School of Computing
Second CIA Exam – May 2023

Course Code: CSE209 **Course Name:** Data Structures & Algorithms
Duration: 90 minutes Max Marks: 50

PART A

Answer all the questions **(10 x 2 = 20)**

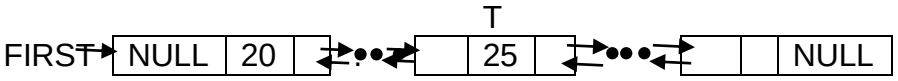
1. Write an algorithm to insert an element into beginning of a singly linked list.

$Algorithm\ INSERT\_AT\_BEG(first, x)$
1. $T = GETNODE()$
2. $T \rightarrow data = x$
3. $T \rightarrow link = first$
4. $first = T$
5. $return$

2. Write the algorithm to attach a new ploynomial term at the end of the polynomial which is stored as a singly linked list.

$Algorithm\ INSERT\_AT\_END(first, last, c, e)$
1. $T = GETNODE()$
2. $T \rightarrow data = x$
3. $T \rightarrow link = NULL$
4. $if\ first = NULL$
5. $\quad first = last = T$
6. $else$
7. $\quad last \rightarrow link = T$
8. $\quad last = T$
9. $endif$
10. $return$

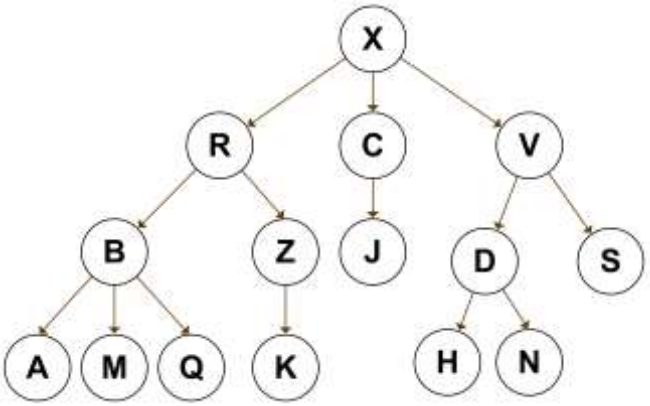
3. Let T be the address of the node to be deleted from a non-empty doubly linked list as shown below. Write the pseudocode to delete the node T.



$Algorithm\ DELETE\_DLLNODE(first, last, T)$
1. $if\ T \rightarrow next\ \neq NULL$
2. $\quad T \rightarrow next \rightarrow prev = T \rightarrow prev$
3. $else$
4. $\quad last = T \rightarrow prev$
5. $\quad last \rightarrow next = NULL$
6. $end\ if$
7. $if\ T \rightarrow prev\ \neq NULL$
8. $\quad T \rightarrow prev \rightarrow next = T \rightarrow next$
9. $else$
10. $\quad first = T \rightarrow next$
11. $\quad first \rightarrow prev = NULL$
12. $end\ if$

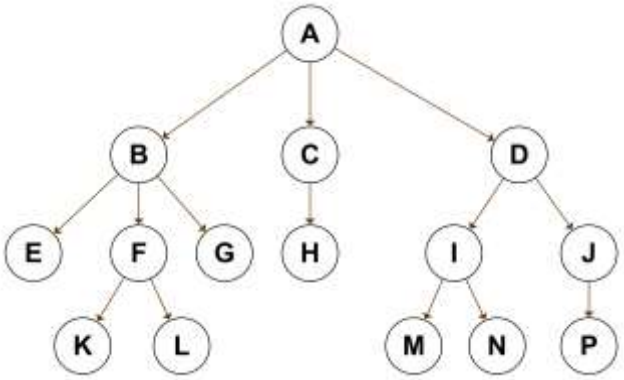
13. $RETNODE(T)$
14. $return$

4. Identify the siblings of **Q** in the following general tree.



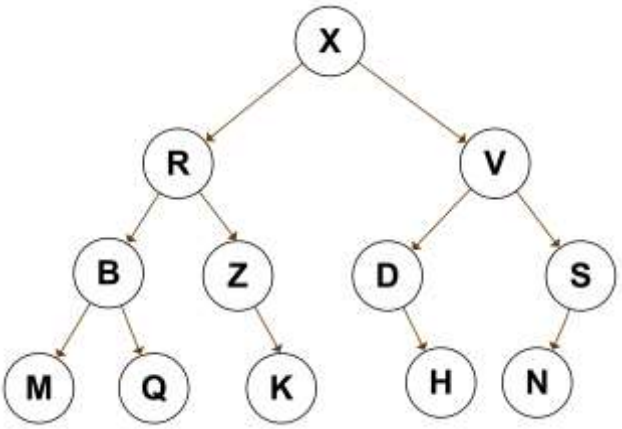
$A\ and\ M\ are\ siblings\ of\ B$

5. Write the parenthetical representation for the following general tree:



$(A\ (B(E\ F(K\ L)\ G)C(H)D(I(M\ N)J(P))))$

6. Represent the following binary tree as a sequential array.



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
X	R	V	B	Z	D	S	M	Q	-	K	-	H	N	-

