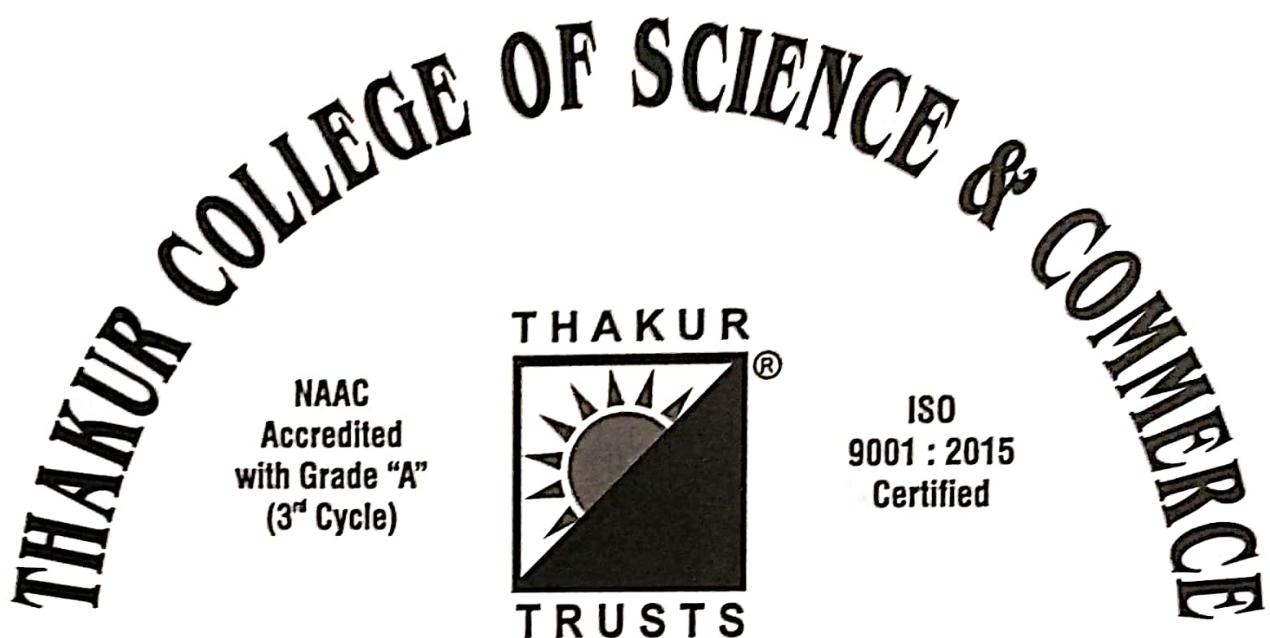


PERFORMANCE

Term	Remarks	Staff Member's Signature
I	Complete	A-V
II	Complete	A-V



Degree College
Computer Journal
CERTIFICATE

SEMESTER II UID No. _____

Class Fy BSc CS Roll No. 1709 Year 2019-20

This is to certify that the work entered in this journal
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who has worked for the year 2019-20 in the Computer
Laboratory.

A-Alwe

Teacher In-Charge

Head of Department

Date : 27.02.20

Examiner

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PRACTICAL - 1

Topic: Basics of R Software

- R is a software for statistical analysis and data computing.
- It is an effective data handling software and outcome storage is possible.
- It is capable of graphical display.
- Its a free software

1. Solve the following

$$1. \quad 4+6+8 \div 2-5$$

$$> 4+6+8/2-5$$

[1] 9

$$2. \quad 2^2 + |-3| + \sqrt{45}$$

$$> 2^2 + \text{abs}(-3) + \text{sqrt}(45)$$

[1] 13.7082

$$3. \quad 5^3 + 7 \times 5 \times 8 + 46 \div 5$$

$$> 5^3 + 7 * 5 * 8 + 46 / 5$$

[1] 414.2

$$4. \quad \sqrt{4^2 + 5 \times 3 + 7} \div 6$$

$$> \sqrt{4^2 + 5 * 3 + 7} / 6$$

[1] 5.671567

28

5. round off

$$46 \div 7 + 9 \times 8$$

> round (46/7 + 9*8)

[1] 79

Q.2.

1. >c(2,3,5,7)*2

[1] 4 6 10 14

2. >c(2,3,5,7)*c(2,3)

[1] 4, 9, 10, 21

3. >c(2,3,5,7)*c(2,3,6,2)

[1] 4 9 30 14

4. >c(1,6,2,3)*c(-2,-3,-4,-1)

[1] -2 -18 -8 3

5. >c(2,3,5,7)^2

[1] 4 9 25 49

6. >c(4,6,8,9,4,5)^1c(1,2,3)

[1] 4 36 512 9 16 125

7. >c(6,2,7,5)/c(4,5)

[1] 1.50 0.40 1.75 1.00

Q.3.

$$x = 20$$

$$y = 30$$

$$z = 2$$

" $x^2 + y^3 + z$
 > $x^12 + y^13 + z$
 [1] 27402

2. $\sqrt{x^2 + y}$
 > sqrt($x^12 + y$)
 [1] 20.73644

3. $x^12 + y^12$
 [1] 1300

Q.4.

```
>x<-matrix(nrow=4, ncol=2, data=c(1,2,3,4,5,6,7,8))
   [,1] [,2]
[1,]    1    5
[2,]    2    6
[3,]    3    7
[4,]    4    8
```

85

Q.5- Find $x+y$, $2x+3y$

$$x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix} \quad y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

> $x = \text{matrix}(nrow=3, ncol=3, data=c(4, 7, 9, -2, 0, -5, 6, 7, 3))$

> $y = \text{matrix}(nrow=3, ncol=3, data=c(10, 12, 15, -5, -4, -6, 7, 9, 5))$

> $x+y$

$$\begin{bmatrix} [1,] & 14 & -7 & 13 \\ [2,] & 19 & -4 & 16 \\ [3,] & 24 & -11 & 8 \end{bmatrix}$$

> $2x+3y$

$$\begin{bmatrix} [1,] & 38 & -19 & 33 \\ [2,] & 50 & -12 & 41 \\ [3,] & 63 & -28 & 21 \end{bmatrix}$$

c6 Marks of statistic of cs student

59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40,
50, 32, 36, 29, 35, 39

> $x = c(59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58,$
 $54, 40, 50, 32, 36, 29, 35, 39)$

> length(x)

[1] 20

> breaks = seq(20, 60, 5)

> a = cut(x, breaks, right = FALSE)

> b = table(a)

> c = transform(b)

