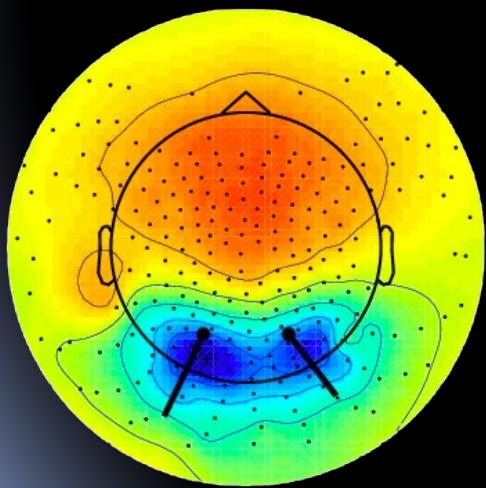
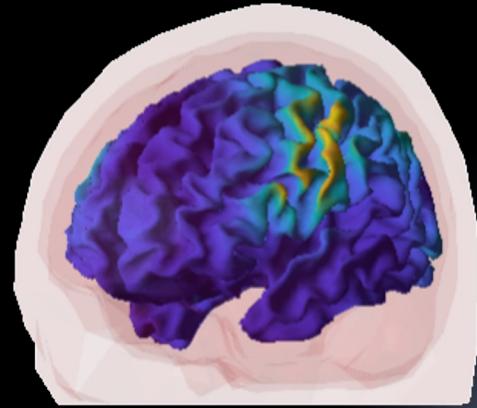
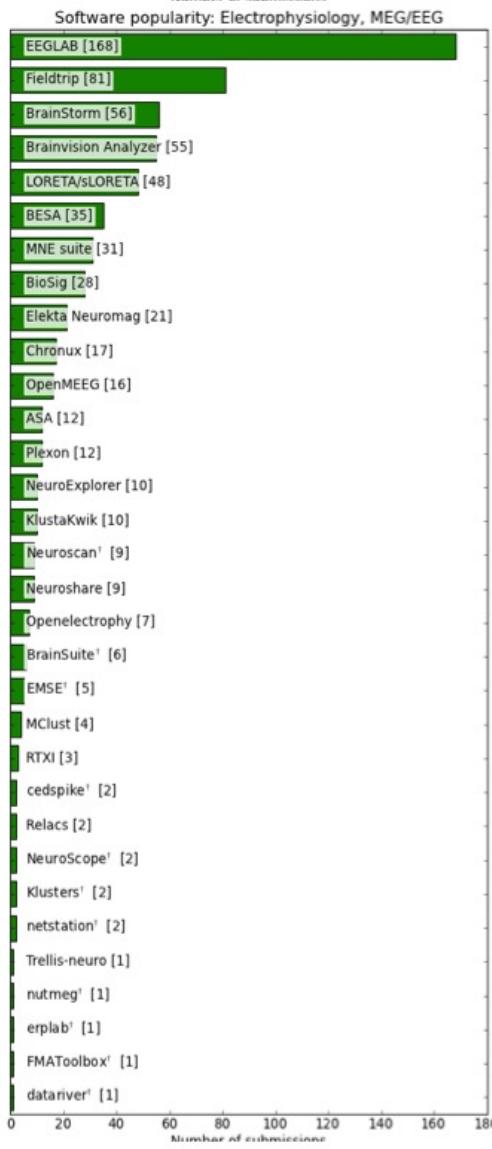


Network Dynamics in EEG

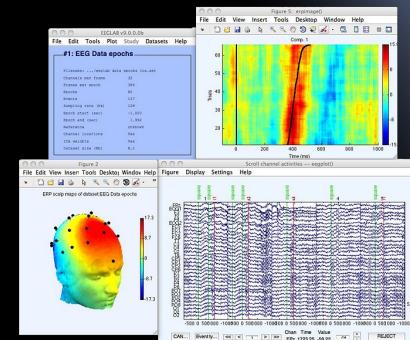


Arnaud Delorme



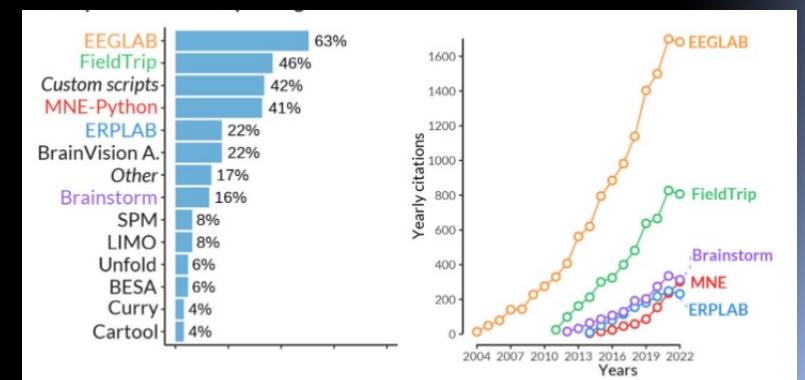


EEGLAB



<http://eeglab.org>

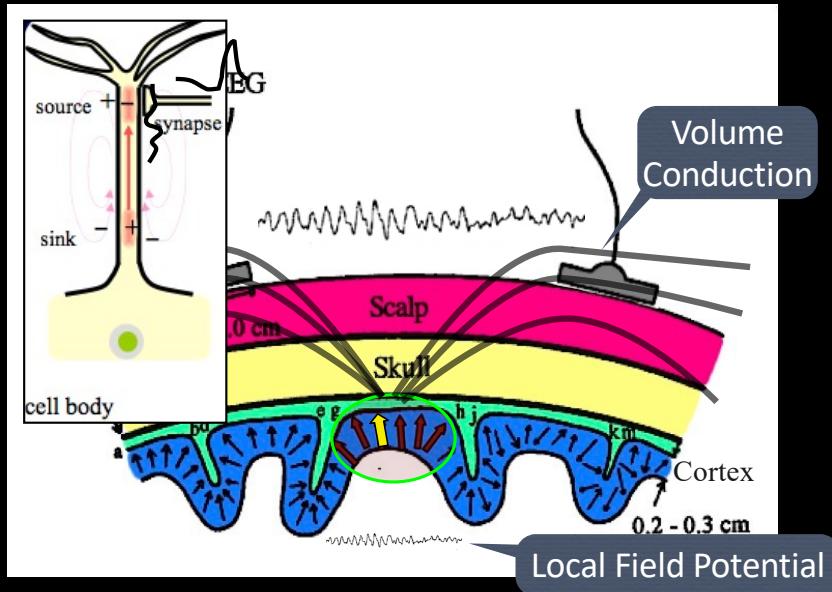
- ▶ Collection of over 350 functions (70,000 lines of code)
- ▶ About 1M download over the past 23 years
- ▶ About 6,500 users on the discussion list and 19,000 on the diffusion list
- ▶ 150 plugins



Biophysics of EEG



Hans Berger
(1873-1971)



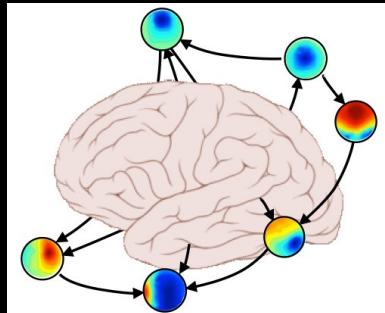
Synchronicity of cell excitation determines amplitude and rhythm of the EEG signal

Connectivity analysis

Aspet, 2025



Tim Mullen



SIFT

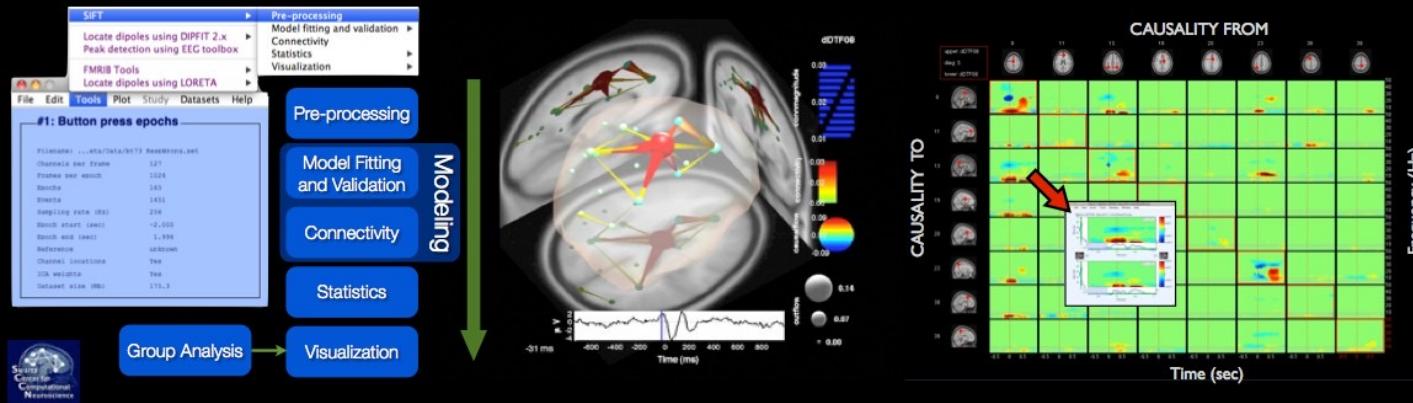
Source Information Flow Toolbox

<http://sccn.ucsd.edu/wiki/SIFT>

Mullen, et al, *Journal of Neuroscience Methods* (in prep, 2012)

Mullen, et al, *Society for Neuroscience*, 2010

Delorme, Mullen, Kothe et al, *Computational Intelligence and Neuroscience*, vol 12, 2011

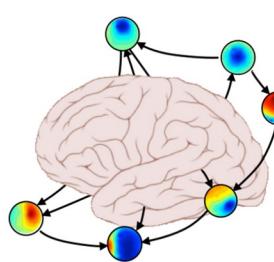


- A toolbox for (source-space) electrophysiological information flow and causality analysis (single- or multi-subject) integrated into EEGLAB
- Emphasis on vector autoregression and time-frequency domain approaches
- Standard and novel interactive visualization methods for exploratory analysis of connectivity across time, frequency, and spatial location

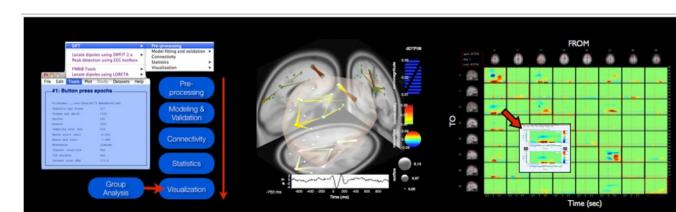
https://sccn.ucsd.edu/wiki/SIFT

Google Google maps Change adresse # IONS slack # OpenBrain psiq Phone PICS » Other Bookmarks Log in

SIFT



SIFT
Source Information Flow Toolbox
Version 0.1-Alpha



Contents [hide]

1 Welcome to the repository for the Source Information Flow Toolbox (SIFT)
1.1 SIFT Downloads
1.2 Citing SIFT
2 SIFT Online Handbook and User Manual

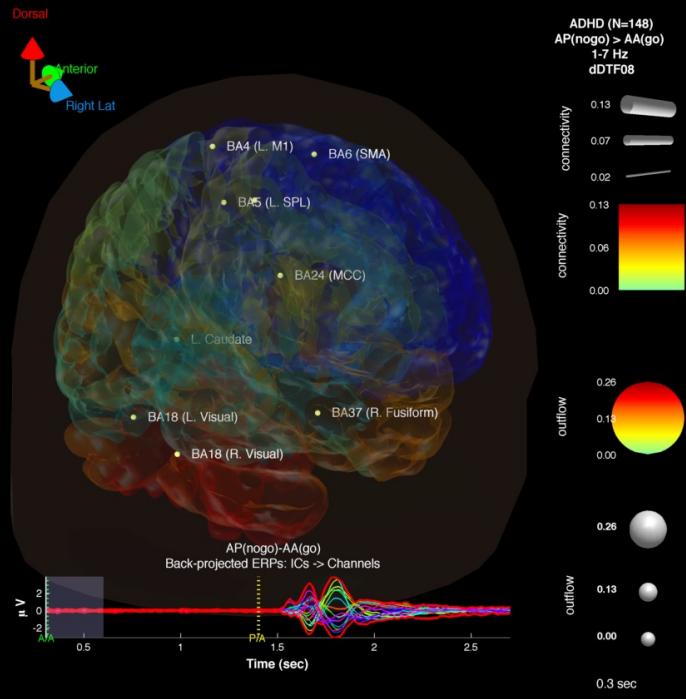
Welcome to the repository for the Source Information Flow Toolbox (SIFT)

Developed and Maintained by: Tim Mullen (SCCN, INC, UCSD)
Web: <http://www.antillipsi.net/>
Email: <Tim's first name> (at) sccn (dot) ucsd (dot) edu

SIFT is an EEGLAB-compatible toolbox for analysis and visualization of multivariate causality and information flow between sources of electrophysiological (EEG/ECoG/MEG) activity. It consists of a suite of command-line functions with an integrated Graphical User Interface for easy access to multiple features. There are currently four modules: data preprocessing, model fitting and connectivity estimation, statistical analysis, and visualization.

