

## Instructions

- Make a document (either in .doc and .pdf) containing code, results. Named the file using both of your Roll nos. *i.e.* 140100001\_140100002
- Write Up: (i) Software in which code is written, (ii) output results for each case, and (iii) explanation of results.
- Please upload all assignments to turnitin

## Assignment 6

**Due date: 23/10/2017, time: 12 midnight**

### **Solution of Ordinary Differential Equation**

#### **Question: 1**

Write a program to solve the following ODE using (i) Euler Method, (ii) Modified Euler Method and (iii) Trapezoidal Method.

1.  $\frac{dy}{dx} = \log(x + y)$ . At  $y(0) = 2$ , at  $x = 1.2$  and  $x = 1.4$  with  $h = 0.2$

For both Backward Euler and Trapezoidal Methods, the code should solve the implicit equation iteratively for  $y_{(n+1)}$ . The first guess for both cases should be the one predicted using forward Euler method.

In code, there should be an option of choosing number of iterations.

- I. For  $n = 0$ , the code should iterate till the solution converges. The convergence criterion can be chosen as  $10^{-6}$ .
- II. For  $n = 1$ , it will be a simple predictor-corrector scheme.
- III. For  $n = 10$ , only 10 iterations will be computed.
- IV. Use the following values of  $h$ : (i)  $10^{-4}$ , (ii)  $10^{-3}$  and (iii)  $10^{-2}$ .
- V. Carry out solution till  $x = 5$

#### **Results to report:**

The following graphs should be plotted:

1. Solutions obtained from forward Euler, backward Euler (converged), trapezoidal (converged).
2. Plot the variation of residual with iterations
3. In each case, and for each  $h$ : Compare Backward Euler and Trapezoidal methods with different values of  $n$ .