

- bmgarch: An R-Package for Bayesian Multivariate
- ₂ GARCH models
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Software

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Introduction

Generalized autoregressive conditional heteroskedasticity models (GARCH) and their multivariate extension (MGARCH) are part of the economists' toolbox ever since their introduction in the early 1980ies (Bollerslev, 1986; Engle, 1982; Tsay, 2013). Typically, the goal is to generate forecasts of volatility and covolatility for the next day or the near future in time series of assets or market indices. While GARCH models are primarily used in the econometric context, they can be used to capture and forecast heteroskedasticity in any time series. In fact, Rast et al. (2020) presented a parameterization for predicting and capturing within-person variability in human behavior in intensive longitudinal designs.

The main focus of MGARCH models is the estimation of the $p \times p$ conditional covariance matrix \mathbf{H}_t that varies over t=1,...,N time points and defines the (co-)volatility of p time series as $\boldsymbol{\epsilon}_t = \mathbf{H}_t^{1/2} \boldsymbol{\eta}_t$, where $\boldsymbol{\epsilon}_t$ is a $p \times 1$ vector of returns or residuals, assuming a process with a conditional mean of zero. $\boldsymbol{\eta}_t$ is a serially independent multivariate white noise process with covariance matrix \mathbf{I}_p . While conceptually straightforward, the crux is to define a model that maintains stationarity of the variances and covariances among the time series for all time points as well as positive definiteness for all \mathbf{H}_t . As such, a substantial amount of research of the past decades revolved around parameterizations of the conditional covariance matrix that fulfill all those desiderata (for a comparison of some of the most common parameterizations see Almeida et al., 2018).

Statement of need

While there are a number of readily available packages for univariate GARCH models in R, multivariate implementations are scarcely available. Currently, we are aware of only two packages in the Comprehensive R Archive Network (CRAN). One is mgarchBEKK (Schmidbauer et al., 2016) which implements BEKK as well as a bivariate asymmetric GARCH model. The other is rmgarch (Ghalanos, 2019), which includes DCC, GO-GARCH and Copula-GARCH models. Both packages are based on maximum likelihood methods. Moreover, some MGARCH models are implemented in proprietary software (such as Stata), but their focus is mostly limited to CCC, DCC, and VCC models without the option of estimating the location (e.g. time-varying mean returns) and scale (e.g. time-varying volatility) at the same time (Carnero & Eratalay, 2014). Again, these propietary solutions are based on maximum likelihood methods, while in contrast, bmgarch implements Bayesian methods for parameter estimation and inference.

At this current time, bmgarch implements a CCC (Bollerslev, 1990), DCC (Engle, 2002), pdBEKK (Rast et al., 2020), and a BEKK (Engle & Kroner, 1995) model based on either Gaussian or Student-t distributed innovations. All parameterizations allow arbitrary ARCH

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- and GARCH orders. The Bayesian framework is ideally suited to handle the necessary constraints imposed on the MGARCH specifications to both keep the solution stationary and all
- $_{ ext{41}}$ t conditional covariance matrices \mathbf{H}_t positive definite. Moreover, the model allows one to
- 42 examine the posterior distribution in order to obtain the full range of Bayesian inference.
- 43 The model parameters are estimated using the probabilistic programming language Stan Stan
- Development Team (2016), which also allows one to use stan related diagnostics implemented
- in rstan Stan Development Team (2020).

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- The package is designed to take multivariate time series only. Hence, in terms of data, the minimum requirement is a data frame or matrix with at least two columns, representing the
- time series. Note that bmgarch currently does not support missing values in time series, nor
- in the predictor variables.
- The default behavior in bmgarch is to estimate a CCC(1,1) parameterized model of order
- $_{
 m 52}$ $\,$ 1 for the ARCH and GARCH components assuming Student-t distributed innovations and a
- constant means (zero, typically) structure. The model is fit using 4 chains with 2000 iterations
- each (half of those are warm-up and the other half are sampling). As such, the minimum call
- will be bmgarch(data = X) with X being a matrix or data frame with at least 2 columns.
- $_{56}$ In order to include the effect of an external predictor variable on the unconditional and constant
- covariance term C, one can include a predictor Y of the same dimension as X with bmgarch (da ta = X, xC = Y). Further, bmgarch takes a number of model related arguments governing
- the type of parameterization (parameterization = {"CCC", "DCC", "BEKK", "pdBEKK"
- the type of parameterization (parameterization ($Q = \{1, ..., t-1\}$) and ARCH ($Q = \{1, ..., t-1\}$)
- processes, the mean structure (meanstructure = {"constant", "arma"}) and the type
- of distribution (distribution = {"Student_t", "Gaussian"}). The function also takes
- arguments with respect to sampling (number of iterations and number of chains) as well
- as whether data should be z-standardized before sampling (standardize_data = {FALSE,
- TRUE}) this last argument can facilitate the estimation process.
- Objects of the bmgarch family can be passed to the plot() function, print(), and summar
 - y() for a summary table.
- Moreover, each estimated model can be passed to the forecasting() function to generate m-
- $_{99}$ ahead forecasts of variances, correlations, and, if the ARMA(1,1) is enabled, means. Moreover,
- bmgarch integrates model ensemble techniques to generate model weighted forecasts (and
- ₇₁ estimates) based on Bayesian model averaging and stacking techniques described by Yao et
- al. (2018) and Bürkner et al. (2020). The forecasted objects can again be plotted and
- summarized via the corresponding generic functions.

Summary

- 75 The bmgarch package implements four MGARCH parameterizations and estimates all param-
- eters via a Bayesian framework. Sampling from the posterior distribution is based on HMC
- $_{77}$ and is implemented via stan. The bmgarch objects can be printed and plotted as well as
- ₇₈ passed on to a forecasting function that runs either simple or ensemble forecasts.



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