91)
$$T(n) = 3T (n/2) + n^2$$

 $T(n) = aT(n/6) + f(n^2)$
 $a > 1, b > 1$
On compaining
 $a = 3, b = 2, f(n) = n^2$
Now, $C = log = log = 1.584$
 $n^2 = n^{1.584} \le n^2$
 $f(n) > n^2$
 $T(n) = o(n^2)$

92)
$$T(n) = 4T(n/2) + n^2$$

 $\rightarrow a/1, b/1$
 $a = 4, b = 2, f(n) = n^2$
 $c = \log_2 4 = 2$
 $n^2 = n^2 = f(n) = n^2$
 $\therefore T(n) = o(n^2 \log_2 n)$

93)
$$T(n)_{2}T(n/2)+2^{n}$$
 $A=1$
 $b=2$
 $f(n)_{2}2^{n}$
 $c=\log a=\log c=0$
 $h^{c}=h^{o}=1$
 $f(n)>h^{c}$
 $T(n)_{2}\theta(2^{n})$

95)
$$T(n) = 16T(n/4) + n$$
 $\Rightarrow a = 16, b = 4$
 $f(n) = n$
 $c = \log 16 = \log (4)^2 = 2\log 4$
 $= 2^4 = \log n^2$
 $f(n) < f(n) = n$
 $f(n) < f(n) = n$
 $f(n) < f(n) = n$

90)
$$T(n)=2T(n/2)+n\log n$$

 $\rightarrow a=2, b=2$
 $f(n)=n\log n$
 $c=\log 2=1$
 $n^c=n^2=n$
 $n \log n > n$
 $f(n) > n^c$
 $T(n) = 0 (n \log n)$

X

g7) T(n) = 2T(n/2) + n/lagn → a=2, b=2, f(n)= n/logn C= lag 2 = 1 nc=n1=n · n < n · . f(n) < nc · . T(n) = 0 (n) 98) T(n)=2T(n/4)+n0.51 -> a = 2, b = 4, f(n) = n0.51 $C = \log_{10} a = \log_{10} 2 = 0.5$ $n^{c} = n^{0.5}$ $n^{o} \le n^{o.5}$ \$(n)>nc .. T(n): 0 (nº.51) gg) T(n) 2 0.5 T(n/2) + 1/n \rightarrow a=0.5, b=2a 1/1 but here a is 0.5

so me cannet apply Master's Theorem.

910) T(n)= 16T(n/4)+n! -> a=16, b=4, f(n)=n! · · · C = lag a z lag 16 2 2 $n^{c} = n^{2}$ As n/ >n²

 $T(n) = \theta(n!)$

911) 4T(n/2) + lag n -, a=4, b=e, f(n)=lagn C = lega - leg 4 = 2 ne = n2 (n). legn : lagn < n2 4(n)(n° T(n): 0 (nc) = 0 (n2) Q12) T(n) 2 squt(n) T(n/2) + logn _, a= In, b=2 C= lego = legon = 1 legon · · · z leg n < leg (n) · + (n)>nc T(n) = 0 (f(n)) = 0 (leg (n)) (13) T(n)=3T(n/2)+n \rightarrow a=3; b=2; f(n)=nC = lag a = lag 3 = 1.5849 nc = n 1.5489 n < n1.5849 \Rightarrow $f(n) < n^c$ T(n)=0(n1.5849) Q14) T(n) = 3T(n/3) + sgrt (n) $\rightarrow a=3, b=3$ C = leg a = leg 3 = 1 $n^{c} = n^{1} = n$ As sgut (n) < n f(n)<nc T(n) 20(n)

$$g(5)$$
 $T(n) = 4T(n/2) + n$
 $\rightarrow 0 = 4, b = 2$
 $C = laga = lag_2 = 2$
 $h^{c} = n^{2}$
 $n < n^{2}$ (for any constant)
 $f(n) < n^{c}$
 $f(n) = 0 (n^{2})$

$$g_{16}$$
) $T(n) = 3T(n/4) + n \log n$
 $\rightarrow a = 3, b = 4, f(n) = n \log n$
 $C = \log_{6} a = \log_{4} 3 = 0.792$
 $n^{c} = n^{0.792}$
 $n^{0.792} < n \log n$
 $T(n) = 0 (n \log n)$

$$g_{17}) T(n) = 3T(n/3) + n/2$$

$$\rightarrow a = 3; b = 3$$

$$c = \log_{3} a = \log_{3} 3 = 1$$

$$f(n) = n/2$$

$$\therefore n^{c} = n' = n$$

$$A = n/2 < n$$

$$f(n) < n^{c}$$

$$f(n) = O(n)$$

$$f(n) = GT(n/3) + n^{2} \log n$$

$$A = G; b = 3$$

$$C = \log_{b} a = \log_{3} G = 1.6309$$

$$n^{c} = n^{1.6309}$$

As $n^{1.6309} < n^{2} \log n$
 $\therefore T(n)_{20} (n^{2} \log n)$

$$g(9) T(n) = 4T(n/p) \frac{1}{n+1} + n/\log n$$

$$\Rightarrow a = 4, b = 2, f(n) = \frac{n}{\log n}$$

$$c = \log a = \log_2 4 = 2$$

$$e = n^2$$

$$e = n^2$$

$$\log n = n^2$$

$$\log n$$

$$T(n) = o(n^2)$$

 $\begin{array}{l}
g20) T(n) = 64T(n/8) - n^{2} \log n \\
\rightarrow \alpha = 64 \ b = 8 \\
C = \log_{10} \alpha = \log_{10} 64 = \log_{10} (8)^{2} \\
C = 2 \\
N^{c} = n^{2} \\
\therefore n^{2} \log_{10} n > n^{2} \\
T(n) = O(n^{2} \log_{10})
\end{array}$

$$\begin{array}{c} g_{21}) \ T(n) = 7T (n/3) + n^2 \\ \rightarrow a = 7; b = 3; f(n) = n^2 \\ C = log_b a = log_3 7 = 1.7712 \\ n^c = n^{1.7712} \\ n^{1.7712} < n^2 \\ T(n) = 0 (n^2) \end{array}$$