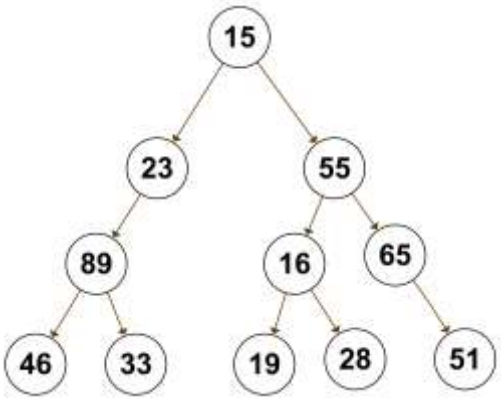
7. Define height of a binary tree.

   $Height\ of\ a\ binary\ tree\ is\ defined\ as\ the\ number\ of\ edges\ required\ to\ reach\ the\ farthest\ leaf\ from\ the\ root.$

8. What is the maximum number of nodes in a binary tree of height h?

   $Max.No.of\ nodes\ in\ a\ binary\ tree\ of\ height\ h = 2^{h+1} - 1$

9. Find the inorder traversal of the following binary tree



   $Inorder\ traversal$: 46, 89, 33, 23, 15, 19, 16, 28, 55, 65, 51

10. Write the algorithm to find the maximum element in a binary search tree.

```
Algorithm MAXIMUM_BST(root)
1. T = root
2. while T → rchild ≠ NULL
3.       T = T → rchild
4. end while
5. return T → data
```

PART B

Answer any THREE questions **(3 x 10 = 30)**

11. Write the algorithm for adding two polynomials represented using singly linked list that store non-zero terms.

```
Algorithm ADD_POLY(P, Q)
1.  R.First = R.Last = NULL
2.  t1 = P.First
3.  t2 = Q.First
4.  while t1 != NULL and t2 != NULL
5.     if t1→exp > t2→exp
6.        R = INSERT_AT_LAST(R, t1→coef, t1→exp)
7.        t1 = t1→link
8.     else if t1→exp < t2→exp
9.        R = INSERT_AT_LAST(R, t2→coef, t2→exp)
10.       t2 = t2→link
11.    else
12.       coef = t1→coef + t2→coef
```

13. $exp = t1 \rightarrow exp$
14. $if\ coef\ != 0$
15. $R = INSERT\_AT\_LAST(R, coef, t2 \rightarrow exp)$
16. $end\ if$
17. $t1 = t1 \rightarrow link$
18. $t2 = t2 \rightarrow link$
19. $end\ if$
20. $end\ while$
21. $while\ t1\ != NULL$
22. $R = INSERT\_AT\_LAST(R, t1 \rightarrow coef, t1 \rightarrow exp)$
23. $t1 = t1 \rightarrow link$
24. $end\ while$
25. $while\ t2\ != NULL$
26. $R = INSERT\_AT\_LAST(R, t2 \rightarrow coef, t2 \rightarrow exp)$
27. $t2 = t2 \rightarrow link$
28. $end\ while$
29. $Return\ R$

Algorithm INSERT_AT_LAST $(P, coef, exp)$

1. $n = Allocate\_Node()$
2. $n \rightarrow coef = coef$
3. $n \rightarrow exp = exp$
4. $n \rightarrow link = NULL$
5. $if\ P.First = NULL$
6. $n \rightarrow link = P.First$
7. $P.First = P.Last = n$
8. $else$
9. $P.Last \rightarrow link = n$
10. $P.Last = n$
11. $end\ if$
12. $Return\ P$

12. Write the algorithms to perform insertion, deletion, and search operations in an ordered singly linked list with first pointer.

