

## 6(a) LALR Parser

**G:**      $S \rightarrow Aa$   
          $S \rightarrow bAc$   
          $S \rightarrow Bc$   
          $S \rightarrow bBa$   
          $A \rightarrow d$   
          $B \rightarrow a$

### Computation of LR(1) Items Set for G

#### (1) Augmented Grammar

**G':**      $S' \rightarrow S$   
          $S \rightarrow Aa$                      $(R_1)$   
          $S \rightarrow bAc$                     $(R_2)$   
          $S \rightarrow Bc$                      $(R_3)$   
          $S \rightarrow bBa$                     $(R_4)$   
          $A \rightarrow d$                        $(R_5)$   
          $B \rightarrow a$                        $(R_6)$

#### (2) CLOSURE ( $S' \rightarrow S$ )

$S' \rightarrow .S, \$$   
 $S \rightarrow .Aa, \$$   
 $S \rightarrow .bAc, \$$   
 $S \rightarrow .Bc, \$$   
 $S \rightarrow .bBa, \$$   
 $A \rightarrow .d, a \mid \$$   
 $B \rightarrow .a, c \mid \$ \dots\dots (I_0)$

#### (3) GOTO()

**GOTO ( $I_0, S$ ):**  $S' \rightarrow S., \$ \dots\dots (I_1)$

**GOTO ( $I_0, A$ ):**  $S \rightarrow A.a, \$ \dots\dots (I_2)$

**GOTO ( $I_0, B$ ):**  $S \rightarrow B.c, \$ \dots\dots (I_3)$

**GOTO ( $I_0, a$ ):**  $B \rightarrow a., c \mid \$ \dots\dots (I_4)$

**GOTO ( $I_0, b$ ):**  $S \rightarrow b.Ac, \$$   
                  $S \rightarrow b.Ba, \$$   
                  $A \rightarrow .d, c \mid \$$   
                  $B \rightarrow .a, a \mid \$ \dots\dots (I_5)$

**GOTO ( $I_0, d$ ):**  $A \rightarrow d., a \mid \$ \dots\dots (I_6)$

**GOTO ( $I_2, a$ ):**  $S \rightarrow Aa., \$ \dots\dots (I_7)$

**GOTO (I<sub>3</sub>, c):**  $S \rightarrow Bc., \$ \dots(I_8)$

**GOTO (I<sub>5</sub>, A):**  $S \rightarrow bA.c, \$ \dots(I_9)$

**GOTO (I<sub>5</sub>, B):**  $S \rightarrow bB.a, \$ \dots(I_{10})$

**GOTO (I<sub>5</sub>, a):**  $B \rightarrow a., a | \$ \dots(I_{11})$

**GOTO (I<sub>5</sub>, d):**  $A \rightarrow d., c | \$ \dots(I_{12})$

**GOTO (I<sub>9</sub>, c):**  $S \rightarrow bAc., \$ \dots(I_{13})$

**GOTO (I<sub>10</sub>, a):**  $S \rightarrow bBa., \$ \dots(I_{14})$

**(4) LR(1) Items set Grouping**

By Merging I<sub>4</sub> and I<sub>11</sub>:  $B \rightarrow a., a | c | \$ \dots(I_{411})$

By Merging I<sub>6</sub> and I<sub>12</sub>:  $A \rightarrow d., a | c | \$ \dots(I_{612})$

**(5) LALR Parsing Table**

State	ACTION					GOTO		
	a	b	c	d	\$	S	A	B
0	S <sub>411</sub>	S <sub>5</sub>		S <sub>612</sub>		1	2	3
1					ACC			
2	S <sub>7</sub>							
3			S <sub>8</sub>					
411	R <sub>5</sub>		R <sub>5</sub>		R <sub>5</sub>			
5	S <sub>411</sub>			S <sub>612</sub>		9	10	
612	R <sub>6</sub>		R <sub>6</sub>		R <sub>6</sub>			
7					R <sub>1</sub>			
8					R <sub>3</sub>			
9			S <sub>13</sub>					
10	S <sub>14</sub>							
13					R <sub>2</sub>			
14					R <sub>4</sub>			

## 6(b) CLR Parser

## 6(a) LALR Parser

G:      $S \rightarrow (L)$   
        $S \rightarrow id$   
        $L \rightarrow L * S$   
        $L \rightarrow S$

### Computation of LR(1) Items Set for G

#### (1) Augmented Grammar

G':      $S' \rightarrow S$   
          $S \rightarrow (L)$                  ( $R_1$ )  
          $S \rightarrow id$                    ( $R_2$ )  
          $L \rightarrow L * S$                ( $R_3$ )  
          $L \rightarrow S$                     ( $R_4$ )

#### (2) CLOSURE ( $S' \rightarrow S$ )

$S' \rightarrow .S, \$$   
 $S \rightarrow .(L), \$$   
 $S \rightarrow .id, \$ \dots (I_0)$

#### (3) GOTO()

**GOTO ( $I_0, S$ ):**  $S' \rightarrow S., \$ \dots (I_1)$

**GOTO ( $I_0, ()$ ):**  $S \rightarrow (.L), \$$   
                   $L \rightarrow .L * S, * | ) | \$$   
                   $L \rightarrow .S, * | ) | \$$   
                   $S \rightarrow .(L), * | ) | \$$   
                   $S \rightarrow .id, * | ) | \$ \dots (I_2)$

