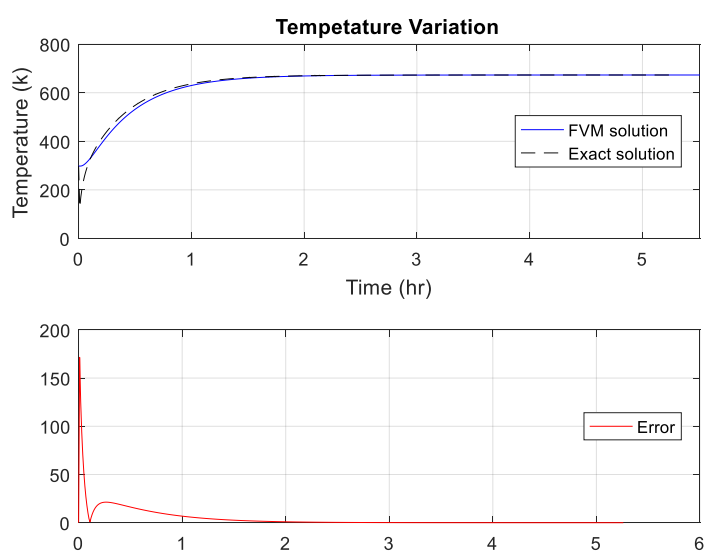
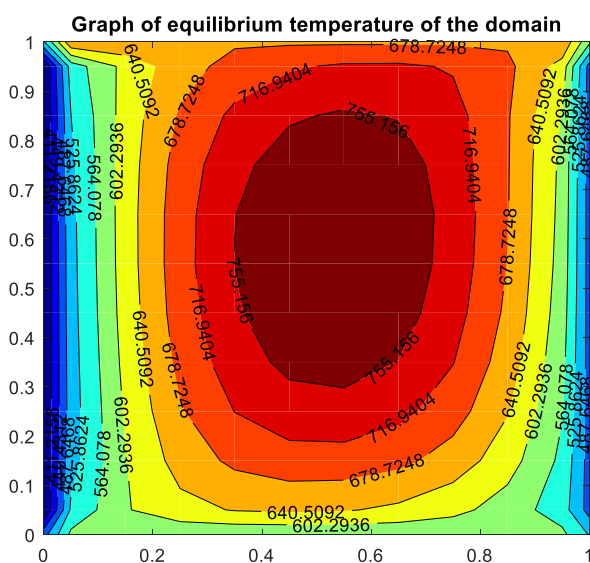




## ASSIGNMENT 2

## COMPUTATIONAL FLUID DYNAMICS AND HEAT TRANSFER



Assignment 2: Transient Heat Conduction

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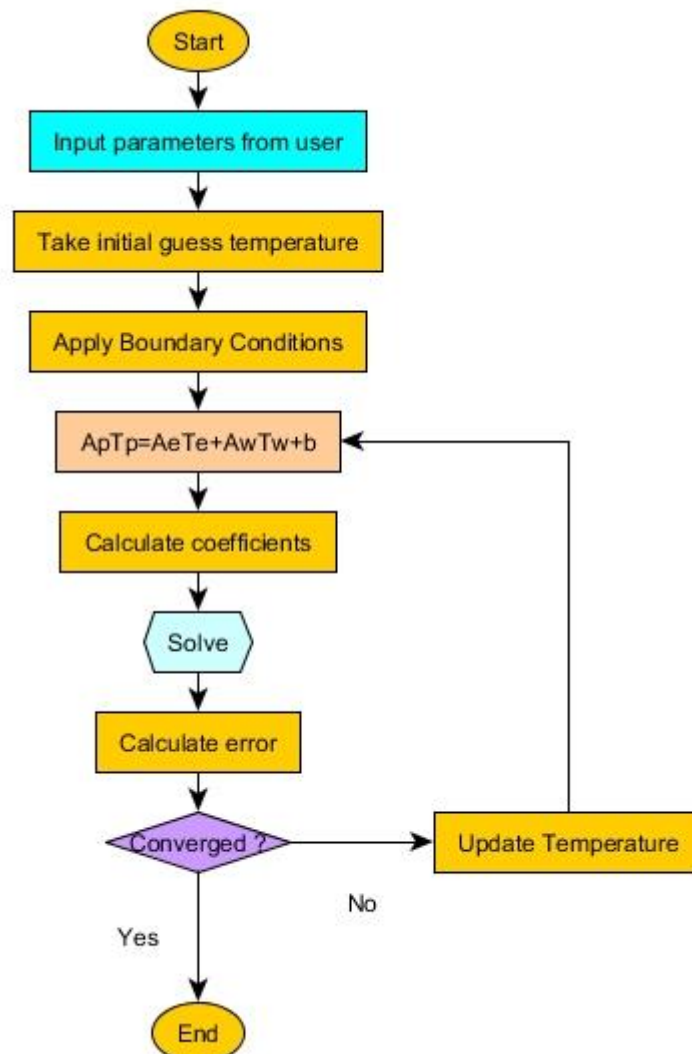
---

Problem 1:

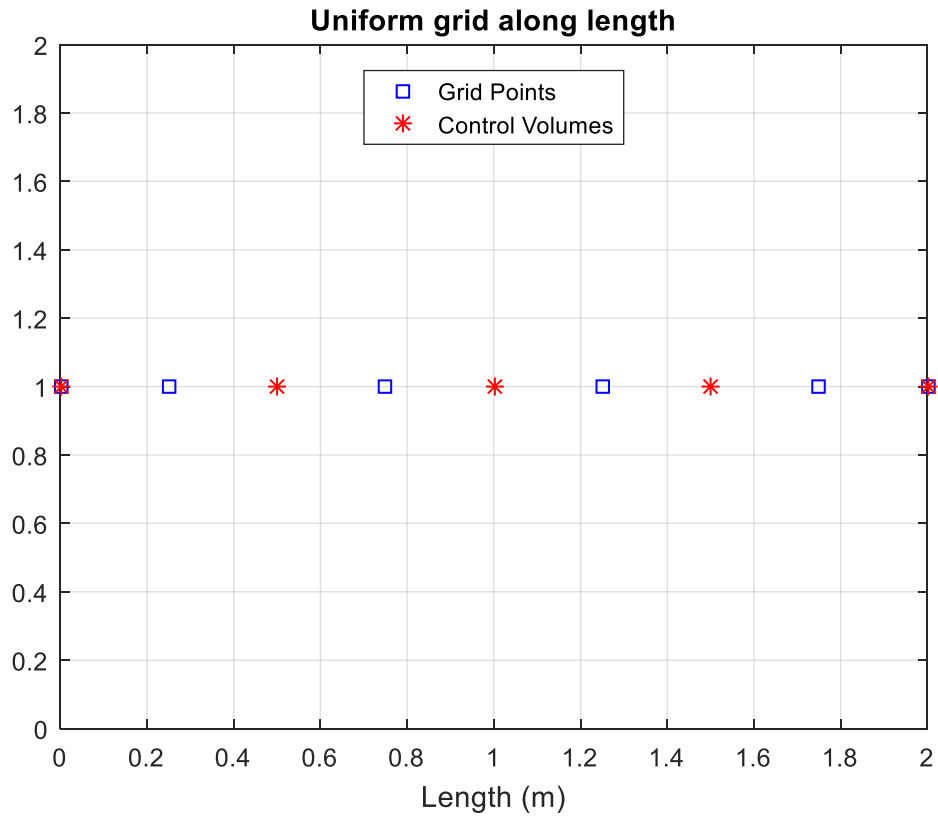
One-dimensional stainless steel bar of width 2 m and a constant thermal diffusivity of  $1 \text{ m}^2/\text{hr}$ . The bar is initially ( $t=0$ ) at a uniform temperature of  $25^\circ\text{C}$ . At  $t > 0$ , the surface temperatures of the left ( $x = 0$ ) and right ( $x = L$ ) faces are suddenly increased to  $400^\circ\text{C}$ , and maintained at this temperature thereafter. There are no sources within the wall. Determine the time at which the middle length temperature reaches  $400^\circ\text{C}$ . Plot the temperature distribution at middle length from 0 to 1 hr in steps of 0.1 hr. Plot the time-temperature graph along  $x$  direction. Solve the problem with the fully explicit method using FVM. Choose appropriate grid size taking into account of the stability criterion as discussed in class.

