

*Equinox- equal day/night  
Solstice- longest day/night*

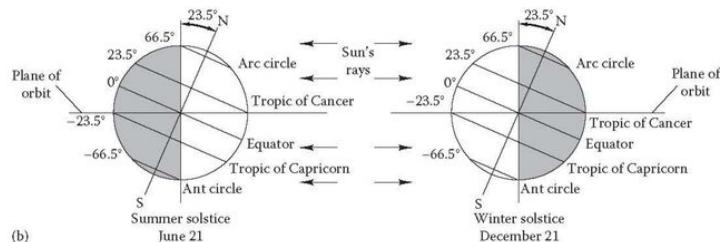


Figure 4.1 Geometry of the earth's orbit and inclination of polar axis: (a) entire orbit and (b) enlarged detail, solstices.

From Boyle, 2004

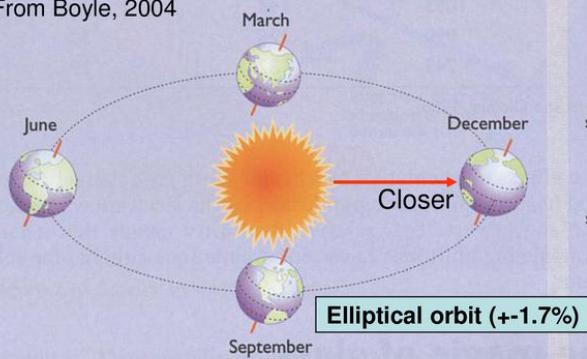
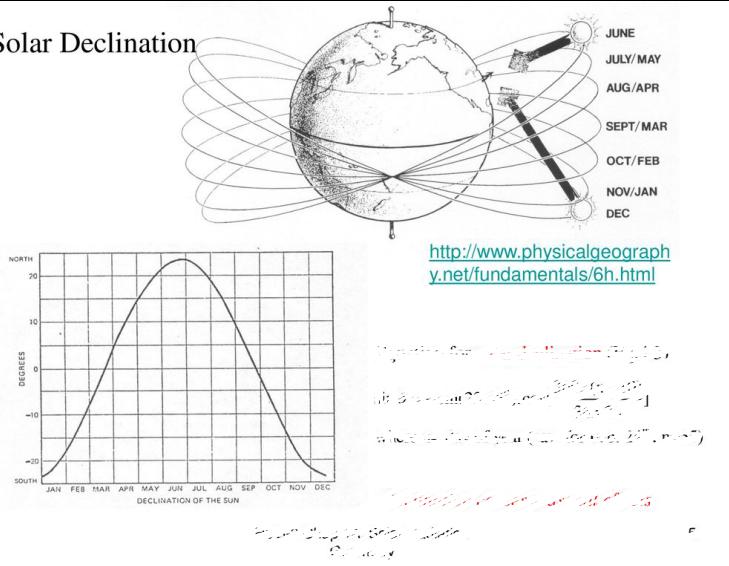


Figure 2.9 The earth revolves around the sun with its axis tilted at an angle of  $23.5^\circ$

Figure 2.10 The tilt of the earth's axis creates summer and winter

### Solar Declination



### TERRESTRIAL SOLAR RADIATION

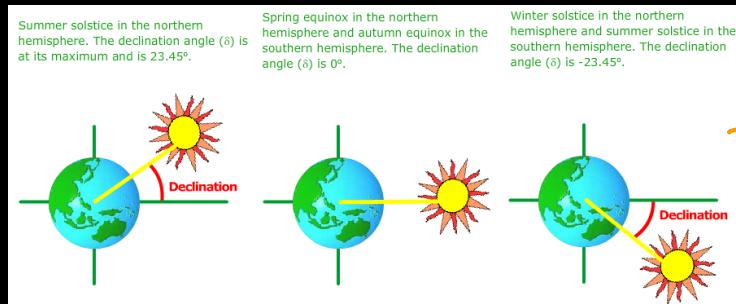
TIDE

Solar Radiation on Earth  
Surface is relatively constant, but slightly varies due to

- atmospheric effect, including absorption and scattering
- local variation of atmosphere
- latitude of the location.
- the season of the year and time of the day.