> c

		Freq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

A
✓
25/11

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39

40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59

PRACTICAL - 2

Topic : Probability Distribution

Q.1 Check whether the following are p.m.f or not

x	$P(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

Since $P(2) = -0.5$, it cannot be a p.m.f
as in p.m.f $P(x) \geq 0 \forall x$

Q2	x	1	2	3	4	5
	$P(x)$	0.2	0.2	0.3	0.2	0.2

It cannot be a p.m.f. As in p.m.f
 $\sum P(x) = 1$

Q.3	x	10	20	30	40	50
	$P(x)$	0.2	0.2	0.35	0.15	0.1

Code:

```
> pprob=c(0.2, 0.2, 0.35, 0.15, 0.1)
> sum(pprob)
[1] 1
```

Q.2
i. find c.d.f for the following p.m.f and sketch the graph

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

$$F(x) = 0 \quad x < 10$$

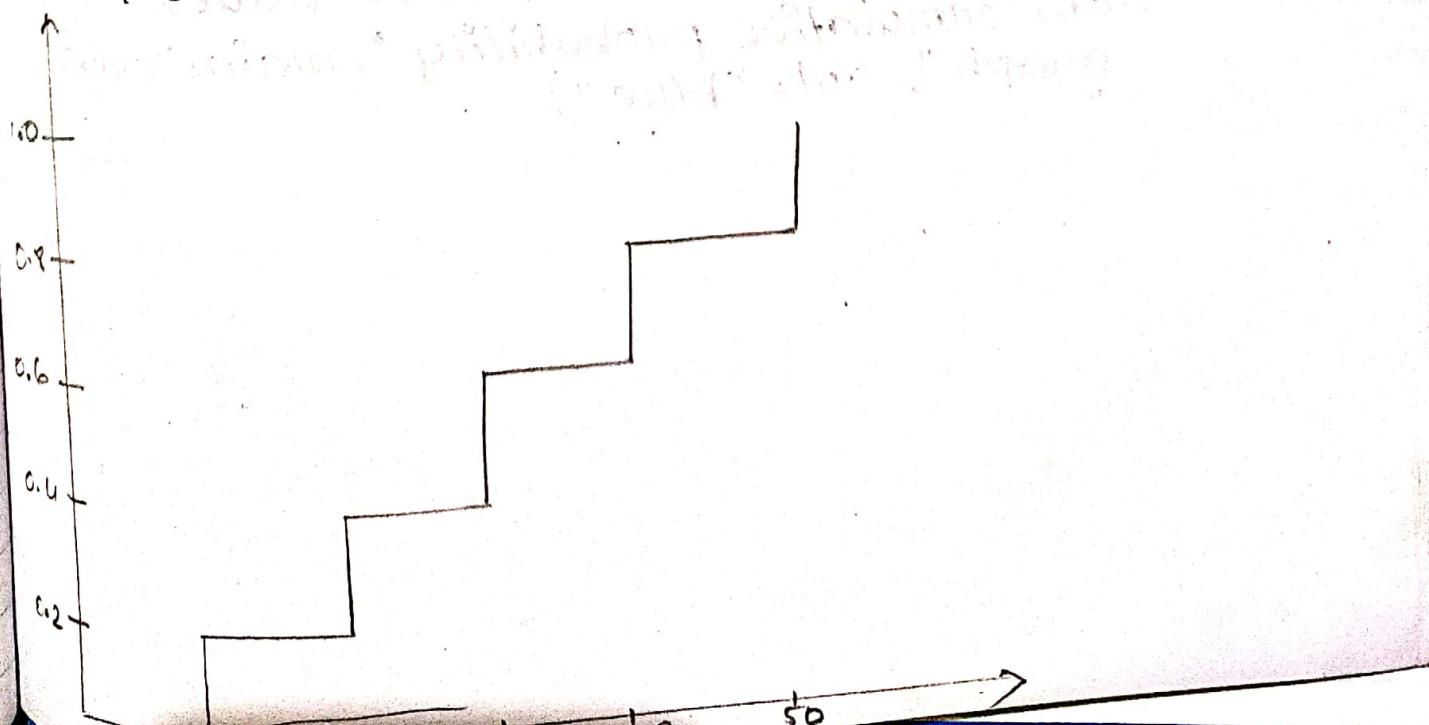
$$0.2 \quad 10 \leq x < 20$$

$$0.4 \quad 20 \leq x < 30$$

$$0.75 \quad 30 \leq x < 40$$

$$0.95 \quad 40 \leq x < 50$$

$$1.0 \quad x \geq 50$$



868

प्र०.	X	1	2	3	4	5	6
	P(X)	0.15	0.25	0.1	0.2	0.2	0.1

$$\begin{aligned}F(x) &= 0 & x < 1 \\&= 0.15 & 1 \leq x < 2 \\&= 0.25 & 2 \leq x < 3 \\&= 0.1 & 3 \leq x < 4 \\&= 0.2 & 4 \leq x < 5 \\&= 0.2 & 5 \leq x < 6 \\&= 0.1 & x \geq 6\end{aligned}$$

> prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

> sum(prob)

[1] 1

> cumsum(prob)

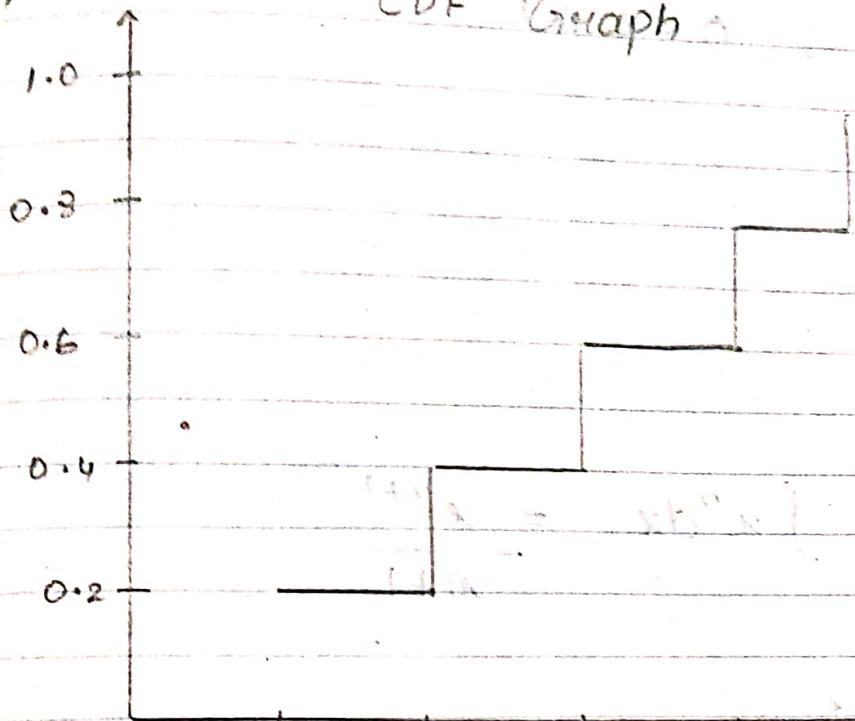
[1] 0.15 0.40 0.50 0.70 0.90 1.00

> x = c(1, 2, 3, 4, 5, 6)