---

Algorithm



## Grid details and the implemented boundary condition



**Fig 1.** Generated grid for the given Cartesian geometry

### Boundary Conditions

- On the left boundary uniform temperature 673K is applied
- On the right boundary uniform temperature 673K is applied

### Governing Equation

$$\alpha \frac{\partial^2 T}{\partial x^2} = \frac{\partial T}{\partial t}$$

### Integrating Governing equation over the control volume

$$\int_t^{t+\Delta t} \int_w^e \frac{\partial T}{\partial t} \cdot dt \cdot dx = \alpha \int_t^{t+\Delta t} \int_w^e \frac{\partial^2 T}{\partial x^2} \cdot dt \cdot dx$$

### Explicit scheme used for evaluation of the temperature.

$$(T_P^n - T_P^o) \cdot \Delta x = \alpha \left[ \frac{(T_E^o - T_P^o)}{\delta x_e} + \frac{(T_P^o - T_W^o)}{\delta x_w} \right] \cdot \Delta t$$

### Final Discretized form

$$T_P^n = \left( \frac{\alpha \Delta t}{\Delta x \cdot \delta x_e} \right) T_E^o + \left( 1 - \frac{\alpha \Delta t}{\Delta x \cdot \delta x_e} - \frac{\alpha \Delta t}{\Delta x \cdot \delta x_w} \right) T_P^o + \left( \frac{\alpha \Delta t}{\Delta x \cdot \delta x_w} \right) T_W^o$$

### Stability Criteria

$$\frac{\alpha \Delta t}{\Delta x} \left( \frac{1}{\delta x_e} + \frac{1}{\delta x_w} \right) \leq 1$$

### For the first point

$$\delta x_e = \Delta x$$

$$\delta x_w = \Delta x / 2$$

### For all other points

$$\delta x_e = \Delta x$$

$$\delta x_w = \Delta x$$

### By taking the critical value amongst the two will give us

$$\frac{\alpha \Delta t}{\Delta x^2} \leq \frac{1}{3} \quad \dots \text{Eq. (1)}$$

The designed code takes care of the stability based on the Eq.1. The correct value for  $\Delta t$  and  $\Delta x$  will be displayed as output. Code will reiterate till the user gives the correct input as per the stability criteria.

## Code of the problem

```
%=====
% Assignment 2 CHDHT ME 415
% Problem Number 1. 1D Transient Problem
% Program uses FVM to solve the problem of 1D conduction
% Heat generation is not present
% Designed only for rectangular co-ordinate system
%
% AUTHOR:
% Sanit P. Bhatkar (173109003@iitb.ac.in)
% Roll No: 173109003
% Place: IIT BOMBAY.
%=====

%% Input of Variables %%

clc
clearvars
fprintf('\n===== Unsteady Heat conduction in solid =====');
fprintf('\n\n----- INPUT ----- \n');

%flag is used for correct stability input
flag=1;
error=1;
% l=2;
% alp=1;
% dt=0.01;
% dl=0.5;

eps=0.001;
l=input('\nLength of the domain in m: ');
alp=input('Thermal diffusivity m^2/hr: ');
dt=input('\nInput unit time step in hr: ');
dl=input('Input unit grid size in m: ');

%% Stability Criteria %%

%CFL criteria is used for stability of the scheme

fprintf('\n----- Stability Criteria ----- \n');

while flag > 0

if dt/((dl)^2)<= 1/(3*alp)
    %Only when correct input is given, the loop will stop
    fprintf('\nScheme is stable for dt= %d and dx= %d\n',dt,dl);
    flag=0;
else

    fprintf('\nScheme is unstable for dt= %d and dx= %d\n',dt,dl);
    %Stable value of dt
    dtt=((dl)^2)/(3*alp);
    fprintf('\nFor stability choose dt less than dt= %d for dx= %d\n',dtt,dl);
    fprintf('or');

    %Stable value of dx
    dxx=(3*alp*dt)^0.5;
    fprintf('\nFor stability choose dx greater than dx= %d for dt= %d\n',dxx,dt);

    %flag is used for correct stability input
    dt=input('\nInput unit time step: ');
```

```

    dl=input('Input unit grid size: ');

end

end

%% Grid Formation %%

%=====FINITE VOLUME METHOD=====

%STEP 1: Divide domain into finite sized subdomain called control volumes

%Our domain is uniform
%But boundary and the first point grid space is different
%That is why separate calculation is done
%sx represents the number of points in a grid in x direction
%NOTE: dl has to be some multiple of length

sx=(l/dl)+2;
x(1,1)=0;
x(sx,1)=l;
x(2,1)=x(1,1)+(dl/2);
for m=3:sx-1
    x(m,1)=x(m-1,1)+dl;
end

%STEP 2: Integrate governing equation over boundaries of control volume

%STEP 3: Profile assumption

%Piecewise linear profile is assumed for integral
%We will get equation of type
%ApnTpn=ApoTpo+AwoTwo+AeoTeo
%Assuming isotropic material and uniform control volume

%% Boundary Conditions %%

% tbw=400+273;
% tbe=400+273;
tbe=input('\nInput west boundary condition in degree C: ');
tbw=input('Input west boundary condition in degree C: ');
tbe=tbe+273;
tbw=tbw+273;

%Initial Condition
% Tini=25+273;
Tini=input('Input initial condition in degree C: ');
Tini=Tini+273;

%% Actual Solution %%

%st represents the time step number

st=1;
T(st,1:sx)=Tini;
T_steady(st,1:sx)=tbw;

while error>eps
%As the final time is not known, loop is run till steady state is reached