Algorithm INSERT_OSLL $(FIRST, x)$

1. $T = GETNODE()$
2. $T \rightarrow data = x$
3. $T \rightarrow link = NULL$
4. $if\ FIRST = NULL\ or\ FIRST \rightarrow data \geq x$
5. $T \rightarrow link = FIRST$
6. $FIRST = T$
7. $else$
8. $temp = FIRST$
9. $while\ temp \rightarrow link\ != NULL\ \&\&\ temp \rightarrow link \rightarrow data < x$
10. $temp = temp \rightarrow link$
11. $end\ while$
12. $T \rightarrow link = temp \rightarrow link$
13. $temp \rightarrow link = T$

14. $endif$
15. $return$

Algorithm DELETE_OSLL($FIRST, x$)

1. $if\ FIRST = NULL\ or\ FIRST \rightarrow data > x$
2. $\quad print\ "Element\ not\ present\ in\ the\ list"$
3. $\quad return$
4. $end\ if$
5. $if\ FIRST \rightarrow data = x$
6. $\quad T = FIRST$
7. $\quad FIRST = FIRST \rightarrow link$
8. $else$
9. $\quad prev = FIRST$
10. $\quad cur = FIRST \rightarrow link$
11. $\quad while\ cur\ != NULL\ and\ cur \rightarrow data < x$
12. $\quad\quad prev = cur$
13. $\quad\quad cur = cur \rightarrow link$
14. $\quad end\ while$
15. $\quad if\ cur \rightarrow data = x$
16. $\quad\quad T = cur$
17. $\quad\quad prev \rightarrow link = cur \rightarrow link$
18. $\quad else$
19. $\quad\quad print\ "Element\ not\ present\ in\ the\ list"$
20. $\quad\quad return$
21. $\quad end\ if$
22. $endif$
23. $RETNODE(T)$
24. $return$

Algorithm SEARCH_OSLL($FIRST, x$)

1. $if\ FIRST = NULL\ or\ FIRST \rightarrow data > x$
2. $\quad return - 1$
3. $end\ if$
4. $p = 1$
5. $T = FIRST$
6. $while\ T \neq NULL\ and\ T \rightarrow data < x$
7. $\quad p = p + 1$
8. $\quad T = T \rightarrow link$
9. $end\ while$
10. $if\ T = NULL\ or\ T \rightarrow data > x$
11. $\quad return - 1$
12. $else$
13. $\quad return\ p$
14. $end\ if$

13. Write the algorithms to perform insertion at beginning, insertion at end, insertion at specific location into a circular doubly linked list.

Algorithm INSERT_AT_BEG_CDLL($FIRST, LAST, x$)

1. $T = GETNODE()$

2. $T \rightarrow data = x$
3. $T \rightarrow prev = T \rightarrow next = NULL$
4. $if\ FIRST = NULL$
5. $\quad T \rightarrow prev = T \rightarrow next = T$
6. $\quad FIRST = LAST = T$
7. $else$
8. $\quad T \rightarrow prev = LAST$
9. $\quad T \rightarrow next = FIRST$
10. $\quad LAST \rightarrow next = T$
11. $\quad FIRST \rightarrow prev = T$
12. $\quad FIRST = T$
13. $return$

***Algorithm INSERT_AT_END_CDLL*($FIRST, LAST, x$)**

1. $T = GETNODE()$
2. $T \rightarrow data = x$
3. $T \rightarrow prev = T \rightarrow next = NULL$
4. $if\ FIRST = NULL$
5. $\quad T \rightarrow prev = T \rightarrow next = T$
6. $\quad FIRST = LAST = T$
7. $else$
8. $\quad T \rightarrow prev = LAST$
9. $\quad T \rightarrow next = FIRST$
10. $\quad LAST \rightarrow next = T$
11. $\quad FIRST \rightarrow prev = T$
12. $\quad LAST = T$
13. $return$

***Algorithm INSERT_AT_POS_CDLL*($FIRST, LAST, x, p$)**

1. $T = GETNODE()$
2. $T \rightarrow data = x$
3. $T \rightarrow prev = T \rightarrow next = NULL$
4. $if\ FIRST = NULL$
5. $\quad T \rightarrow prev = T \rightarrow next = T$
6. $\quad FIRST = LAST = T$
7. $\quad return$
8. $if\ p = 1$
9. $\quad T \rightarrow prev = LAST$
10. $\quad T \rightarrow next = FIRST$
11. $\quad LAST \rightarrow next = T$
12. $\quad FIRST \rightarrow prev = T$
13. $\quad FIRST = T$
14. $\quad return$
15. $count = 1$
16. $cur = FIRST$
17. $while\ cur \rightarrow next\ \neq FIRST\ and\ count < p - 1$
18. $\quad count = count + 1$
19. $\quad cur = cur \rightarrow next$
20. $T \rightarrow prev = cur$

21. $T \rightarrow next = cur \rightarrow next$
22. $cur \rightarrow next \rightarrow prev = T$
23. $cur \rightarrow next = T$
24. $if\ LAST = cur$
25. $\quad LAST = T$
26. $return$

14. Construct a binary search tree for the following input sequence:
    45, 11, 34, 87, 56, 72, 89, 51, 68, 35, 22, 19, 69, 9