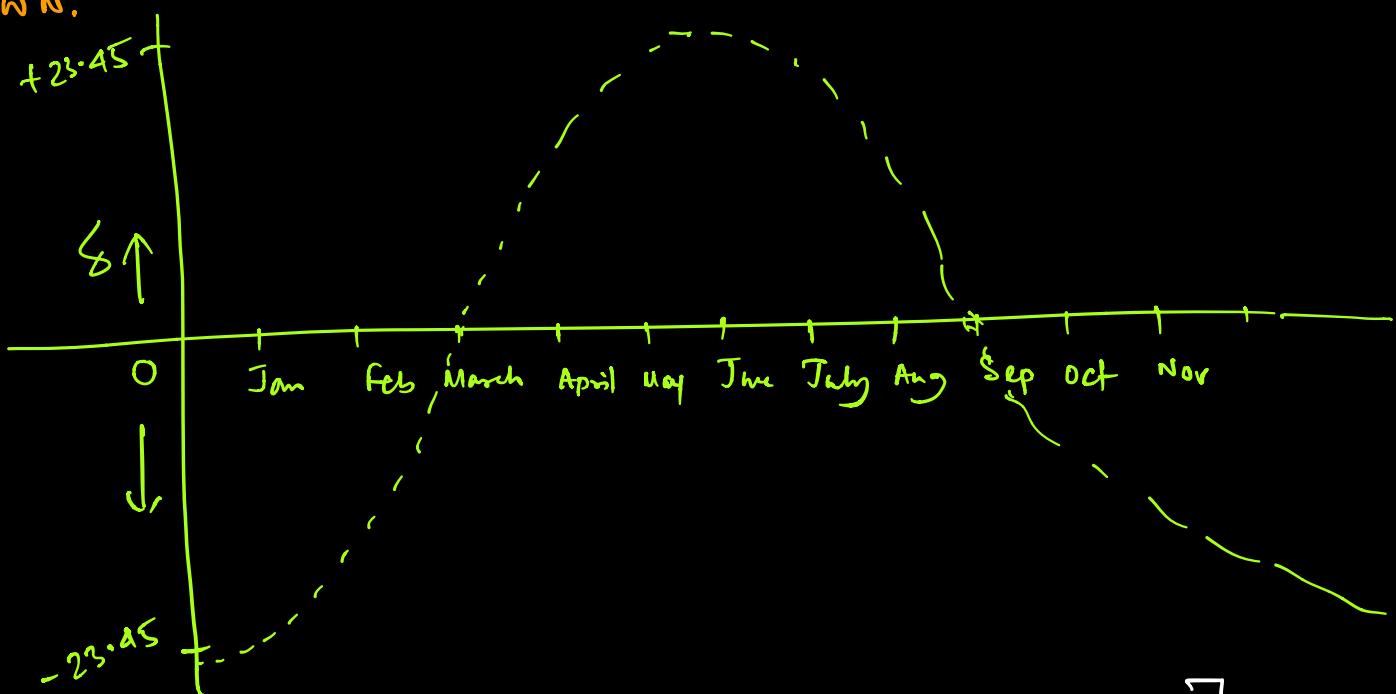
## DECLINATION ANGLE

THE DECLINATION ANGLE, DENOTES ' $\delta$ ' VARIES SEASONALLY DUE TO THE TILT OF THE EARTH ON ITS AXIS OF ROTATION AND THE ROTATION OF EARTH AROUND SUN. IF THE EARTH WAS NOT TILTED ON ITS AXIS, THEN  $\delta = 0$ . ALWAYS. HOWEVER THE EARTH IS TILTED, by  $23.45^\circ$  AND THE DECLINATION ANGLE VARIES  $+/- 23.45^\circ$ . ONLY AT THE SPRING AND FALL EQUINOXES,  $\delta$  is zero.



THE SEASONAL VARIATION OF DECLINATION ANGLE IS SHOWN.

