rather than discrete points). WODEN was designed with the Australian MWA Epoch of Reionisation (EoR) processing pipeline in mind, which uses a calibration and foreground removal software called the RTS (Mitchell et al., 2008) in search of signals from the very first stars (see Yoshiura et al. (2021) for a recent use of this pipeline). The RTS creates a sky model 51 using the same formalism above, however the code is not optimised enough to handle the 52 volume of sources to simulate the entire sky. To test the RTS method of sky generation, we therefore needed a fast and discretised method. Another excellent CUDA accelerated simulation package, OSKAR, addresses these two points. However, the RTS also generates 55 parts of the sky model via shapelets (see Line et al. (2020) for an overview), which OSKAR cannot. Furthermore, in real data, the precession of the Earth's rotational axis causes sources to move from the sky coordinates as specified in the RA, DEC J2000 coordinate system. The 58 RTS is designed to undo this precession, and so a simulation fed into the RTS should contain 59 precession. WODEN adds in this precession using the same method as the RTS to be consistent. This unique combination of CUDA, shapelet foregrounds, the MWA FEE primary beam, along 61 with source precession, created the need for WODEN. These effects should not preclude other calibration packages from using WODEN outputs however, meaning WODEN is not limited to feeding data into the RTS alone.

# **Example application**

In Line et al. (2020), we compared two methods to model Fornax A: a combination of point and elliptical Gaussians, compared to shapelets (see Figure 1). We were able to quickly compare the computational efficiency of the methods using a desktop, and comment on their respective strengths and weaknesses in regard to foreground removal for EoR purposes. Furthermore, as we could control the simulations, we could compare the methods in the absence of other processing systematics that are present in the real data from the MWA, which dominated the comparison when using the RTS alone.



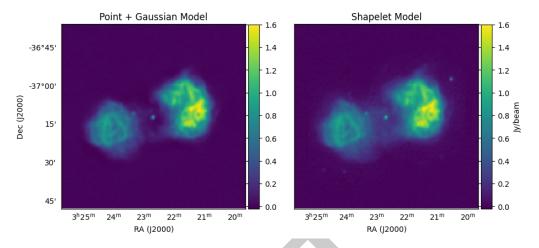


Figure 1: Two methods to simulate Fornax A visibilities are compared here (both imaged using WSClean (Offringa et al., 2014; Offringa & Smirnov, 2017)), with point and elliptical Gaussians on the left, and shapelets on the right.

## Documentation

- The documentation for WODEN can be found here on readthedocs, including a detailed instal-
- lation guide, ways to test a local installation, details of the calculations WODEN makes under
- the hood, and worked examples, which are also included in the github repo.

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