```

```

st=st+1;
T(st,1)=tbw;
T(st,sx)=tbe;

for j=2:sx-1

    dxe=x(j+1)-x(j);
    dxw=x(j)-x(j-1);
    r=(alp*dt)/dl;

    ae=r/dxe;
    aw=r/dxw;
    ap=1-ae-aw;

    %Worked out formula
    T(st,j)=aw*T(st-1,j-1)+ap*T(st-1,j)+ae*T(st-1,j+1);

end

%Absolute error definition is used
%for checking the steady state condition
error=abs(T(st,round(sx/2))-tbw);

end

%% Analytic Solution

te=1;
error=1;
Te(1,1:sx)=Tini;

while error>eps

    %te represents the time step number
    te=te+1;
    Te(te,1)=tbw;
    Te(te,sx)=tbe;

    for j=2:sx-1

        sum=0;

        %Analytic solution
        for m=1:1000
            p=exp(-(m*pi/l)^2*alp*te*dt);
            p=p*((1-(-1)^m)/(m*pi));
            p=p*sin(pi*x(j)*m/l);
            sum=sum+p;
            Te(te,j)=tbw+2*(Tini-tbw)*sum;
        end

    end

    %Absolute error definition is used
    %for checking the steady state condition
    error=abs(Te(te,round(sx/2))-tbw);

end

```

```

%% Output

%Kelvin to degree C converion
T=T-273;
Te=Te-273;
%===== OUTPUT =====

fprintf('\n\n----- OUTPUT ----- \n\n');

end_time=(st-1)*dt;
fprintf('Time required for attending steady state by FVM is %dhr',end_time);

end_exact=(te-1)*dt;
fprintf('\nTime required for attending steady state by exact solution is
%dhr',end_exact);

figure (1)
%Grid point plotting
%Blue squares represent the actual points
y=ones(1,sx);
plot(x,y,'bs');
title('Uniform grid along length')
grid on
hold on

%Control Volume plotting
yy=ones(1,sx-1);
xx(1,1)=x(1,1);
xx(sx-1,1)=x(sx,1);
for i=2:sx-2
    xx(i)=(x(i+1)+x(i))/2;
end
plot(xx,yy,'r*');
legend('Grid Points','Control Volumes','Location','North');
xlabel('Length (m)');
hold off

figure (2)

subplot(2,1,1)
%FVM solution plot
t=0:dt:end_time;
[n n]=size(t);

plot(t,T(1:n,round(sx/2)),'b')
title('Tempetature Variation in degree C')
hold on

%Exact solution plot
tt=0:dt:end_exact;
[n n]=size(tt);
plot(tt,Te(1:n,round(sx/2)),'--k')

hold on
grid on
xlabel('Time (hr)');
ylabel('Temperature in degree C');
xlim([0,end_time])
hold off
legend('FVM solution','Exact solution','Location','East');

```



```
subplot(2,1,2)
%Error calculation
dummy=T(1:n,1:sx);
error=abs(Te-dummy);
plot(tt,error(1:n,round(sx/2)),'r')
legend('Error','Location','East');
grid on
```

```
[g k]=size(T);
figure(3)
for i=1:(1/(10*dt)):g
    plot(x,T(i,1:k));
    hold on
end
hold off
grid on
title(' Time-Temperature graph along x-direction');
xlabel(' Length m ');
ylabel(' Temperature in degree C ');
```

```
%
```

---

## Results and Discussion

### A. Time required to reach steady state

===== Unsteady Heat conduction in solid =====

----- INPUT -----

Length of the domain in m: 2

Thermal diffusivity  $\text{m}^2/\text{hr}$ : 1

Input unit time step in hr: 0.1

Input unit grid size in m: 0.5

----- Stability Criteria -----

Scheme is unstable for  $\text{dt} = 1.000000\text{e-}01$  and  $\text{dx} = 5.000000\text{e-}01$

For stability choose  $\text{dt}$  less than  $\text{dt} = 8.333333\text{e-}02$  for  $\text{dx} = 5.000000\text{e-}01$

or

For stability choose  $\text{dx}$  greater than  $\text{dx} = 5.477226\text{e-}01$  for  $\text{dt} = 1.000000\text{e-}01$

Input unit time step: 0.01

Input unit grid size: 0.5

Scheme is stable for  $\text{dt} = 1.000000\text{e-}02$  and  $\text{dx} = 5.000000\text{e-}01$