> plot(x, cumsum(prob), "s", xlab = "values",
ylab = "cumulative probability", main = "c.d.f
graph", col = "blue")

cumulative Frequency

CDF Graph



Q3 Check whether the following is p.d.f or not

$$i) f(x) = 3 - 2x ; \quad 0 \leq x \leq 1$$

$$\int_0^1 f(x) dx$$

$$= \int_0^1 (3 - 2x) dx$$

$$= \int_0^1 3dx - \int_0^1 2x dx$$

$$= [3x - x^2]_0^1$$

$$= 2$$

$$99 \quad f(x) = 3x^2 ; \quad 0 < x < 1$$

$$\int_0^1 f(x)$$

$$= \int_0^1 3x^2$$

$$= 3 \int_0^1 x^2$$

$$= \left[\frac{3x^3}{3} \right]_0^1 \quad \int x^n dx = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

to = 1 to 1 big A - problems! 3rd problem

PRACTICAL - 3

BN

Topic: Binomial Distribution

$$i. P(X=x) = dbinom(x, n, p)$$

$$ii. P(X \leq x) = pbinom(x, n, p)$$

$$iii. P(X > x) = 1 - pbinom(x, n, p)$$

$$iv. If x is unknown and P_i is given as \\ P(X \leq x) = qbinom(P_i, n, p)$$

- Q.1 Find the probability of exactly 10 success in 100 trials with $p=0.1$
- Q.2 Suppose there are 12 mcqs. Each question has 5 options out of which one is correct. Find the probability of having i. Exactly 4 correct answers ii. Atmost 4 correct answers iii. More than 5 correct answers $P=1/5$
- Q.3 Find the complete distribution when $n=5, p=0.1$
- Q.4. $n=12, p=0.25$. Find the following probabilities
 i. $P(X=5)$ ii. $P(X \leq 5)$ iii. $P(X \geq 7)$ iv. $P(5 \leq X \leq 7)$
- Q.5. A probability of a salesman making a sale to a customer is 0.15. Find the probability of i. No sells out of 10 customers ii. More than 3 sales out of 20 customers
- Q.6. A salesman has a 20% probability of making a sale to a customer out of 30 customers minimum number of sales he can make with 88% probability.

Q.7.

X follows binomial distribution with $n=10$, $p=0.2$.
plot the graph of p.m.f. and c.d.f.

(0, 0.0) starting from

(0, 0.0) and going to

(0, 0.0) ending at

in step of 1.0 but ending at 1.0

(0, 0.0) ending at 1.0

distribution of number of failures to paddocks with the

average 2 and variance 0.8. If 0.8 off target
to paddocks will fail, whereas if 0.8 fails to
failures is treated as success. Assume a pistol is given

20 successive frames & with each 0.8 failure

0.8 random failure. Find the probability of

a 0.8 failure pistol after 10 shots. $P(X=0.8)$

is random error (excess) (excess) to 0.8

on shot. It is also unacceptable in the paddocks

as paddocks will fail. $P(X \geq 0.8)$ to actual

value & make small amount of 0.8 for the

failure to paddocks. 0.8 is random error

and random error of 0.8 has mean 0.8 & standard deviation 0.8

probability of 0.8 failure to paddocks is 0.8

and random error of 0.8 has mean 0.8 & standard deviation 0.8

Answers

(5-8 Q&A 66-67) working

- Q.1
 $\text{>} \text{dbinom}(10, 100, 0.1)$
 [1] 0.1318653
- Q.2
 $\text{>} \text{dbinom}(4, 12, 0.2)$
 [1] 0.1328756
 $\text{>} \text{pbinom}(4, 12, 0.2)$
 [1] 0.9274445
 $\text{>} 1 - \text{pbinom}(5, 12, 0.2)$
 [1] 0.01940528
- Q.3
 $\text{>} \text{dbinom}(0:5, 5, 0.1)$
 [1] 0.59049 0.32805 0.07290 0.00816 0.00045 0.00000
- Q.4
 $\text{>} \text{dbinom}(5, 12, 0.25)$
 [1] 0.1032414
 $\text{>} \text{pbinom}(5, 12, 0.25)$
 [1] 0.9455978
 $\text{>} 1 - \text{pbinom}(7, 12, 0.25)$
 [1] 0.00278151
 $\text{>} \text{dbinom}(6, 12, 0.25)$
 [1] 0.04014945
- Q.5
 $\text{>} \text{dbinom}(10, 10, 0.15)$
 [1] 0.1968744
 $\text{>} 1 - \text{pbinom}(3, 20, 0.15)$
 [1] 0.3522748