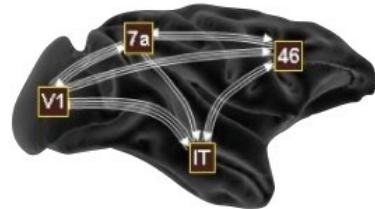
The Dynamic Brain

- A key goal: To model temporal changes in neural dynamics and information flow that index and predict task-relevant changes in cognitive state and behavior
- Open Challenges:
 - Non-invasive measures (source inference)
 - Robustness and Validity (constraints statistics)
 - Scalability (multivariate)
 - Temporal Specificity / Non stationarity / Single-trial (dynamics)
 - Multi-subject Inference
 - Usability and Data Visualization (software)



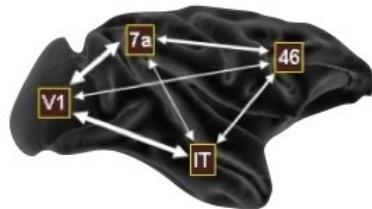
(Bullmore and Sporns, *Nature*, 2009)

Structural



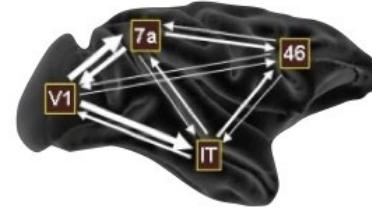
state-invariant,
anatomical

Functional



dynamic, state-dependent,
correlative, symmetric

Effective

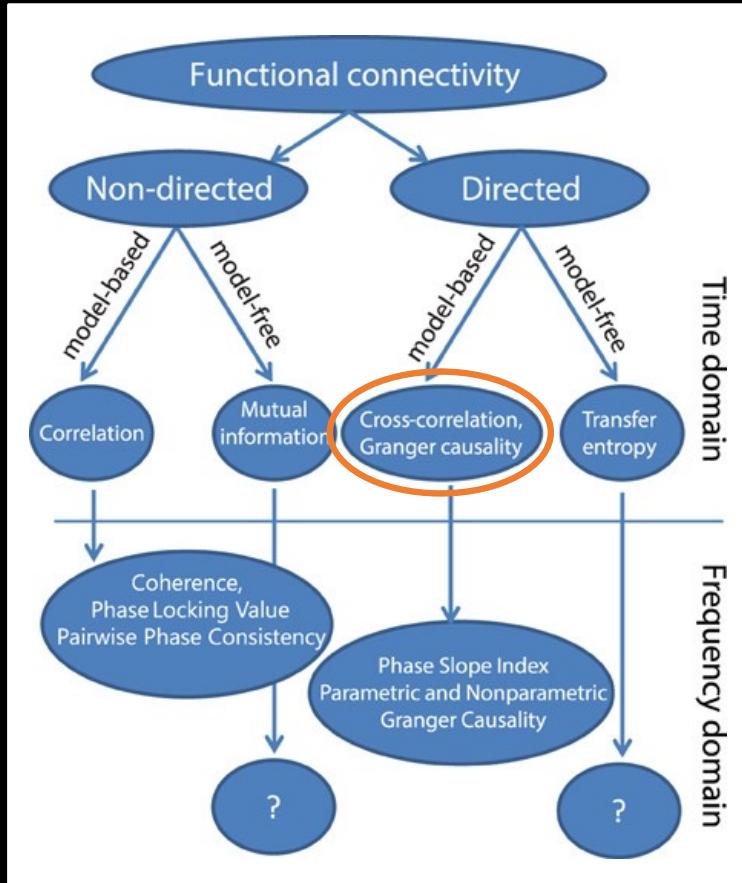


dynamic, state-dependent,
asymmetric, causal,
information flow

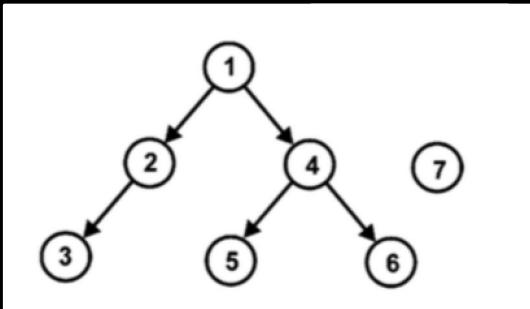
Hours-Years

milliseconds-seconds

Temporal Scale



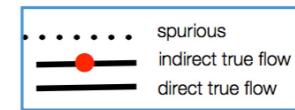
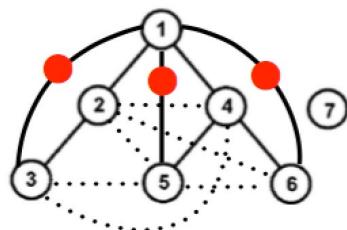
Bastos AM, Schoffelen J-M: A Tutorial Review of Functional Connectivity Analysis Methods and Their Interpretational Pitfalls. *Front Sys Neurosci* 2016, 9:413.



Coherency

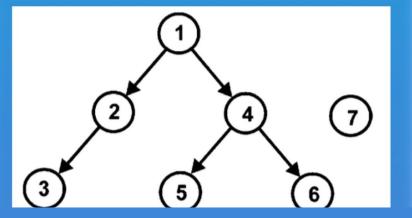
$$C_{ij}(f) = \frac{S_{ij}(f)}{\sqrt{S_{ii}(f)S_{jj}(f)}}$$

(Bendat and Piersol, 1986)

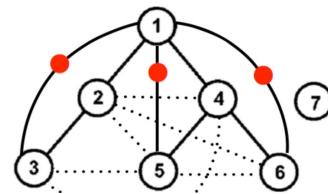


Bivariate measures such as coherence (but also original GC), find spurious connections between nodes if they share a common input.

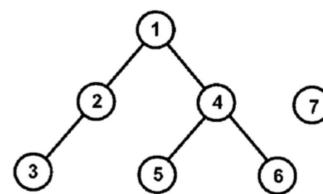
Ground Truth



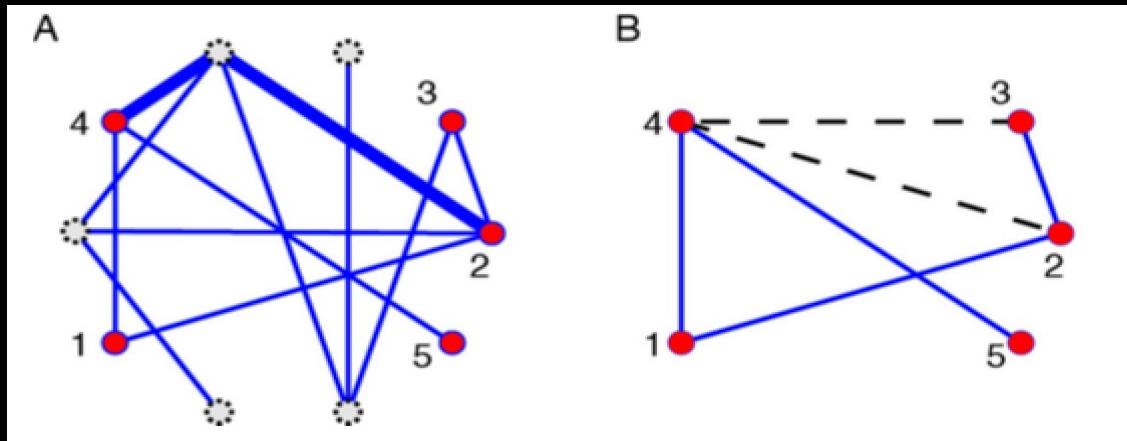
Coherence



Partial coherence



A deeper problem – unobserved nodes



With EEG, it's unavoidable that there will be contributing network nodes (e.g. thalamus) that we cannot observe.

We also can't be sure ICA will identify all important sources...

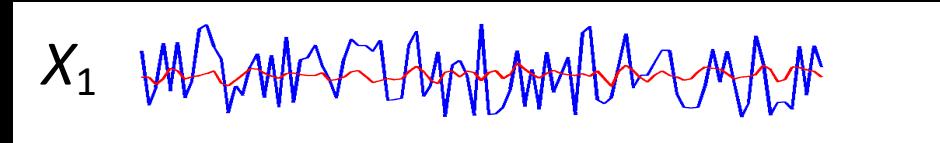
Granger-causality



- A measure of *statistical* causality based on prediction.
- Widely used in time-series econometrics.
- Nobel Prize in economics, 2003.

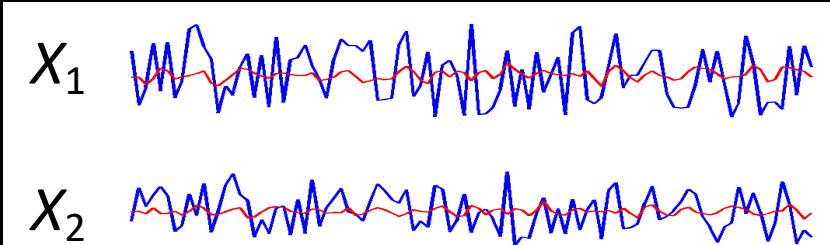
If a signal A causes a signal B, then knowledge of the past of both A and B should improve the predictability of B, as compared to knowledge of B alone.

AR Models (prediction of future of a signal by its past)

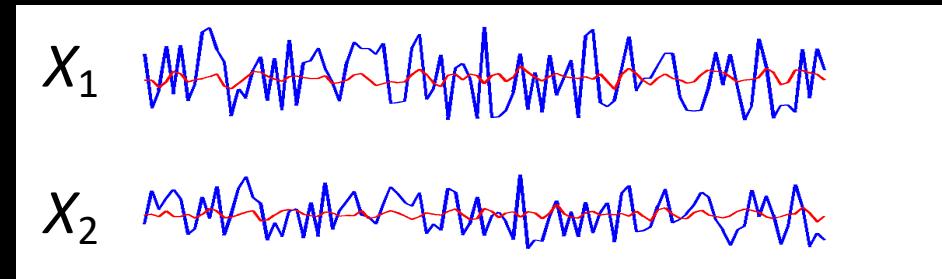


$$X_1(t) = -0.5X_1(t-1) + 0.3X_1(t-2) + 0.1X_1(t-3) \dots$$

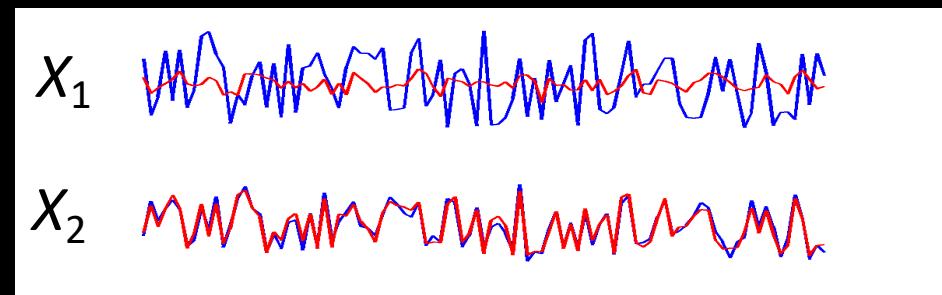
AR Models (prediction of future of a signal by its past)



AR Models (prediction of future of a signal by its past)

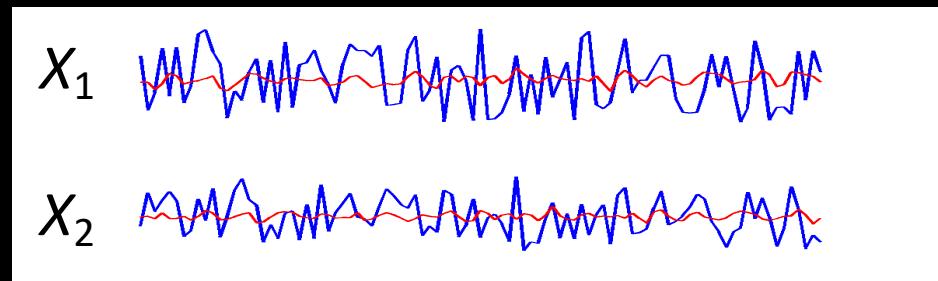


VAR Models (prediction of future of a signal by its past + the other signal's past)

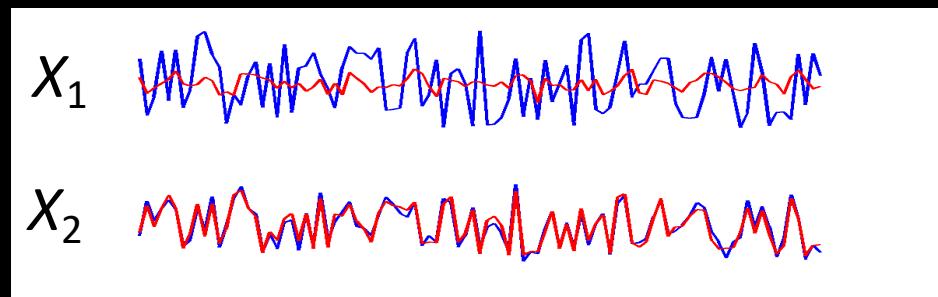


Incorporating information about X_1 improves the prediction of X_2 ! We say " X_1 granger causes X_2 "

AR Models (prediction of future of a signal by its past)



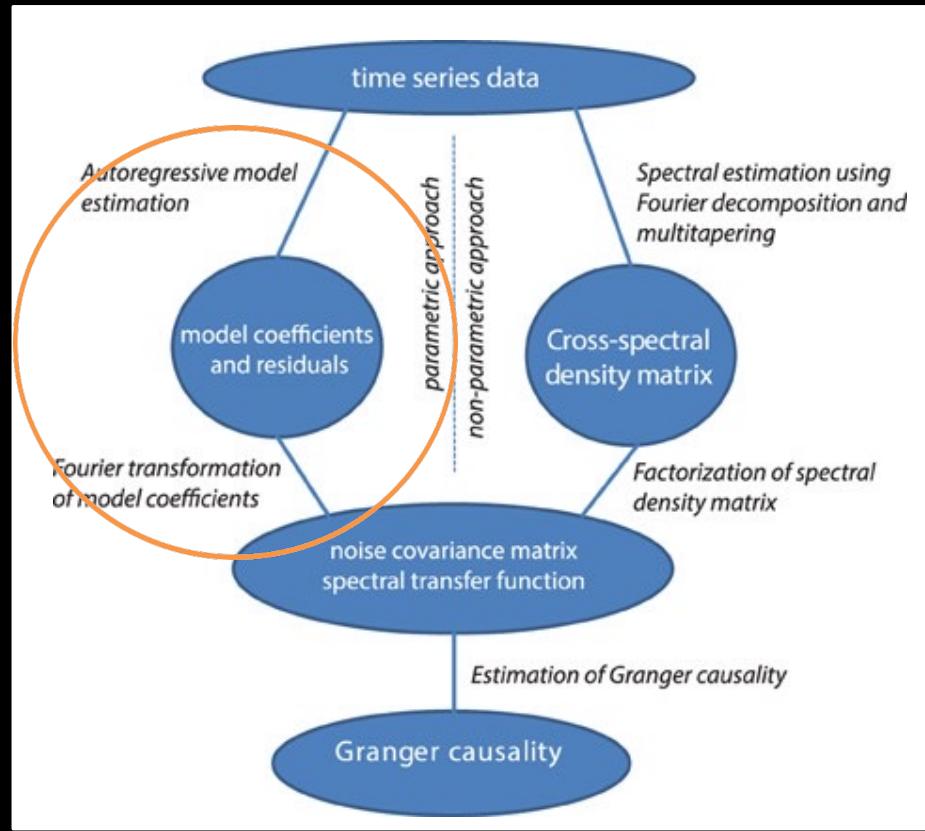
VAR Models (prediction of future of a signal by its past + the other signal's past)