Input west boundary condition in degree C: 400

Input west boundary condition in degree C: 400

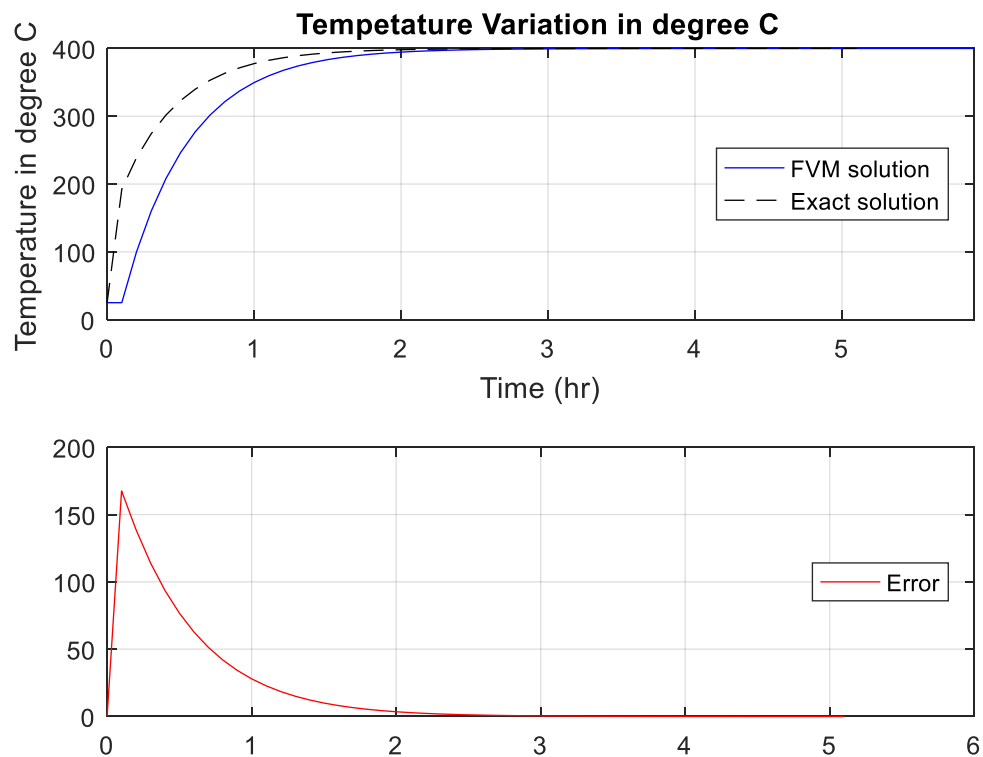
Input initial condition in degree C: 25

----- OUTPUT -----

Time required for attending steady state by FVM is 5.510000e+00hr

Time required for attending steady state by exact solution is 5.260000e+00hr

### B. Temperature plot at middle length with $\Delta t = 0.1\text{hr}$



===== Unsteady Heat conduction in solid =====

----- INPUT -----

Length of the domain in m: 2