10

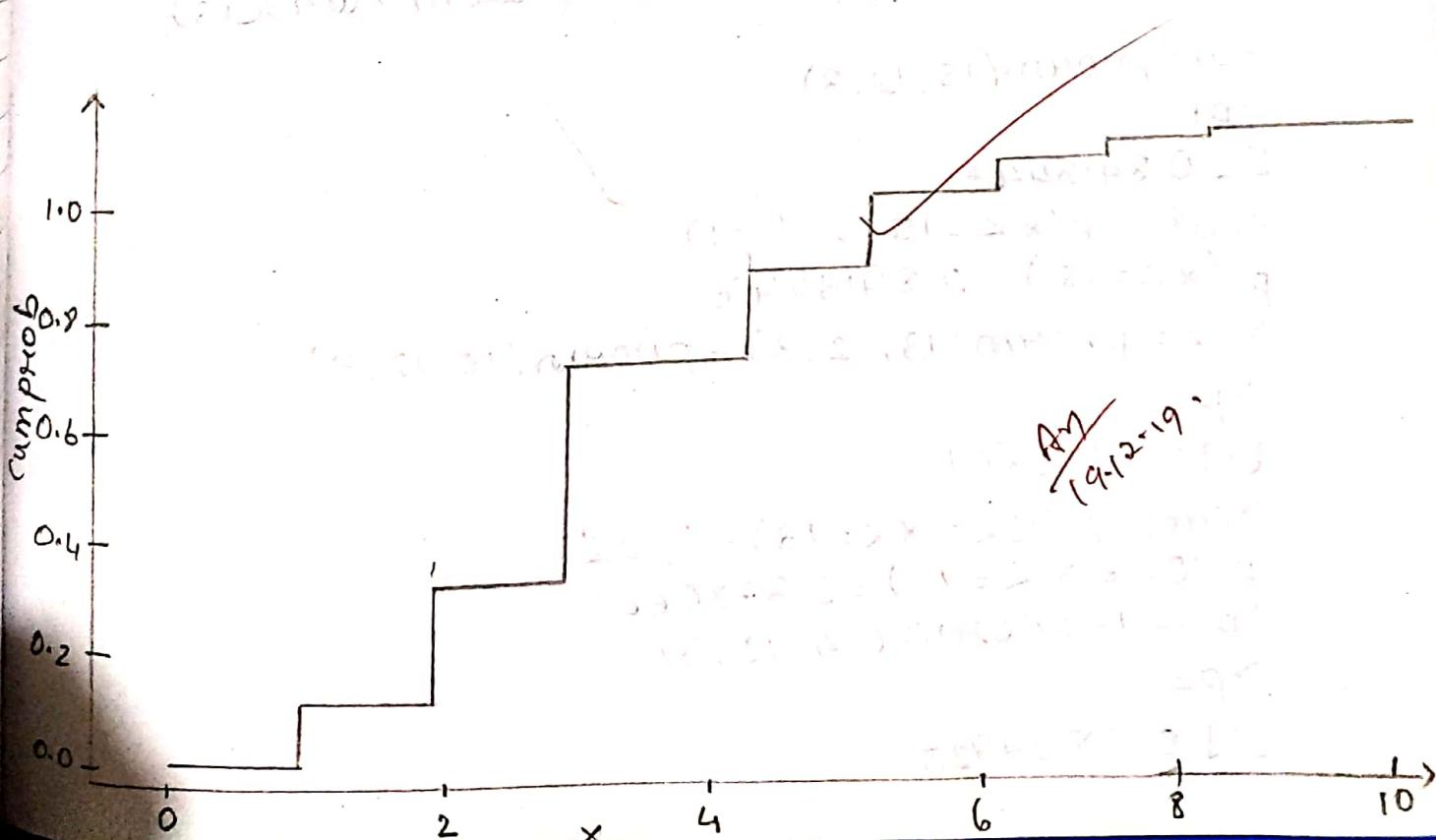
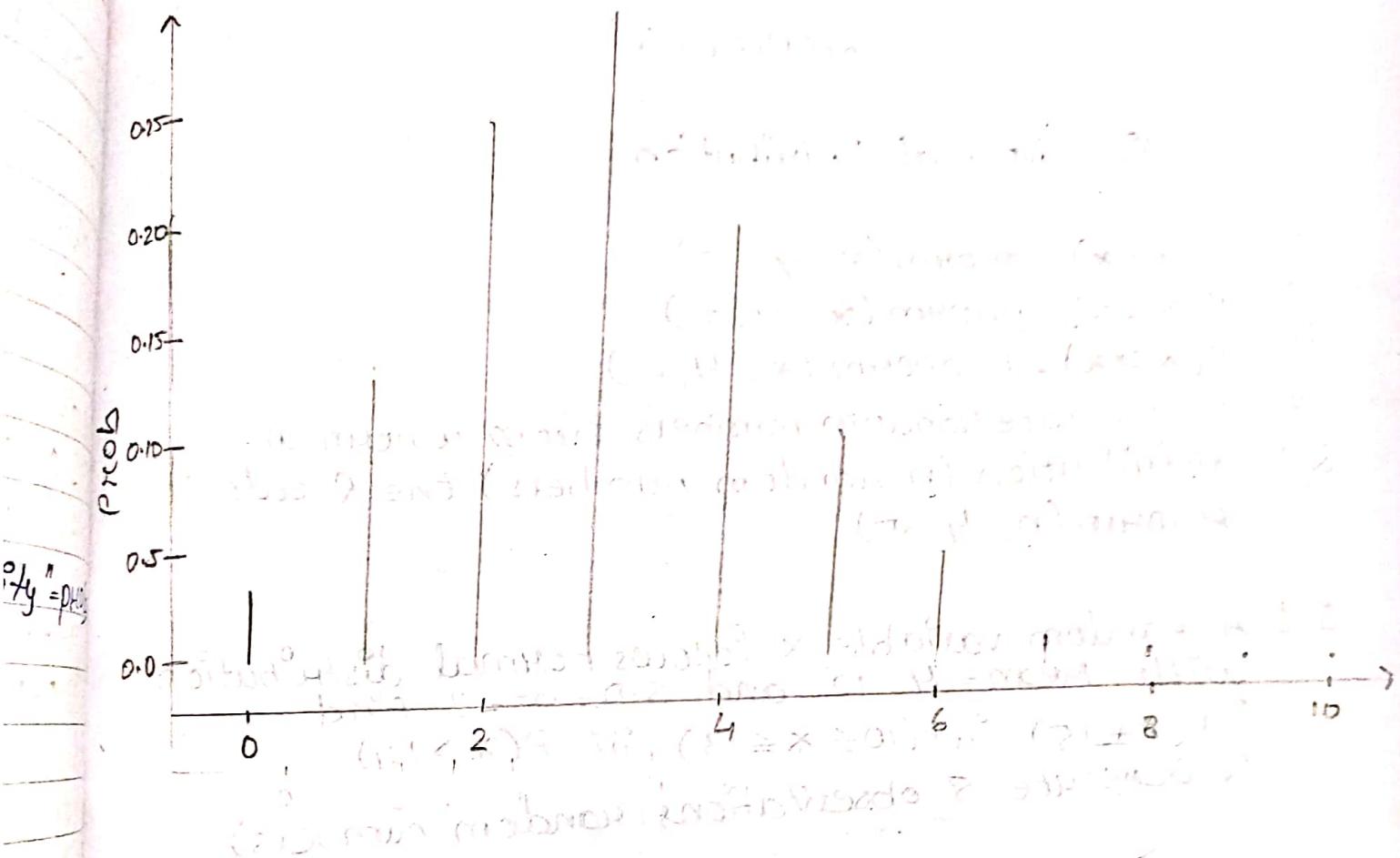
Q.6

```
> qbinom(0.88, 30, 0.2)  
[1] 9
```

Q.7

```
> n = 10  
> p = 0.3  
> x = 0:n  
> prob = dbinom(x, n, p)  
> cumprob = pbisnom(x, n, p)  
> d = data.frame("xvalues"=x, "probability"=prob)  
> print(d)
```

	xvalues	probability
1	0	0.0282
2	1	0.1210
3	2	0.2334
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.0367
8	7	0.0090
9	8	0.0014
10	9	0.0001
11	10	0.0000



PRACTICAL - 4

Aim : Normal Distribution

- i. $P(x = x) = \text{dnorm}(x, \mu, \sigma)$
- ii. $P(x \leq x) = \text{pnorm}(x, \mu, \sigma)$
- iii. $P(x > x) = 1 - \text{pnorm}(x, \mu, \sigma)$
- iv. To generate random numbers from a normal distribution (n random numbers) the R code is $\text{rnorm}(n, \mu, \sigma)$

- Q.1 A random variable x follows normal distribution with Mean = $\mu = 12$ and S.D = $\sigma = 3$. Find
- i. $P(x \leq 15)$
 - ii. $P(10 \leq x \leq 13)$
 - iii. $P(x > 14)$
 - iv. Generate 5 observations (random numbers)

```
>p1 = pnorm(15, 12, 3)
>p1
[1] 0.8413447
>cat("P(x <= 15) = ", p1)
P(x <= 15) = 0.8413447
>p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)
>p2
[1] 0.3780661
>cat("P(10 <= x <= 13) = ", p2)
P(10 <= x <= 13) = 0.3780661
>p3 = 1 - pnorm(14, 12, 3)
>p3
[1] 0.2524925
```