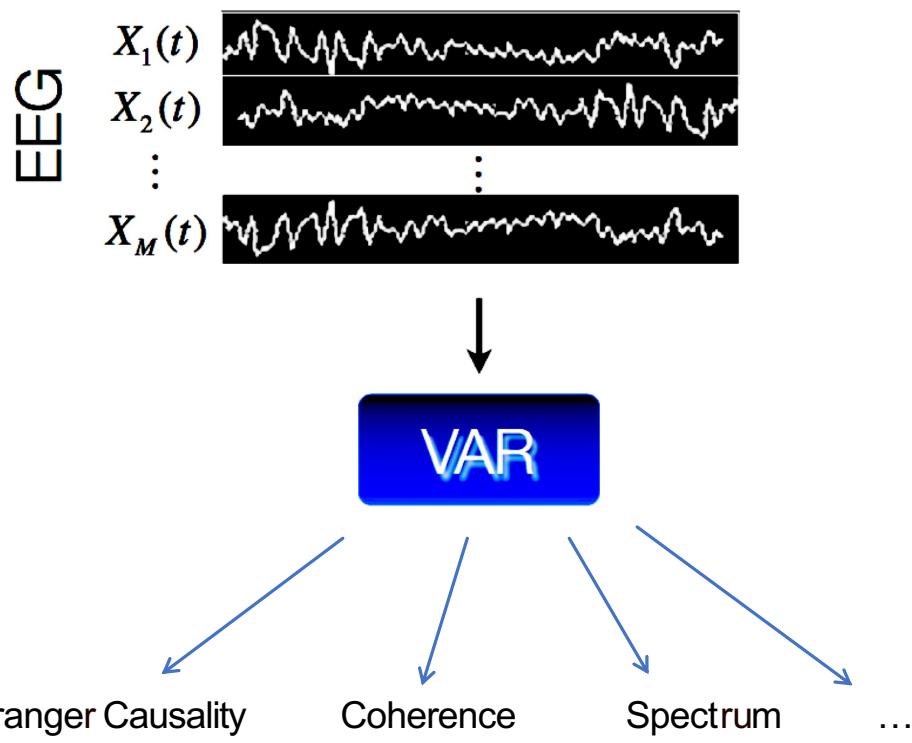
$$X_1(t) = -0.5X_1(t-1) + 0.3X_2(t-1) + \dots$$

$$X_2(t) = -5X_1(t-1) - 0.1X_2(t-1) + \dots$$

Incorporating information about X_1 improves the prediction of X_2 ! We say " X_1 granger causes X_2 "

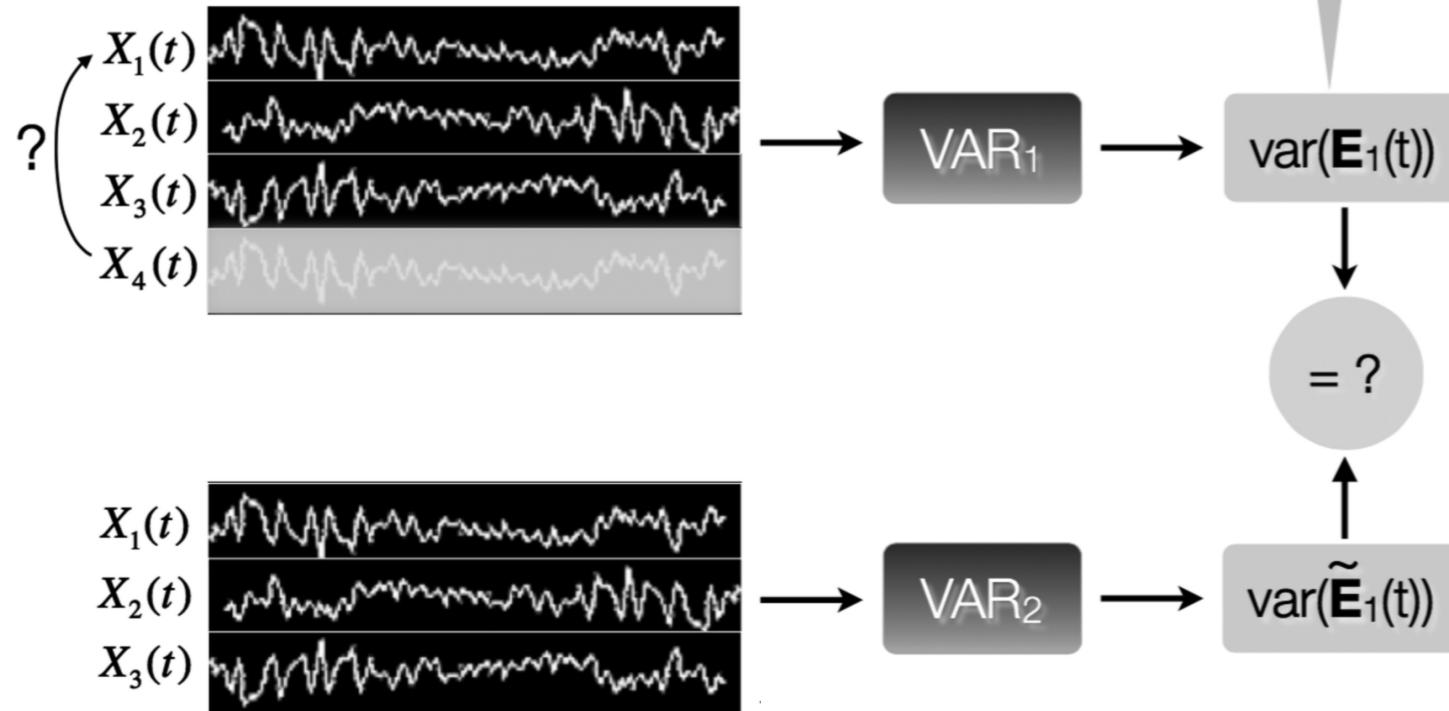


Vector Autoregressive (VAR / MAR / MVAR) Modeling



Granger Causality

Does X_4 granger-cause X_1 ?
(conditioned on X_2, X_3)



Granger-causality quiz

$$\begin{aligned} X_1(t) &= -0.5X_1(t-1) + 0X_2(t-1) + E_1(t) \\ X_2(t) &= 0.7X_1(t-1) + 0.2X_2(t-1) + E_2(t) \end{aligned}$$

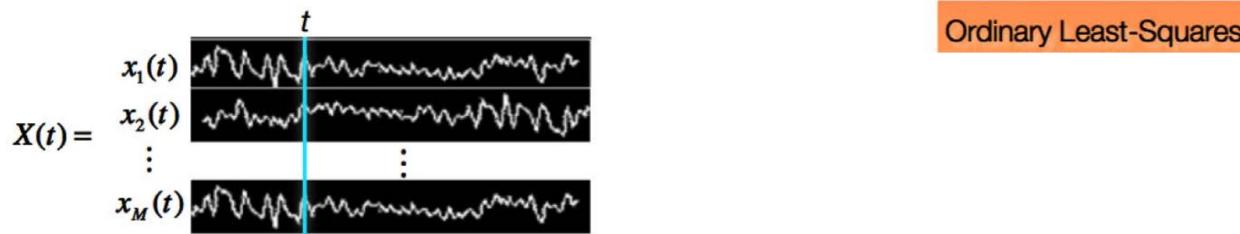
The diagram illustrates causal relationships between two variables, X_1 and X_2 . A red curved arrow points from $X_1(t)$ to $X_2(t)$, indicating that X_1 Granger-causes X_2 . A green curved arrow points from $X_2(t-1)$ to $X_1(t)$, indicating that X_2 Granger-causes X_1 .

Which causal structure does this model correspond to?



The Linear Vector Auto-regressive (VAR) Model

VAR[p] model



$$\mathbf{X}(t) = \sum_{k=1}^p \mathbf{A}^{(k)}(t) \mathbf{X}(t-k) + \mathbf{E}(t)$$

model order

M-channel data vector at current time t

$M \times M$ matrix of (possibly time-varying) model coefficients indicating variable dependencies at lag k

random noise process

multichannel data k samples in the past

$$\mathbf{A}^{(k)}(t) = \begin{pmatrix} a_{11}^{(k)}(t) & \dots & a_{1M}^{(k)}(t) \\ \vdots & \ddots & \vdots \\ a_{M1}^{(k)}(t) & \dots & a_{MM}^{(k)}(t) \end{pmatrix} \quad \mathbf{E}(t) = N(\mathbf{0}, \mathbf{V})$$

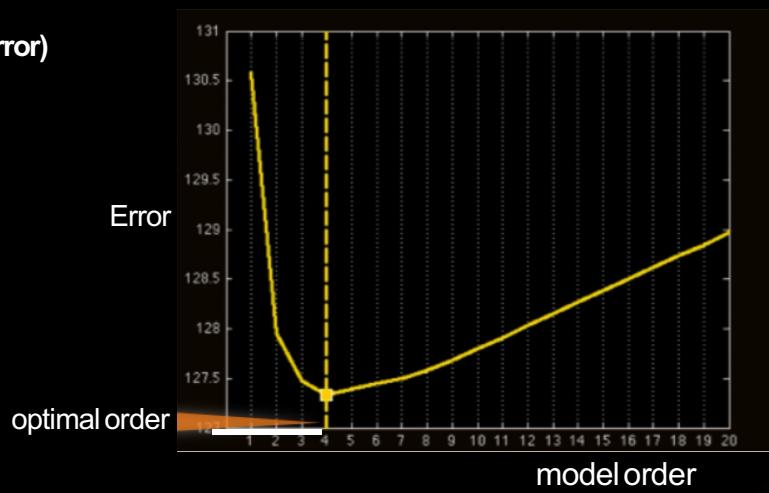
Selecting a VAR Model Order

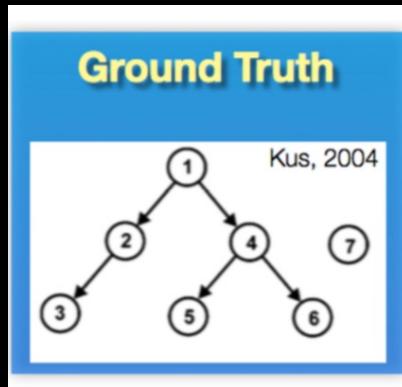
- Model order is typically determined by minimizing information criteria such as Akaike Information Criterion (AIC) for varying model order (p):

$$AIC(p) = 2\log(\det(V)) + M2p/N \quad \leftarrow \text{Penalizes high model orders (parsimony)}$$

↑
entropy rate (amount of prediction error)

- Optimal model order depends on sampling rate (higher sampling rate often requires higher model orders)

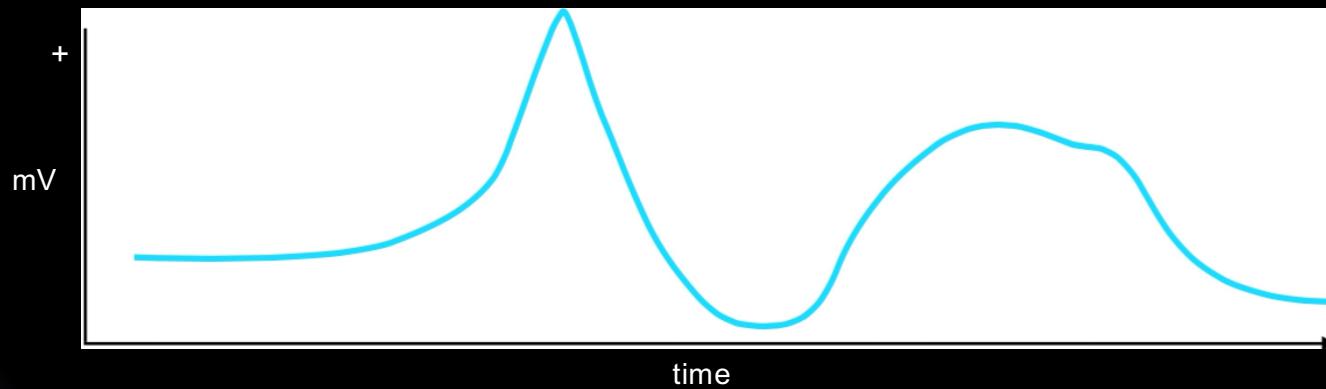




Functional		Effective	
<div style="display: flex; align-items: center;"> Bivariate Coherency </div> $C_{ij}(f) = \frac{S_{ij}(f)}{\sqrt{S_{ii}(f)S_{jj}(f)}}$ <p>(Bendat and Piersol, 1986)</p>	<div style="display: flex; align-items: center;"> Multivariate Partial Coherence </div> $P_{ij}(f) = \frac{S_{ij}^{-1}(f)}{\sqrt{S_{ii}^{-1}(f)S_{jj}^{-1}(f)}}$ <p>(Bendat and Piersol, 1986; Dalhaus, 2000)</p>	<div style="display: flex; align-items: center;"> Granger-Geweke Causality </div> $F_{ij}(f) = \frac{\Sigma_{jj} - (\Sigma_{ij}^2 / \Sigma_{ii}) H_{ij}(f) ^2}{S_{ii}(f)}$ <p>(Geweke, 1982; Bressler et al., 2007)</p>	<div style="display: flex; align-items: center;"> Partial Directed Coherence </div> $\pi_{ij}^2(f) = \frac{ A_{ij}(f) ^2}{\sum_{k=1}^M A_{kj}(f) ^2}$ <p>(Baccalá and Sameshima, 2001)</p>

