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BATCH	A
EXP NO:	6th

AIM:	(Graph Algorithm - Single source shortest path algorithm. Dijkstra Algorithms
THEORY:	<p>The Single-Source Shortest Path (SSSP) problem consists of finding the shortest paths between a given</p> <ol style="list-style-type: none"> <li>1. vertex <math>v</math> and all other vertices in the graph</li> <li>2. Bellman Ford algorithm works by overestimating the length of the path from the starting vertex to all other vertices.</li> <li>3. Then it iteratively relaxes those estimates by finding new paths that are shorter than the previously overestimated paths.</li> <li>4. Dijkstra algorithm is a single-source shortest path algorithm. Here, single-source means that only one source is given, and we have to find the shortest path from the source to all the nodes.</li> </ol> <p><b>5. ALGORITHM :</b></p> <p><b>1. Bellman–Ford :</b></p> <ol style="list-style-type: none"> <li>1. function bellmanFordAlgorithm(<math>G, s</math>) // <math>G</math> is the graph and <math>s</math> is the source vertex</li> <li>2. for each vertex <math>V</math> in <math>G</math></li> <li>3. <math>dist[V] \leftarrow \infty</math> // <math>dist</math> is distance</li> <li>4. <math>prev[V] \leftarrow \text{NULL}</math> // <math>prev</math> is previous</li> <li>5. <math>dist[s] \leftarrow 0</math></li> <li>6. for each vertex <math>V</math> in <math>G</math></li> <li>7. for each edge <math>(u,v)</math> in <math>G</math></li> <li>8. <math>temporaryDist \leftarrow dist[u] + edgeweight(u, v)</math></li> <li>9. if <math>temporaryDist &lt; dist[v]</math></li> <li>10. <math>dist[v] \leftarrow temporaryDist</math></li> <li>11. <math>prev[v] \leftarrow u</math></li> <li>12. for each edge <math>(U,V)</math> in <math>G</math></li> <li>13. If <math>dist[U] + edgeweight(U, V) &lt; dist[V]</math></li> <li>14. Error: Negative Cycle Exists</li> <li>15. return <math>dist[], prev[]</math></li> </ol>

## 2. Dijkstra Algorithms :

1. Mark the source node with a current distance of 0 and the rest with infinity.
2. Set the non-visited node with the smallest current distance as the current node.
3. For each neighbor, N of the current node adds the current distance of the adjacent node with the weight of the edge connecting 0->1. If it is smaller than the current distance of Node, set it as the new current distance of N.
4. Mark the current node 1 as visited.
5. Go to step 2 if there are any nodes are unvisited.

## 7. Time Complexity :

### 1. Bellman-Ford

1.  $O(V * E)$
2. Dijkstra Algorithms
1.  $O((V+E)\log V)$

PROGRAM:

```
#include<stdio.h>
#include<stdlib.h>
#include<limits.h>
#include<stdbool.h>

int minDistance(int dist[], bool minSet[], int V)
{
    int min = INT_MAX, min_index;

    for (int v = 0; v < V; v++)
        if (minSet[v] == false && dist[v] <= min)
            min = dist[v], min_index = v;

    return min_index;
}

void printSolution(int dist[], int V)
{
    printf("Vertex\t\tDistance from Source \n");
    for (int i = 0; i < V; i++)
        printf("%d \t\t\t %d\n", i, dist[i]);
}

void dijkstra( int v, int graph[v][v], int source){
```

```

int dist[v];
bool minSet[v];
for(int i=0;i<v;i++){
    dist[i]=INT_MAX;
    minSet[i]=false;
}
dist[source]=0;
for(int count=0;count<v-1;count++){
    int u = minDistance(dist,minSet,v);
    minSet[u]=true;
    for(int i=0;i<v;i++){
        if(!minSet[i] && graph[u][i] && dist[u]!=INT_MAX &&
dist[u]+graph[u][i]<dist[i]){
            dist[i]=dist[u]+graph[u][i];
        }
    }
}
printSolution(dist,v);
}

int main(){
    int v;
    printf("Enter the number of vertices: ");
    scanf("%d",&v);
    int graph[v][v];
    printf("Enter the adjacency matrix: ");
    for(int i=0;i<v;i++){
        for(int j=0;j<v;j++){
            scanf("%d",&graph[i][j]);
        }
    }
    dijkstra(v,graph,0);
    return 0;
}

```

RESULT:

```
e:\c tutorial\output>.\"dijkstra.exe"
Enter the number of vertices: 6
Enter the adjacency matrix:
0 2 5 0 0 0
0 0 1 6 0 0
0 0 0 0 2 0
0 0 0 0 0 1
0 0 0 2 0 4
0 0 0 0 0 0
Vertex          Distance from Source
0
1                2
2                3
3                7
4                5
5                8
```

CONCLUSION:

From this experiment, i have successfully understood how to perform - Single source shortest path algorithm.