> cat("p(x > 14) = ", p3)

$$p(x > 14) = 0.2524925$$

> p4 = rnorm(5, 12, 3)

> p4

[1] 15.254723 16.548505 11.280515 6.419944 12.272460

Q2 X follows normal distribution with $\mu = 10, \sigma = 2$
Find i. $P(X \leq 7)$ ii. $P(5 < X < 12)$ iii. $P(X > 12)$

iv. Generate 10 observations v. Find k such that
 $P(X < k) = 0.4$

> a1 = pnorm(7, 10, 2)

> a1

[1] 0.0668072

> a2 = pnorm(5, 10, 2) - pnorm(12, 10, 2)

> a2

[1] -0.8351351

> a3 = 1 - pnorm(12, 10, 2)

> a3

[1] 0.1586553

> a4 = rnorm(10, 10, 2)

> a4

[1] 11.608931 9.920417 12.637741 8.073354

8.721380 9.193726 9.366824 11.707106

9.537584 10.715006

> a5 = qnorm(0.4, 10, 2)

> a5

[1] 9.493306

Q.3 Generate 5 random numbers from a normal distribution $\mu = 15, \sigma = 4$
 Find Sample Mean, median, S.D and print it.

> x <- rnorm(5, 15, 4)

[1] 10.7649 7.793249 9.953444 13.345904
 17.509668

> am <- mean(x)

> am

[1] 11.87345

> cat("Sample mean is = ", am)

Sample mean is = 11.87345

> me <- median(x)

> me

[1] 10.76499

> cat("Median is = ", me)

Median is = 10.76499

> n <- 5

> v <- (n - 1) * var(x) / n

> v

[1] 11.09965

> cat(

> sd <- sqrt(v)

> sd

[1] 3.331613

> cat(" S.D is = ", sd)

S.D is = 3.331613

Q.4 $x \sim N(80, 100)$, $\sigma = 10$

i. $P(X \leq 40)$

ii. $P(X > 35)$

iii. $P(25 < X < 35)$

iv. Find k such that $P(X < k) = 0.6$

> f1 = pnorm(40, 30, 10)

> f1

[1] 0.8413447

> f2 = 1 - pnorm(35, 30, 10)

> f2

[1] 0.3085375

> f3 = pnorm(25, 30, 10) - pnorm(35, 30, 10)

> f3

[1] -0.3829249

> f4 = qnorm(0.6, 30, 10)

> f4

[1] 32.53347

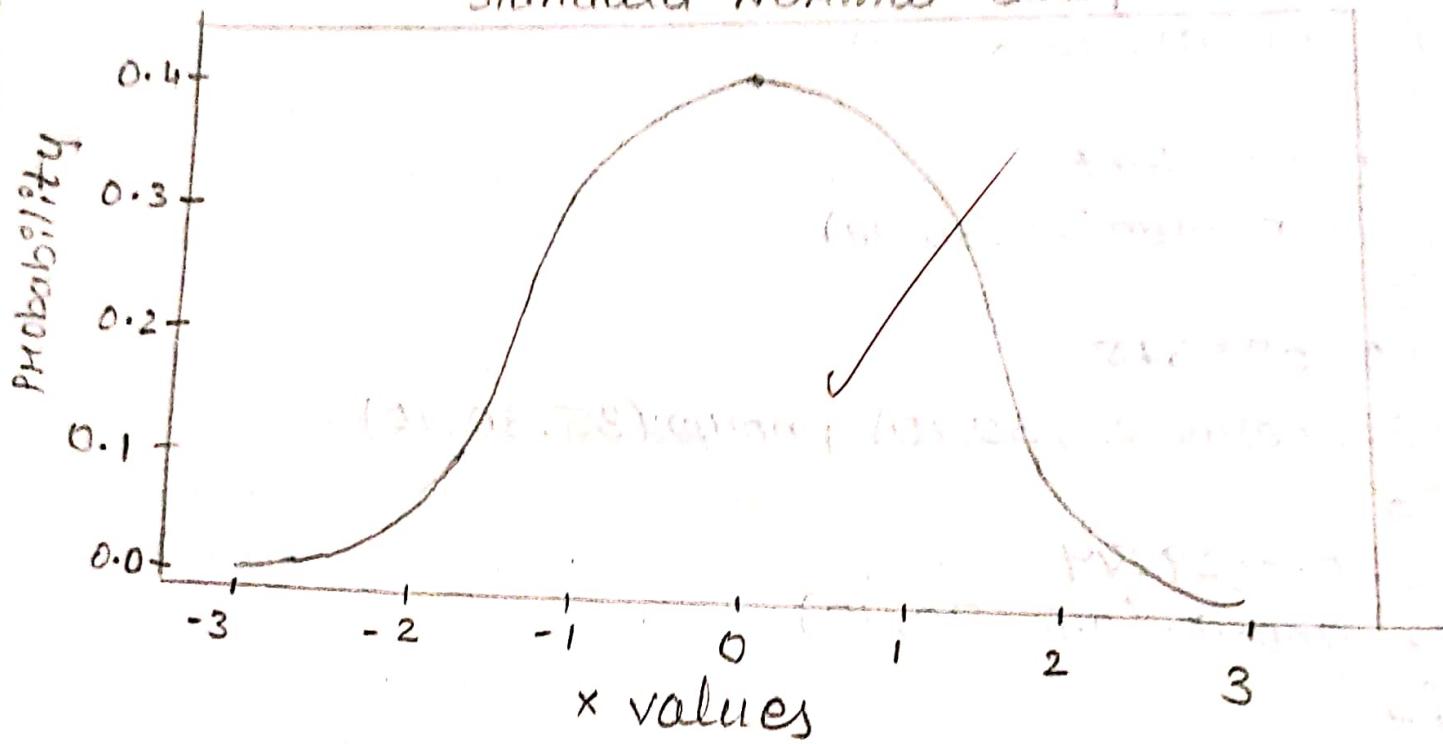
Q.5 Plot the standard normal graph

> x = seq(-3, 3, by = 0.1)

> y = dnorm(x)

> plot(x, y, xlab = "x values", ylab = "probability",
main = "standard normal graph")

Standard Normal Graph



~~2.1.2~~

PRACTICAL - 5

Aim: Normal and t-test

Test the hypothesis $H_0: \mu = 15$, $H_1: \mu \neq 15$
 Random sample of size 400 is drawn and it
 is calculated. Sample mean is 14 and s.d is 3
 Test the hypothesis at 5% level of significance.