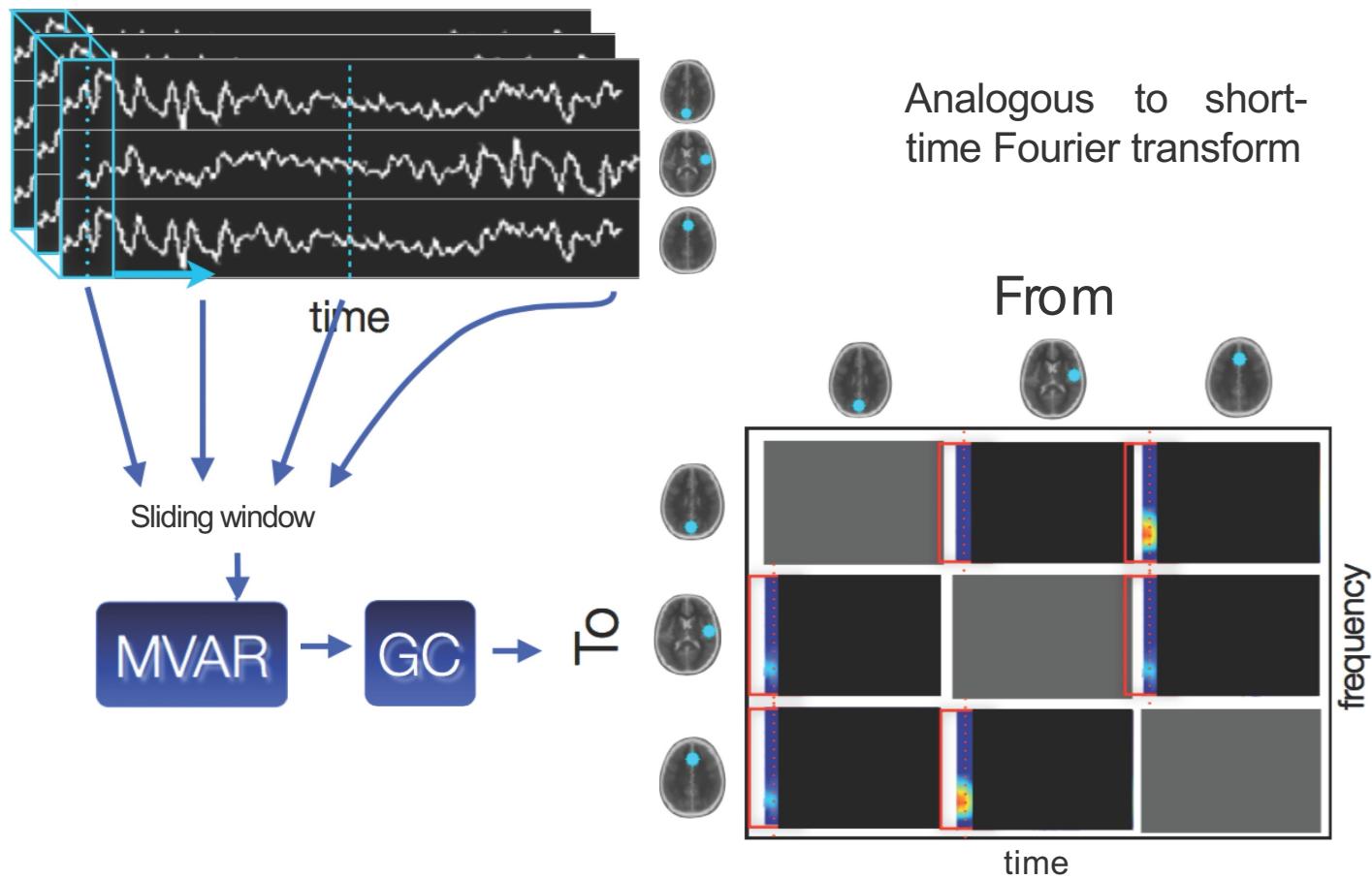
Adapting to Non-Stationarity

- The brain is a **dynamic system** and measured brain activity and coupling can change rapidly with time (non-stationarity)
 - event-related perturbations (ERSP, ERP, etc)
 - structural changes due to learning/feedback
- How can we adapt to non-stationarity?



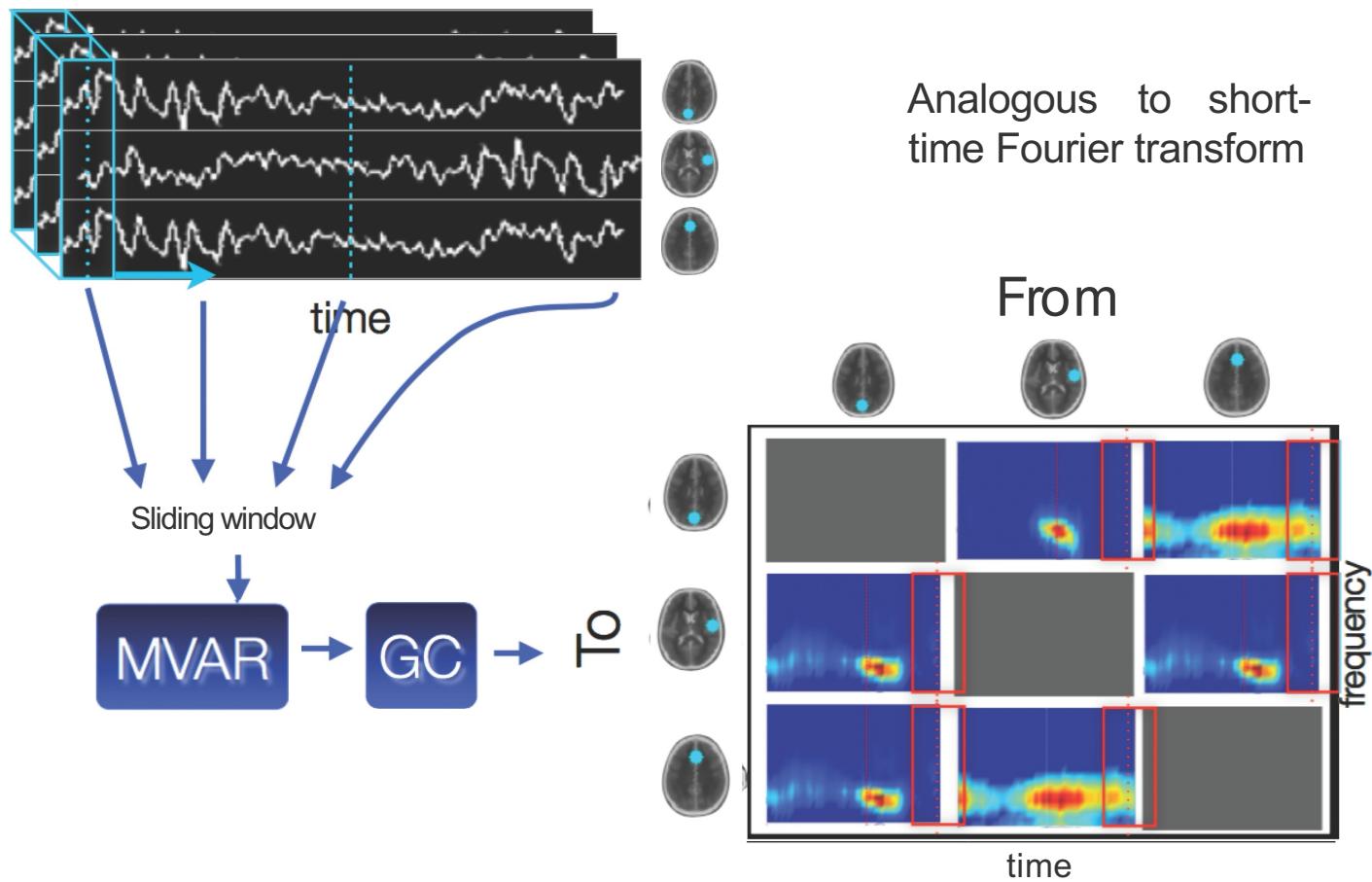
Segmentation-based VAR

(Jansen et al., 1981; Florian and Pfurtscheller, 1995; Ding et al,2000)



Segmentation-based VAR

(Jansen et al., 1981; Florian and Pfurtscheller, 1995; Ding et al,2000)

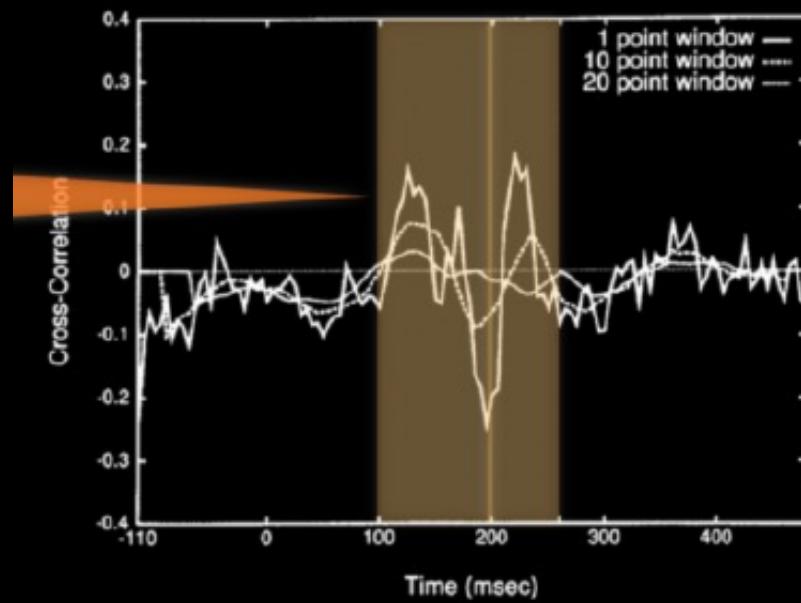


Important Choices

- Model Order
 - Determines complexity of spectrum you can model
 - Larger orders need more data
- Window Length
 - Window must be long enough to contain sufficient data for your chosen model order
 - Must be long enough to encompass the time-scale of interactions
 - Yet not too long as to smear temporal dynamics or include non-stationary data
 - *If trials are present, can optimize AR model over trials*

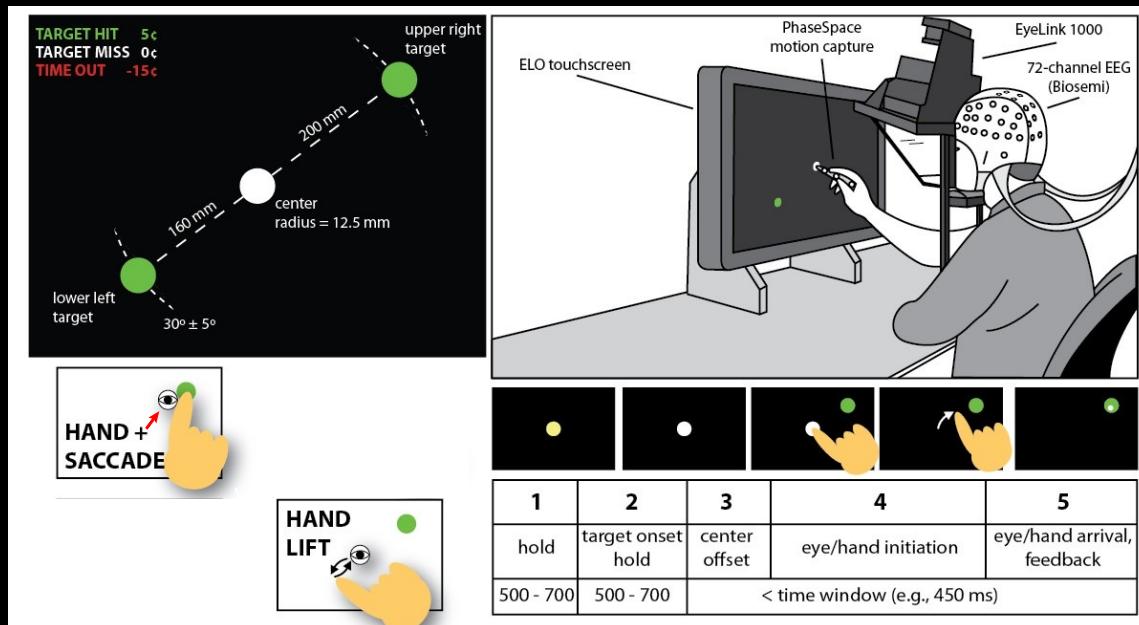
Consideration: Local Stationarity

Too-large windows may not
be locally-stationary

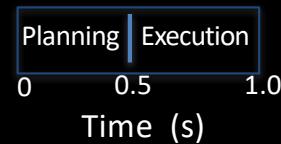


How does brain plan visually guided movements?

- Pointing Task (Park, et al. 2014, *IEEE Trans Neural Syst Rehabil Eng*)



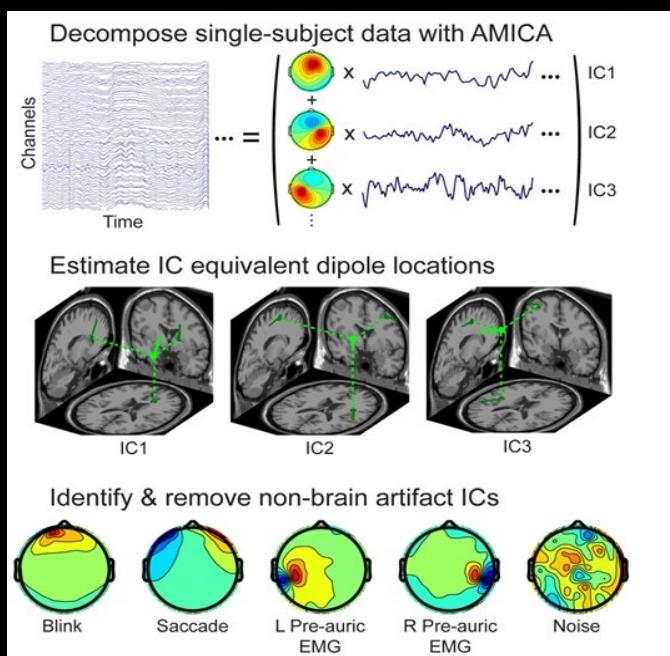
N=10 (right-handed, mean age=21) 70 channel EEG (Biosemi)
512 Hz; 128Hz for connectivity



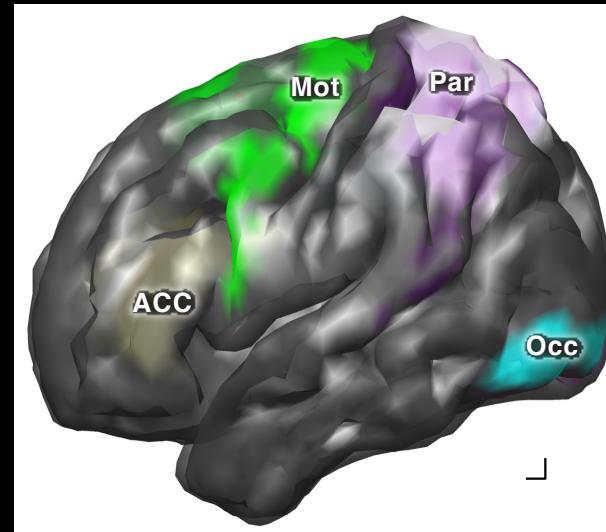
John R. Iversen, Alejandro Ojeda,
Tim Mullen, Markus Plank, Joseph
Snider, Gert Cauwenberghs,
Howard Poizner (2014) EMBC