Thermal diffusivity  $\text{m}^2/\text{hr}$ : 1

Input unit time step in hr: 0.1

Input unit grid size in m: 1

----- Stability Criteria -----

Scheme is stable for  $dt= 1.000000e-01$  and  $dx= 1$

Input west boundary condition in degree C: 400

Input west boundary condition in degree C: 400

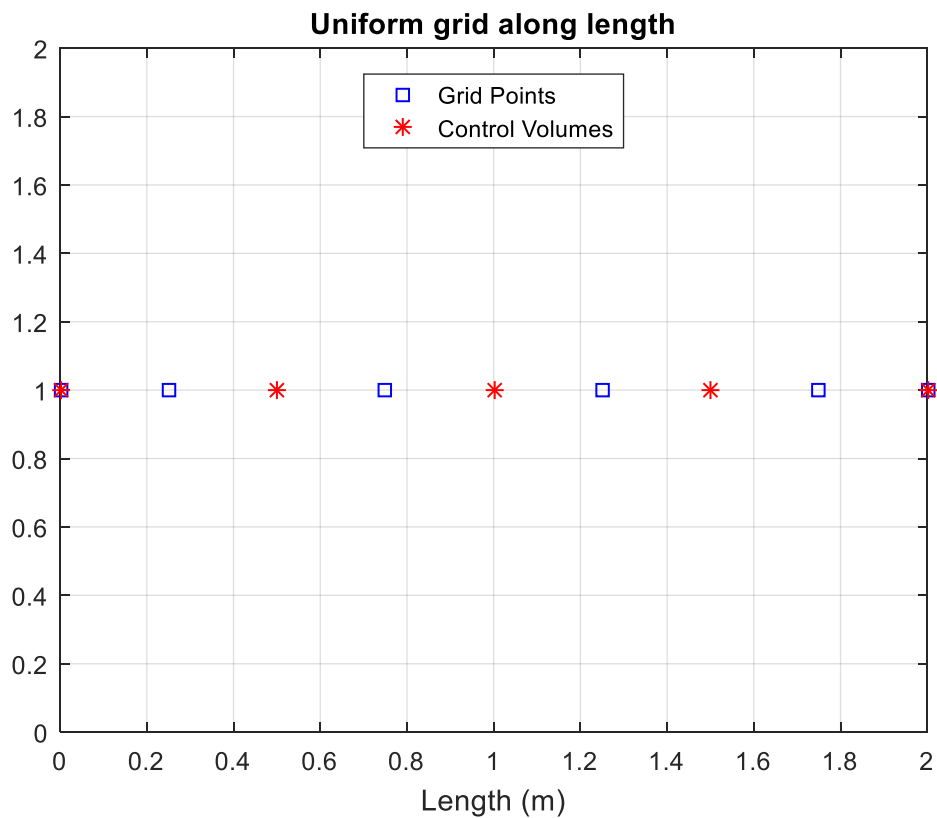
Input initial condition in degree C: 25

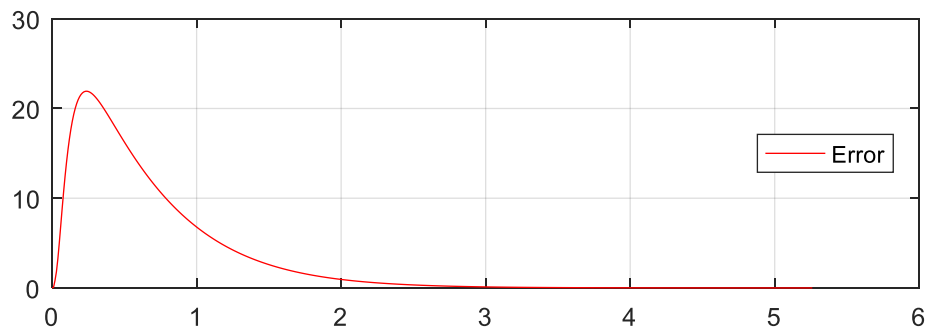
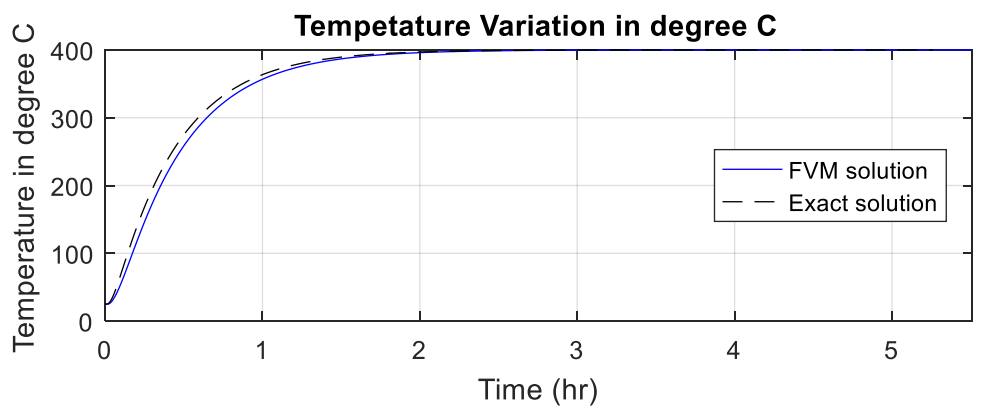
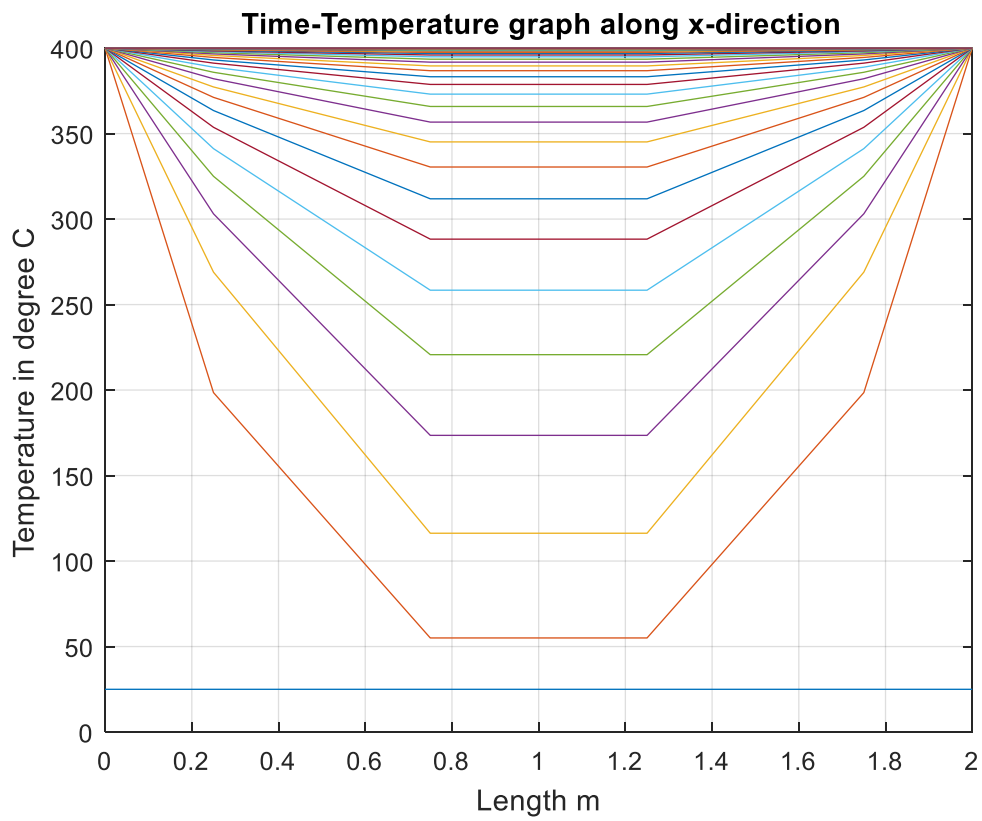
----- OUTPUT -----