> $m_0 = 15$

> $m_x = 14$

> $s_d = 3$

> $n = 400$

> $z_{cal} = (m_x - m_0) / (s_d / (\sqrt{n}))$

> z_{cal}

[1] -6.666667

> cat("calculated value of z is ", "zcal")

calculated value of z is -6.666667

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 2.616796e-11

since pvalue is less than 0.05 we reject

$H_0: \mu = 15$

Test the hypothesis $H_0: \mu = 10$, $H_1: \mu \neq 10$

Random sample of size 400 is drawn and
 its sample mean is 10.2 and s.d is 2.25. Test
 the hypothesis at 5% level of significance

```

> mo = 10
> mx = 10.2
> sd = 2.25
> n = 400
> zcal = (mx - mo) / (sd / sqrt(n))
> zcal
[1] 1.077778
> cat("calculated value of z is = ", zcal)
calculated value of z is = 1.077778
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.07544036

```

since pvalue is more than 0.05 we accept $H_0: \mu = 10$

Q.3. Test the hypothesis $H_0: \text{proportion of smokers in a college is } 0.2$. A sample is collected and it is calculated as 0.125. Test the hypothesis at 5% level of significance (sample size is 400).

```

> P = 0.2
> p = 0.125
> n = 400
> Q = 1 - P
> zcal = (p - P) / (sqrt((P * Q) / n))
> zcal
[1] -4.74

```

>pvalue = 2 * (1 - pnorm(abs(zcal)))

>pvalue

[1] 0.001768346

- Q. Last year Farmer's lost 20% of their crop. Random sample of 60 field are collected and it is found that a field of crops is insect polluted. Test the hypothesis of 1% level of significance.

>p = 0.2

>p = 9/60

>n = 60

>Q = 1 - P

>zcal = $(p - P) / \sqrt{P * Q / n}$

>zcal

[1] -0.96842458

>pvalue = 2 * (1 - pnorm(abs(zcal)))

>pvalue

[1] 0.3329216

- Q. Test the hypothesis $H_0: \mu = 12.5$ from the following sample of 5% level of significance

>x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)

>n = length(x)

>n

[1] 10

>mx = mean(x)

>v = (n-1) * var(x) / n

>s d = sqrt(v)

83:

```
> sd  
[1] 0.1397176  
> m0 = 12.5  
> t = (mx - m0) / (sd / sqrt(n))  
> t  
[1] -8.894909  
> pvalue = 2 * (1 - pnorm (abs(t)))  
> pvalue  
[1] 0
```



Probability of getting 3 or more heads in a row from 10 coin tosses is 0.0000000000000002.

P(roll a spout, 8 or 9, 18-21, 30-31, 61-62, 69-70, 71-72, 81-82, 91-92, 93-94, 95-96, 97-98, 99-100) = 0.0000000000000002

PRACTICAL - 6

Aim: Large sample test

Q1 Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers selected. The sample mean is calculated as 275 and S.D is 30. Test the hypothesis that the population mean is 250 or not at 5% level of significance.

Q2 In a random sample of 1000 students. It is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.8 at 1% of level of significance.

> $m_x = 275$

> $m_0 = 250$

> $n = 100$

> $s_d = .30$

> $z_{cal} = (m_x - m_0) / (s_d / (\sqrt{n}))$

> z_{cal} [1] 8.333333

> $pvalue = 2 * (1 - pnorm(abs(z_{cal})))$

> $pvalue$

[1] 0

Q2

> $P = 0.8$

> $Q = 1 - P$

> $n = 1000$

> $p = 750/1000$

$$>zcal = (p - P) / (\text{sqrt}(P * Q / n))$$

>zcal

[1] -3.952847

$$>pvalue = 2 * (1 - pnorm(\text{abs}(zcal)))$$

>pvalue

[1] 7.72268e-05

since value < 0.05 we reject H_0 at 5% level of significance

- Q.3 Two random sample of size 1000 and 2000 are drawn from two populations with same S.D 2.5. The sample means are 67.5 and 68 respectively. Test the hypothesis $H_0: \mu_1 = \mu_2$ vs $H_1: \mu_1 \neq \mu_2$ at 5% level of significance

- Q.4. A study of noise level in 2 hospital is given below. Test the claim that the hospitals have same level of noise at 1% level of significance

	Hospital A	Hospital B
Size	84	34
mean	61.2	59.4
S.D	7.9	7.85

- Q.5. In a sample of 600 students in a college, 400 use blue ink in another college from a sample of 900 students 450 use blue ink. Test the hypothesis that the proportion

of students using blue pink in two colleges are equal or not at 1% level of significance

```

> n1 = 1000
> n2 = 2000
> mx1 = 67.5
> mx2 = 68
> sd1 = 2.5
> sd2 = 2.5
> zcal = (mx1 - mx2) / sqrt((sd1^2/n1) + (sd2^2/n2))
> zcal
[1] -5.163978
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 2.417564e-07

```

```

> n1 = 84
> n2 = 34
> mx1 = 61.2
> mx2 = 59.4
> sd1 = 7.9
> sd2 = 87.5
> zcal = (mx1 - mx2) / sqrt((sd1^2/n1) + (sd2^2/n2))
> zcal
[1] 1.162528
> cat("calculated value of z is ", zcal)
calculated value of z is 1.162528
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.2450211

```

Qa.

```
> 0.5  
> n1 = 600  
> n2 = 900  
> p1 = 400 / 600  
> p2 = 450 / 900  
> p = (n1 * p1 + n2 * p2) / (n1 + n2)  
> q = 1 - p  
> p  
[1] 0.5666667  
> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))  
> zcal  
[1] 6.381534  
> pvalue = 2 * (1 - pnorm(abs(zcal)))  
> pvalue  
[1] 1.753222e-10
```

Q.6

~~n1 = 200, n2 = 200, p1 = 44/200, p2 = 30/200~~

~~> n1 = 200~~

~~> n2 = 200~~

~~> p1 = 44/200~~

~~> p2 = 30/200~~

~~> p = (n1 * p1 + n2 * p2) / (n1 + n2)~~

~~> q = 1 - p~~

~~> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))~~

~~> pvalue = 2 * (1 - pnorm(abs(zcal)))~~

~~> pvalue~~

[1] 0.0714288

> zcal

[1] 1.802741

\therefore value $> 0.05 \Rightarrow$ mean is accepted.

PRACTICAL-7

Aim: Small sample test

The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from population with the average 66.

$$H_0: \mu = 66$$

t-test(x)

One Sample t-test

data: x

t = 68.319, df = 9, p-value = 1.558e-13

alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:

65.65171 70.14829

sample estimates:

mean of x

67.9

\because value < 0.05 , mean is rejected.

>pvalue = 1.558e-13

>if(pvalue > 0.05) (cat("accept no")) else (cat("reject no"))

reject no

2. 2 groups of students score the following marks. Test the hypothesis that there is no significant difference between the two groups.