THE DECLINATION OF THE SUN IS THE ANGLE BETWEEN THE EQUATOR AND A LINE DRAWN FROM THE CENTRE OF THE EARTH TO THE CENTRE OF THE SUN.



$$[\delta] = \frac{23.45}{365} \sin \left[ \left( \frac{360}{365} \right) (289 + n) \right] \quad (1)$$

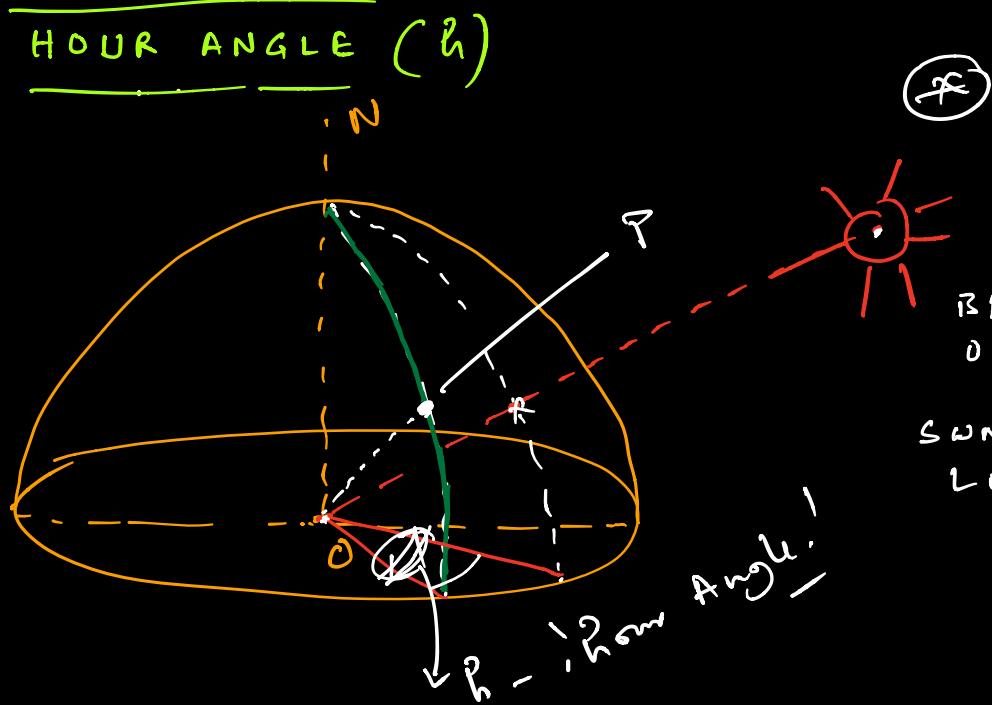
$n$  is the day of the year.

$$[(\text{e.g. Jan 1st}; n=1)]$$

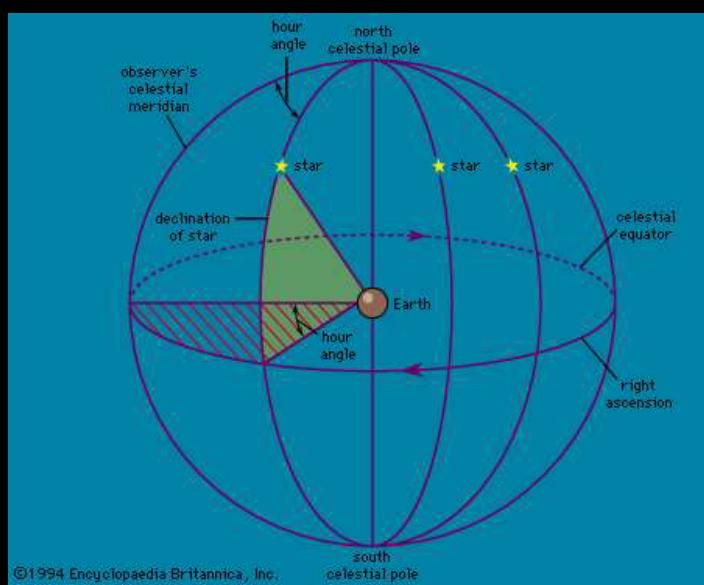
THE EQUATION ALSO ASSUMES

THAT, THE SUN'S ORBIT IS A PERFECT CIRCLE AND THE FACTOR OF  $360/365$  CONVERTS THE DAY NO.