ICA source space analysis

Independent Component Analysis

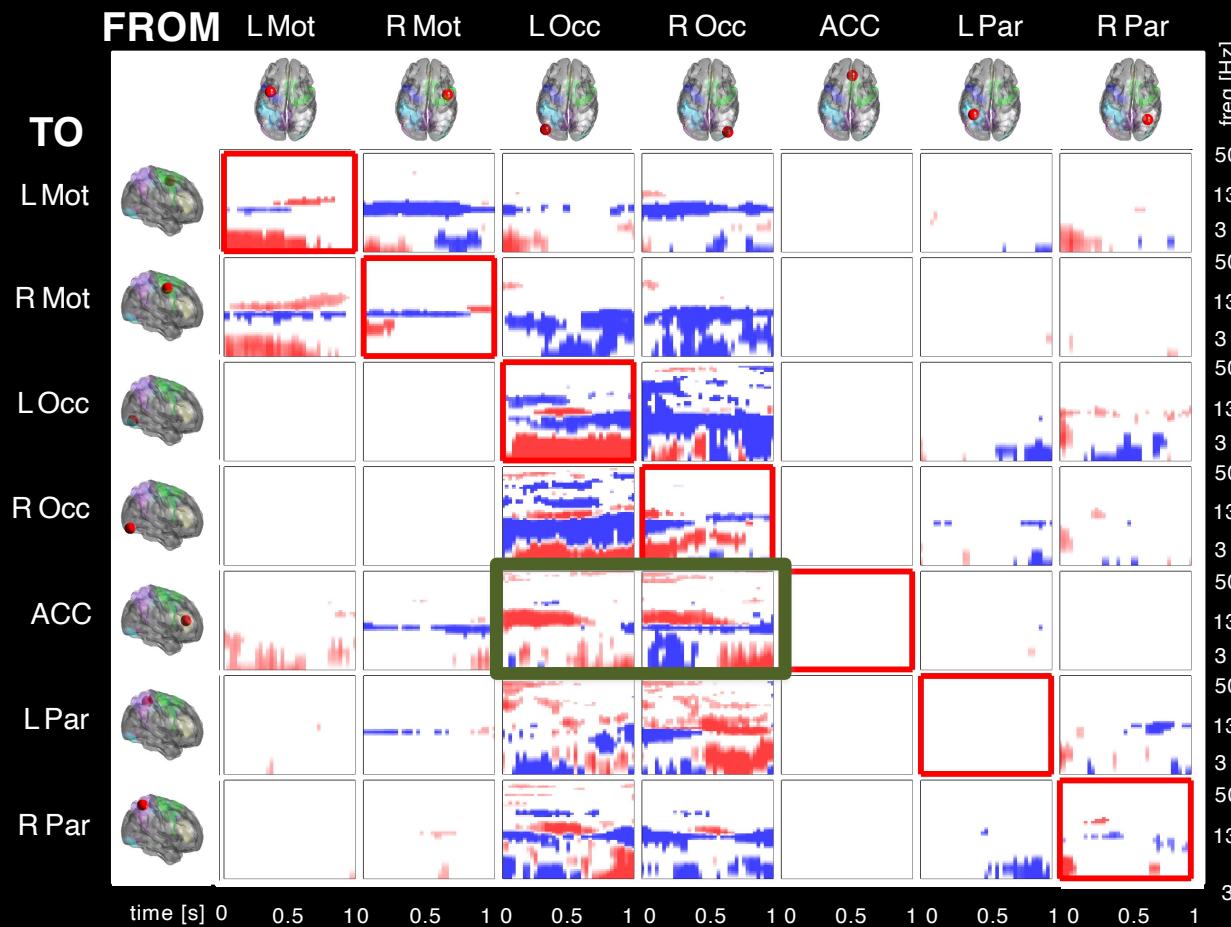


Cortical Regions of Interest



Group SIFT: Project ICs onto cortical surface using LORETA; extract ROI time series.
Advantage: Same ROIs for all subjects enables statistical comparison. (Use BCILAB *srcpot*)

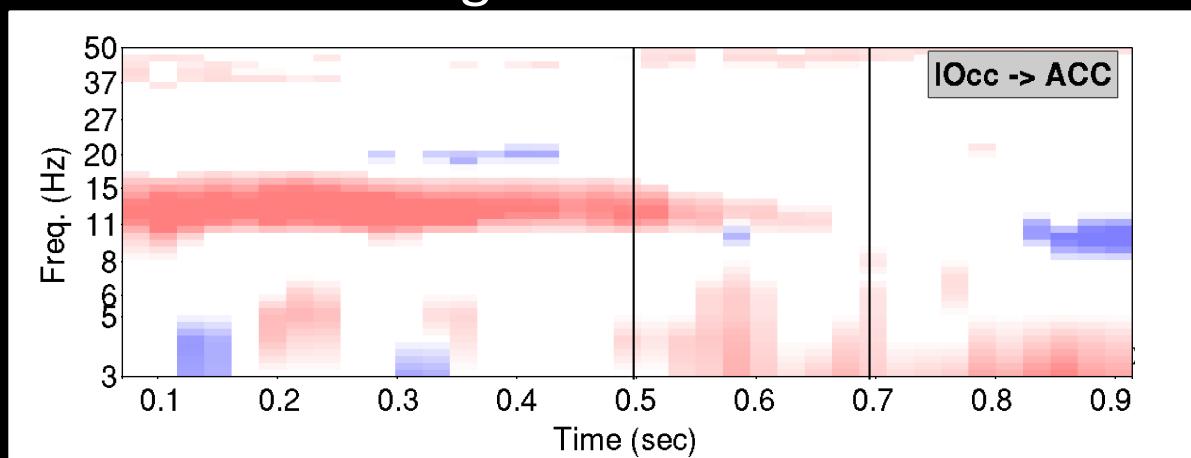
Changed causal flow during reaching



Occipital -> ACC

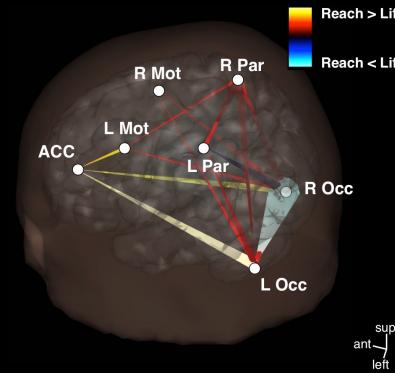
Planning

Execution

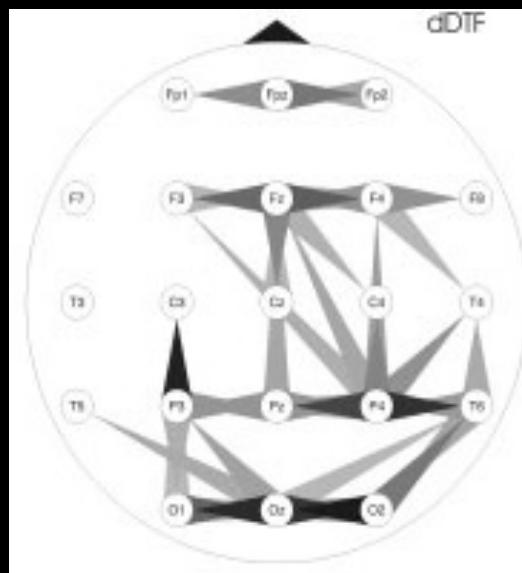


Result discussion

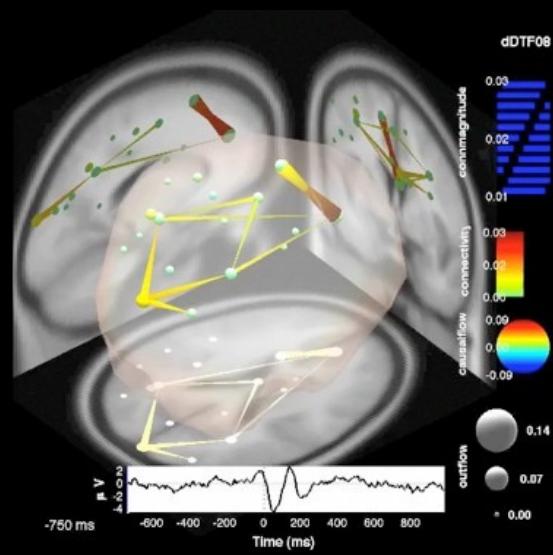
- SIFT is a capable toolkit for causal dynamical analysis at source level
- Parietal network expected for visually guided action (e.g. Heider, et al., 2010)
- ACC more strongly driven by Occipital Motor. Locus for translation of intention into action (Paus, 2001; Srinivasan, et al. 2013). ACC drives SMA (not shown).
- Causal network results depend on the number of nodes
 - E.g. Occipital "ACC could be mediated by region not included in model
 - There will always be a tradeoff between network size and amount of data needed to fit the model.
 - Regularization



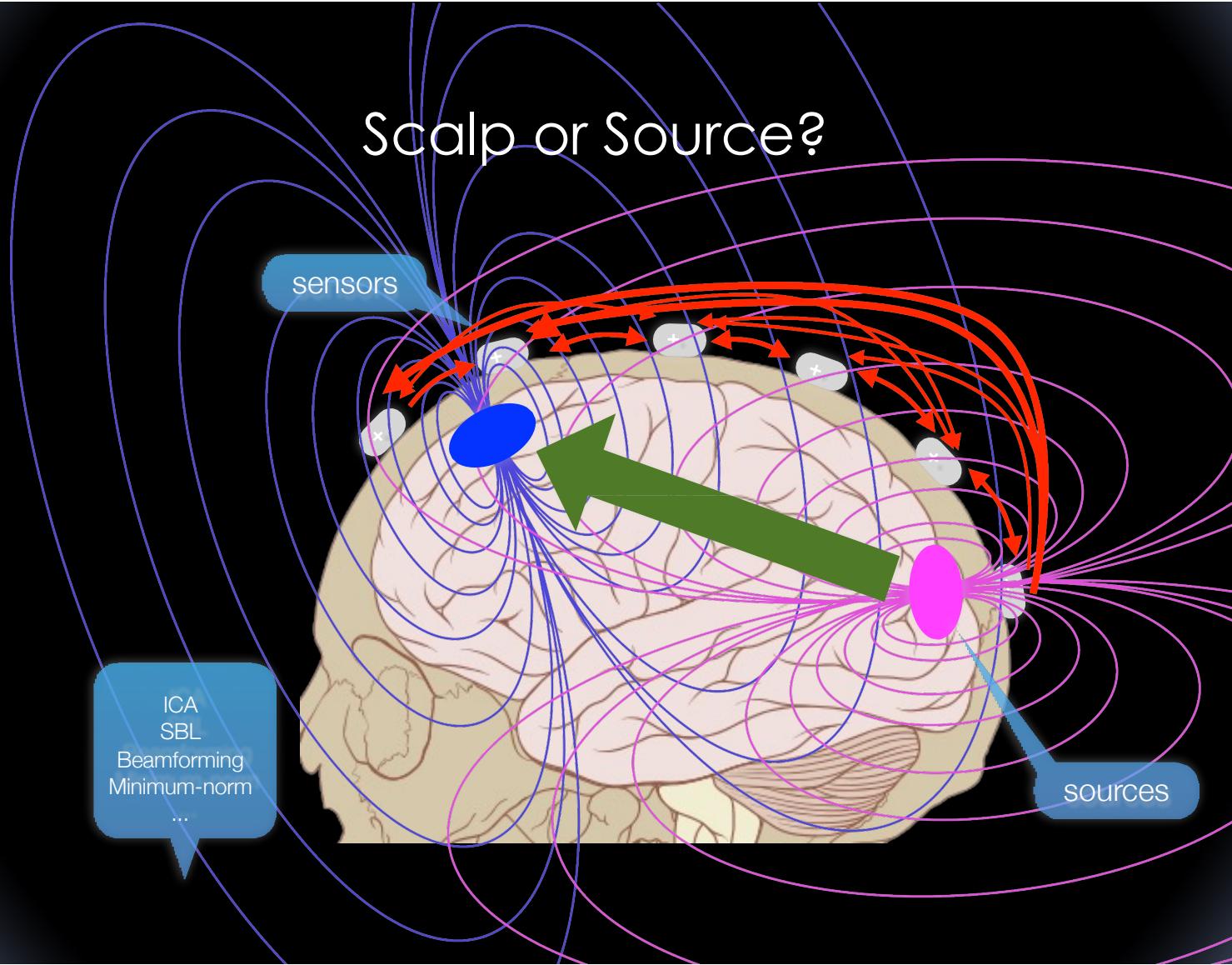
Scalp or Source?

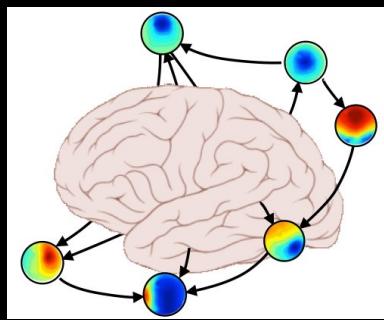


or



Scalp or Source?



