

### Instructions

- Make a document (either in .doc and .pdf) containing code, results. Named the file using both of your Roll nos. *i.e.* 140100001\_140100002
- Write Up: (i) Software in which code is written, (ii) output results for each case, and (iii) explanation of results.
- Please upload all assignments to turnitin

### Assignment 3

**Due date: 08/09/2017, time: 12 midnight**

#### Solver

- A. Write programs for (i) Tri-diagonal Matrix Algorithm (TDMA) and (ii) Gauss-Seidel iteration.
  - B. The programs should first read in the size of the matrix  $N \times N$  and then read the values of the  $N \times N$  matrix elements & the  $N$  elements of vector  $b$ .
  - C. For any problem, the program should identify if the matrix is Tri-diagonal matrix or not.
1. Solve the following equation using TDMA:

$$\begin{aligned}2.04x_1 - x_2 &= 40.8 \\ -x_1 + 2.04x_2 - x_3 &= 0.8 \\ -x_2 + 2.04x_3 - x_4 &= 0.8 \\ -x_3 + 2.04x_4 &= 200.8\end{aligned}$$

2. Solve the following equation using Gauss-Seidel:

$$\begin{aligned}27x_1 + 6x_2 - x_3 &= 85 \\ 6x_1 + 15x_2 + 2x_3 &= 72 \\ x_1 + x_2 + 54x_3 &= 110\end{aligned}$$

- a. Start with an initial guess of  $x_1=0, x_2=0$  and  $x_3=0$ . Solve Iteratively within error norm range  $10^{-4}$  to  $10^{-12}$ . Show how the number of iterations to obtain solution change with error norm.

3. Solve the following equation using Gauss-Seidel:

$$\begin{aligned}3.122x_1 + 0.5756x_2 - 0.1565x_3 - 0.0067x_4 &= 1.571 \\ 0.5756x_1 + 2.93x_2 + 0.1103x_3 - 0.0015x_4 &= -0.9275 \\ -0.1565x_1 + 0.1103x_2 + 4.127x_3 + 0.2051x_4 &= -0.0652 \\ -0.0067x_1 - 0.0015x_2 + 0.2051x_3 + 4.133x_4 &= -0.0178\end{aligned}$$

Start with an initial guess of  $x_1=x_2=x_3=x_4=0$

For Gauss Seidel Iterative problems: Iterate till error norm is less than  $10^{-5}$  and maximum iteration 100. Tabulate successive errors and values of  $x_1, x_2, x_3$  and  $x_4$ . Calculate Norm of the M

matrix (as defined in class -you can do this by hand calculation or use the matrix inversion program you wrote last time)