Time required for attending steady state by FVM is  $5.900000e+00hr$

Time required for attending steady state by exact solution is  $5.100000e+00hr$

### C. Time-Temperature graph along x direction





===== Unsteady Heat conduction in solid =====

----- INPUT -----

Length of the domain in m: 2

Thermal diffusivity  $\text{m}^2/\text{hr}$ : 1

Input unit time step in hr: 0.01

Input unit grid size in m: 0.5

----- Stability Criteria -----

Scheme is stable for  $\text{dt} = 1.000000\text{e-}02$  and  $\text{dx} = 5.000000\text{e-}01$

Input west boundary condition in degree C: 400

Input west boundary condition in degree C: 400

Input initial condition in degree C: 25

----- OUTPUT -----

Time required for attending steady state by FVM is  $5.510000\text{e+}00\text{hr}$

Time required for attending steady state by exact solution is  $5.260000\text{e+}00\text{hr}$

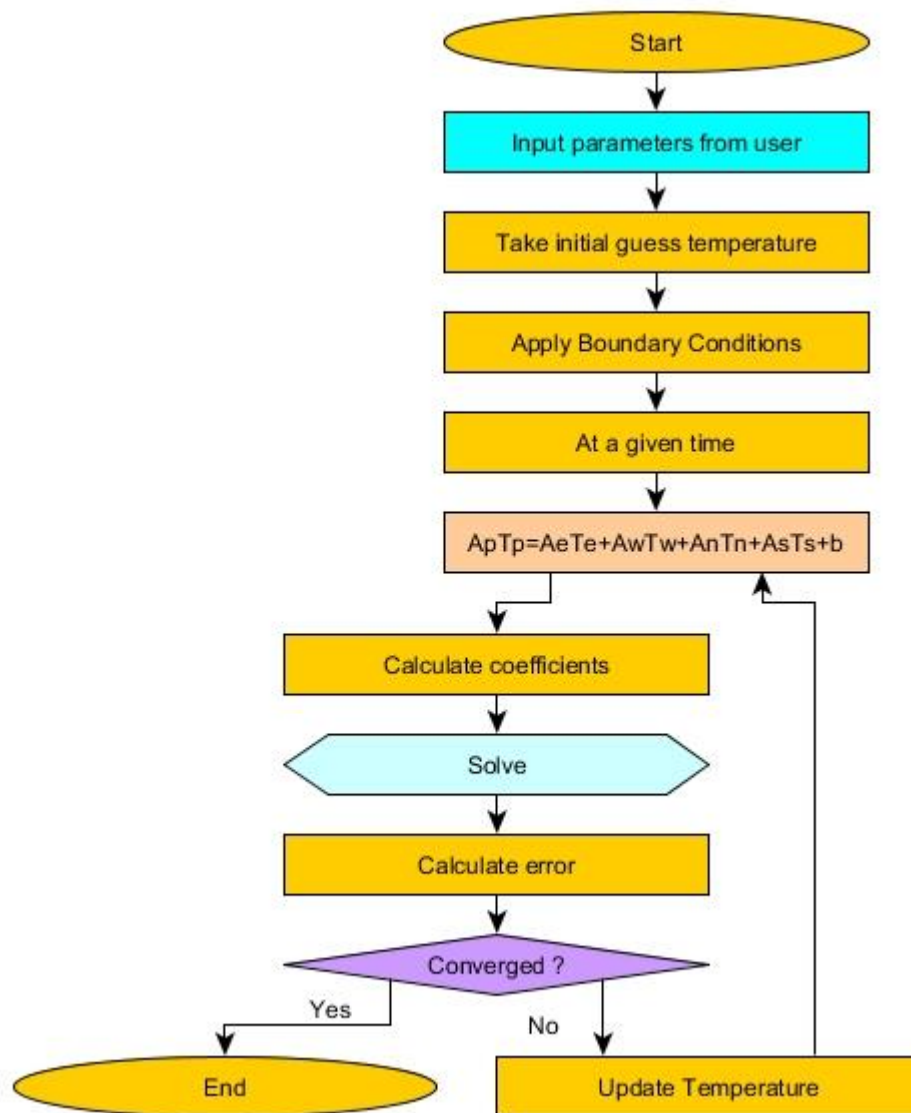
---

## Problem 2:

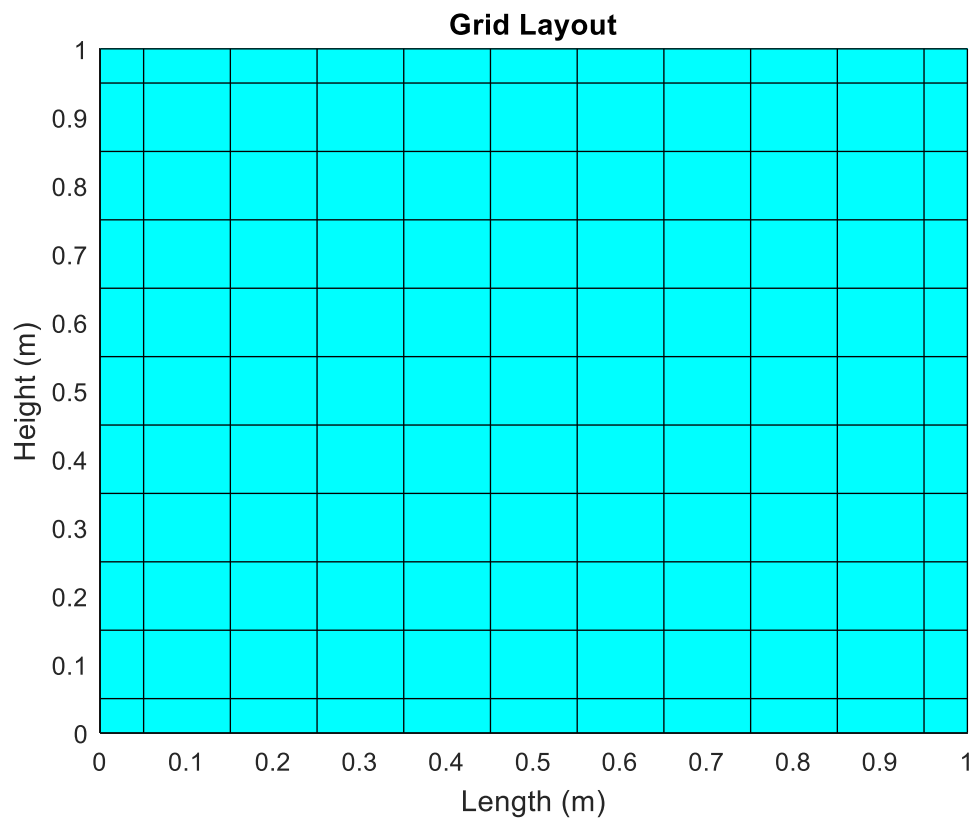
2-D Computational Heat Conduction (CHC) on a uniform grid, with implicit method Consider 2D conduction in a square shaped ( $L_1=1\text{m}$  and  $L_2=1\text{m}$ ) long stainless-steel (density  $\rho$ :  $7750\text{ kg/m}^3$ , specific-heat  $C_p$ :  $500\text{ J/Kg K}$ , thermal-conductivity  $k$ :  $16.2\text{ W/m-K}$ ) plate. The plate is initially at a uniform temperature of  $300^\circ\text{C}$  and is suddenly subjected to a constant temperature of  $T_{wb} = 100^\circ\text{C}$  on the west boundary,  $T_{sb} = 200^\circ\text{C}$  on the south boundary,  $T_{eb} = 300^\circ\text{C}$  on the east boundary, and  $T_{nb} = 400^\circ\text{C}$  on north boundary. Present a CFD application of the code for a volumetric heat generation of 0 and  $50\text{ kW/m}^3$ . Consider maximum number of grid points as  $i_{\text{max}} \times j_{\text{max}}=12 \times 12$  and the steady state convergence tolerance as  $\epsilon_{\text{st}}=10^{-4}$ . Plot the steady state temperature profiles with and without volumetric heat generation.

---

## Algorithm



## Grid details and the implemented boundary condition



**Fig 2.** Generated uniform grid for given Cartesian geometry

### Grid Specifications

A uniform grid was generated. Black lines are passing through the actual points on the domain. Control volume surfaces lie at half the unit distance from them.

### Boundary Conditions

- On the left boundary uniform temperature  $100^{\circ}\text{C}$  is applied
- On the right boundary uniform temperature  $300^{\circ}\text{C}$  is applied
- On the top boundary uniform temperature  $400^{\circ}\text{C}$  is applied
- On the bottom boundary uniform temperature  $200^{\circ}\text{C}$  is applied



### Governing Equation

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + q_g''' = \frac{1}{\alpha} \frac{\partial T}{\partial t}$$

### Integrating Governing equation over the control volume

$$\int_t^{t+\Delta t} \int_s^n \int_w^e \frac{1}{\alpha} \frac{\partial T}{\partial t} dx dy dt = \int_t^{t+\Delta t} \int_s^n \int_w^e \frac{\partial^2 T}{\partial x^2} dx dy dt + \int_t^{t+\Delta t} \int_s^n \int_w^e \frac{\partial^2 T}{\partial y^2} dx dy dt$$

### Implicit scheme used for evaluation of the temperature.

$$(T_P^n - T_P^o) \cdot \frac{\Delta x \Delta y}{\alpha \Delta t} = \left( \left[ \frac{(T_E^n - T_P^n)}{\delta x e} + \frac{(T_P^n - T_W^n)}{\delta x w} \right] \Delta y + \left[ \frac{(T_N^n - T_P^n)}{\delta y n} + \frac{(T_P^n - T_S^n)}{\delta y s} \right] \Delta x + q_g''' \Delta x \Delta y \right)$$

### Final Discretized form

$$a_P^n T_P^n = a_E T_E^n + a_W T_W^n + a_N T_N^n + a_S T_S^n + a_P^o T_P^o + b$$

$$a_E = \frac{\Delta y}{\delta x e}; \quad a_W = \frac{\Delta y}{\delta x w}; \quad a_N = \frac{\Delta x}{\delta y n}; \quad a_S = \frac{\Delta x}{\delta y s};$$

$$a_P^o = \frac{\Delta x \Delta y}{\alpha \Delta t}; \quad b = \frac{q_g'''}{k} \Delta x \Delta y$$

$$a_P^n = \frac{\Delta x \Delta y}{\alpha \Delta t} + \frac{\Delta y}{\delta x e} + \frac{\Delta y}{\delta x w} + \frac{\Delta x}{\delta y n} + \frac{\Delta x}{\delta y s}$$