Group 1 - 18, 22, 21, 17, 20, 17, 23, 20, 22, 21

Group 2 - 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H_0 : There is no difference between two groups.

```
> x=c(18,22,21,17,20,17,23,20,22,21)
```

```
> y=c(16,20,14,21,20,18,13,15,17,21)
```

```
> t.test(x,y)
```

Welch Two Sample t-test

data: x and y

$t = 2.2573$, $df = 16.376$, $p\text{-value} = 0.03798$

alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:

0.1628205 5.0371795

sample estimates:

mean of x mean of y

20.1 17.5

```
> if(0.03798 > 0.05) (cat("accept no")) else(cat("reject no"))
```

reject no

The sales data of six shops before and after a campaign is given below:

Before : 53, 28, 31, 48, 50, 42

After : 58, 29, 30, 55, 56, 45

Test the hypothesis that the campaign is effective or

* not. H_0 : There is no significant difference of sales before and after the campaign.

$x = c(53, 28, 31, 48, 50, 42)$

$y = c(58, 29, 30, 55, 56, 45)$

$t\text{-test}(x, y, \text{paired} = \text{T}, \text{alternative} = \text{"greater"})$

~~Welch Two~~

Paired t-test

data: x, y

$t = -2.7815, df = 5, p\text{-value} = 0.9806$

alternative hypothesis: true difference in means is greater than 0

95 percent confidence interval:

-6.035547

Inf

Sample estimates:

mean of the differences

-3.5

```
> if(0.9806 > 0.05) (cat("accept no")) else(cat("reject no"))
```

~~accept~~ accept no.

- Ques
4. Two medicines are applied to two groups of patient respectively

Group1 - 10, 12, 13, 11, 14

Group2 - 8, 9, 12, 14, 15, 10, 9.

Is there any significant difference between two medicines. H_0 : There is no significant difference

> $x = c(10, 12, 13, 11, 14)$

> $y = c(8, 9, 12, 14, 15, 10, 9)$

> t.test(x, y)

Welch Two Sample t-test

data: x and y

$t = 0.80384$, $df = 9.7594$, $p\text{-value} = 0.4406$

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval:

-1.781171 3.781171

sample estimates:

mean of x mean of y

12

11

```
> if (0.4406 > 0.05) (cat("accept no")) else (cat("reject no"))
accept no.
```

Groups

The following are the weight before & after the diet program. Is the program effective
 before : 120, 125, 115, 130, 123, 119
 after : 100, 114, 95, 90, 115, 99

H_0 : There is no significant difference

> $x = c(120, 125, 115, 130, 123, 119)$

> $y = c(100, 114, 95, 90, 115, 99)$

> $t.test(x, y, paired = T, alternative = "less")$

Paired t-test

data: x and y

$t = 4.3458$, $df = 5$, p-value = 0.9963

alternative hypothesis: true difference in means
 is less than 0

95 percent confidence interval:

-Inf 29.0298

Sample estimate:

mean of the differences

19.83333

```
>if(0.9963 > 0.05) (cat("accept no"))(else (cat(  
  "reject no"))  
accept no
```

AM
V
Z
b'

Answers

Q1 $H_0 = 55$

> $m_0 = 55$

> $m_x = 52$

> $n = 100$

> $sd = 7$

> $z_{\text{cal}} = (m_x - m_0) / (sd / (\sqrt{n}))$

> z_{cal}

[1] -4.285714

> $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

> $p\text{value}$

[1] 1.82153e-05

$\because p\text{value} < 0.05$ we reject H_0

Q2 $H_0 = \mu = 1/2$

> $n_1 = 350$

> $n_2 = 700$

> $p = 350/700$

> $P = 0.5$

> $Q = 1 - P$

> $z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$

> z_{cal}

[1] 0

> $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

> $p\text{value}$

[1] 1

$\because p\text{value} > 0.05$ we accept H_0

55

Q.3 $H_0 = P_2$

> n1 = 1000

> n2 = 1500

> p1 = 20/1000

> p2 = 15/1500

> p = $(n1 * p1 + n2 * p2) / (n1 + n2)$

> q = 1 - p

> p

[1] 0.014

> zcal = $(p1 - p2) / \sqrt{p * q * (1/n1 + 1/n2)}$

> zcal

[1] 2.081283

> pvalue = $2 * (1 - pnorm(\text{abs}(zcal)))$

> pvalue

[1] 0.03740801

Q.4 $\because pvalue < 0.05$ we reject H_0

$H_0 = 100$

> mx = 99

> m0 = 100

> n = 400

> sd = 8

> zcal = $(mx - m0) / (sd / \sqrt{n})$

> zcal

[1] -2.05

> pvalue = $2 * (1 - pnorm(\text{abs}(zcal)))$

> pvalue

[1] 0.01241933

$\therefore pvalue < 0.05$ we reject H_0

Q5 $H_0: \mu = 66$
 > $x = c(63, 63, 68, 69, 71, 71, 72)$
 > t.test(x)

One Sample t-test

data: x

t = 47.94, df = 6, p-value = 5.522e-09

alternative hypothesis: true mean is not equal to 0.

95 percent confidence interval:

64.66479 71.62092

sample estimates:

mean of x

68.14286

∴ pvalue < 0.05 we reject H_0

Q7 $H_0 = 1200$

> m0 = 1200

> mx = 1150

> sd = 125

> n = 100

> zcal = (mx - m0) / (sd / (sqrt(n)))

> zcal

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 6.334248e-05

∴ pvalue < 0.05 we reject H_0

Q.6.

```
> x=c(66, 67, 75, 76, 82, 84, 88, 90, 92)
> y=c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)
> var.test(x, y)
```

F test to compare two variances

data: x and y

$F = 0.70686$, num df = 8, denom df = 10, p-value = 0.6359
alternative hypothesis: true ratio of variances
is not equal to 1

95 percent confidence interval:

0.1833662 3.0360393

sample estimates:

ratio of variances

0.7068567

\therefore pvalue > 0.05 we accept H_0

Q.8

 $H_0 = P_1 \neq P_2$
 $> n_1 = 200$
 $> n_2 = 300$
 $> p_1 = 44/200$
 $> p_2 = 56/300$
 $> p(n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$
 $> q = 1 - p$
 $> p$
 $[1] 0.2$
 $> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

[1] 0.9128709

>pvalue = 2*(1-pnorm(abs(zcal)))

[1] 0.3613104

$\therefore pvalue > 0.05$ we accept H_0

~~$p < 0.05$~~

small ~~alternative~~

plot?

ggplot?

ggplot?

ggplot?

ggplot?