**GOTO ( $I_0, id$ ):**  $S \rightarrow id., \$ \dots (I_3)$

**GOTO ( $I_2, S$ ):**  $L \rightarrow S., * | ) | \$ \dots (I_4)$

**GOTO ( $I_2, L$ ):**  $S \rightarrow (L.), \$$   
                   $L \rightarrow L.*S, * | ) | \$ \dots (I_5)$

**GOTO ( $I_2, ()$ ):**  $S \rightarrow (.L), * | ) | \$$   
                   $L \rightarrow .L * S, * | ) | \$$   
                   $L \rightarrow .S, * | ) | \$$   
                   $S \rightarrow .(L), * | ) | \$$   
                   $S \rightarrow .id, * | ) | \$ \dots (I_6)$

**GOTO ( $I_2, id$ ):**  $S \rightarrow id., * | ) | \$ \dots (I_7)$

**GOTO (I<sub>5</sub>, )):**  $S \rightarrow (L), \$ \dots (I_8)$

**GOTO (I<sub>5</sub>, \*):**  $L \rightarrow L^*.S, * | ) | \$$   
 $S \rightarrow .(L), * | ) | \$$   
 $S \rightarrow .id, * | ) | \$ \dots (I_9)$

**GOTO (I<sub>6</sub>, S):**  $L \rightarrow S., * | ) | \$ \dots (I_4)$

**GOTO (I<sub>6</sub>, L):**  $S \rightarrow (L.), * | ) | \$$   
 $L \rightarrow L.*S, * | ) | \$ \dots (I_{10})$

**GOTO (I<sub>6</sub>, ():**  $S \rightarrow .(L), * | ) | \$$   
 $L \rightarrow .L * S, * | ) | \$$   
 $L \rightarrow .S, * | ) | \$$   
 $S \rightarrow .(L), * | ) | \$$   
 $S \rightarrow .id, * | ) | \$ \dots (I_6)$

**GOTO (I<sub>6</sub>, id):**  $S \rightarrow id., * | ) | \$ \dots (I_7)$

**GOTO (I<sub>9</sub>, S):**  $L \rightarrow L^*.S., * | ) | \$ \dots (I_{11})$

**GOTO (I<sub>9</sub>, ():**  $S \rightarrow .(L), * | ) | \$$   
 $L \rightarrow .L * S, * | ) | \$$   
 $L \rightarrow .S, * | ) | \$$   
 $S \rightarrow .(L), * | ) | \$$   
 $S \rightarrow .id, * | ) | \$ \dots (I_6)$

**GOTO (I<sub>9</sub>, id):**  $S \rightarrow id., * | ) | \$ \dots (I_7)$

**GOTO (I<sub>10</sub>, )):**  $S \rightarrow (L)., * | ) | \$ \dots (I_{12})$

**GOTO (I<sub>10</sub>, \*):**  $L \rightarrow L^*.S, * | ) | \$$   
 $S \rightarrow .(L), * | ) | \$$   
 $S \rightarrow .id, * | ) | \$ \dots (I_9)$

**(4) LALR Parsing Table**

State	ACTION					GOTO	
	id	(	)	*	\$	S	L
0	S <sub>3</sub>	S <sub>2</sub>				1	
1					ACC		
2	S <sub>7</sub>	S <sub>6</sub>				4	5
3					R <sub>2</sub>		
4			R <sub>4</sub>	R <sub>4</sub>	R <sub>4</sub>		
5			S <sub>8</sub>	S <sub>9</sub>			
6	S <sub>7</sub>	S <sub>6</sub>				4	10
7			R <sub>2</sub>	R <sub>2</sub>	R <sub>2</sub>		
8					R <sub>1</sub>		
9	S <sub>7</sub>	S <sub>6</sub>				11	
10			S <sub>12</sub>	S <sub>9</sub>			
11			R <sub>3</sub>	R <sub>3</sub>	R <sub>3</sub>		
12			R <sub>1</sub>	R <sub>1</sub>	R <sub>1</sub>		

**(5). LALR Parsing:** Input string (id\*id\*id)

Highlighted contents on Stack - Handle

Stack	Input buffer	Action Taken
0	(id*id*id)\$	ACTION [0,(] = S <sub>2</sub> – Shift
0(2	id*id*id)\$	ACTION [2, id] = S <sub>7</sub> – Shift
0(2id 7	*id*id)\$	ACTION [7, *] = R <sub>2</sub> & GOTO(2, S) = 4
0(2S4	*id*id)\$	ACTION [4, *] = R <sub>4</sub> & GOTO(2, L) = 5
0(2L5	*id*id)\$	ACTION [5, *] = S <sub>9</sub> – Shift
0(2L5*9	id*id)\$	ACTION [9, id] = S <sub>7</sub> – Shift
0(2L5*9id 7	*id)\$	ACTION [7, *] = R <sub>2</sub> & GOTO(9, S) = 11
0(2L5*9S11	*id)\$	ACTION [11, *] = R <sub>3</sub> & GOTO(2, L) = 5
0(2L5	*id)\$	ACTION [5, *] = S <sub>9</sub> – Shift
0(2L5*9	id)\$	ACTION [9, id] = S <sub>7</sub> – Shift
0(2L5*9id 7	)\$	ACTION [7, ]) = R <sub>2</sub> & GOTO(9, S) = 11
0(2L5*9S11	)\$	ACTION [11, ]) = R <sub>3</sub> & GOTO(2, L) = 5
0(2L5	)\$	ACTION [5, ]) = S <sub>8</sub> Shift
0(2L5)8	\$	ACTION [8, \$] = R <sub>1</sub> & GOTO(0,S) = 1
0S1	\$	ACTION [1, \$] = Accept.