## Code of the problem

```
%=====
% Assignment 2 CHDHT ME 415
% Problem Number 2. 2D Transient Problem
% Program uses FVM to solve the problem of 2D conduction
% Heat generation is present
% Designed only for rectangular co-ordinate system
%
% AUTHOR:
% Sanit P. Bhatkar (173109003@iitb.ac.in)
% Roll No: 173109003
% Place: IIT BOMBAY.
%=====

%% Input of variables %%

clc
clearvars
fprintf('\n===== Unsteady Heat conduction in solid =====');
fprintf('\n\n----- INPUT ----- \n');

% l=1;
% h=1;
% k=16.2;
% rho=7750;
% Cp=500;
% dt=10;
% sx=12;
% sy=12;
% eps=10^-4;
% qg=5e4;

%-----Input from user-----

fprintf('\nMaterial and domain properties -->\n');
l=input('\nLength of domain (m): ');
h=input('Height of domain (m): ');
k=input('Conductivity of Material W/m-k: ');
rho=input('Density of material kg/m3: ');
Cp=input('Specific heat of material J/kg-k: ');
dt=input('\nTime step: ');
sx=input('Number of points along length: ');
sy=input('Number of points along height: ');
eps=input('\nInput Convergence error: ');
qg=input('\nHeat generation rate W/m3: ');
alp=k/(rho*Cp);

%% Boundary Conditions %%

%tbn = temp on north boundary
%tbs = temp on south boundary
%tbe = temp on east boundary
%tbw = temp on west boundary

% tbn=400+273;
% tbs=200+273;
% tbe=300+273;
% tbw=100+273;

fprintf('\nBoundary Conditions -->\n');
tbn=input('\nBoundary condition at north boundary in degree C: ');
```

```

tbs=input('Boundary condition at south boundary in degree C: ');
tbe=input('Boundary condition at east boundary in degree C: ');
tbw=input('Boundary condition at west boundary in degree C: ');

tbn=tbn+273;
tbs=tbs+273;
tbe=tbe+273;
tbw=tbw+273;

%% Grid Formation %%

%=====FINITE VOLUME METHOD=====

%STEP 1: Divide domain into finite sized subdomain called control volumes

%Our domain is uniform
%But boundary and the first point grid space is different
%That is why separate calculation is done
%sx represents the number of points in a grid in x direction
%NOTE: dl has to be some multiple of length

dl=1/(sx-2);
x(1,1)=0;
x(sx,1)=1;
x(2,1)=x(1,1)+(dl/2);
for m=3:sx-1
    x(m,1)=x(m-1,1)+dl;
end

%sy represents the number of points in a grid in y direction

dh=h/(sy-2);
y(1,1)=0;
y(sy,1)=h;
y(2,1)=y(1,1)+(dh/2);

for m=3:sy-1
    y(m,1)=y(m-1,1)+dh;
end

%STEP 2: Integrate governing equation over boundaries of control volume

%STEP 3: Profile assumption

%Piecewise linear profile is assumed for integral
%We will get equation of type
%ApTp=AeTe+AwTw+AnTn+AsTs+B
%Assuming isotropic material and uniform control volume with no heat generation
%We get 4*Tp=Te+Tw+Tn+Ts

%% Method of ADI%%

%Formulating solution of type [A][Tp]=[B]

%Defining matrix for temperature
%T represents matrix for visualization of grids.

T=zeros(sy,sx);
T(1:sy,1:sx)=30+273;

```

```

% T(1:sy,1:sx)= input('\nInitial guess of temperature for the domain: ');
T_ini=T(1,1);

%Application of boundary conditions
T(1,1:sx)=tbn;
T(sy,1:sx)=tbs;
T(1:sy,sx)=tbe;
T(1:sy,1)=tbw;

%At corners discotinuity is present
%To take care of that, average has been taken at the corner
T(1,1)=(tbn+tbw)/2;
T(sy,1)=(tbs+tbw)/2;
T(1,sx)=(tbn+tbe)/2;
T(sy,sx)=(tbe+tbs)/2;

sw_error=1;

xsweep=T;

while sw_error>eps

%% Sweeping along x-direction %%

u(1,1)=tbn;
u(sy,1)=tbs;

for j=2:sx-1

%Defining problem for TDMA
%Forward Elimination

for i=2:sy-1

%dxe is distance from point P to east point
%dxw is distance from point P to west point
%dyn is distance from point P to north point
%dys is distance from point P to south point

dxe=x(j+1,1)-x(j,1);
dxw=x(j,1)-x(j-1,1);
dyn=y(i,1)-y(i-1,1);
dys=y(i+1,1)-y(i,1);

%apTp=aeTe+awTw+anTn+asTs

ae=k*dh/dxe;
aw=k*dh/dxw;
an=k*dl/dyn;
as=k*dl/dys;
apo=rho*Cp*dl*dh/(dt/2);
ap=ae+aw+an+as+apo;
S=(qg)*(dl*dh);

%a represents digonal element
%b and c are upper and lower digonals respectively

```

```

a=ap;

if i==2

    b=as;
    c=0;
    d=ae*T(i,j+1)+aw*T(i,j-1)+S+an*tbn+apo*T(i,j);
    %Forward Elimination
    P(1,1)=b/a;
    Q(1,1)=d/a;

elseif i==sy-1

    b=0;
    c=an;
    d=ae*T(i,j+1)+aw*T(i,j-1)+S+as*tbs+apo*T(i,j);
    %Forward Elimination
    P(i-1,1)=b/(a-c*P(i-2,1));
    Q(i-1,1)=(d+c*Q(i-2,1))/(a-c*P(i-2,1));

else

    b=as;
    c=an;
    d=ae*T(i,j+1)+aw*T(i,j-1)+S+apo*T(i,j);
    %Forward Elimination
    P(i-1,1)=b/(a-c*P(i-2,1));
    Q(i-1,1)=(d+c*Q(i-2,1))/(a-c*P(i-2,1));

end

end

%Back Substitution
u(sy-1,1)=Q(sy-2,1);
for v=sy-2:-1:2
    u(v,1)=P(v-1,1)*u(v+1,1)+Q(v-1,1);
end

xsweep(1:sy,j)=u';

end

ysweep=xsweep;

%% Sweeping along y-direction
u(1,1)=tbw;
u(sx,1)=tbe;

for i=2:sy-1

```

```

%Defining problem for TDMA
%Forward Elimination

for j=2:sx-1

%dxe is distance from point P to east point
%dxw is distance from point P to west point
%dyn is distance from point P to north point
%dys is distance from point P to south point

dxe=x(j+1,1)-x(j,1);
dxw=x(j,1)-x(j-1,1);
dyn=y(i,1)-y(i-1,1);
dys=y(i+1,1)-y(i,1);

%apTp=aeTe+awTw+anTn+asTs

ae=k*dh/dxe;
aw=k*dh/dxw;
an=k*dl/dyn;
as=k*dl/dys;
apo=rho*Cp*dl*dh/(dt/2);
ap=ae+aw+an+as+apo;
S=(qg)*(dl*dh);

%a represents digonal element
%b and c are upper and lower digonals respectively

a=ap;

if j==2

    b=ae;
    c=0;
    d=an*T(i-1,j)+as*T(i+1,j)+S+aw*tbw+apo*T(i,j);
    %Forward Elimination
    P(1,1)=b/a;
    Q(1,1)=d/a;

elseif j==sy-1

    b=0;
    c=aw;
    d=an*T(i-1,j)+as*T(i+1,j)+S+ae*tbe+apo*T(i,j);
    %Forward Elimination
    P(j-1,1)=b/(a-c*P(j-2,1));
    Q(j-1,1)=(d+c*Q(j-2,1))/(a-c*P(j-2,1));

else

    b=ae;
    c=aw;
    d=an*T(i-1,j)+as*T(i+1,j)+S+apo*T(i,j);
    %Forward Elimination
    P(j-1,1)=b/(a-c*P(j-2,1));
    Q(j-1,1)=(d+c*Q(j-2,1))/(a-c*P(j-2,1));