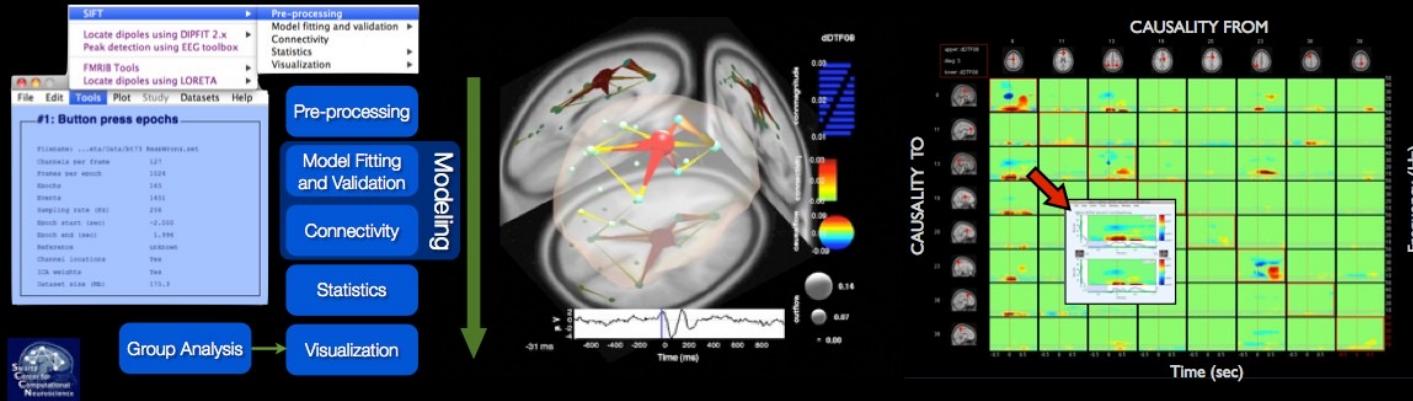


<http://sccn.ucsd.edu/wiki/SIFT>

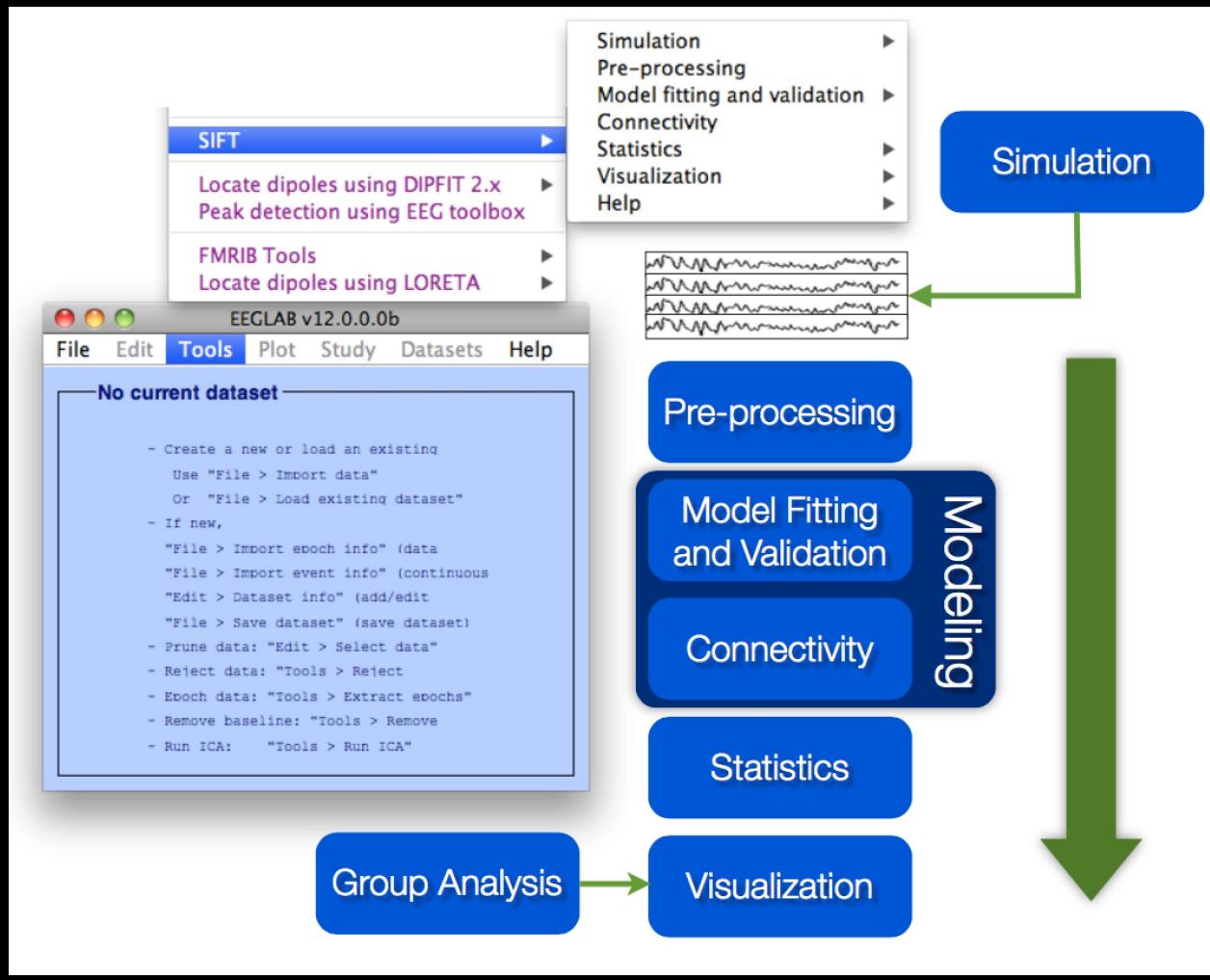
Mullen, et al, *Journal of Neuroscience Methods* (in prep, 2012)

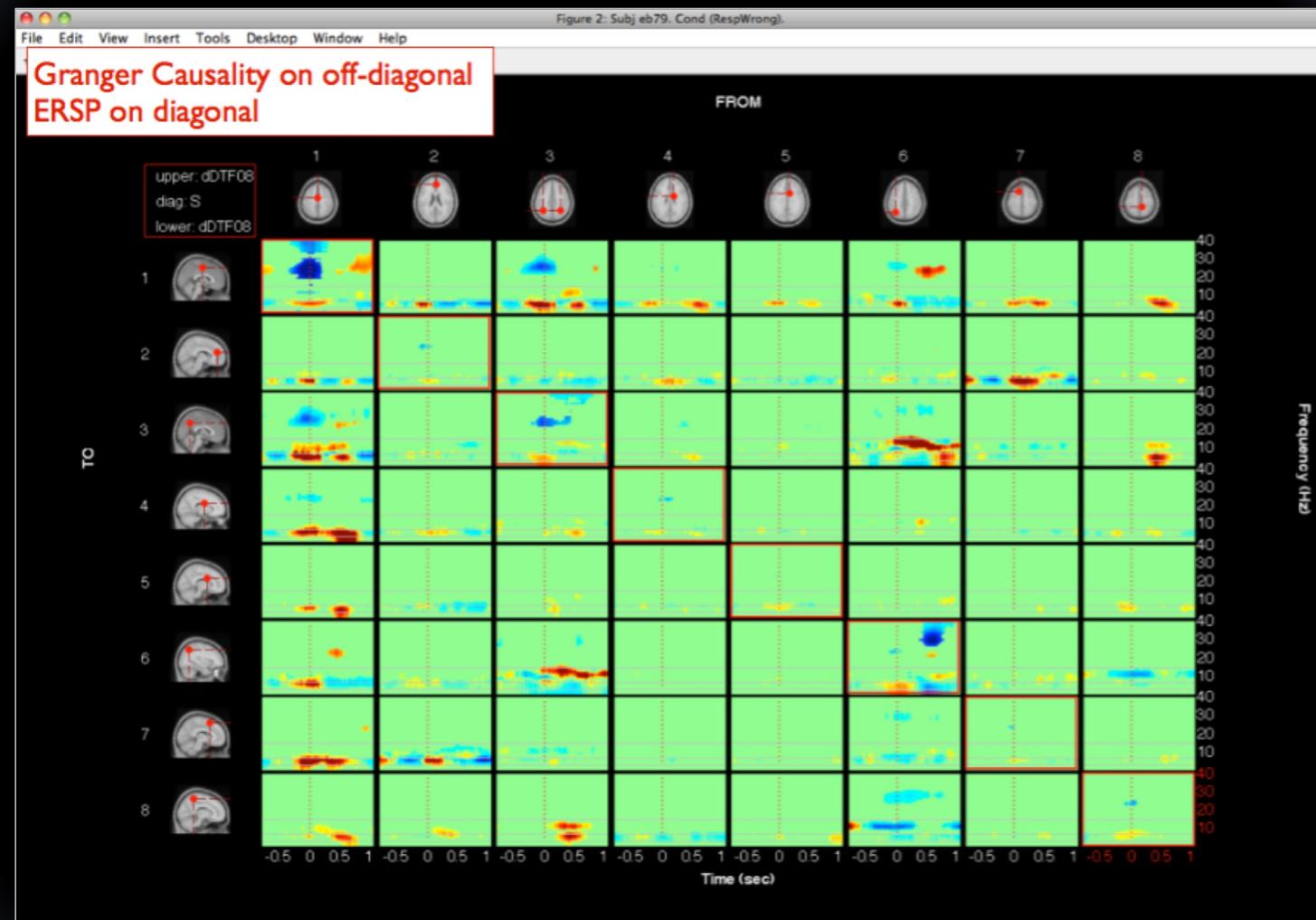
Mullen, et al, *Society for Neuroscience*, 2010

Delorme, Mullen, Kothe et al, *Computational Intelligence and Neuroscience*, vol 12, 2011



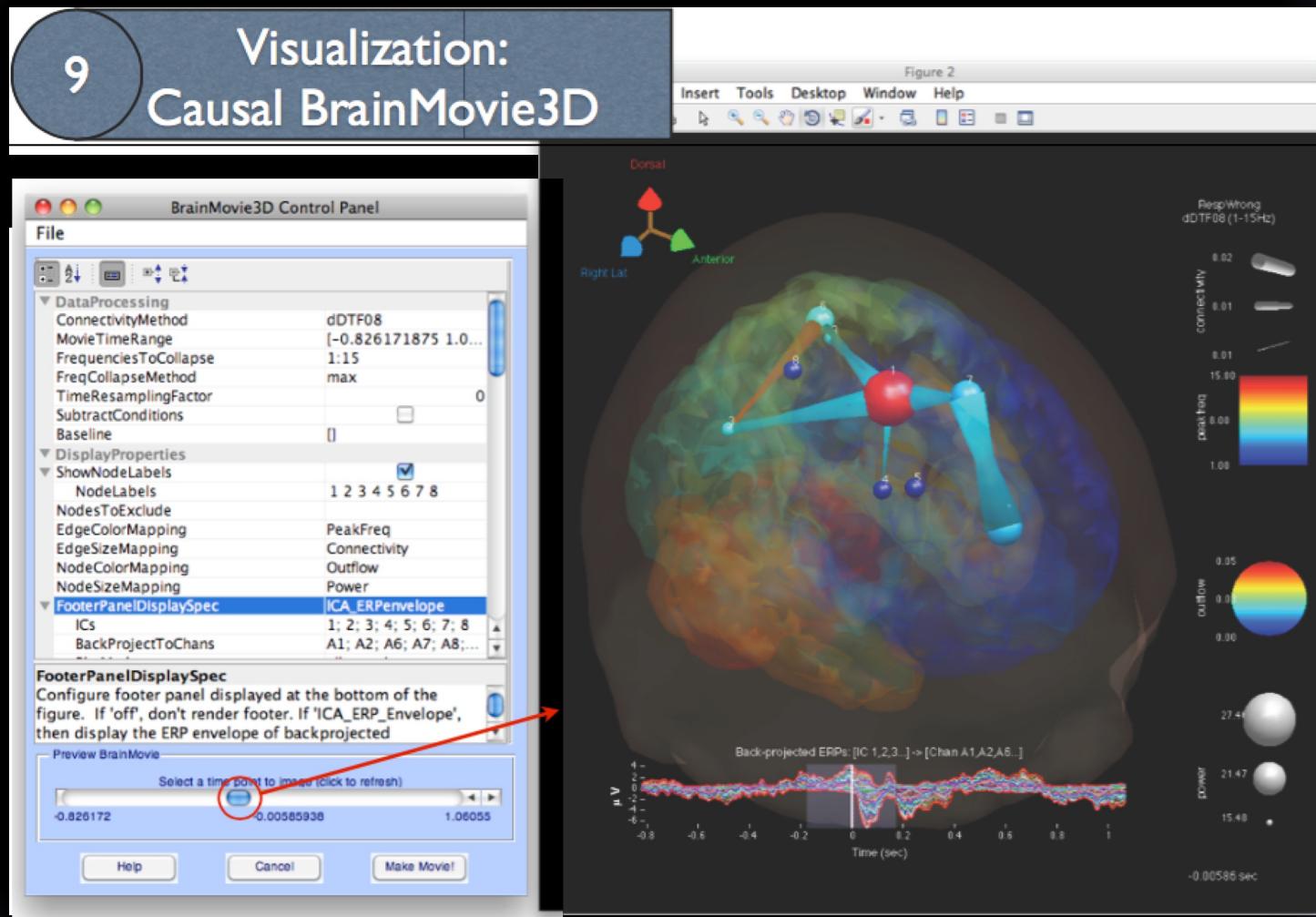
- A toolbox for (source-space) electrophysiological information flow and causality analysis (single- or multi-subject) integrated into the EEGLAB software environment.
- Emphasis on vector autoregression and time-frequency domain approaches
- Standard and novel interactive visualization methods for exploratory analysis of connectivity across time, frequency, and spatial location





9

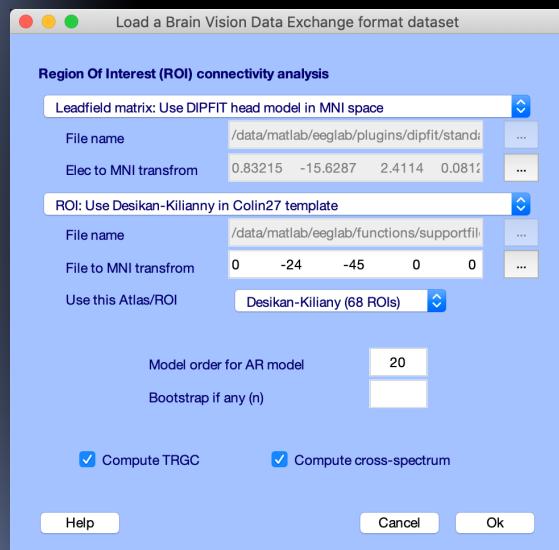
Visualization: Causal BrainMovie3D



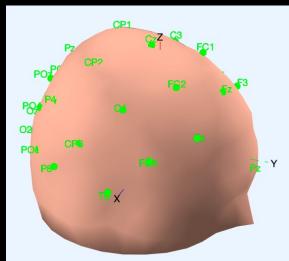
Time-Frequency Analysis of EEG Time series

More Connectivity analysis

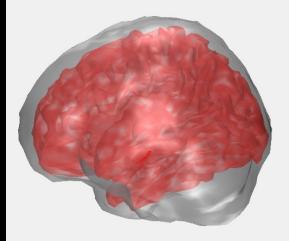
EEGLAB ROI connectivity plugin



Align electrodes
with scalp model



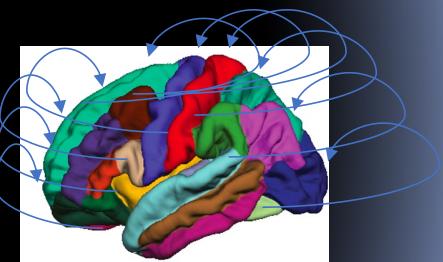
Align atlas with cortex model



Distributed source modeling



Group voxels in regions
and compute connectivity



Measures **TRGC**, GC, TRPDC,
PDC, TRDTF, DTF and **CS**

Haufe, S., Nikulin, V. V., Miller, K. R., & Nolte, G. (2013). A critical assessment of connectivity measures for EEG data: a simulation study. *Neuroimage*, 64, 120-133.