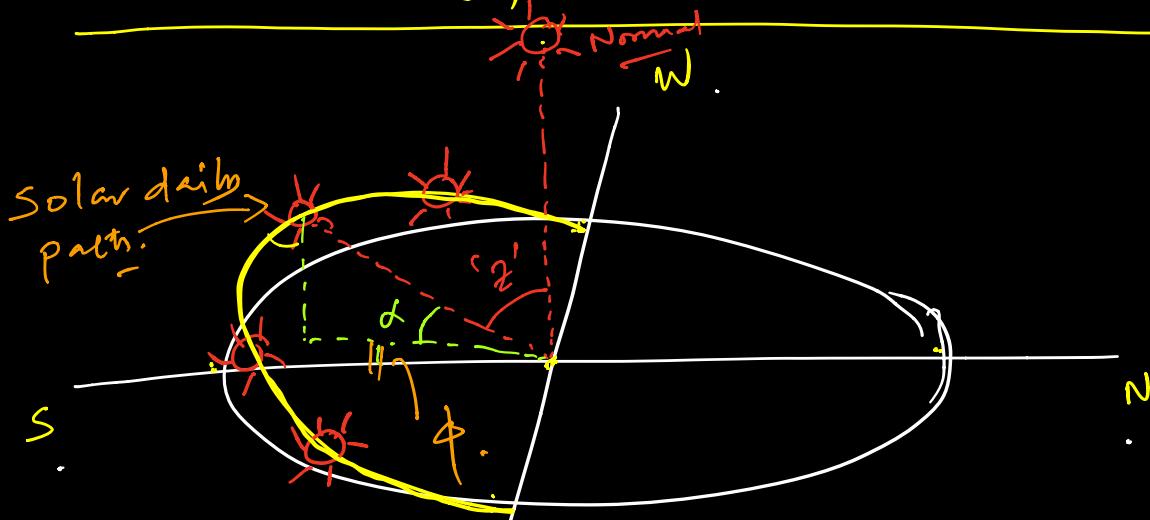
TO A POSITION IN THE ORBIT.

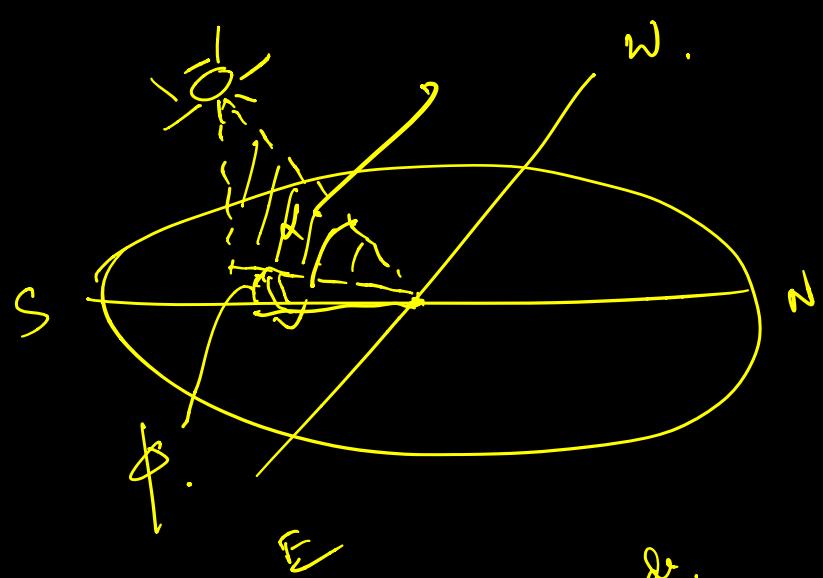
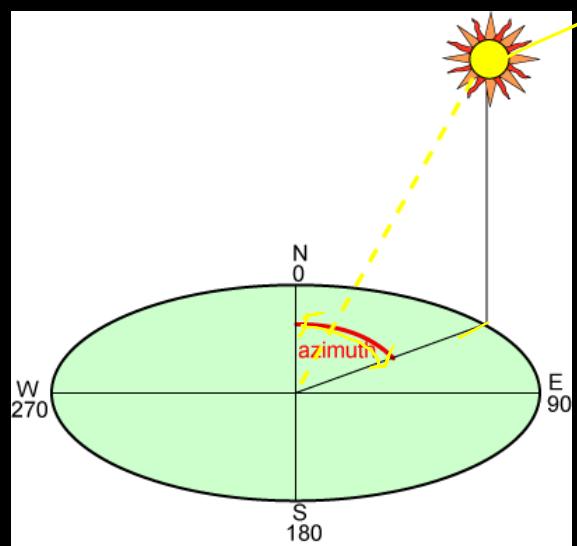


THE ANGLE MEASURED ON THE EARTH'S EQUATORIAL PLANE BETWEEN THE PROJECTION OF THE SUN-EARTH CENTRE LINE.