5. Implement K-means and add to mllib API
function part

(2) (2, 10, 18, 0, 0) 2000

2000

2000

(4) (20, 0, 0, 0, 0) 2000

2000

2000

2000 2000

2000 2000

2000 2000

2000 2000

2000 2000

2000 2000

PRACTICAL - 9

Topic: Chi square tests & ANOVA

- Q.1 Use the following data to test whether the condition of the home and the condition of the child is independent or not.

		condition of home	
		Clean	Dirty
Condition of child	Clean	70	50
	Fairly clean	80	20
	Dirty	35	45

H_0 : condition of the home and child is independent

```

>x=c(70,80,35,50,20,45)
>m=3
>n=2
>y=matrix(x,nrow=m,ncol=n)
>y

```

	[,1]	[,2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

> $pV = \text{chisq.test}(y)$
 > pV

Person's Chi-squared test:

data: y

χ^2 -squared = 25.646, df = 2, p-value = 2.698e-06

$\therefore pV < 0.05$ we reject H_0

Q2 Test hypothesis that vaccination and diseases are independent or not

		Vaccine	
		Affective	Not Affective
Affective	Affective	70	46
	Not Affective	35	37

H_0 : Disease and the vaccine are independent

> $x = c(70, 35, 46, 37)$

> $m = 2$

> $n = 2$

> $y = \text{matrix}(x, nrow = m, ncol = n)$

> y

	[, 1]	[, 2]
[1,]	70	46
[2,]	35	37

```
> pr = chisq.test(y)
> pr
```

Pearson's Chi-squared test with Yates' continuity correction

data: y
 χ^2 -squared = 2.0275, df = 1, p-value = 0.1545

$\therefore pr > 0.05$ we accept H_0

Q3 Perform a ANOVA for the following data

Type	Observation			
A	50	52		
B	53	55	53	
C	60	58	57	56
D	52	54	54	55

H_0 : The means are equal for A, B, C, D

```
> x1 = c(50, 52)
> x2 = c(53, 55, 53)
> x3 = c(60, 58, 57, 56)
> x4 = c(52, 54, 54, 55)
> d = stack(b1 = x1, b2 = x2, b3 = x3, b4 = x4)
> names(d)
[1] "values" "ind"
```

> oneway.test(values ~ ind, data=d, var.equal=T)

One-way analysis of means

data: values and ind

F = 11.735, num df = 3, denom df = 9, p-value = 0.00183

∴ pr < 0.05 we reject H₀

> anova = aov(values ~ ind, data=d).

> summary(anova)

~~anova for multiple groups~~

Df Sum Sq Mean Sq F value Pr(>F)

ind	3	71.06	23.688	11.73	0.00183
-----	---	-------	--------	-------	---------

Residuals 9 18.17

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '1'

Q4 The following data gives the life of the tyre
of four ~~gm~~ brand

Type	Life
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 16

H_0 : The average life of tyres are equal.

```
> x1 = c(20, 23, 18, 17, 18, 22, 24)
> x2 = c(19, 15, 17, 20, 16, 17)
> x3 = c(21, 19, 22, 17, 20)
> x4 = c(15, 14, 16, 18, 14, 16)
> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
> names(d)
[1] "values" "ind"
> oneway.test(values ~ ind, data=d, var.equal=TRUE)
```

One way analysis of means

data: values and ind

$F = 6.8445$, num df = 3, denom df = 20,
p-value = 0.002849

$\therefore p < 0.05$ we reject H_0

Q.5.

```
> x = read.csv("C:/Users/Administrator/Desktop/marks.csv")
```

```
> print(x)
```

```
> am = mean(x$stats)
```

```
> am
```

```
[1] 7
```

```
> me = median(x$stats)
```

```
> me
```

```
[1] 38.5
```

> n = length(x \$ stats)
 > v = (n-1) * var(x \$ stats) / n
 > r
 [1] 160
 > sd = sqrt(v)
 > sd
 [1] 12.64911
 > am1 = mean(x \$ maths)
 > am1
 [1] 39.4
 > med1 = median(x \$ maths)
 > med1
 [1] 37
 > n1 = length(x \$ maths)
 > v1 = (n1-1) * var(x \$ maths) / n1
 > v1
 [1] 231.04
 > sd1 = sqrt(v1)
 > sd1
 [1] 15.2
 > cor(x \$ stats, x \$ maths)
 [1] 0.830618

~~AN
70.02~~

PRACTICAL - 10

Topic: Non-parametric test

- Q.1 Following are the amount of sulphur-oxide emitted by some industry. In 20 days Apply sign test to test the hypothesis that the population median is 21.5 at 5% LOS

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26

H_0 : Population median is 21.5

> $x = c(-\dots-)$

> $m_e = 21.5$

> $sp = \text{length}(x[x > m_e])$

> $sn = \text{length}(x[x < m_e])$

> $n = sp + sn$

> n

[1] 20

> $pv = \text{pbinom}(sp, n, 0.5)$

> pv

[1] 0.4119015

$\therefore pv > 0.05$ we ^{accept} ~~reject~~ H_0

Note: If the alternative (H_1) & ~~H₀~~ is met or $m_e <$ than $pv = \text{pbinom}(sp, n, 0.5)$

If the alternative is $m_e >$ than $pV = pb\text{inom}(sn, n, 0.5)$

Following is the data of 10 observation. Apply sign test. Test the hypothesis that the population median is 625 against the alternative. It is more than 625.

612, 619, 631, 628, 643, 640, 655, 649, 670, 663

$\geq x = c(- \dots)$ $H_0:$ Population median is 625

$m_e = 625$

$sp = \text{length}(x[x > m_e])$

$sn = \text{length}(x[x < m_e])$

$n = sp + sn$

n

[1] 10

$pV = pb\text{inom}(sn, n, 0.5)$

pV

[1] 0.0546875

$\therefore pV > 0.05$ we accept H_0

Following are the values of a sample. Test the hypothesis that the population median is 60 against the alternative it is more than 60 at 5% LOS using Wilcoxon signed Rank test.

63, 65, 60, 89, 61, 71, 88, 81, 69, 62, 63, 39, 72,

69, 48, 66, 72, 63, 87, 69

$H_0:$ Population median = 60

$H_1:$ Population median > 60

> $x = c(\dots)$

> $wilcox.test(x, alter = "greater", mu = 60)$

Wilcoxon signed rank test with continuity correction

data: x

V = 145, p-value = 0.02298

alternative hypothesis: true location is greater than 60

$\therefore p < 0.05$ we reject H_0

Note: If the alternative is less than
 $alter = "less"$

If the alternative is equal to that
 $alter = "two sided"$

Q.4 Using WSR test. Test the population median is 12 or less than 12

15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26

> $x = c(\dots)$

> $wilcox.test(x, alter = "less", mu = 12)$

Wilcoxon signed Rank test with continuity correction

data: x

V = 66, p-value = 0.9986

alternative hypothesis: true location is less than 12

$\therefore p > 0.05$ we accept H_0

Q. The weights of students before or after they stop smoking are given below using WRT test that there is no significant change

Before: 65, 75, 75, 62, 72

After: 72, 74, 72, 66, 73

H_0 : Before and after there is no change

H_1 : There is change

$>x = c(\dots)$

$>y = c(\dots)$

$>d = x - y$

$> wilcox.test(d, alter = "two.sided", mu = 0)$

wilcoxon signed Rank test with continuity correction

data: d

$V = 4.5$ p-value = 0.4982

alternative hypothesis: true location is not equal to 0

$\therefore p > 0.05$ we accept H_0

An
27.02.21