Connectivity analysis using EEG

Volumetric
atlases

AFNI MNI



Brainnetome

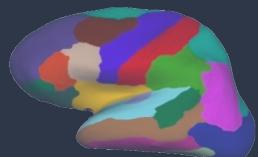


Schaefer 2018

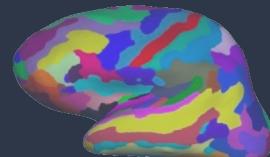


Surface
atlases

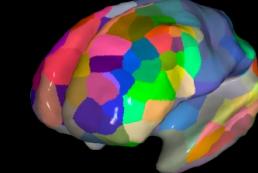
Desikan Kiliansy



Destrieux



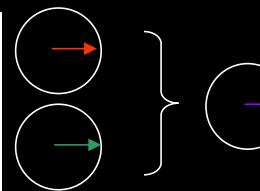
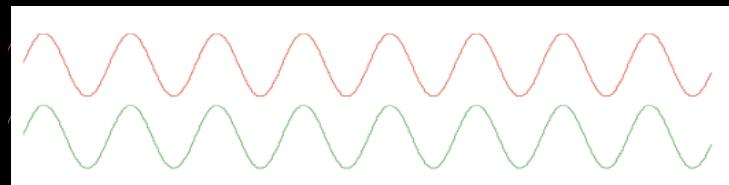
PrAGMATiC



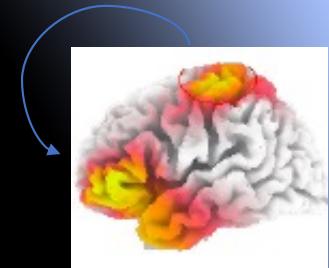
Cross-coherence amplitude and phase

2 areas, comparison on the same trials

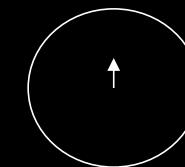
Trial 1



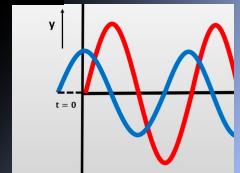
Coherence amplitude 1
Phase coherence 0



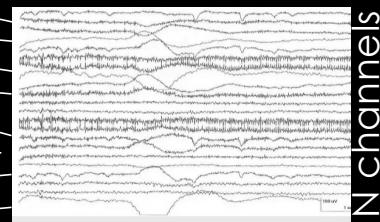
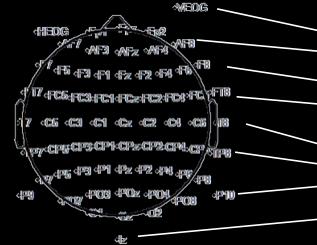
COHERENCE = $\text{mean}(\text{phase vector})$



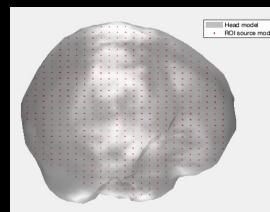
Norm 0.33
Phase 90 degree



Channel space (~100 dim)

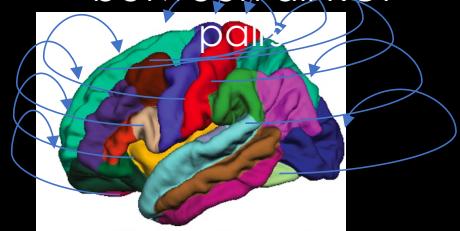


Source space (~10,000)



M voxels x 3

Compute connectivity between all ROI pairs



First ROI



Dim ~ 2 to 4



Second ROI



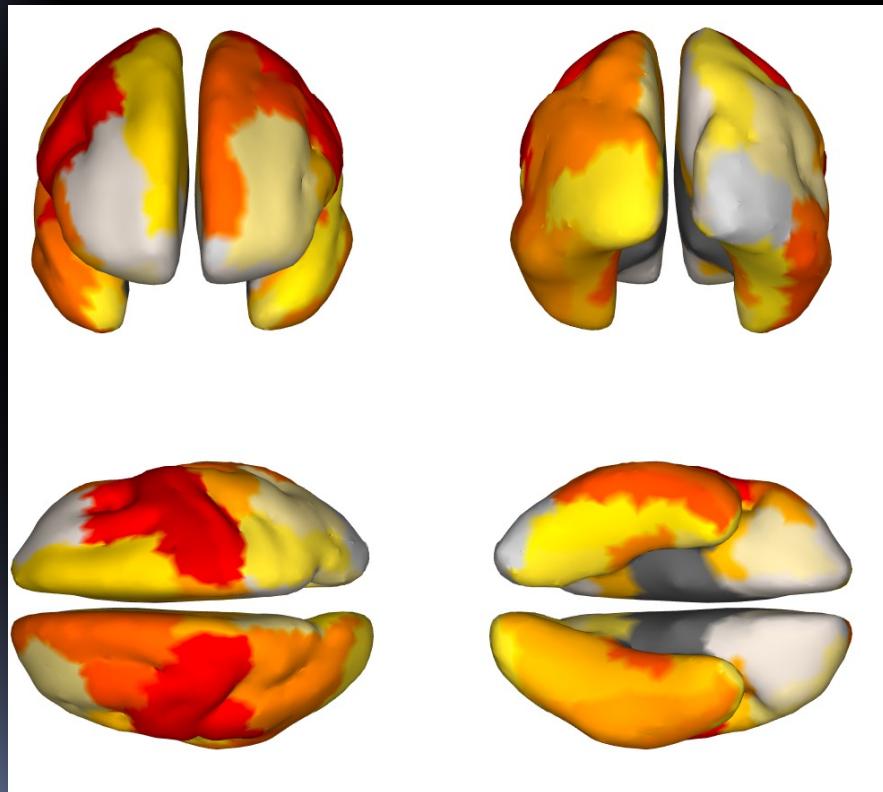
PCA



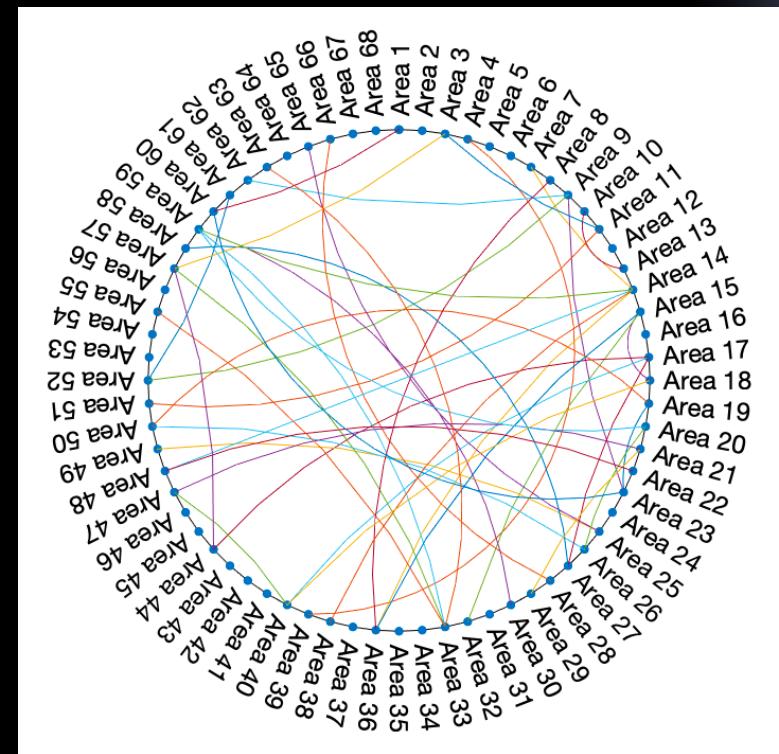
Dim ~ 2 to 4

Pairwise connectivity
TRGC, GC, TRPDC,
PDC, TRDTF, DTF and CS

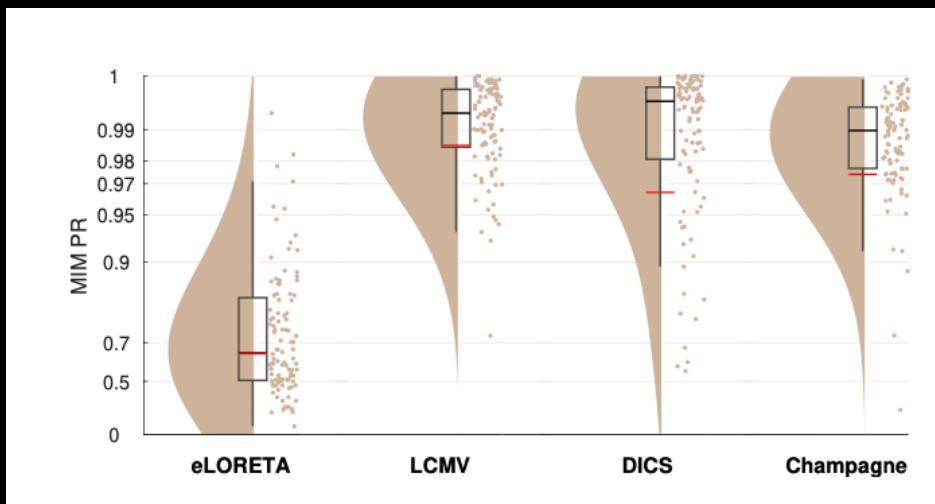
Red regions are highly interacting



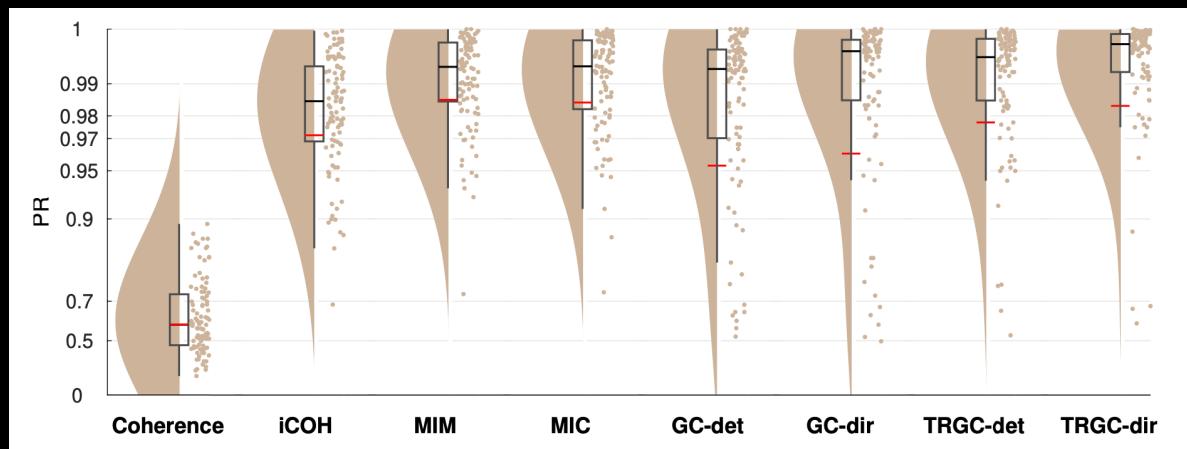
Connectivity matrix between 68 ROIs



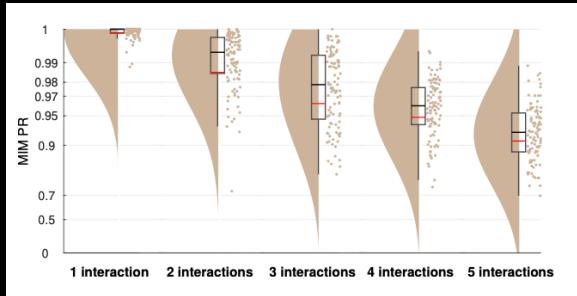
Inverse method



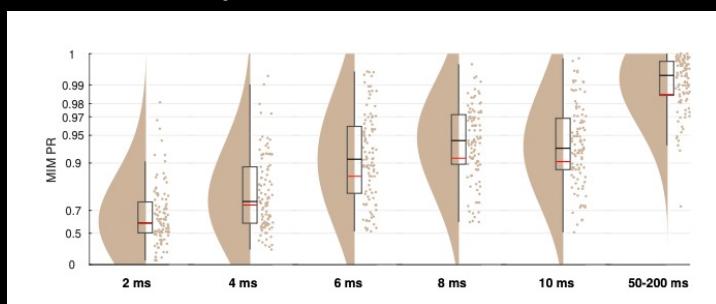
Connectivity method



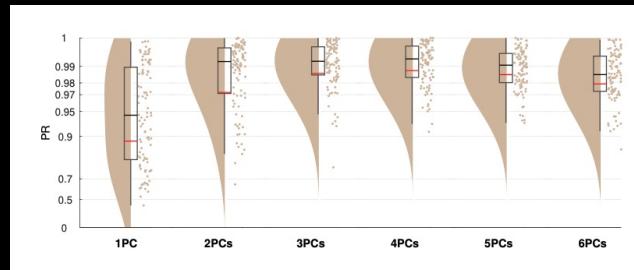
Number of interactions



Delay between sources



Number of PCA comp.