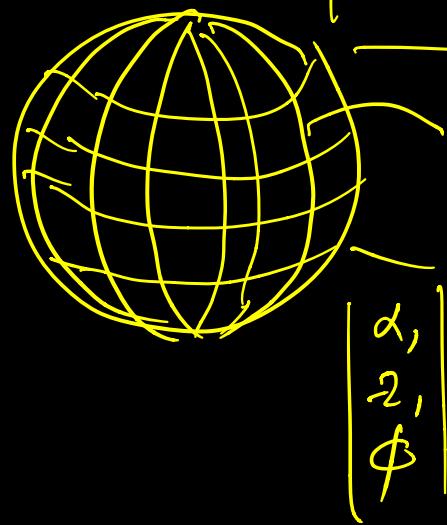
ZENTTH ANGLE, ALTITUDE ANGLE ( $\alpha$ ) and AZIMUTH ANGLE ( $\phi$ )





$$\cos \alpha = \sin \delta = \sin L \sin \delta + \cos L \cos \delta \cos h.$$

$$\sin \phi = \cos \delta \frac{\sin h}{\cos \alpha} \quad (3)$$



Sun rise and Sun set.

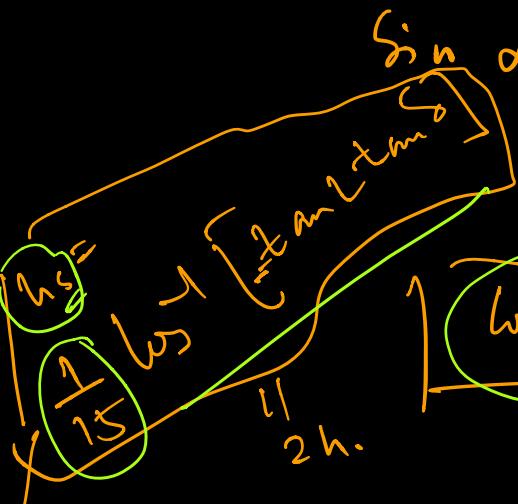
Sun set.,  $h_s$  hour angle at  
At Sun set condition,  $\sin \text{set.} = h_s$

$$\alpha = 0$$

$$\sin \alpha = \sin 0 = \sin L \sin \delta + \cos L \cos \delta \cos h_s$$

$$0 = \sin L \sin \delta$$

$$+ \cos L \cos \delta \cos h_s.$$



$$\cos h_s = - \tan L \tan \delta$$

$$h_s = \cos^{-1} [- \tan L \tan \delta] i-$$

PROBLEM → FIND THE SOLAR ALTITUDE ( $\alpha$ ) AND AZIMUTH ANGLE AT 2 hrs. AFTER LOCAL SOLAR NOON. ON JUNG<sup>184</sup>. FOR A CITY LOCATED AT  $40^{\circ}$ N. LATITUDE. ALSO FIND THE SUNRISE AND SUNSET TIME AND THE DAY LENGTH.

$$h = +30^{\circ}, \quad h = 152$$

$$L = 40^{\circ} \text{N.}$$

$$\alpha, \phi$$

$$\left. \begin{aligned} \text{Total day length} \\ = \frac{2}{15} \text{ hrs} \left[ -\tan L \right] \end{aligned} \right\}$$

$$\delta = 23.45 \quad \sin \left[ \frac{360}{365} (289 + 152) \right]$$

$$= +22^{\circ}$$

$$\left. \begin{aligned} \text{Total day length} \\ = \frac{2}{15} \text{ hrs} \left[ -\tan L + \tan \delta \right] \end{aligned} \right\}$$

$$= \frac{2}{15} \text{ hrs} \left[ -\tan 40 + \tan 22^{\circ} \right]$$

$$\boxed{\alpha = 58.9^{\circ}}$$

$$\boxed{\phi = 63.9^{\circ}}$$

$$\boxed{\sin \phi = \cos \delta \frac{\sin L}{\cos \alpha}}$$

$$\left. \begin{aligned} \text{day length} &= 14.6 \text{ hr.} \end{aligned} \right\}$$

$$\text{What time of sunset} \quad 12.00 \text{ noon} + 7.3 \quad \text{M} \quad 7.3 \text{h.}$$