```

```

end

end

%Back Substitution
u(sx-1,1)=Q(sx-2,1);
for v=sy-2:-1:2
    u(v,1)=P(v-1,1)*u(v+1,1)+Q(v-1,1);
end

ysweep(i,1:sx)=u';

end

sw_error=abs(ysweep-T);
sw_error=max(max(sw_error));
T=ysweep;

end

%% Output %%

%For conversion from kelvin to degree C
T=T-273;
figure(1)
r=ones(sy,sx);
map = [0,1,1];
colormap(map)
pcolor(x,y,r)
title('Grid Layout');
xlabel('Length (m)');
ylabel('Height (m)');
%Plot of the temperature contours as the output.

figure(2)
colormap jet
contourf(x,y,flipud(T),10,'showtext','on')
colorbar
title('Graph of equilibrium temperature in degree C of the domain')

%

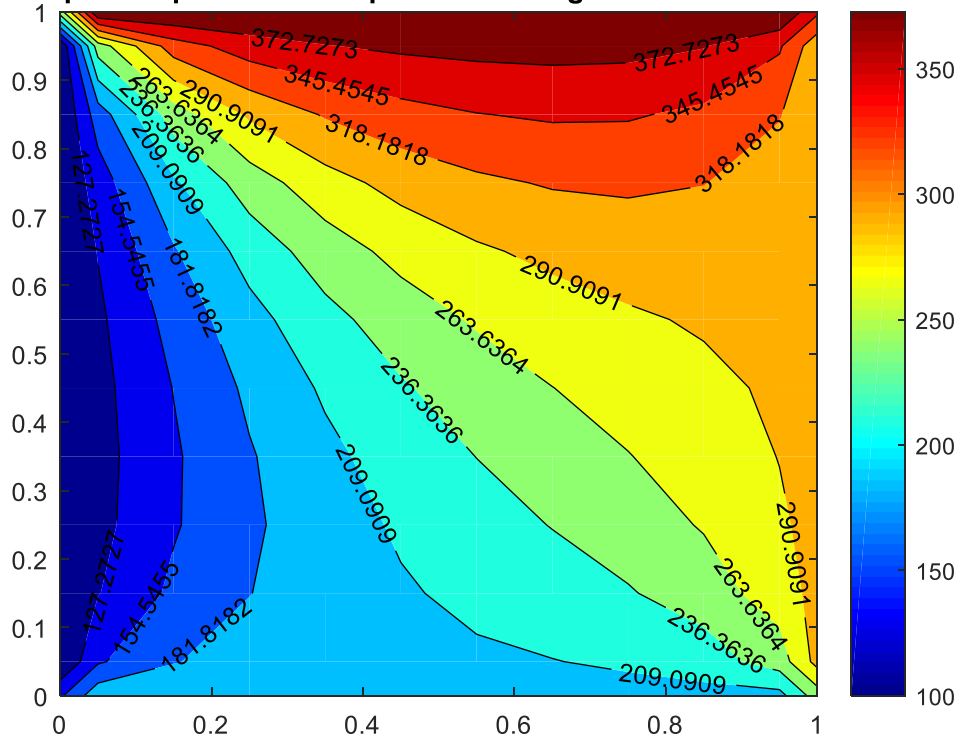
```

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## Results and Discussion

### A. Steady state temperature profile without heat generation

Graph of equilibrium temperature in degree C of the domain



===== Unsteady Heat conduction in solid =====

----- INPUT -----

Material and domain properties -->

Length of domain (m): 1

Height of domain (m): 1

Conductivity of Material W/m-k: 16.2

Density of material kg/m<sup>3</sup>: 7750

Specific heat of material J/kg-k: 500

Time step: 1000

Number of points along length: 12

Number of points along height: 12

Input Convergence error: 1e-4

Heat generation rate W/m<sup>3</sup>: 0

Boundary Conditions -->

Boundary condition at north boundary in degree C: 400

Boundary condition at south boundary in degree C: 200

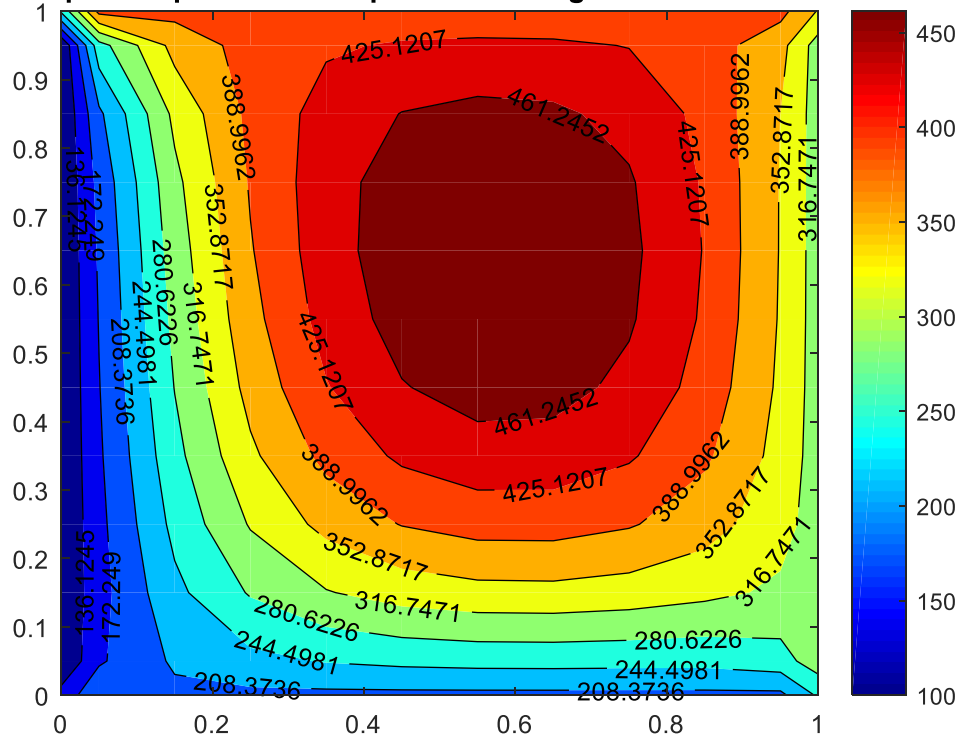
Boundary condition at east boundary in degree C: 300

Boundary condition at west boundary in degree C: 100



## B. Steady state temperature profile without heat generation

Graph of equilibrium temperature in degree C of the domain



===== Unsteady Heat conduction in solid =====

----- INPUT -----

Material and domain properties -->

Length of domain (m): 1

Height of domain (m): 1

Conductivity of Material W/m-k: 16.2

Density of material kg/m<sup>3</sup>: 7750

Specific heat of material J/kg-k: 500

Time step: 1000

Number of points along length: 12

Number of points along height: 12

Input Convergence error: 1e-4

Heat generation rate W/m<sup>3</sup>: 5e4

Boundary Conditions -->

Boundary condition at north boundary in degree C: 400

Boundary condition at south boundary in degree C: 200

Boundary condition at east boundary in degree C: 300

Boundary condition at west boundary in degree C: 100