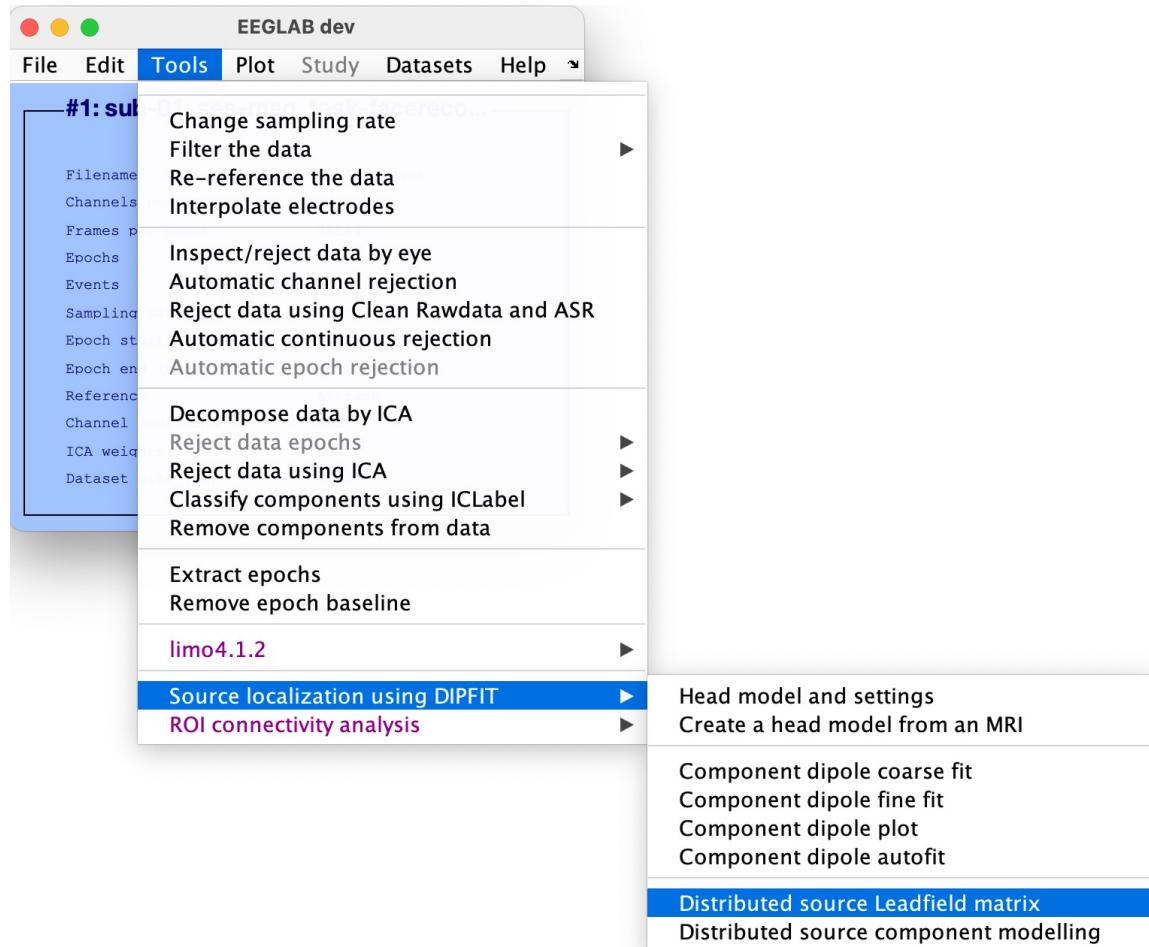


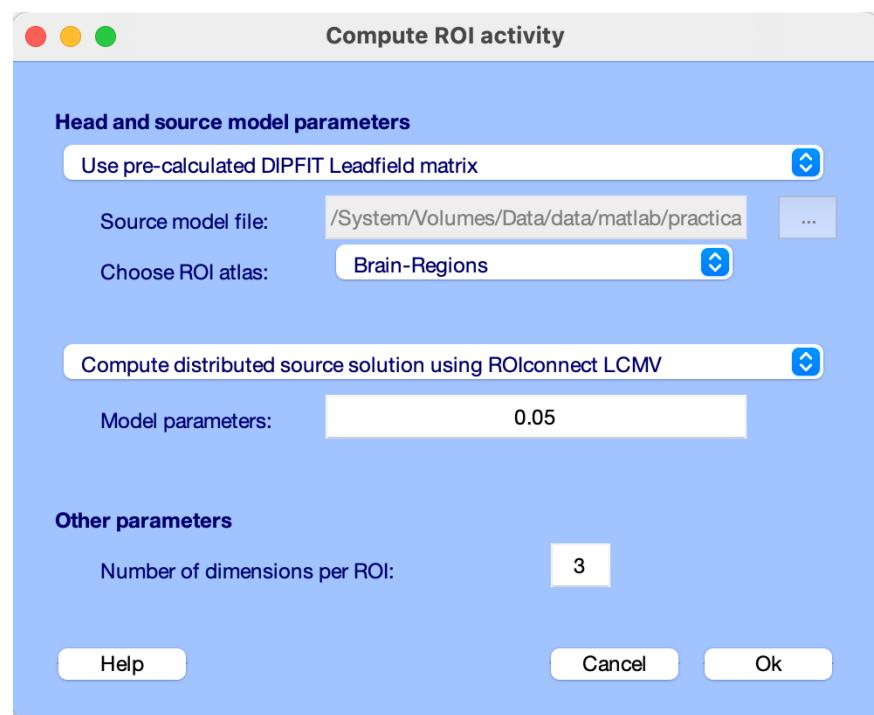
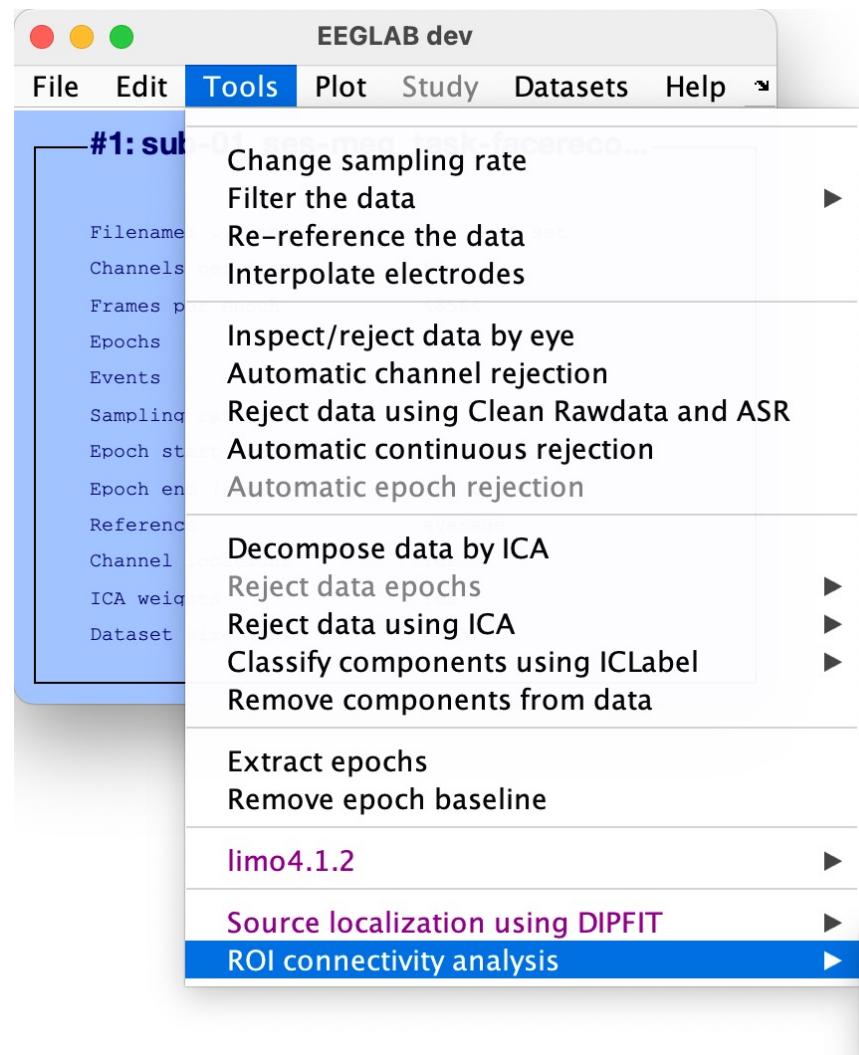
Data intake

- Stationary continuous data
- About 100 Hz
- 2 second data chunks (or epochs)
- Same length of data for each condition
- No dynamics – static image

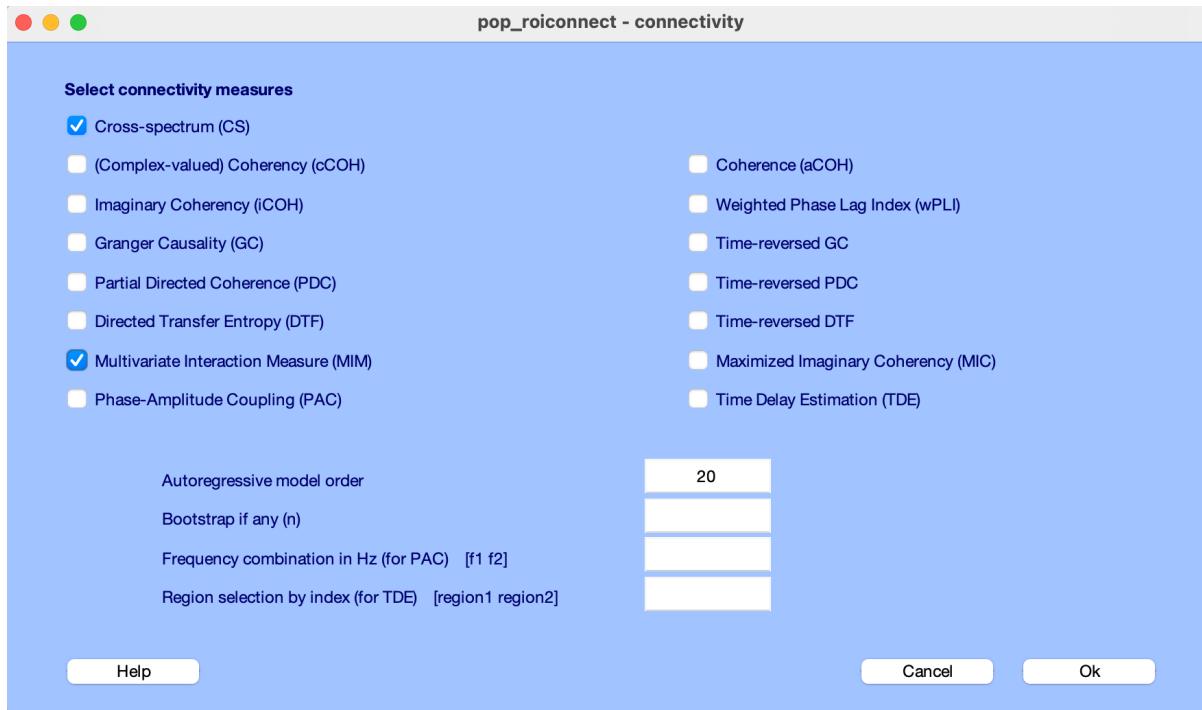
Exercise

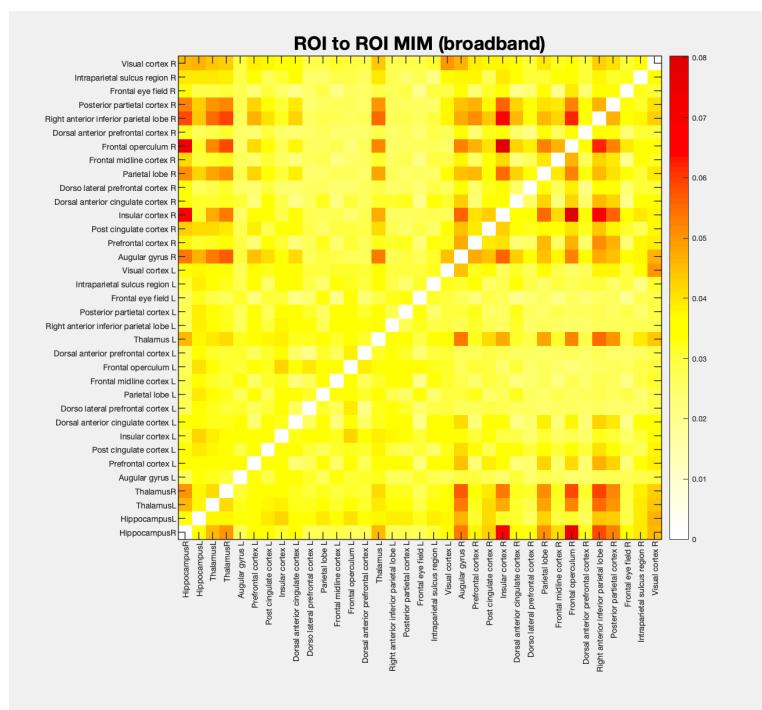
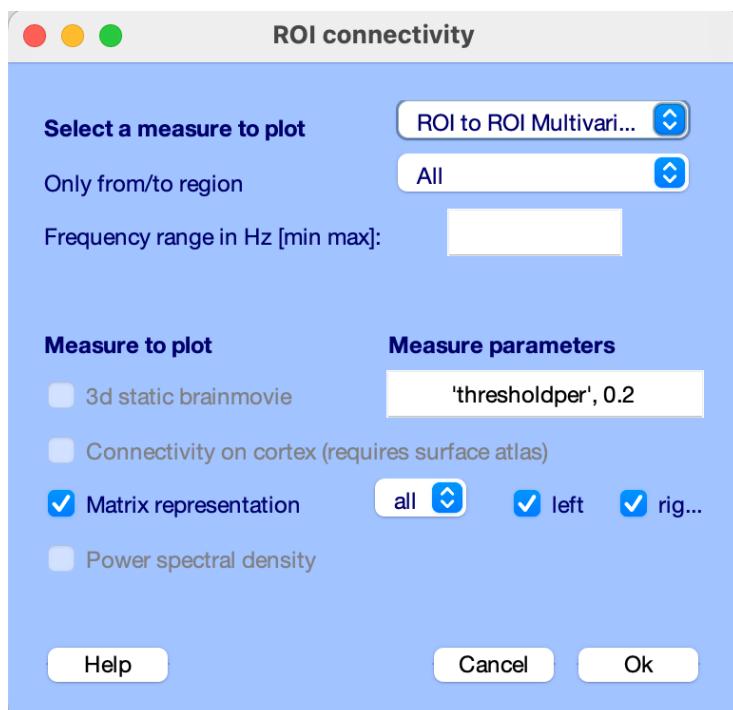
Load .set file using menu item *File > Load existing dataset*
‘ds000117_pruned/derivatives/meg_derivatives/sub-01/ses-meg/meg/wh_S01_run_01_preprocessing_data_session_1_out.set’





Compute ROI activity
Compute ROI connectivity
Plot ROI connectivity





Exercise

- ▶ Compute leadfield
- ▶ Compute ROI activity
- ▶ Compute ROI connectivity
- ▶ Plot ROI connectivity

The end/La fin

